# seer: R package for feature-based forecast model selection

Thiyanga S Talagala Rob J Hyndman George Athanasopoulos

Monash University, Australia

UseR, 2018

# Large collections of time series



• Forecasting demand for thousands of products across multiple warehouses.

#### Objective

Develop a framework that automates the selection of the most appropriate forecasting method for a given time series by using an array of features computed from the time series.

## Objective

Develop a framework that automates the selection of the most appropriate forecasting method for a given time series by using an array of features computed from the time series.

#### Basic idea:

### Objective

Develop a framework that automates the selection of the most appropriate forecasting method for a given time series by using an array of features computed from the time series.

- Basic idea:
  - Transform a given time series  $y = \{y_1, y_2, \dots, y_n\}$  to a feature vector  $F = (f_1(y), f_2(y), \dots, f_p(y))'$ .
- Examples for time series features

### Objective

Develop a framework that automates the selection of the most appropriate forecasting method for a given time series by using an array of features computed from the time series.

#### Basic idea:

- Examples for time series features
  - strength of trend

## Objective

Develop a framework that automates the selection of the most appropriate forecasting method for a given time series by using an array of features computed from the time series.

#### Basic idea:

- Examples for time series features
  - strength of trend
  - strength of seasonality

## Objective

Develop a framework that automates the selection of the most appropriate forecasting method for a given time series by using an array of features computed from the time series.

#### Basic idea:

- Examples for time series features
  - strength of trend
  - strength of seasonality
  - lag-1 autocorrelation

## Objective

Develop a framework that automates the selection of the most appropriate forecasting method for a given time series by using an array of features computed from the time series.

#### • Basic idea:

- Examples for time series features
  - strength of trend
  - strength of seasonality
  - lag-1 autocorrelation
  - spectral entropy

- length
- strength of seasonality
- strength of trend
- linearity
- curvature
- spikiness
- stability
- lumpiness
- first ACF value of remainder series
- parameter estimates of Holt's linear trend method

- spectral entropy
- Hurst exponent
- nonlinearity
- parameter estimates of Holt-Winters' additive method
- unit root test statistics
- first ACF value of residual series of linear trend model
- ACF and PACF based features - calculated on both the raw and differenced series

# Methodology: FFORMS

#### FFORMS: Feature-based FORecast Model Selection

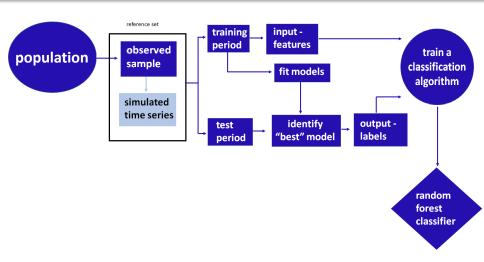
#### Offline

• A classification algorithm (the meta-learner) is trained.

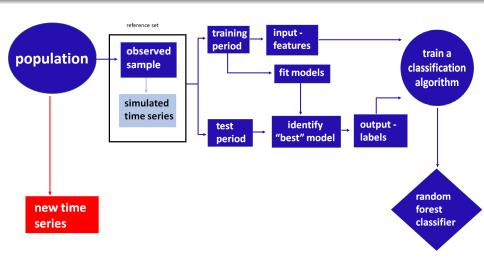
#### Online

 Calculate the features of a time series and use the pre-trained classifier to identify the best forecasting method.

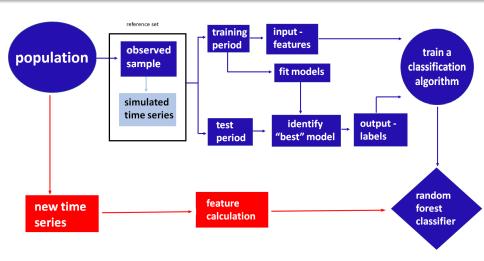
# FFORMS: "offline" part of the algorithm



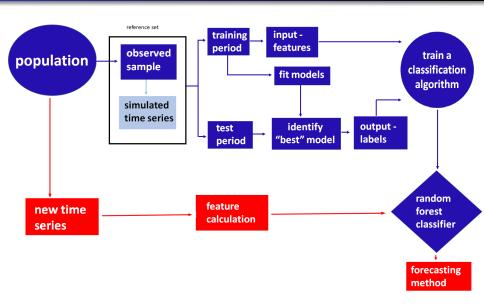
# FFORMS: "online" part of the algorithm



# FFORMS: "online" part of the algorithm



# FFORMS: "online" part of the algorithm



## Installation

```
devtools::install_github("thiyangt/seer")
library(seer)
```



#### Installation

```
devtools::install_github("thiyangt/seer")
library(seer)
```



#### **Example datasets**

observed time series - M1 yearly series (181)

```
library(Mcomp)
yearlym1 <- subset(M1, "yearly")</pre>
```

#### Installation

```
devtools::install_github("thiyangt/seer")
library(seer)
```



#### **Example datasets**

observed time series - M1 yearly series (181)

```
library(Mcomp)
yearlym1 <- subset(M1, "yearly")</pre>
```

new time series - M3 yearly series (645)

```
yearlym3 <- subset(M3, "yearly")</pre>
```

## Input: features

#

#

#

```
cal features(yearlym1[1:3], database="M3",
h=6, highfreq=FALSE)
# A tibble: 3 x 25
 entropy lumpiness stability hurst trend spikiness linearity curvature
   <dbl>
            <dbl> <dbl> <dbl> <dbl> <dbl> <
                                         <dbl>
                                                 <dbl>
                                                          <dbl>
                                                 4.46
   0.683 0.0400 0.977 0.985 0.985 0.00000132
                                                          0.705
  0.711 0.0790 0.894 0.988 0.989 0.00000154
                                                 4.47
                                                          0.613
3 0.716 0.0160 0.858 0.987 0.989 0.00000113
                                                          0.695
                                                  4.60
  ... with 17 more variables: e acf1 <dbl>, y acf1 <dbl>,
```

lmres\_acf1 <dbl>, ur\_pp <dbl>, ur\_kpss <dbl>, N <int>, y\_acf5 <dbl>,

diff1y acf5 <dbl>, diff2y acf5 <dbl>, alpha <dbl>, beta <dbl>

diff1y\_acf1 <dbl>, diff2y\_acf1 <dbl>, y\_pacf5 <dbl>,
diff1y\_pacf5 <dbl>, diff2y\_pacf5 <dbl>, nonlinearity <dbl>,

# Output: labels

```
fcast accuracy(yearlym1[1:3],
  models=c("arima","ets","rw","rwd","theta","nn"),
  database="M3", cal MASE, h=6, length out=1)
$accuracy
        arima
                  ets
                           rw
                                 rwd theta
                                                       nn
YAF2 10.527612 10.319029 13.52428 10.527612 12.088375 11.756990
YAF3 5.713867 7.704409 7.78949 5.225965 6.225463 6.700781
YAF4 8.633590 8.091416 11.55633 8.440105 9.952742 10.784962
$ARIMA
                  YAF2
                                          YAF3
"ARIMA(0,1,0) with drift" "ARIMA(0,1,1) with drift"
                  YAF4
"ARIMA(0,1,2) with drift"
$ETS
       YAF2
                  YAF3
                              YAF4
"ETS(A,A,N)" "ETS(M,A,N)" "ETS(M,A,N)"
```

#### Reference set

```
accuracy_m1 <- fcast_accuracy(tslist=yearlym1,
models= c("arima","ets","rw","rwd", "theta", "nn"),
database ="M1", cal_MASE)

features_m1 <- cal_features(yearlym1, database="M1", highfreq = FALSE)

reference_set <- prepare_trainingset(accuracy_set = accuracy_m1,
feature_set = features_m1)
head(reference_set$trainingset, 1)</pre>
```

```
# A tibble: 1 \times 26
 entropy lumpiness stability hurst trend spikiness linearity curvature
   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
                                                               <dbl>
   0.683 0.0400 0.977 0.985 0.985 0.00000132 4.46
                                                               0.705
# ... with 18 more variables: e_acf1 <dbl>, y_acf1 <dbl>,
   diff1y_acf1 <dbl>, diff2y_acf1 <dbl>, y_pacf5 <dbl>,
#
#
   diff1y_pacf5 <dbl>, diff2y_pacf5 <dbl>, nonlinearity <dbl>,
   lmres_acf1 <dbl>, ur_pp <dbl>, ur_kpss <dbl>, N <int>, y_acf5 <dbl>,
#
   diff1y_acf5 <dbl>, diff2y_acf5 <dbl>, alpha <dbl>, beta <dbl>,
#
#
  classlabels <chr>
```

## FFORMS classifier

```
##
                              3
                                                            6
                                                                      7
## ETS-trend
                  rwd
                            rwd
                                      rwd
                                                rwd
                                                          rwd
                                                                    rwd
##
                    9
                            10
                                                12
                                                          13
                                                                     14
                            rwd
                                      rwd ETS-trend
##
        rwd
                  rwd
                                                          rwd
                                                                    rwd
         15
                  16
                            17
                                      18
##
                                                 19
                                                          20
##
         nn
                  rwd
                            rwd
                                      rwd
                                                rwd
                                                        ARIMA
## 10 Levels: ARIMA ARMA/AR/MA ETS-dampedtrend ... wn
```

# Generate point foecasts and 95% prediction intervals

```
rf_forecast(fforms$predictions[1:2],
tslist=yearlym3[1:2], database="M3",
function_name="cal_MASE", h=6, accuracy=TRUE)
```

```
## $mean
##
           [,1] [,2] [,3] [,4] [,5]
## [1,] 5486.429 6035.865 6585.301 7134.737 7684.173 8233.609
## [2,] 4402.227 4574.454 4746.681 4918.908 5091.135 5263.362
##
## $lower
##
          [,1] [,2] [,3] [,4] [,5] [,6]
## [1,] 4984.162 4893.098 4629.135 4199.745 3606.858 2848.8735
## [2,] 2890.401 2366.671 1959.916 1608.186 1288.666 990.2221
##
## $upper
           [,1] [,2] [,3] [,4] [,5] [,6]
##
## [1,] 5988.696 7178.632 8541.467 10069.729 11761.488 13618.344
## [2,] 5914.053 6782.236 7533.445 8229.629 8893.603 9536.501
##
## $accuracy
## [1] 1.5636089 0.6123443
```

# Augmenting the observed sample with simutated time series

## lapply(yearlym1[1], sim\_arimabased, Nsim=2)

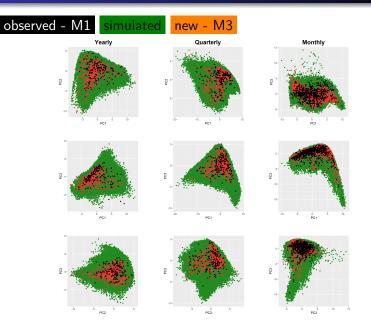
```
## $YAF2
## $YAF2[[1]]
## Time Series:
## Start = 1972
## End = 1993
## Frequency = 1
         3600.00 15158.97 38653.24 61436.41 111298.11 85898.46 177282.98
## [8] 171711.97 163492.36 177853.14 216154.50 263424.00 260655.68 265410.40
## [15] 307030.65 371226.22 413602.53 462569.21 460368.35 465142.08 490847.33
## [22] 505928.59
##
## $YAF2[[2]]
## Time Series:
## Start = 1972
## End = 1993
## Frequency = 1
## [1] 3600.00
                 14657.36 32971.60 80537.55 146425.27 142443.09 190979.40
## [8] 238906.76 266580.96 273224.47 278253.14 282840.62 332403.58 375570.08
## [15] 361558.06 363810.01 377489.10 462165.08 510598.86 476927.75 520308.58
## [22] 600756.76
```

# Augmenting the observed sample with simutated time series

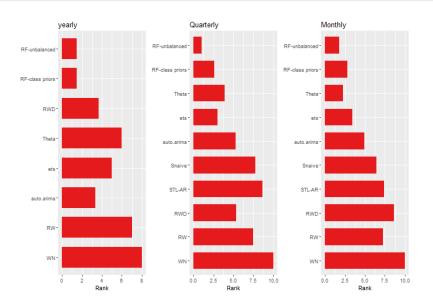
```
lapply(yearlym1[1], sim_arimabased, Nsim=2)
```

```
## $YAF2
## $YAF2[[1]]
## Time Series:
## Start = 1972
## End = 1993
## Frequency = 1
## [1] 3600.00 15158.97 38653.24 61436.41 111298.11 85898.46 177282.98
## [8] 171711.97 163492.36 177853.14 216154.50 263424.00 260655.68 265410.40
## [15] 307030.65 371226.22 413602.53 462569.21 460368.35 465142.08 490847.33
## [22] 505928.59
##
## $YAF2[[2]]
## Time Series:
## Start = 1972
## End = 1993
## Frequency = 1
## [1] 3600.00 14657.36 32971.60 80537.55 146425.27 142443.09 190979.40
## [8] 238906.76 266580.96 273224.47 278253.14 282840.62 332403.58 375570.08
## [15] 361558.06 363810.01 377489.10 462165.08 510598.86 476927.75 520308.58
## [22] 600756.76
lapply(yearlym1[1], sim_etsbased, Nsim=2)
lapply(yearlym1[1], sim mstlbased, Nsim=2)
```

# Application: Distribution of time series in the PCA space



## Results



• FFORMS: framework for forecast model selection using meta-learning based on time series features.

- FFORMS: framework for forecast model selection using meta-learning based on time series features.
- FFORMS algorithm uses the knowledge of the past performance of candidate forecast models on a collection of time series in order to identify the best forecasting method for a new series.

- FFORMS: framework for forecast model selection using meta-learning based on time series features.
- FFORMS algorithm uses the knowledge of the past performance of candidate forecast models on a collection of time series in order to identify the best forecasting method for a new series.
- For real-time forecasting, our framework involves only the calculation of features, the selection of a forecast method based on the FFORMS random forest classifier, and the calculation of the forecasts from the chosen model.

- FFORMS: framework for forecast model selection using meta-learning based on time series features.
- FFORMS algorithm uses the knowledge of the past performance of candidate forecast models on a collection of time series in order to identify the best forecasting method for a new series.
- For real-time forecasting, our framework involves only the calculation of features, the selection of a forecast method based on the FFORMS random forest classifier, and the calculation of the forecasts from the chosen model.
- We have also introduced a simple set of time series features that are useful in identifying the "best" forecast method for a given time series.



available at: https://github.com/thiyangt/seer



available at: https://github.com/thiyangt/seer

paper: https://robjhyndman.com/publications/fforms/

Email: thiyanga.talagala@monash.edu

twitter: thiyangt