

Muffix Sassif – TRD

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1 Геометрия

1.1 2D

```
class Pt:
    def dot(self, other):
        return self.x * other.x + self.y * other.y

    def cross(self, other):
        return self.x * other.y - self.y * other.x

    @staticmethod
    def get_straight(self, other):
        a = self.y - other.y
        b = other.x - self.x
        c = self.cross(other)
        return a, b, c

class Straight:

    def __eq__(self, other):
        if self.b != 0 or other.b != 0:
            return self.a * other.b == other.a * self.b
        and self.c * other.b == other.c * self.b
        val1 = math.sqrt(self.a ** 2 + self.b ** 2)
        val2 = math.sqrt(other.a ** 2 + other.b ** 2)
        a1, c1 = self.a / val1, self.c / val1
        a2, c2 = other.a / val2, other.c / val2
        if (a1 < 0) != (a2 < 0):
            a1, a2, c1, c2 = a1, -a2, c1, -c2
        return a1 == a2 and c1 == c2

    def perpendicular(self, point: Pt):
        return Straight(-self.b, self.a, self.b * point
            .x - self.a * point.y)

    def get_value(self, point):
        return self.a * point.x + self.b * point.y +
            self.c

    def intersection(self, other):
        d = Pt(self.a, self.b).cross(Pt(other.a, other.
            b))
        dx = Pt(self.c, self.b).cross(Pt(other.c, other
            .b))
        dy = Pt(self.a, self.c).cross(Pt(other.a, other
            .c))
        return Pt(-dx / d, -dy / d)
```

```
def dist_from_point(self, point):
    val = math.sqrt(self.a ** 2 + self.b ** 2)
    return abs(Straight(self.a / val, self.b / val,
        self.c / val).get_value(point))

def parallel(self, dist):
    val = math.sqrt(self.a ** 2 + self.b ** 2)
    return Straight(self.a, self.b, self.c - dist *
        val)

def is_parallel(self, other):
    return self.a * other.b == self.b * other.a

def is_perpendicular(self, other):
    per = Straight(-self.b, self.a, 0)
    return per.a * other.b == per.b * other.a

class Triangle:
    def intersection_medians(self):
        return (self.A + self.B + self.C) / 3

    def intersection_altitudes(self):
        st1 = Straight(self.A, self.B).perpendicular(
            self.C)
        st2 = Straight(self.A, self.C).perpendicular(
            self.B)
        return st1.intersection(st2)

    def intersection_middle_pers(self):
        st1 = Straight(self.A, self.B).perpendicular((
            self.A + self.B) / 2)
        st2 = Straight(self.A, self.C).perpendicular((
            self.A + self.C) / 2)
        return st1.intersection(st2)

class Circle:
    def intersect_straight(self, st):
        pt = st.get_point()
        A = st.a ** 2 + st.b ** 2
        B = 2 * (-st.b * (pt.x - self.center.x) + st.a
            * (pt.y - self.center.y))
        C = (pt.x - self.center.x) ** 2 + (pt.y - self.
            center.y) ** 2 - self.radius ** 2
        D = B ** 2 - 4 * A * C
        if D < 0:
            return []
        D = math.sqrt(D)
```

```
vector = Pt(-st.b, st.a)
if D == 0:
    t = -B / (2 * A)
    return [pt + t * vector]
t1 = (-B - D) / (2 * A)
t2 = (-B + D) / (2 * A)
return [pt + t1 * vector, pt + t2 * vector]

def intersect_circle(self, other):
    x1, x2 = self.center.x, other.center.x
    y1, y2 = self.center.y, other.center.y
    a = -2 * (x1 - x2)
    b = -2 * (y1 - y2)
    c = (x1 ** 2 - x2 ** 2) + (y1 ** 2 - y2 ** 2) -
        (self.radius ** 2 - other.radius ** 2)
    return self.intersect_straight(Straight(a, b, c
        ))

def is_own(self, pt):
    return (pt.x - self.center.x) ** 2 + (pt.y -
        self.center.y) ** 2 == self.radius ** 2

def tangent_pts(self, pt):
    if self.is_own(pt):
        return [pt]
    cir = Circle(pt, math.sqrt(abs(pt - self.center
        ) ** 2 - self.radius ** 2))
    return self.intersect_circle(cir)

def dist_by_circle(self, pt1, pt2):
    pt1 -= self.center
    pt2 -= self.center
    ang = (pt1.polar_angle() - pt2.polar_angle()) %
        (2 * math.pi)
    ang = min(ang, 2 * math.pi - ang)
    return self.radius * ang
```

1.2 3D

```
// TODO
```

1.3 Выпуклая оболочка

```
Pt start(0, 0);

bool comp(Pt a, Pt b) {
    ll ang = (a - start).cross(b - start);
    if (ang < 0) {
```

```

        return false;
    } else if (ang > 0) {
        return true;
    }
    return abs(start - a) < abs(start - b);
}

vector<Pt> convex_hull(vector<Pt> points) {
    int n = points.size();
    start = points[0];
    for (auto x : points) {
        start = min(start, x);
    }
    sort(points.begin(), points.end(), comp);
    vector<Pt> s = {points[0], points[1]};
    for (int i = 2; i < n; i++) {
        int k = s.size();
        while (k > 1 && (s[k - 1] - s[k - 2]).cross(
            points[i] - s[k - 1]) <= 0) {
            s.pop_back();
            k = s.size();
        }
        s.push_back(points[i]);
    }
    return s;
}

```

1.4 Касательные из точки

```
// TODO
```

1.5 Касательные параллельные прямой

```
// TODO
```

2 Графы

2.1 Венгерский алгоритм

```

vector<int> venger(vector<vector<int>> arr) {
    int n = (int) arr.size() - 1;
    vector<int> u(n + 1), v(n + 1), p(n + 1), way(n + 1);
    for (int i = 1; i <= n; i++) {
        p[0] = i;
        int ind = 0;
        vector<int> minv(n + 1, INF), used(n + 1);

```

```

        do {
            used[ind] = 1;
            int ind2 = p[ind], dlt = INF, ind3 = 0;
            for (int j = 1; j <= n; j++)
                if (!used[j]) {
                    int cur = arr[ind2][j] - u[ind2] -
                        v[j];

                    if (cur < minv[j]) {
                        minv[j] = cur;
                        way[j] = ind;
                    }
                    if (minv[j] < dlt) {
                        dlt = minv[j], ind3 = j;
                    }
                }
            for (int j = 0; j <= n; j++)
                if (used[j]) {
                    u[p[j]] += dlt;
                    v[j] -= dlt;
                } else {
                    minv[j] -= dlt;
                }
            ind = ind3;
        } while (p[ind] != 0);
        do {
            int ind3 = way[ind];
            p[ind] = p[ind3];
            ind = ind3;
        } while (ind);
    }
    vector<int> ans(n + 1);
    for (int j = 1; j <= n; j++) {
        ans[p[j]] = j;
    }
    return ans;
}

```

2.2 Дейкстра за квадрат

```
// TODO
```

2.3 Диниц

```

vector<edge> g[MAXN];
pair<int, int> pred[MAXN];
int d[MAXN];
int inds[MAXN];

```

```

bool dfs(int v, int final, int W) {
    if (v == final) {
        return true;
    }
    for (int i = inds[v]; i < (int) g[v].size(); i++) {
        auto e = g[v][i];
        if (e.f + W <= e.c && d[v] + 1 == d[e.v]) {
            pred[e.v] = {v, i};
            bool flag = dfs(e.v, final, W);
            if (flag) {
                return true;
            }
            inds[v]++;
        } else {
            inds[v]++;
        }
    }
    return false;
}

bool bfs(int start, int final, int W) {
    fill(d, d + MAXN, INF);
    d[start] = 0;
    deque<int> q = {start};
    while (!q.empty()) {
        int v = q.front();
        q.pop_front();
        for (auto e : g[v]) {
            if (e.f + W <= e.c && d[e.v] > d[v] + 1) {
                d[e.v] = d[v] + 1;
                q.push_back(e.v);
            }
        }
    }
    if (d[final] == INF) {
        return false;
    }
    fill(inds, inds + MAXN, 0);
    while (dfs(start, final, W)) {
        int v = final;
        int x = INF;
        while (v != start) {
            int ind = pred[v].second;
            v = pred[v].first;
            x = min(x, g[v][ind].c - g[v][ind].f);
        }
        v = final;
        while (v != start) {
            int ind = pred[v].second;
            v = pred[v].first;

```

```

        g[v][ind].f += x;
        g[g[v][ind].v][g[v][ind].ind].f -= x;
    }
}
return true;
}

void Dinic(int start, int final) {
    int W = (1LL << 30);
    do {
        while (bfs(start, final, W));
        W /= 2;
    } while (W >= 1);
}

signed main() {
    vector<pair<int, int>> edges;
    for (int i = 0; i < m; i++) {
        int u, v, c;
        cin >> u >> v >> c;
        edges.emplace_back(u, v);
        g[u].push_back({v, 0, c, (int) g[v].size()});
        g[v].push_back({u, 0, c, (int) g[u].size() -
1});
    }
    Dinic(1, n);
    int res = 0;
    for (auto e : g[1]) {
        res += e.f;
    }
    vector<int> ans;
    for (int i = 0; i < m; i++) {
        int u = edges[i].first, v = edges[i].second;
        if ((d[u] != INF && d[v] == INF) || (d[u] ==
INF && d[v] != INF)) {
            ans.push_back(i + 1);
        }
    }
}

```

2.4 KCC

```

void dfs1(int v) {
    vis[v] = 1;
    for (auto u : g[v]) {
        if (!vis[u]) {
            dfs1(u);
        }
    }
}

```

```

    topsort.push_back(v);
}

void dfs2(int v) {
    vis[v] = 1;
    for (auto u : rg[v]) {
        if (!vis[u]) {
            dfs2(u);
        }
    }
    comp.push_back(v);
}

signed main() {
    for (int i = 1; i <= n; i++)
        if (!vis[i])
            dfs1(i);
    reverse(topsort.begin(), topsort.end());
    for (int j = 1; j <= n; j++) {
        int vert = topsort[j - 1];
        if (!vis[vert])
            dfs2(vert);
    }
}

```

2.5 Минкост (Джонсон)

```

using cost_t = ll;
using flow_t = int;

const int MAXN = 10000;
const int MAXM = 25000 * 2;
const cost_t INFw = 1e12;
const flow_t INFf = 10;

struct Edge {
    int v, u;
    flow_t f, c;
    cost_t w;
};

Edge edg[MAXN];
int esz = 0;
vector<int> graph[MAXN];
ll dist[MAXN];
ll pot[MAXN];
int S, T;
int NUMV;

```

```

int pre[MAXN];
bitset<MAXN> inQ;

flow_t get_flow() {
    int v = T;
    if (pre[v] == -1)
        return 0;
    flow_t f = INFf;
    do {
        int ei = pre[v];
        Edge &e = edg[ei];
        f = min(f, e.c - e.f);
        if (f == 0)
            return 0;
        v = e.v;
    } while (v != S);
    v = T;
    do {
        int ei = pre[v];
        edg[ei].f += f;
        edg[ei ^ 1].f -= f;
        v = edg[ei].v;
    } while (v != S);
    return f;
}

void spfa() {
    fill(dist, dist + NUMV, INFw);
    dist[S] = 0;
    deque<int> Q = {S};
    inQ[S] = true;
    while (!Q.empty()) {
        int v = Q.front();
        Q.pop_front();
        inQ[v] = false;
        cost_t d = dist[v];
        for (int ei : graph[v]) {
            Edge &e = edg[ei];
            if (e.f == e.c)
                continue;
            cost_t w = e.w + pot[v] - pot[e.u];
            if (dist[e.u] <= d + w)
                continue;
            pre[e.u] = ei;
            dist[e.u] = d + w;
            if (!inQ[e.u]) {
                inQ[e.u] = true;
                Q.push_back(e.u);
            }
        }
    }
}

```

```

    }
    for (int i = 0; i < NUMV; ++i)
        pot[i] += dist[i];
}

cost_t mincost() {
    spfa(); // pot[i] = 0 // or ford_bellman
    flow_t f = 0;
    while (true) {
        flow_t ff = get_flow();
        if (ff == 0)
            break;
        f += ff;
        spfa(); // or dijkstra
    }
    cost_t res = 0;
    for (int i = 0; i < esz; ++i)
        res += edg[i].f * edg[i].w;
    res /= 2;
    return res;
}

void add_edge(int v, int u, int c, int w) {
    edg[esz] = {v, u, 0, c, w};
    edg[esz + 1] = {u, v, 0, 0, -w};
    graph[v].push_back(esz);
    graph[u].push_back(esz + 1);
    esz += 2;
}

signed main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
    int n, m;
    cin >> n >> m;
    S = 0;
    T = n - 1;
    NUMV = n;
    for (int i = 0; i < m; ++i) {
        int v, u, c, w;
        cin >> v >> u >> c >> w;
        v--, u--;
        add_edge(v, u, c, w);
    }
    cost_t ans = mincost();
    cout << ans;
}

```

2.6 Мосты

```

void dfs(int v, int par) {
    vis[v] = 1;
    up[v] = tin[v] = timer++;
    for (auto u : g[v]) {
        if (!vis[u]) {
            dfs(u, v);
            up[v] = min(up[v], up[u]);
        } else if (u != par) {
            up[v] = min(up[v], tin[u]);
        }
        if (up[u] > tin[v]) {
            bridges.emplace_back(v, u);
        }
    }
}

```

2.7 Паросочетания

```

bool dfs(int v, int c) {
    if (used[v] == c) return false;
    used[v] = c;
    for (auto u : g[v]) {
        if (res[u] == -1) {
            res[u] = v;
            return true;
        }
    }
    for (auto u : g[v]) {
        if (dfs(res[u], c)) {
            res[u] = v;
            return true;
        }
    }
    return false;
}

signed main() {
    for (int i = 0; i < s; ++i) {
        ans += dfs(i, i + 1);
    }
}

```

2.8 Точки сочленения

```

void dfs(int v, int par) {
    vis[v] = 1;
    up[v] = tin[v] = timer++;
    int child = 0;

```

```

    for (auto u : g[v]) {
        if (!vis[u]) {
            dfs(u, v);
            up[v] = min(up[v], up[u]);
            if (up[u] >= tin[v] && par != -1) {
                points.insert(v);
            }
            child++;
        } else if (u != par) {
            up[v] = min(up[v], tin[u]);
        }
    }
    if (par == -1 && child >= 2) {
        points.insert(v);
    }
}

```

2.9 Эдмондс-Карп

```

struct edge {
    int v, f, c, ind;
};

vector<edge> g[MAXN];

bool bfs(int start, int final, int W) {
    vector<int> d(MAXN, INF);
    vector<pair<int, int>> pred(MAXN);
    d[start] = 0;
    deque<int> q = {start};
    while (!q.empty()) {
        int v = q.front();
        q.pop_front();
        for (int i = 0; i < (int) g[v].size(); i++) {
            auto e = g[v][i];
            if (e.f + W <= e.c && d[e.v] > d[v] + 1) {
                d[e.v] = d[v] + 1;
                pred[e.v] = {v, i};
                q.push_back(e.v);
            }
        }
    }
    if (d[final] == INF) {
        return false;
    }
    int v = final;
    int x = INF;
    while (v != start) {
        int ind = pred[v].second;

```

```

        v = pred[v].first;
        x = min(x, g[v][ind].c - g[v][ind].f);
    }
    v = final;
    while (v != start) {
        int ind = pred[v].second;
        v = pred[v].first;
        g[v][ind].f += x;
        g[g[v][ind].v][g[v][ind].ind].f -= x;
    }
    return true;
}

signed main() {
    for (int i = 0; i < m; i++) {
        int u, v, c;
        cin >> u >> v >> c;
        g[u].push_back({v, 0, c, (int) g[v].size()});
        g[v].push_back({u, 0, 0, (int) g[u].size() -
1});
    }
    int W = (1 << 30);
    do {
        while (bfs(1, n, W));
        W /= 2;
    } while (W >= 1);
    int res = 0;
    for (auto e : g[1]) {
        res += e.f;
    }
}

```

2.10 Эйлеров цикл

```
// TODO
```

3 ДП

3.1 СХТ

```

pair<ld, ld> inter(Line a, Line b) {
    ld x = (b.b - a.b) / (a.k - b.k);
    ld y = a.k * x + a.b;
    return {x, y};
}

void add_line(ld k, ld b, vector<Line> &s, vector<pair<
ld, ld>> &pts) {

```

```

    while (s.size() >= 2) {
        pair<ld, ld> x1 = inter(s.back(), s[s.size() -
2]);
        pair<ld, ld> x2 = inter(s[s.size() - 2], {k, b
});
        if (x1 > x2) {
            break;
        }
        pts.pop_back();
        s.pop_back();
    }
    if (!s.empty()) {
        pts.push_back(inter(s.back(), {k, b}));
    }
    s.push_back({k, b});
}

ld bin_search(vector<Line> &s, ld x) {
    int l = 0, r = s.size();
    while (l + 1 < r) {
        int m = (r + l) / 2;
        auto kek = inter(s[m - 1], s[m]);
        if (kek.first >= x) {
            l = m;
        } else {
            r = m;
        }
    }
    return s[l].k * x + s[l].b;
}

```

3.2 Li Chao

```

// max

struct Line {
    int k, b;

    int f(int x) {
        return k * x + b;
    }
};

```

```

struct ST {
    vector<Line> st;

    ST(int n) {
        Line ln = {0LL, -INF};
        st.resize(4 * n, ln);
    }

```

```

}

void upd(int i, int l, int r, Line ln) {
    int child = 1;
    Line ln1 = ln;
    int m = (l + r) / 2;
    if (ln.f(m) > st[i].f(m)) {
        if (ln.k < st[i].k) {
            child = 2;
        }
        ln1 = st[i];
        st[i] = ln;
    } else {
        if (st[i].k < ln.k) {
            child = 2;
        }
    }
    if (l + 1 < r) {
        if (child == 1) {
            upd(i * 2 + 1, l, m, ln1);
        } else {
            upd(i * 2 + 2, m, r, ln1);
        }
    }

    int res(int i, int l, int r, int x) {
        if (l + 1 == r) {
            return st[i].f(x);
        }
        int m = (l + r) / 2;
        int val = st[i].f(x);
        if (x < m) {
            val = max(val, res(i * 2 + 1, l, m, x));
        } else {
            val = max(val, res(i * 2 + 2, m, r, x));
        }
        return val;
    }
};

```

3.3 SOS-dp

```

// dp initial fill, a[] is given array, mb extra zeros
for (int i = 0; i < (1 << N); i++) {
    dp[i] = a[i];
}

```

```
// Classic SOS-dp, goal: dp[mask] = \sum a[submasks of mask]
for (int i = 0; i < N; i++) {
    for (int mask = 0; mask < (1 << N); mask++) {
        if ((mask >> i) & 1) {
            dp[mask] += dp[mask ^ (1 << i)];
        }
    }
}

// Overmasks SOS-dp, goal: dp[mask] = \sum a[overmasks of mask]
for (int i = 0; i < N; i++) {
    for (int mask = (1 << N) - 1; mask >= 0; mask--) {
        if (((mask >> i) & 1) == 0) {
            dp[mask] += dp[mask ^ (1 << i)];
        }
    }
}

// to inverse SOS-dp (restore original array by SOS-dp array):
// use same code, but -= instead of += in dp transitions
```

3.4 НБИ

```
vector<int> lis(vector<int> a) { // 0-indexation ({a_0, ..., a_{n-1}})
    int n = (int) a.size();
    vector<int> dp(n + 1, INF), ind(n + 1), par(n + 1);
    // INF > all a[i] required
    ind[0] = -INF;
    dp[0] = -INF;
    for (int i = 0; i < n; i++) {
        int l = upper_bound(dp.begin(), dp.end(), a[i]) - dp.begin();
        if (dp[l - 1] < a[i] && a[i] < dp[l]) {
            dp[l] = a[i];
            ind[l] = i;
            par[i] = ind[l - 1];
        }
    }
    vector<int> ans; // exact values
    for (int l = n; l >= 0; l--) {
        if (dp[l] < INF) {
            int pi = ind[l];
            ans.resize(l);
            for (int i = 0; i < l; i++) {
```

```
                ans[i] = a[pi]; // =pi if need indices
                pi = par[pi];
            }
        }
        return {};
    }
}
```

3.5 НОБИ

```
vector<int> LCIS(vector<int> a, vector<int> b) { // 1-indexation ({0, a_1, ..., a_n}, {0, b_1, ..., b_m})
    int n = (int) a.size() - 1, m = (int) b.size() - 1;
    vector<int> dp(m + 1), dp2(m + 1), par(m + 1);
    for (int i = 1; i <= n; i++) {
        int best = 0, best_idx = 0;
        for (int j = 1; j <= m; j++) {
            dp2[j] = dp[j];
            if (a[i] == b[j]) {
                dp2[j] = max(dp2[j], best + 1);
                par[j] = best_idx;
            }
            if (a[i] > b[j] && best < dp[j]) {
                best = dp[j];
                best_idx = j;
            }
        }
        swap(dp, dp2);
    }
    int pj = 0;
    for (int j = 1; j <= m; j++) {
        if (dp[pj] < dp[j]) {
            pj = j;
        }
    }
    vector<int> ans; // exact values
    while (pj > 0) {
        ans.push_back(b[pj]);
        pj = par[pj];
    }
    reverse(ans.begin(), ans.end());
    return ans;
}
```

4 Деревья

4.1 Centroid

```
void sizes(int v, int p) {
    sz[v] = 1;
    for (auto u : g[v]) {
        if (u != p && !used[u]) {
            sizes(u, v);
            sz[v] += sz[u];
        }
    }
}

int centroid(int v, int p, int n) {
    for (int u : g[v]) {
        if (sz[u] > n / 2 && u != p && !used[u]) {
            return centroid(u, v, n);
        }
    }
    return v;
}

void dfs(int v, int p) {
    .....
    for (auto u : g[v]) {
        if (u != p && !used[u]) {
            dfs(u, v);
        }
    }
}

void solve(int v) {
    sizes(v, -1);
    .....
    for (auto u : g[v]) {
        if (!used[u]) {
            .....
            dfs(u, v);
            .....
        }
    }
    .....
    used[v] = 1;
    for (int u : g[v]) {
        if (!used[u]) {
            solve(centroid(u, v, sz[u]));
        }
    }
}

int main() {
```

```

    sizes(0, -1);
    solve(centroid(0, -1, n));
}

```

4.2 HLD

```

const int MAXN = 50500;
const int INF = (int) 1e15;
const int L = 20;
vector<int> g[MAXN];
int sz[MAXN];
int depth[MAXN];

vector<vector<int>> up(MAXN, vector<int>(L + 1));

```

```

void dfs(int v, int p) {
    up[v][0] = p;
    for (int i = 1; i <= L; i++) {
        up[v][i] = up[up[v][i - 1]][i - 1];
    }
    for (int u : g[v]) {
        if (u != p) {
            dfs(u, v);
        }
    }
}

```

```

int lca(int u, int v) {
    if (u == v) {
        return u;
    }
    int du = depth[u], dv = depth[v];
    if (du < dv) {
        swap(du, dv);
        swap(u, v);
    }
    for (int i = L; i >= 0; i--) {
        if (du - (int) pow(2, i) >= dv) {
            u = up[u][i];
            du -= (int) pow(2, i);
        }
    }
    if (u == v) {
        return u;
    }
    for (int i = L; i >= 0; i--) {
        if (up[u][i] != up[v][i]) {
            u = up[u][i];
            v = up[v][i];
        }
    }
}

```

```

    }
}
return up[u][0];
}

void dfs1(int v, int p) {
    sz[v] = 1;
    for (int u : g[v]) {
        if (u != p) {
            dfs1(u, v);
            sz[v] += sz[u];
        }
    }
}

int cnt = 0;
int nn[MAXN];
int pred[MAXN];
int rup[MAXN];

void dfs2(int v, int p, int root, int dep = 0) {
    depth[v] = dep;
    nn[v] = cnt++;
    pred[v] = p;
    rup[v] = root;
    int mx = 0;
    int vert = -1;
    for (int u : g[v]) {
        if (u != p) {
            if (mx < sz[u]) {
                mx = sz[u];
                vert = u;
            }
        }
    }
    if (vert != -1) {
        dfs2(vert, v, root, dep + 1);
    }
    for (int u : g[v]) {
        if (u != p && u != vert) {
            dfs2(u, v, u, dep + 1);
        }
    }
}

ST st({});
int n;

int mx_path_up(int u, int v) {
    if (depth[u] < depth[v]) {

```

```

        swap(u, v);
    }
    int res = -INF;
    while (true) {
        int root = rup[u];
        if (depth[root] <= depth[v]) {
            res = max(res, st.rmq(0, 0, n, nn[v], nn[u]
+ 1));
            break;
        }
        res = max(res, st.rmq(0, 0, n, nn[root], nn[u]
+ 1));
        u = pred[rup[u]];
    }
    return res;
}

int mx_path(int u, int v) {
    int vert = lca(u, v);
    return max(mx_path_up(u, vert), mx_path_up(v, vert)
);
}

void change(int u, int qd) {
    st.update(0, 0, n, nn[u], qd);
}

signed main() {
    cin >> n;
    vector<int> hs(n);
    for (auto &x : hs) {
        cin >> x;
    }
    for (int i = 0; i < n - 1; i++) {
        cin >> u1 >> v1;
        g[u1].push_back(v1);
        g[v1].push_back(u1);
    }
    dfs1(1, -1);
    dfs(1, 1);
    dfs2(1, -1, 1);
    vector<int> nhs(n);
    for (int i = 1; i <= n; i++) {
        nhs[nn[i]] = hs[i - 1];
    }
    st = *new ST(nhs);
    char op;
    int q;
    cin >> q;
    while (q--) {

```



```

    cin >> op >> v1 >> u1;
    if (op == '?') {
        cout << mx_path(u1, v1) << endl;
    } else {
        change(v1, u1);
    }
}

```

4.3 Link-cut

```

struct Node {
    Node *ch[2];
    Node *p;
    bool rev;
    int sz;

    Node () {
        ch[0] = nullptr;
        ch[1] = nullptr;
        p = nullptr;
        rev = false;
        sz = 1;
    }
};

int size(Node *v) {
    return (v ? v->sz : 0);
}

int chnum(Node *v) {
    return v->p->ch[1] == v;
}

bool isroot(Node *v) {
    return v->p == nullptr || v->p->ch[chnum(v)] != v;
}

void push(Node *v) {
    if (v->rev) {
        if (v->ch[0])
            v->ch[0]->rev ^= 1;
        if (v->ch[1])
            v->ch[1]->rev ^= 1;
        swap(v->ch[0], v->ch[1]);
        v->rev = false;
    }
}

```

```

void pull(Node *v) {
    v->sz = size(v->ch[1]) + size(v->ch[0]) + 1;
}

void attach(Node *v, Node *p, int num) {
    if (p)
        p->ch[num] = v;
    if (v)
        v->p = p;
}

void rotate(Node *v) {
    Node *p = v->p;
    push(p);
    push(v);
    int num = chnum(v);
    Node *u = v->ch[1 - num];
    if (!isroot(v->p))
        attach(v, p->p, chnum(p));
    else
        v->p = p->p;
    attach(u, p, num);
    attach(p, v, 1 - num);
    pull(p);
    pull(v);
}

void splay(Node *v) {
    push(v);
    while (!isroot(v)) {
        if (!isroot(v->p)) {
            if (chnum(v) == chnum(v->p))
                rotate(v->p);
            else
                rotate(v);
        }
        rotate(v);
    }
}

void expose(Node *v) {
    splay(v);
    v->ch[1] = nullptr;
    pull(v);
    while (v->p != nullptr) {
        Node *p = v->p;
        splay(p);
        attach(v, p, 1);
        pull(p);
        splay(v);
    }
}

```

```

}
}

void makeroot(Node *v) {
    expose(v);
    v->rev ^= 1;
    push(v);
}

void link(Node *v, Node *u) {
    makeroot(v);
    makeroot(u);
    u->p = v;
}

void cut(Node *v, Node *u) {
    makeroot(u);
    makeroot(v);
    v->ch[1] = nullptr;
    u->p = nullptr;
}

int get(Node *v, Node *u) {
    makeroot(u);
    makeroot(v);
    Node *w = u;
    while (!isroot(w))
        w = w->p;
    return (w == v ? size(v) - 1 : -1);
}

const int MAXN = 100010;
Node *nodes[MAXN];

int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
    cout.tie(nullptr);
    int n, q;
    cin >> n >> q;
    for (int i = 0; i < n; ++i)
        nodes[i] = new Node();
    while (q--) {
        string s;
        int a, b;
        cin >> s >> a >> b;
        a--, b--;
        if (s[0] == 'g')
            cout << get(nodes[a], nodes[b]) << '\n';
        else if (s[0] == 'l')

```

```

        link(nodes[a], nodes[b]);
    else
        cut(nodes[a], nodes[b]);
    }
}

```

5 Другое

5.1 Slope trick

// Дан массив a_n . Сделать минимальное кол-во ± 1 , чтобы a_n стал неубывающим.

```

void solve() {
    int n;
    cin >> n;
    vector<int> a(n);
    for (int i = 0; i < n; i++) {
        cin >> a[i];
    }
    int ans = 0;
    multiset<int> now;
    for (int i = 0; i < n; i++) {
        now.insert(a[i]);
        ans += (*now.rbegin() - a[i]);
        now.erase(now.find(*now.rbegin()));
        now.insert(a[i]);
    }
    cout << ans << '\n';
}

```

5.2 attribute_packed

// TODO

5.3 ordered_set

```

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

using namespace __gnu_pbds;

typedef tree<int, null_type, less<>, rb_tree_tag,
    tree_order_statistics_node_update> ordered_set;

//st.find_by_order(index);
//st.order_of_key(key);

```

5.4 pragma

```

#pragma GCC optimize("Ofast,fast-math,unroll-loops,no-
    stack-protector,inline")
#pragma GCC target("sse,sse2,sse3,ssse3,sse4,sse4.1,
    sse4.2,avx,avx2,abm,mmx,popcnt")

```

5.5 Аллокатор Копелиовича

// TODO

6 Математика

6.1 2-SAT

// TODO

6.2 FFT mod

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;
#define int long long

const int MOD = 998244353; // 7*17 * 2^23 + 1
const int GEN = 3;
//const int MOD = 7340033; // 7 * 2^20 + 1
//const int GEN = 5;
//const int MOD = 469762049; // 7 * 2^26 + 1
//const int GEN = 30;

const int LOG = 20;
const int MAXN = 1 << LOG;
int tail[MAXN + 1];
int OMEGA[MAXN + 1];

int binpow(int x, int p) {
    int res = 1;
    while (p > 0) {
        if (p & 1)
            res = res * 1ll * x % MOD;
        x = x * 1ll * x % MOD;
    }
}

```

```

        p >= 1;
    }
    return res;
}

int omega(int n, int k) {
    return OMEGA[MAXN / n * k];
}

int gettail(int x, int lg) {
    return tail[x] >> (LOG - lg);
}

void calcomega() {
    ll one = binpow(GEN, (MOD - 1) / MAXN);
    OMEGA[0] = 1;
    for (int i = 1; i < MAXN; ++i) {
        OMEGA[i] = OMEGA[i - 1] * one % MOD;
    }
}

void calctail() {
    int n = MAXN;
    for (int x = 0; x < n; ++x) {
        int res = 0;
        for (int i = 0; i < LOG; ++i) {
            res += ((x >> i) & 1) << (LOG - i - 1);
        }
        tail[x] = res;
    }
}

// Without precalc, tail[], OMEGA[]
//
//ll omega(int n, int k) {
//    return binpow(GEN, (MOD - 1) / n * k);
//}
//
//int gettail(int x, int lg) {
//    int res = 0;
//    for (int i = 0; i < lg; ++i)
//        res += ((x >> i) & 1) << (lg - i - 1);
//    return res;
//}

void fft(vector<int> &A, int lg) {
    int n = 1 << lg;
    for (int i = 0; i < n; ++i) {
        int j = gettail(i, lg);
        if (i < j)

```

```

        swap(A[i], A[j]);
    }
    for (int len = 2; len <= n; len *= 2) {
        for (int i = 0; i < n; i += len) {
            for (int j = 0; j < len / 2; ++j) {
                auto v = A[i + j];
                auto u = A[i + j + len / 2] * 111 *
omega(len, j) % MOD;
                A[i + j] = (v + u) % MOD;
                A[i + j + len / 2] = (v - u + MOD) %
MOD;
            }
        }
    }
}

int inverse(int x) {
    return binpow(x, MOD - 2);
}

void invfft(vector<int> &A, int lg) {
    int n = 1 << lg;
    fft(A, lg);
    for (auto &el : A)
        el = el * 111 * inverse(n % MOD) % MOD;
    reverse(A.begin() + 1, A.end());
}

vector<int> mul(vector<int> A, vector<int> B) {
    int lg = 32 - __builtin_clz(A.size() + B.size() -
1);
    int n = 1 << lg;
    A.resize(n, 0);
    B.resize(n, 0);
    fft(A, lg);
    fft(B, lg);
    for (int i = 0; i < n; ++i)
        A[i] = A[i] * 111 * B[i] % MOD;
    invfft(A, lg);
    return A;
}

signed main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
    calctail();
    calcomega();
    int n, m;
    cin >> n >> m;
    vector<int> A(n), B(m);

```

```

    for (int &el : A)
        cin >> el;
    for (int &el : B)
        cin >> el;
    auto C = mul(A, B);
    for (auto el : C)
        cout << el << '␣';
}

6.3 FFT

const double PI = acos(-1);
const int LOG = 19;
const int MAXN = 1 << LOG;

struct comp {
    double x, y;
    comp() : x(0), y(0) {}
    comp(double x, double y) : x(x), y(y) {}
    comp(int x) : x(x), y(0) {}
    comp operator+(const comp &o) const {
        return comp(x + o.x, y + o.y);
    }
    comp operator-(const comp &o) const {
        return comp(x - o.x, y - o.y);
    }
    comp operator*(const comp &o) const {
        return comp(x * o.x - y * o.y, x * o.y + y * o.
x);
    }
    comp operator/(const int k) const {
        return comp(x / k, y / k);
    }
    comp conj() const {
        return comp(x, -y);
    }
};

comp OMEGA[MAXN + 10];
int tail[MAXN + 10];

comp omega(int n, int k) {
    return OMEGA[MAXN / n * k];
}

void calcomega() {
    for (int i = 0; i < MAXN; ++i) {
        double x = 2 * PI * i / MAXN;
        OMEGA[i] = {cos(x), sin(x)};
    }
}

```

```

    }
}

void calctail() {
    tail[0] = 0;
    for (int i = 1; i < MAXN; ++i) {
        tail[i] = (tail[i >> 1] >> 1) | ((i & 1) << (
LOG - 1));
    }
}

void fft(vector<comp> &A) {
    int n = A.size();
    for (int i = 0; i < n; ++i) {
        if (i < tail[i])
            swap(A[i], A[tail[i]]);
    }
    for (int len = 2; len <= n; len *= 2) {
        for (int i = 0; i < n; i += len) {
            for (int j = 0; j < len / 2; ++j) {
                auto v = A[i + j];
                auto u = A[i + j + len / 2] * omega(len
, j);

                A[i + j] = v + u;
                A[i + j + len / 2] = v - u;
            }
        }
    }
}

void fft2(vector<comp> &A, vector<comp> &B) {
    int n = A.size();
    vector<comp> C(n);
    for (int i = 0; i < n; ++i) {
        C[i].x = A[i].x;
        C[i].y = B[i].x;
    }
    fft(C);
    C.push_back(C[0]);
    for (int i = 0; i < n; ++i) {
        A[i] = (C[i] + C[n - i].conj()) / 2;
        B[i] = (C[i] - C[n - i].conj()) / 2 * comp(0,
-1);
    }
}

void invfft(vector<comp> &A) {
    fft(A);
    for (auto &el : A)
        el = el / MAXN;
    reverse(A.begin() + 1, A.end());
}

```

```
}

vector<int> mul(vector<int> &a, vector<int> &b) {
    vector<comp> A(MAXN, 0), B(MAXN, 0);
    for (int i = 0; i < (int)a.size(); ++i)
        A[i] = a[i];
    for (int i = 0; i < (int)b.size(); ++i)
        B[i] = b[i];
    fft2(A, B);
    for (int i = 0; i < MAXN; ++i)
        A[i] = A[i] * B[i];
    invfft(A);
    vector<int> c(MAXN);
    for (int i = 0; i < MAXN; ++i) {
        int x = round(A[i].x);
        c[i] = x;
    }
    while (!c.empty() && c.back() == 0)
        c.pop_back();
    return c;
}

signed main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
    calcomega();
    calctail();
    string sa, sb;
    cin >> sa >> sb;
    reverse(sa.begin(), sa.end());
    reverse(sb.begin(), sb.end());
    vector<int> a(sa.size()), b(sb.size());
    bool minus = false;
    if (sa.back() == '-') {
        minus ^= true;
        sa.pop_back();
    }
    if (sb.back() == '-') {
        minus ^= true;
        sb.pop_back();
    }
    for (int i = 0; i < (int)sa.size(); ++i)
        a[i] = sa[i] - '0';
    for (int i = 0; i < (int)sb.size(); ++i)
        b[i] = sb[i] - '0';
    auto c = mul(a, b);
    int shift = 0;
    for (int i = 0; i < (int)c.size(); ++i) {
        int x = c[i] + shift;
        c[i] = x % 10;
```

```
        shift = x / 10;
    }
    while (shift > 0) {
        c.push_back(shift % 10);
        shift /= 10;
    }
    while (!c.empty() && c.back() == 0)
        c.pop_back();
    if (c.empty()) {
        cout << 0;
        return 0;
    }
    if (minus)
        cout << '-';
    for (int i = c.size() - 1; i >= 0; --i)
        cout << c[i];
}
```

6.4 Гаусс

```
// TODO битовый
// TODO дабловый
// TODO по модулю
```

6.5 Диофантовы уравнения

```
def bezout(a, b):
    x, xx, y, yy = 1, 0, 0, 1
    while b:
        q = a // b
        a, b = b, a % b
        x, xx = xx, x - xx*q
        y, yy = yy, y - yy*q
    return (a, x, y)

a, b, c = map(int, input().split())
d, k, l = bezout(a, b)
q = c // d
x, y = q*k, q*l
if c % d == 0:
    x -= x // (b//d) * (b//d)
    y = (c-a*x) // b
```

6.6 КТО

```
// TODO
```

6.7 Код Грея

```
// TODO
```

6.8 Линейное решето

```
// TODO
```

6.9 Ро-Поллард

```
// TODO
```

6.10 Символ Якоби, Лежандра

```
// TODO
```

7 Строки

7.1 Z-функция

```
int main() {
    vector<int> z(n, 0);
    z[0] = n;
    int l = 0, r = 0;
    for (int i = 1; i < n; i++) {
        if (i < r) {
            z[i] = min(z[i - l], r - i);
        }
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
        {
            z[i]++;
        }
        if (i + z[i] > r) {
            l = i;
            r = i + z[i];
        }
    }
}
```

7.2 Ахо-Корасик

```
int cntv = 1;

void add(string &s) {
    static int cnt_s = 1;
```

```

int v = 0;
for (char el : s) {
    if (go[v][el - 'a'] == 0) {
        go[v][el - 'a'] = cntv;
        par[cntv] = v;
        par_c[cntv] = el;
        cntv++;
    }
    v = go[v][el - 'a'];
}
term[v].push_back(cnt_s++);
}

void bfs() {
    deque<int> q = {0};
    while (!q.empty()) {
        int v = q.front();
        q.pop_front();
        if (v > 0) {
            if (par[v] == 0) {
                suf[v] = 0;
            } else {
                suf[v] = go[suf[par[v]]][par_c[v] - 'a'];
            }
            g[suf[v]].push_back(v);
        }
        for (int c = 0; c < 26; c++) {
            if (go[v][c] == 0) {
                go[v][c] = go[suf[v]][c];
            } else {
                q.push_back(go[v][c]);
            }
        }
    }
}

```

7.3 Префикс-функция

```

int main() {
    vector<int> pref(n, 0);
    int ans = 0;
    for (int i = 1; i < n; i++) {
        while (ans > 0 && s[ans] != s[i]) {
            ans = pref[ans - 1];
        }
        if (s[i] == s[ans]) {
            ans++;
        }
    }
}

```

```

        pref[i] = ans;
    }
}

```

7.4 Суффиксный автомат

```

struct Node {
    int go[26];
    int suf;
    int len;
};
Node verts[MAXN];
int cnt_v = 1;
int max_v = 0;

void add(char c) {
    c -= 'a';
    int nv = cnt_v++;
    verts[max_v].go[c] = nv;
    verts[nv].len = verts[max_v].len + 1;
    int v = max_v;
    while (v != 0) {
        if (verts[verts[v].suf].go[c] == 0) {
            v = verts[v].suf;
            verts[v].go[c] = nv;
            verts[nv].len = max(verts[nv].len, verts[v].len + 1);
            continue;
        }
        int vv = verts[v].suf, uu = verts[vv].go[c];
        if (verts[vv].len + 1 == verts[uu].len) {
            verts[nv].suf = uu;
            break;
        }
        int v2 = cnt_v++;
        for (int c2 = 0; c2 < 26; c2++) {
            verts[v2].go[c2] = verts[uu].go[c2];
        }
        int to = verts[vv].go[c];
        do {
            if (verts[vv].go[c] == to) {
                verts[vv].go[c] = v2;
                verts[v2].len = max(verts[v2].len,
verts[vv].len + 1);
            } else {
                break;
            }
            vv = verts[vv].suf;
        } while (vv != 0);
    }
}

```

```

        if (verts[vv].go[c] == to) {
            verts[vv].go[c] = v2;
            verts[v2].len = max(verts[v2].len, verts[vv].len + 1);
        }
        verts[v2].suf = verts[uu].suf;
        verts[uu].suf = verts[nv].suf = v2;
        break;
    }
    max_v = nv;
}

```

7.5 Суффиксный массив

```

vector<int> build_suff_arr(string s) {
    s.push_back('#');
    int n = s.size();
    vector<int> suf(n), c(n);
    vector<int> cnt(MAX);
    for (int i = 0; i < n; i++) {
        cnt[s[i] - '#']++;
    }
    vector<int> pos(MAX);
    for (int i = 1; i < MAX; i++) {
        pos[i] = pos[i - 1] + cnt[i - 1];
    }
    for (int i = 0; i < n; i++) {
        suf[pos[s[i] - '#']++] = i;
    }
    int cls = -1;
    for (int i = 0; i < n; i++) {
        if (i == 0 || s[suf[i]] != s[suf[i - 1]]) {
            cls++;
        }
        c[suf[i]] = cls;
    }
    for (int L = 1; L < n; L *= 2) {
        fill(cnt.begin(), cnt.end(), 0);
        for (int i = 0; i < n; i++) {
            cnt[c[i]]++;
        }
        pos[0] = 0;
        for (int i = 1; i < n; i++) {
            pos[i] = pos[i - 1] + cnt[i - 1];
        }
        for (int i = 0; i < n; i++) {
            suf[i] = (suf[i] - L + n) % n;
        }
    }
    vector<int> new_suf(n), new_c(n);
}

```

```

    for (int i = 0; i < n; i++) {
        int where = pos[c[suf[i]]];
        new_suf[where] = suf[i];
        pos[c[suf[i]]]++;
    }
    cls = -1;
    for (int i = 0; i < n; i++) {
        if (i == 0) {
            cls++;
            new_c[new_suf[i]] = cls;
            continue;
        }
        pair<int, int> prev = {c[new_suf[i - 1]], c[
(new_suf[i - 1] + L) % n]};
        pair<int, int> now = {c[new_suf[i]], c[(
new_suf[i] + L) % n]};
        if (prev != now) {
            cls++;
        }
        new_c[new_suf[i]] = cls;
    }
    swap(c, new_c);
    swap(suf, new_suf);
}
vector<int> res;
for (int i = 1; i < n; i++) {
    res.push_back(suf[i]);
}
return res;
}

vector<int> lcp_neighboring(string &s, vector<int> &suf
) {
    int n = s.size();
    vector<int> lcp(n), where(n);
    for (int i = 0; i < n; i++) {
        where[suf[i]] = i;
    }
    int k = 0;
    for (int j = 0; j < n; j++) {
        int pos = where[j];
        if (pos == n - 1) {
            k = 0;
            lcp[pos] = 0;
        } else {
            k = max(0LL, k - 1);
            while (s[j + k] == s[suf[pos + 1] + k]) {
                k++;
                if (j + k >= n || suf[pos + 1] + k >= n
) {

```

```

                break;
            }
        }
        lcp[pos] = k;
    }
    return lcp;
}

int sol(int k, string s) {
    int n = s.size();
    vector<int> suf = build_suff_arr(s);
    vector<int> lcp = lcp_neighboring(s, suf);
    vector<int> where(n);
    for (int i = 0; i < n; i++) {
        where[suf[i]] = i;
    }
    Sparse_Table st(lcp);
    int ans = 0;
    for (int i = 0; i < n - k; i++) {
        ans += st.rmql(where[i], where[i + k]);
    }
    return ans;
}

```

8 Структуры данных

8.1 Disjoint Sparse Table

// TODO

8.2 Segment Tree Beats

// min=, sum

```

struct ST {
    vector<int> st, mx, mx_cnt, sec_mx;

    ST(int n) {
        st.resize(n * 4, 0);
        mx.resize(n * 4, 0);
        mx_cnt.resize(n * 4, 0);
        sec_mx.resize(n * 4, 0);
        build(0, 0, n);
    }

    void upd_from_children(int v) {
        st[v] = st[v * 2 + 1] + st[v * 2 + 2];
    }
}

```

```

    mx[v] = max(mx[v * 2 + 1], mx[v * 2 + 2]);
    mx_cnt[v] = 0;
    sec_mx[v] = max(sec_mx[v * 2 + 1], sec_mx[v * 2
+ 2]);
    if (mx[v * 2 + 1] == mx[v]) {
        mx_cnt[v] += mx_cnt[v * 2 + 1];
    } else {
        sec_mx[v] = max(sec_mx[v], mx[v * 2 + 1]);
    }
    if (mx[v * 2 + 2] == mx[v]) {
        mx_cnt[v] += mx_cnt[v * 2 + 2];
    } else {
        sec_mx[v] = max(sec_mx[v], mx[v * 2 + 2]);
    }
}

void build(int i, int l, int r) {
    if (l + 1 == r) {
        st[i] = mx[i] = 0;
        mx_cnt[i] = 1;
        sec_mx[i] = -INF;
        return;
    }
    int m = (r + 1) / 2;
    build(i * 2 + 1, l, m);
    build(i * 2 + 2, m, r);
    upd_from_children(i);
}

void push_min_eq(int v, int val) {
    if (mx[v] > val) {
        st[v] -= (mx[v] - val) * mx_cnt[v];
        mx[v] = val;
    }
}

void push(int i) {
    push_min_eq(i * 2 + 1, mx[i]);
    push_min_eq(i * 2 + 2, mx[i]);
}

void update(int i, int l, int r, int ql, int qr,
int val) {
    if (mx[i] <= val) {
        return;
    }
    if (ql == l && qr == r && sec_mx[i] < val) {
        push_min_eq(i, val);
        return;
    }
}

```

```

    push(i);
    int m = (r + 1) / 2;
    if (qr <= m) {
        update(i * 2 + 1, l, m, ql, qr, val);
    } else if (ql >= m) {
        update(i * 2 + 2, m, r, ql, qr, val);
    } else {
        update(i * 2 + 1, l, m, ql, m, val);
        update(i * 2 + 2, m, r, m, qr, val);
    }
    upd_from_children(i);
}

int sum(int i, int l, int r, int ql, int qr) {
    if (l == ql && r == qr) {
        return st[i];
    }
    push(i);
    int m = (r + 1) / 2;
    if (qr <= m) {
        return sum(i * 2 + 1, l, m, ql, qr);
    }
    if (ql >= m) {
        return sum(i * 2 + 2, m, r, ql, qr);
    }
    return sum(i * 2 + 1, l, m, ql, m) + sum(i * 2
+ 2, m, r, m, qr);
}
};

```

8.3 ДД по неявному

```

pair<Node *, Node *> split(Node *t, int k) {
    if (!now)
        return {nullptr, nullptr};
    int szl = size(t->l);
    if (k <= szl) {
        auto [l, r] = split(t->l, k);
        t->l = r;
        pull(t);
        return {l, t};
    } else {
        auto [l, r] = split(t->r, k - szl - 1);
        t->r = l;
        pull(t);
        return {t, r};
    }
}

```

```

Node *merge(Node *l, Node *r) {
    if (!l)
        return r;
    if (!r)
        return l;
    if (l->y < r->y) {
        l->r = merge(l->r, r);
        pull(l);
        return l;
    } else {
        r->l = merge(l, r->l);
        pull(r);
        return r;
    }
}

void insert(Node *&root, int pos, int val) {
    Node *new_v = new Node(val);
    auto [l, r] = split(root, pos);
    root = merge(merge(l, new_v), r);
}

void erase(Node *&root, int pos) {
    auto [lm, r] = split(root, pos + 1);
    auto [l, m] = split(lm, pos);
    root = merge(l, r);
}

int sum(Node *v) {
    return v ? v->sm : 0;
}

```

```

// query [l, r]
int query(Node *&root, int ql, int qr) {
    auto [lm, r] = split(root, qr);
    auto [l, m] = split(lm, ql);
    int res = sum(m);
    root = merge(merge(l, m), r);
    return res;
}

```

8.4 ДД

```

pair<Node *, Node *> split(Node *t, int x) {
    if (!t)
        return {nullptr, nullptr};
    if (x <= t->x) {
        auto [l, r] = split(t->l, x);

```

```

        t->l = r;
        pull(t);
        return {l, t};
    } else {
        auto [l, r] = split(t->r, x);
        t->r = l;
        pull(t);
        return {t, r};
    }
}

```

```

Node *merge(Node *l, Node *r) {
    if (!l)
        return r;
    if (!r)
        return l;
    if (l->y < r->y) {
        l->r = merge(l->r, r);
        pull(l);
        return l;
    } else {
        r->l = merge(l, r->l);
        pull(r);
        return r;
    }
}

```

```

void insert(Node *&root, int val) {
    Node *new_v = new Node(val);
    auto [l, r] = split(root, val);
    root = merge(merge(l, new_v), r);
}

```

```

void erase(Node *&root, int val) {
    auto [lm, r] = split(root, val + 1);
    auto [l, m] = split(lm, val);
    root = merge(l, r);
}

```

```

int sum(Node *v) {
    return v ? v->sm : 0;
}

```

```

// query [l, r]
int query(Node *&root, int ql, int qr) {
    auto [lm, r] = split(root, qr);
    auto [l, m] = split(lm, ql);
    int res = sum(m);
    root = merge(merge(l, m), r);
    return res;
}

```

```

}

8.5 Персистентное ДД по неявному

mt19937 rnd(228);

struct Node;
int size(Node *);
int sum(Node *);

struct Node {
    Node *l, *r;
    int val, sz, sm;

    Node(int val) : val(val), sz(1), sm(val) {
        l = r = nullptr;
    }
    Node(int val, Node *l, Node *r) : val(val), l(l), r(r) {
        sz = 1 + size(l) + size(r);
        sm = val + sum(l) + sum(r);
    }
};

int size(Node *v) {
    return v ? v->sz : 0;
}

int sum(Node *v) {
    return v ? v->sm : 0;
}

pair<Node *, Node *> split(Node *t, int x) {
    if (!t)
        return {nullptr, nullptr};
    int lsz = size(t->l);
    if (lsz >= x) {
        auto [l, r] = split(t->l, x);
        auto v = new Node(t->val, r, t->r);
        return {l, v};
    } else {
        auto [l, r] = split(t->r, x - lsz - 1);
        auto v = new Node(t->val, t->l, l);
        return {v, r};
    }
}

bool chooseleft(int lsz, int rsz) {
    return rnd() % (lsz + rsz) < lsz;
}

```

```

}

Node *merge(Node *l, Node *r) {
    if (!l)
        return r;
    if (!r)
        return l;
    if (chooseleft(l->sz, r->sz)) {
        auto rr = merge(l->r, r);
        auto v = new Node(l->val, l->l, rr);
        return v;
    } else {
        auto ll = merge(l, r->l);
        auto v = new Node(r->val, ll, r->r);
        return v;
    }
}

Node *insert(Node *root, int pos, int val) {
    Node *new_v = new Node(val);
    auto [l, r] = split(root, pos);
    return merge(merge(l, new_v), r);
}

Node *erase(Node *root, int pos) {
    auto [lm, r] = split(root, pos + 1);
    auto [l, m] = split(lm, pos);
    return merge(l, r);
}

// query [l, r)
pair<int, Node *> query(Node *root, int ql, int qr) {
    auto [lm, r] = split(root, qr);
    auto [l, m] = split(lm, ql);
    int res = sum(m);
    auto new_root = merge(merge(l, m), r);
    return {res, new_root};
}

8.6 Персистентное ДО

// left: v ? v->l : nullptr (same for right)
// sum: v ? v->sm : 0

// v can be nullptr. returns new root of subtree
Node *update(Node *v, int l, int r, int qi, int qx) {
    if (qi < l || r <= qi)
        return v;
    if (l + 1 == r)

```

```

        return new Node(qx);
    int m = (l + r) / 2;
    Node *u = new Node();
    u->l = update(left(v), l, m, qi, qx);
    u->r = update(right(v), m, r, qi, qx);
    u->sm = sum(u->l) + sum(u->r);
    return u;
}

int get(Node *v, int l, int r, int ql, int qr) {
    if (!v || qr <= l || r <= ql)
        return 0;
    if (ql <= l && r <= qr)
        return v->sm;
    int m = (l + r) / 2;
    auto a = get(v->l, l, m, ql, qr);
    auto b = get(v->r, m, r, ql, qr);
    return a + b;
}

8.7 Спарсы

struct SparseTable {
    vector<vector<int>>> st;
    vector<int> max2;

    SparseTable(vector<int> &a) {
        int n = a.size();
        st.push_back(a);
        for (int i = 1; (1 << i) <= n; i++) {
            st.emplace_back(n - (1 << i) + 1);
            for (int p = 0; p < st[i].size(); p++) {
                st[i][p] = min(st[i - 1][p], st[i - 1][p + (1 << (i - 1))]);
            }
            st.push_back(st[i - 1]);
            for (int p = 0; p + (1 << (i - 1)) <= n; ++p) {
                st[i][p] = min(st[i - 1][p], st[i - 1][p + (1 << (i - 1))]);
            }
        }
        // max2[i] = i ? (32 - __builtin_clz(i - 1)) : 0
        max2.resize(n + 1);
        max2[0] = -1;
        max2[1] = 0;
        for (int i = 2; i <= n; i++)
            max2[i] = max2[i / 2] + 1;
    }
}

```



```

// min a[l..r)
int rmq(int l, int r) {
    int i = max2[r - l];
    return min(st[i][l], st[i][r - (1 << i)]);
}
};

```

8.8 Фенвик (pref += x)

```

// a[left..right] += delta; get_sum a[1..pos]
//
//void update(left, right, delta)
// T1.add(left, delta)
// T1.add(right + 1, -delta);
// T2.add(left, delta * (left - 1))
// T2.add(right + 1, -delta * right);
//
//int getSum(pos)
// return T1.sum(pos) * pos - T2.sum(pos)

```

8.9 Фенвик

```

// Нумерация с 0

```

```

struct FenwickTree {
    int n;
    vector<vector<vector<int>>> ft;

    FenwickTree(int n) : n(n) {
        ft.resize(n + 1, vector<vector<int>>>(n + 1, vector<
            int>(n + 1)));
    }
}

```

```

// a[x][y][z] += d
void upd(int x, int y, int z, int d) {
    x++, y++, z++;
    for (int x1 = x; x1 <= n; x1 += x1 & -x1) {
        for (int y1 = y; y1 <= n; y1 += y1 & -y1) {
            for (int z1 = z; z1 <= n; z1 += z1 & -z1) {
                ft[x1][y1][z1] += d;
            }
        }
    }
}
}

```

```

// sum a[0..x][0..y][0..z)
int rsq(int x, int y, int z) {
    int ans = 0;

```

```

for (int x1 = x; x1 > 0; x1 -= x1 & -x1) {
    for (int y1 = y; y1 > 0; y1 -= y1 & -y1) {
        for (int z1 = z; z1 > 0; z1 -= z1 & -z1) {
            ans += ft[x1][y1][z1];
        }
    }
}
return ans;
}
}

```

```

// sum a[x1..x2][y1..y2][z1..z2)
int sum_3d(int x1, int x2, int y1, int y2, int z1,
    int z2) {
    int ans = rsq(x2, y2, z2);
    ans -= rsq(x1, y2, z2) + rsq(x2, y1, z2) + rsq(x2,
        y2, z1);
    ans += rsq(x1, y1, z2) + rsq(x1, y2, z1) + rsq(x2,
        y1, z1);
    ans -= rsq(x1, y1, z1);
    return ans;
}
};

```