$Muffix \ Sassif-TRD$

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Геометрия

1.1 3D

```
double eps = 1e-7;
struct Pt {
  double x:
  double y;
  double z;
  Pt(double x_-, double y_-, double z_-) : x(x_-), y(y_-), z(
    z_{-}) {}
  Pt operator-(const Pt& other) const {
    return {x - other.x, y - other.y, z - other.z};
  }
  Pt operator+(const Pt& other) const {
    return {x + other.x, y + other.y, z + other.z};
  Pt operator/(const double& a) const {
    return {x / a, y / a, z / a};
  Pt operator*(const double& a) const {
    return {x * a, y * a, z * a};
  Pt cross(const Pt& p2) const {
    double nx = y * p2.z - z * p2.y;
    double ny = z * p2.x - x * p2.z;
    double nz = x * p2.y - y * p2.x;
    return {nx, ny, nz};
  bool operator==(const Pt% pt) const {
    return abs(x - pt.x) < eps && abs(y - pt.y) < eps &&
     abs(z - pt.z) < eps;
  double dist() {
    return sqrtl(x * x + y * y + z * z);
  }
};
struct Plane {
  double a, b, c, d;
```

```
Plane(double a_, double b_, double c_, double d_) : a( pair<Pt, Pt> intersect(Plane pl1, Plane pl2) {
    a_{-}), b(b_{-}), c(c_{-}), d(d_{-}) {
    double kek = sqrtl(a * a + b * b + c * c);
    if (kek < eps) return;</pre>
    a /= kek;
    b /= kek;
    c /= kek:
    d /= kek:
  double get_val(Pt p) {
    return a * p.x + b * p.y + c * p.z + d;
 bool on_plane(Pt p) {
    return abs(get_val(p)) / sqrtl(a * a + b * b + c * c
    ) < eps;
 }
 Pt proj(Pt p) {
    double t = (a * p.x + b * p.y + c * p.z + d) / (a *
    a + b * b + c * c;
   return p - Pt(a, b, c) * t;
 }
};
bool on_line(Pt p1, Pt p2, Pt p3) {
 return (p2 - p1).cross(p3 - p1) == Pt(0, 0, 0);
Plane get_plane(Pt p1, Pt p2, Pt p3) {
 Pt norm = (p2 - p1).cross(p3 - p1);
 Plane pl(norm.x, norm.y, norm.z, 0);
 pl.d = -pl.get_val(p1);
 return pl;
pair<pair<double, double>, pair<double, double>> get_xy(
    double a, double b, double c) {
 if (abs(a) > eps) {
    double y1 = 0, y2 = 10;
   return \{(-c - b * y1) / a, y1\}, \{(-c - b * y2) / a,
     y2}};
  double x1 = 0, x2 = 10;
 return {{x1, (-c - a * x1) / b}, {x2, (-c - a * x2) /
    b}};
```

```
if (abs(pl2.a) < eps && abs(pl2.b) < eps && abs(pl2.c)</pre>
   < eps) {
  assert(false);
if (abs(pl2.a) > eps) {
  double nd = pl1.d - pl1.a * pl2.d / pl2.a;
  double nc = pl1.c - pl1.a * pl2.c / pl2.a;
  double nb = pl1.b - pl1.a * pl2.b / pl2.a;
  if (abs(nc) < eps && abs(nb) < eps) {</pre>
   // плоскости параллельны (могут совпадать)
    return {Pt(0, 0, 0), Pt(0, 0, 0)};
  auto [yz1, yz2] = get_xy(nb, nc, nd);
  double x1 = (-p12.d - p12.c * yz1.second - p12.b *
  yz1.first) / pl2.a;
  double x2 = (-pl2.d - pl2.c * yz2.second - pl2.b *
  yz2.first) / pl2.a;
  return {Pt(x1, yz1.first, yz1.second), Pt(x2, yz2.
  first, yz2.second)};
Plane copy_pl1(pl1.c, pl1.a, pl1.b, pl1.d);
Plane copy_pl2(pl2.c, pl2.a, pl2.b, pl2.d);
auto [p1, p2] = intersect(copy_pl1, copy_pl2);
return {Pt(p1.y, p1.z, p1.x), Pt(p2.y, p2.z, p2.x)};
```

Вектор, прямая, окружность

```
//// Вектор ////
struct vctr {
 dbl x, y;
 vctr() {}
 vctr(dbl x, dbl y) : x(x), y(y) {}
 dbl operator%(const vctr &o) const { return x * o.x +
   y * o.y; }
 dbl operator*(const vctr &o) const { return x * o.y -
    y * o.x; }
 vctr operator+(const vctr &o) const { return {x + o.x,
    v + o.v; }
 vctr operator-(const vctr &o) const { return {x - o.x,
    y - o.y; }
 vctr operator-() const { return {-x, -y}; }
 vctr operator*(const dbl d) const { return {x * d, y *
    d}; }
```

```
vctr operator/(const dbl d) const { return {x / d, y /
     d}; }
  void operator+=(const vctr &o) { x += o.x, y += o.y; }
  void operator==(const vctr &o) { x -= o.x, y -= o.y; }
  dbl dist2() const { return x * x + y * y; }
  dbl dist() const { return sqrtl(dist2()); }
  vctr norm() const { return *this / dist(); }
};
dbl angle_between(const vctr &a, const vctr &b) {
  return atan2(b * a, b % a);
// y > 0 ? 0 : 1
bool is2plane(const vctr &a) {
  return sign(a.y) < 0 \mid \mid (sign(a.y) == 0 \&\& sign(a.x) <
}
bool cmp_angle(const vctr &a, const vctr &b) {
  bool pla = is2plane(a);
  bool plb = is2plane(b);
  if (pla != plb)
    return pla < plb;</pre>
  return sign(a * b) > 0;
/// Прямая ////
struct line {
  dbl a, b, c;
  line() {}
  line(dbl a, dbl b, dbl c) : a(a), b(b), c(c) {}
  line(const vctr A, const vctr B) {
    a = A.v - B.v;
    b = B.x - A.x;
    c = A * B;
    assert(a != 0 || b != 0);
  void operator*=(dbl x) { a *= x, b *= x, c *= x; }
  void operator/=(dbl x) { a /= x, b /= x, c /= x; }
  dbl get(const vctr P) const { return a * P.x + b * P.y
     + c: }
  vctr anyPoint() const {
    dbl x = -a * c / (a * a + b * b);
    dbl y = -b * c / (a * a + b * b);
    return vctr(x, y);
```

```
}
  void normalize() {
    dbl d = sqrtl(a * a + b * b);
    a /= d;
    b /= d;
    c /= d;
 }
};
bool isparallel(line 11, line 12) {
 return vctr(l1.a, l1.b) * vctr(l2.a, l2.b) == 0;
vctr intersection(const line &11, const line &12) {
 dbl x = (11.c * 12.b - 12.c * 11.b) / (12.a * 11.b -
    12.b * 11.a):
  dbl v = -(11.c * 12.a - 12.c * 11.a) / (12.a * 11.b -
    12.b * 11.a);
 return vctr(x, v):
// Серединный перпендикуляр (не биссектриса!)
line bisection(const vctr A, const vctr B) {
 vctr M = (A + B) / 2;
 vctr AB = B - A;
 vctr norm = vctr(AB.y, -AB.x);
 return line(M, M + norm);
//// Окружность ////
struct circle {
  dbl x, y, r;
  circle() {}
  circle(dbl x, dbl y, dbl r) : x(x), y(y), r(r) {}
  circle(vctr P, dbl r) : x(P.x), y(P.y), r(r) {}
  circle(const vctr A, const vctr B) {
    vctr C = (A + B) / 2;
    x = C.x, y = C.y;
    r = (A - B).dist() / 2;
  circle(const vctr A, const vctr B, const vctr C) {
    line 11 = bisection(A, B);
    line 12 = bisection(B, C);
    vctr P = intersection(11, 12);
    x = P.x, y = P.y;
    r = (P - A).dist();
 }
```

```
bool isin(const vctr P) const {
   return (vctr(x, y) - P).dist2() <= r * r;
}
  vctr cent() const { return vctr(x, y); }
};</pre>
```

1.3 Выпуклая оболочка

```
vctr minvctr(INF, INF);
bool cmp_convex_hull(const vctr &a, const vctr &b) {
 vctr A = a - minvctr;
 vctr B = b - minvctr;
  auto sign_prod = sign(A * B);
  if (sign_prod != 0)
   return sign_prod > 0;
 return A.dist2() < B.dist2();</pre>
// minvctr updates here
vector<vctr> get_convex_hull(vector<vctr> arr) {
 minvctr = rotate_min_vctr(arr);
  vector<vctr> hull:
  sort(arr.begin(), arr.end(), cmp_convex_hull);
 for (vctr &el : arr) {
   while (hull.size() > 1 && sign((hull.back() - hull[
    hull.size() - 2]) * (el - hull.back())) <= 0)
     hull.pop_back();
   hull.push_back(el);
 return hull;
```

1.4 Задача 16

```
bool isInSameHalf(vctr p, vctr r1, vctr r2) {
   return sign((r2 - r1) % (p - r1)) >= 0;
}

dbl distPointPoint(vctr a, vctr b) {
   return (a - b).dist();
}

dbl distPointLine(vctr a, vctr l1, vctr l2) {
   line l(l1, l2);
   l.normalize();
```

```
return abs(l.get(a));
dbl distPointRay(vctr a, vctr r1, vctr r2) {
  if (!isInSameHalf(a, r1, r2))
    return distPointPoint(a, r1);
  return distPointLine(a, r1, r2);
dbl distPointSeg(vctr a, vctr s1, vctr s2) {
  return max(distPointRay(a, s1, s2),
             distPointRay(a, s2, s1));
bool isIntersectionLineLine(line 11, line 12) {
  dbl znam = 11.b * 12.a - 11.a * 12.b;
  return sign(znam) != 0;
vctr intersectionLineLine(line 11, line 12) {
  dbl znam = 11.b * 12.a - 11.a * 12.b;
  dbl y = -(11.c * 12.a - 12.c * 11.a) / znam;
  dbl x = -(11.c * 12.b - 12.c * 11.b) / -znam;
  return vctr(x, y);
}
vctr getPointOnLine(line 1) {
  if (sign(1.b) != 0)
    return vctr(0, -1.c / 1.b);
  return vctr(-1.c / 1.a, 0);
}
dbl distLineLine(vctr 11a, vctr 11b, vctr 12a, vctr 12b)
  line 11(11a, 11b);
  line 12(12a, 12b);
  if (isIntersectionLineLine(11, 12))
    return 0;
  vctr p = getPointOnLine(l1);
  12.normalize():
  return abs(12.get(p));
dbl distRayLine(vctr r1, vctr r2, vctr l1, vctr l2) {
  line r(r1, r2);
  line 1(11, 12);
  if (!isIntersectionLineLine(1, r))
    return distLineLine(r1, r2, l1, l2);
  vctr p = intersectionLineLine(1, r);
```

```
if (isInSameHalf(p, r1, r2))
   return 0;
 return distPointLine(r1, l1, l2);
dbl distSegLine(vctr s1, vctr s2, vctr l1, vctr l2) {
 return max(distRayLine(s1, s2, l1, l2),
             distRayLine(s2, s1, l1, l2));
dbl distRayRay(vctr r1a, vctr r1b, vctr r2a, vctr r2b) {
 line r1(r1a, r1b);
 line r2(r2a, r2b);
 if (!isIntersectionLineLine(r1, r2)) {
    if (isInSameHalf(r1a, r2a, r2b) || isInSameHalf(r2a,
     r1a, r1b))
     return distLineLine(r1a, r1b, r2a, r2b);
    else
      return distPointPoint(r1a, r2a);
 }
 vctr p = intersectionLineLine(r1, r2);
 if (isInSameHalf(p, r1a, r1b) && isInSameHalf(p, r2a,
    r2b))
   return 0:
 return min(distPointRay(r1a, r2a, r2b),
             distPointRay(r2a, r1a, r1b));
dbl distSegRay(vctr s1, vctr s2, vctr r1, vctr r2) {
 return max(distRayRay(s1, s2, r1, r2),
             distRayRay(s2, s1, r1, r2));
dbl distSegSeg(vctr s1a, vctr s1b, vctr s2a, vctr s2b) {
 return max(distSegRay(s1a, s1b, s2a, s2b),
             distSegRay(s1a, s1b, s2b, s2a));
```

1.5 Касательные из точки

```
int i2 = (i + (1 << k)) % n;
if (sign((p[i1] - a) * (p[i] - a)) == val)
    i = i1;
if (sign((p[i2] - a) * (p[i] - a)) == val)
    i = i2;
}
return i;
};
return {findWithSign(1), findWithSign(-1)};
}</pre>
```

1.6 Касательные параллельные прямой

```
// find point with max signed distance to line
int tangent_parallel_line(const vector<vctr> &p, line l)
        {
    int n = p.size();
    int i = 0;
    int logn = 31 - __builtin_clz(n);
    for (int k = logn; k >= 0; --k) {
        int i1 = (i - (1 << k) + n) % n;
        int i2 = (i + (1 << k)) % n;
        if (l.get(p[i1]) > l.get(p[i]))
              i = i1;
        if (l.get(p[i2]) > l.get(p[i]))
              i = i2;
    }
    return i;
}
```

1.7 Лежит ли точка в многоугольнике

```
// P starts with minvctr
bool is_point_in_poly(vctr A, vector<vctr> &P) {
    int n = P.size();
    if (sign(A * P[1]) > 0)
        return false;
    int ind = lower_bound(P.begin(), P.end(), A,
        cmp_convex_hull) - P.begin();
    if (ind == n || ind == 0)
        return false;
    if (ind == 0)
        ind++;
    vctr B = A - P[ind - 1];
    vctr C = P[ind] - P[ind - 1];
    return sign(C * B) >= 0;
}
```

1.8 Минимальная окружность

покрывающая

```
mt19937 rnd(179);
circle MinDisk2(vector<vctr> &p, vctr A, vctr B, int sz)
 circle w(A, B);
 for (int i = 0; i < sz; ++i) {</pre>
   if (w.isin(p[i]))
      continue:
   w = circle(A, B, p[i]);
 return w;
circle MinDisk1(vector<vctr> &p, vctr A, int sz) {
  shuffle(p.begin(), p.begin() + sz, rnd);
 circle w(A, p[0]);
 for (int i = 1; i < sz; ++i) {</pre>
   if (w.isin(p[i]))
      continue;
   w = MinDisk2(p, A, p[i], i);
 return w;
circle MinDisk(vector<vctr> &p) {
 int sz = p.size();
 if (sz == 1)
   return circle(p[0], 0);
 shuffle(p.begin(), p.end(), rnd);
 circle w(p[0], p[1]);
 for (int i = 2; i < sz; ++i) {</pre>
   if (w.isin(p[i]))
      continue:
   w = MinDisk1(p, p[i], i);
 }
 return w;
```

1.9 Многоугольники

```
// Сдвиг многоугольника, чтобы начинался с минимального вектора
vctr rotate_min_vctr(vector<vctr> &pts) {
  int ind = 0;
  for (int i = 1; i < pts.size(); ++i) {
```

```
if (is2plane(pts[i] - pts[ind]))
    ind = i;
}
rotate(pts.begin(), pts.begin() + ind, pts.end());
return pts[0];
}

// Список вершин -> список рёбер
vector<vctr> poly_to_edges(const vector<vctr> &A) {
    vector<vctr> edg(A.size());
    for (int i = 0; i < A.size(); ++i)
        edg[i] = A[(i + 1) % A.size()] - A[i];
    return edg;
}</pre>
```

1.10 Пересечение полуплоскостей

```
// half plane: ax+by+c > 0
// bounding box MUST have
vector<int> intersection_half_planes_inds(const vector<</pre>
   line> &ls) {
 int n = (int)ls.size();
 vector<int> lsi(n):
 iota(lsi.begin(), lsi.end(), 0);
 sort(lsi.begin(), lsi.end(), [&](int i, int j) {
   vctr aa(ls[i].a, ls[i].b);
   vctr bb(ls[i].a, ls[i].b);
   bool pla = is2plane(aa);
   bool plb = is2plane(bb);
   if (pla != plb)
     return pla < plb;</pre>
   return aa * bb > 0;
 });
 vector<line> st;
 vector<int> inds:
 for (int ii = 0; ii < 2 * n; ++ii) {</pre>
   int i = lsi[ii % n];
   if (st.empty()) {
      st.push_back(ls[i]);
      inds.push_back(i);
      continue;
   vctr p = intersection(ls[i], st.back());
   bool pp = isparallel(ls[i], st.back());
   bool bad = false;
   while (st.size() >= 2) {
     if (!pp && sign(st[st.size() - 2].get(p)) >= 0)
```

```
break:
      else if (pp && sign(st.back().get(ls[i].anyPoint()
   )) <= 0) {
       bad = true;
        break;
      st.pop_back();
     inds.pop_back();
     p = intersection(ls[i], st.back());
     pp = isparallel(ls[i], st.back());
   if (!bad) {
      st.push_back(ls[i]);
     inds.push_back(i);
 }
 vector<int> cnt(n, 0):
 for (int i : inds)
   cnt[i]++:
 vector<int> good;
 for (int i : inds) {
   if (cnt[i]-- == 2)
      good.push_back(i);
 return good;
vector<vctr> intersection_half_planes(vector<line> &ls)
 vector<int> inter = intersection_half_planes_inds(ls);
 int n = inter.size();
 vector<vctr> pts;
 for (int i = 0; i < n; ++i) {</pre>
   int j = (i + 1) \% n;
   vctr P = intersection(ls[inter[i]], ls[inter[j]]);
   if (pts.empty() || sign(pts.back().x - P.x) != 0
         || sign(pts.back().y - P.y) != 0)
     pts.push_back(P);
 return pts;
```

1.11 Пересечение с окружностью

```
bool is_intersection_line_circ(line 1, circle c) {
   l.normalize();
   dbl d = abs(l.get(c.cent()));
   return d < c.r - EPS;</pre>
```

```
}
vector<vctr> intersection_line_circ(line 1, circle c) {
  1.normalize();
  dbl d = abs(l.get(c.cent()));
  vctr per = vctr(l.a, l.b).norm() * d;
  vctr a = c.cent() + per;
  if (sign(abs(l.get(a)) - d) > 0)
    a = c.cent() - per;
  if (sign(c.r - d) == 0)
    return {a}:
  dbl k = sqrtl(c.r * c.r - d * d);
  vctr par = vctr(-1.b, 1.a).norm() * k;
  return {a + par, a - par};
vector<vctr> intersection circ circ(circle a, circle b)
  line 1(2 * (b.x - a.x).
         2 * (b.y - a.y),
         b.r * b.r - a.r * a.r
             + (a.x * a.x + a.y * a.y)
             - (b.x * b.x + b.y * b.y);
  if (sign(1.a) == 0 && sign(1.b) == 0)
    return {};
  return intersection_line_circ(1, a);
vector<vctr> tangent_vctr_circ(vctr v, circle c) {
  dbl d = (c.cent() - v).dist();
  dbl k = sqrtl(d * d - c.r * c.r);
  circle c2(v.x, v.y, k);
  return intersection_circ_circ(c, c2);
```

1.12 Проверка на пересечение отрезков

```
bool is_intersection_seg(vctr A, vctr B, vctr C, vctr D)
    {
    for (int i = 0; i < 2; ++i) {
        auto l1 = A.x, r1 = B.x, l2 = C.x, r2 = D.x;
        if (l1 > r1) swap(l1, r1);
        if (l2 > r2) swap(l2, r2);
        if (max(l1, l2) > min(r1, r2))
            return false;
        swap(A.x, A.y);
        swap(B.x, B.y);
        swap(C.x, C.y);
```

```
swap(D.x, D.y);
}
for (int _ = 0; _ < 2; ++_) {
  auto v1 = (B - A) * (C - A);
  auto v2 = (B - A) * (D - A);
  if (sign(v1) * sign(v2) == 1)
    return false;
  swap(A, C);
  swap(B, D);
}
return true;</pre>
```

1.13 Сумма Минковского

```
vector<vctr> minkowski_sum(const vector<vctr> &A, const
    vector<vctr> &B) {
    auto edgA = poly_to_edges(A);
    auto edgB = poly_to_edges(B);
    vector<vctr> edgC(A.size() + B.size());
    merge(edgA.begin(), edgA.end(), edgB.begin(), edgB.end
        (), edgC.begin(), cmp_angle);
    vector<vctr> C(edgC.size());
    C[0] = A[0] + B[0];
    for (int i = 0; i + 1 < C.size(); ++i)
        C[i + 1] = C[i] + edgC[i];
    return C;
}</pre>
```

1.14 Формула Эйлера

- \bullet V число вершин выпуклого многогранника (планарного графа)
- Е число рёбер
- F число граней (если планарный граф, то включая внешнюю)

```
Тогда V - E + F = 2
```

2 Графы

2.1 2-SAT

```
for (int i = 1; i <= n; ++i) {</pre>
 not_v[i] = i + n;
 not_v[i + n] = i;
for (int i = 0; i < m; ++i) {</pre>
  cin >> u >> v:
  g[not_v[v]].push_back(u);
  g[not_v[u]].push_back(v);
 rg[u].push_back(not_v[v]);
 rg[v].push_back(not_v[u]);
// делаем КСС, получаем сотр
for (int v = 1; v \le n; ++v) {
  if (comp[v] == comp[not_v[v]]) {
    cout << "UNSATISFIABLE\n";</pre>
    return 0;
 }
for (int v = 1; v <= n; ++v)</pre>
  cout << (comp[v] > comp[not_v[v]] ? v : not_v[v]);
```

2.2 Венгерский алгоритм

```
pair<int, vector<int>> venger(vector<vector<int>> a) {
// ищет минимальное по стоимости
// работает только при n <= m
// a - массив весов (n+1)\times(m+1)
// a[0][...] = a[...][0] = 0
// возвращает ans[i] = j если взяли ребро a[i][j]
  int n = (int) a.size() - 1;
  int m = (int) a[0].size() - 1;
  vector < int > u(n + 1), v(m + 1), p(m + 1), way(m + 1);
  for (int i = 1; i <= n; ++i) {</pre>
    p[0] = i;
    int i0 = 0;
    vector<int> minv(m + 1, INF);
    vector<char> used(m + 1, false);
    do {
      used[j0] = true;
      int i0 = p[j0], delta = INF, j1;
      for (int j = 1; j <= m; ++j)
        if (!used[j]) {
          int cur = a[i0][j] - u[i0] - v[j];
          if (cur < minv[j])</pre>
            minv[j] = cur, way[j] = j0;
          if (minv[j] < delta)</pre>
            delta = minv[j], j1 = j;
```

```
for (int j = 0; j <= m; ++j)</pre>
      if (used[i])
        u[p[j]] += delta, v[j] -= delta;
        minv[j] -= delta;
    j0 = j1;
 } while (p[j0] != 0);
  do {
    int j1 = way[j0];
    p[j0] = p[j1];
    j0 = j1;
 } while (j0);
int cost = -v[0];
vector<int> ans(n + 1);
for (int j = 1; j <= m; ++j)</pre>
  ans[p[j]] = j;
return {cost, ans};
```

2.3 Вершинная двусвязность

```
struct edge {
  int u, ind;
  bool operator<(const edge &other) const {</pre>
    return u < other.u;</pre>
  }
}:
vector<int> stack_;
void paint(int v, int pr = -1) {
  used[v] = pr;
  up[v] = tin[v] = ++timer;
  for (auto e: g[v]) {
    if (e.u == pr) {
      continue;
    }
    if (!used[e.u]) {
      stack_.push_back(e.ind);
      paint(e.u, v);
      if (up[e.u] >= tin[v]) {
        ++mx_col;
        while (true) {
          int cur_edge = stack_.back();
          col[cur_edge] = mx_col;
          stack_.pop_back();
```

```
if (cur_edge == e.ind) {
            break;
          }
        }
      up[v] = min(up[v], up[e.u]);
   } else if (tin[e.u] < tin[v]) {</pre>
      stack_.push_back(e.ind);
      up[v] = min(up[v], tin[e.u]);
   } else if (up[v] > tin[e.u]) {
      up[v] = up[e.u];
   }
 }
signed main() {
 int n, m;
 cin >> n >> m;
 for (int i = 0; i < m; ++i) {</pre>
   int u, v;
   cin >> u >> v;
   g[u].push_back({v, i});
    g[v].push_back({u, i});
 for (int v = 1; v <= n; ++v) {</pre>
    sort(all(g[v]));
 for (int v = 1; v <= n; ++v) {</pre>
   if (!used[v]) {
      paint(v);
 for (int v = 1; v <= n; ++v) {</pre>
   int len = g[v].size();
   for (int i = 1; i < len; ++i) {</pre>
     if (col[g[v][i].ind] == 0) {
        col[g[v][i].ind] = col[g[v][i-1].ind];
     }
   }
 }
```

2.4 Дейкстра за квадрат

```
// 0-based
pair<vector<int>, vector<int>> dijkstra(int start, int n
) {
  vector<int> dist(n, INF);
```

```
vector<int> pred(n, -1);
vector<int> used(n);
dist[start] = 0;
for (int _ = 0; _ < n; ++_) {</pre>
  int v = -1;
  for (int i = 0; i < n; ++i) {</pre>
    if (!used[i])
      if (v == -1 || dist[v] > dist[i])
        v = i;
  if (v == -1) break;
  for (auto [u, w] : g[v]) {
    if (dist[u] > w + dist[v]) {
      dist[u] = w + dist[v];
      pred[u] = v;
    }
  }
  used[v] = 1;
return {dist, pred};
```

2.5 Диниц

```
struct edge {
 int v, f, c, ind;
};
vector<edge> g[MAXN];
pair<int, int> pred[MAXN];
int d[MAXN];
int inds[MAXN];
bool dfs(int v, int final, int W) {
  if (v == final) {
    return true;
 }
  for (int i = inds[v]; i < (int) g[v].size(); i++) {</pre>
    auto e = g[v][i];
    if (e.f + W \le e.c \&\& d[v] + 1 == d[e.v]) {
      pred[e.v] = {v, i};
      bool flag = dfs(e.v, final, W);
      if (flag) {
        return true;
      inds[v]++;
    } else {
      inds[v]++;
```

8

```
}
  }
  return false;
}
bool bfs(int start, int final, int W) {
  fill(d, d + MAXN, INF);
  d[start] = 0;
  deque<int> q = {start};
  while (!q.empty()) {
    int v = q.front();
    q.pop_front();
    for (auto e : g[v]) {
      if (e.f + W \le e.c \&\& d[e.v] > d[v] + 1) {
        d[e.v] = d[v] + 1;
        q.push_back(e.v);
      }
    }
  if (d[final] == INF) {
    return false;
  fill(inds, inds + MAXN, 0);
  while (dfs(start, final, W)) {
    int v = final;
    int x = INF;
    while (v != start) {
      int ind = pred[v].second;
      v = pred[v].first;
      x = min(x, g[v][ind].c - g[v][ind].f);
    }
    v = final:
    while (v != start) {
      int ind = pred[v].second;
      v = pred[v].first;
      g[v][ind].f += x;
      g[g[v][ind].v][g[v][ind].ind].f == x;
    }
  }
  return true;
void Dinic(int start, int final) {
  int W = (1LL << 30);
  do {
    while (bfs(start, final, W));
    W /= 2;
  } while (W >= 1);
```

```
signed main() {
 int n, m;
 vector<pair<int, int>> edges;
 for (int i = 0; i < m; i++) {</pre>
   int u, v, c;
   cin >> u >> v >> c;
   edges.emplace_back(u, v);
   g[u].push_back({v, 0, c, (int) g[v].size()});
   // если ребро - ориентированно,
   // то обратная сарасіту = 0
   g[v].push_back({u, 0, c, (int) g[u].size() - 1});
 int start = 1, target = n;
 Dinic(start, target);
 int res = 0;
 for (auto e : g[start]) {
   res += e.f;
 vector<int> cut;
 for (int i = 0; i < m; i++) {</pre>
   int u = edges[i].first, v = edges[i].second;
   if ((d[u] != INF && d[v] == INF) ||
        (d[u] == INF && d[v] != INF)) {
      cut.push_back(i + 1);
   }
 }
```

2.6 KCC

```
void dfs1(int v, vector<int> &topsort) {
    used[v] = 1;
    for (auto u : g[v]) {
        if (!used[u]) {
            dfs1(u, topsort);
        }
    }
    topsort.push_back(v);
}

void dfs2(int v, int col) {
    comp[v] = col;
    for (auto u : rg[v]) {
        if (!comp[u]) {
            dfs2(u, col);
        }
    }
}
```

```
signed main() {
  vector<int> topsort;
  for (int v = 1; v <= n; ++v)
    if (!used[v])
      dfs1(v, topsort);
  reverse(all(topsort));
  for (int j = 1; j <= n; ++j)
    if (!comp[topsort[j - 1]])
      dfs2(topsort[j - 1], j);
}</pre>
```

2.7 Минкост (Джонсон)

```
using cost_t = 11;
using flow_t = int;
const int MAXN = 10000;
const int MAXM = 25000 * 2;
const cost_t INFw = 1e12;
const flow_t INFf = 10;
struct Edge {
 int v, u;
 flow_t f, c;
  cost_t w;
};
Edge edg[MAXM];
int esz = 0;
vector<int> graph[MAXN];
11 dist[MAXN];
11 pot[MAXN];
int S, T;
int NUMV;
int pre[MAXN];
bitset<MAXN> inQ;
flow_t get_flow() {
 int v = T:
  if (pre[v] == -1)
   return 0;
  flow_t f = INFf;
  do {
    int ei = pre[v];
    Edge &e = edg[ei];
```

```
f = min(f, e.c - e.f);
   if (f == 0)
     return 0;
   v = e.v;
 } while (v != S);
 v = T:
 do {
   int ei = pre[v];
   edg[ei].f += f;
   edg[ei ^ 1].f -= f;
   v = edg[ei].v;
 } while (v != S);
 return f;
void spfa() {
 fill(dist, dist + NUMV, INFw);
 dist[S] = 0;
 deque<int> Q = {S};
 inQ[S] = true;
 while (!Q.empty()) {
   int v = Q.front();
   Q.pop_front();
   inQ[v] = false;
   cost_t d = dist[v];
   for (int ei : graph[v]) {
      Edge &e = edg[ei];
      if (e.f == e.c)
        continue:
      cost_t w = e.w + pot[v] - pot[e.u];
      if (dist[e.u] <= d + w)</pre>
        continue:
      pre[e.u] = ei;
      dist[e.u] = d + w;
      if (!inO[e.u]) {
        inQ[e.u] = true;
        Q.push_back(e.u);
     }
   }
 for (int i = 0; i < NUMV; ++i)</pre>
    pot[i] += dist[i];
cost_t mincost() {
 spfa(); // pot[i] = 0 // or ford_bellman
 flow_t f = 0;
 while (true) {
   flow_t ff = get_flow();
```

```
if (ff == 0)
      break:
   f += ff:
    spfa(); // or dijkstra
 cost_t res = 0;
 for (int i = 0; i < esz; ++i)</pre>
   res += edg[i].f * edg[i].w;
 res /= 2:
 return res;
void add_edge(int v, int u, int c, int w) {
 edg[esz] = \{v, u, 0, c, w\};
 edg[esz + 1] = \{u, v, 0, 0, -w\};
 graph[v].push_back(esz);
 graph[u].push_back(esz + 1);
 esz += 2;
signed main() {
 ios_base::sync_with_stdio(false);
 cin.tie(nullptr);
 int n, m;
 cin >> n >> m;
 S = 0;
 T = n - 1;
 NUMV = n:
 for (int i = 0; i < m; ++i) {</pre>
   int v, u, c, w;
    cin >> v >> u >> c >> w;
   v--, u--;
    add_edge(v, u, c, w);
 }
 cost_t ans = mincost();
 cout << ans;</pre>
```

2.8 Мосты

```
void dfs(int v, int par) {
  vis[v] = 1;
  up[v] = tin[v] = timer++;
  for (auto u : g[v]) {
    if (!vis[u]) {
      dfs(u, v);
      up[v] = min(up[v], up[u]);
    } else if (u != par) {
```

```
up[v] = min(up[v], tin[u]);
}
if (up[u] > tin[v]) {
    bridges.emplace_back(v, u);
}
}
```

2.9 Паросочетания

```
int dfs(int v, int c) {
 if (used[v] == c) return 0:
 used[v] = c;
 for (auto u : g[v]) {
   if (res[u] == -1) {
     res[u] = v;
     return 1;
 }
 for (auto u : g[v]) {
   if (dfs(res[u], c)) {
     res[u] = v;
     return 1;
   }
 }
 return 0;
signed main() {
 // n - в левой доле, m - в правой
 fill(res, res + m, -1);
 for (int i = 0; i < n; ++i) {</pre>
    ans += dfs(i, i + 1):
 }
```

2.10 Точки сочленения

```
void dfs(int v, int par) {
  vis[v] = 1;
  up[v] = tin[v] = timer++;
  int child = 0;
  for (auto u : g[v]) {
    if (!vis[u]) {
      dfs(u, v);
      up[v] = min(up[v], up[u]);
    if (up[u] >= tin[v] && par != -1) {
```

```
points.insert(v);
}
    child++;
} else if (u != par) {
    up[v] = min(up[v], tin[u]);
}
if (par == -1 && child >= 2) {
    points.insert(v);
}
```

2.11 Эдмондс-Карп

```
struct edge {
 int v, f, c, ind;
vector<edge> g[MAXN];
bool bfs(int start, int final, int W) {
 vector<int> d(MAXN, INF);
 vector<pair<int, int>> pred(MAXN);
 d[start] = 0;
 deque<int> q = {start};
 while (!q.empty()) {
   int v = q.front();
   q.pop_front();
   for (int i = 0; i < (int) g[v].size(); i++) {</pre>
      auto e = g[v][i];
      if (e.f + W \le e.c \&\& d[e.v] > d[v] + 1) {
        d[e.v] = d[v] + 1;
        pred[e.v] = {v, i};
        q.push_back(e.v);
   }
 if (d[final] == INF) {
   return false;
 int v = final:
 int x = INF;
 while (v != start) {
   int ind = pred[v].second;
   v = pred[v].first;
   x = min(x, g[v][ind].c - g[v][ind].f);
 v = final;
```

```
while (v != start) {
   int ind = pred[v].second;
   v = pred[v].first;
   g[v][ind].f += x;
   g[g[v][ind].v][g[v][ind].ind].f == x;
 return true;
signed main() {
 int n, m;
 for (int i = 0; i < m; i++) {</pre>
   int u, v, c;
   cin >> u >> v >> c;
   g[u].push_back({v, 0, c, (int) g[v].size()});
   g[v].push_back({u, 0, 0, (int) g[u].size() - 1});
 }
 int start = 1, final = n;
 int W = (1 << 30):
 do {
   while (bfs(start, final, W));
   W /= 2:
 } while (W >= 1);
 int res = 0:
 for (auto e : g[start]) {
   res += e.f;
 }
```

2.12 Эйлеров цикл

```
// unconnected graph, deleting edges, set<int> g[N];
for (int v = 0; v < n; v++) {
 if (!g[v].empty()) {
   vector<int> ccl;
   vector<int> s = {v};
    while (!s.empty()) {
     int u = s.back();
     if (g[u].empty()) {
       ccl.pb(u);
       s.pop_back();
     } else {
       int u2 = *g[u].begin();
       g[u].erase(u2);
       g[u2].erase(u);
        s.pb(u2);
   }
```

3 ДП

```
CHT
3.1
struct Line {
 ld k, b;
};
pair<ld, ld> inter(Line a, Line b) {
 1d x = (b.b - a.b) / (a.k - b.k);
 ld v = a.k * x + a.b;
 return {x, y};
void add_line(ld k, ld b, vector<Line> &s, vector<pair</pre>
    ld, ld>> &pts) {
  while (s.size() >= 2) {
    pair<ld, ld> x1 = inter(s.back(), s[s.size() - 2]);
    pair<1d, 1d > x2 = inter(s[s.size() - 2], \{k, b\});
    if (x1 > x2) {
      break;
    pts.pop_back();
    s.pop_back();
  if (!s.empty()) {
    pts.push_back(inter(s.back(), {k, b}));
  s.push_back({k, b});
ld bin_search(vector<Line> &s, ld x) {
 int 1 = 0, r = s.size();
  while (1 + 1 < r) {
    int m = (r + 1) / 2;
    auto kek = inter(s[m - 1], s[m]);
    if (kek.first >= x) {
     1 = m:
   } else {
      r = m;
```

```
return s[1].k * x + s[1].b;
}
```

3.2 Li Chao

```
// MAXIMUM
struct Line {
  int k. b:
  int f(int x) {
    return k * x + b;
  }
};
struct ST {
  vector<Line> st;
  ST(int n) {
    Line ln = {OLL, -INF};
    st.resize(4 * n, ln);
  }
  void upd(int i, int l, int r, Line ln) {
    int child = 1;
    Line ln1 = ln;
    int m = (1 + r) / 2:
    if (ln.f(m) > st[i].f(m)) {
      if (ln.k < st[i].k) {</pre>
        child = 2:
      ln1 = st[i];
      st[i] = ln;
    } else {
      if (st[i].k < ln.k) {</pre>
        child = 2;
      }
    }
    if (1 + 1 < r) {
      if (child == 1) {
        upd(i * 2 + 1, 1, m, ln1);
      } else {
        upd(i * 2 + 2, m, r, ln1);
    }
  }
  int res(int i, int l, int r, int x) {
    if (1 + 1 == r) {
```

```
return st[i].f(x);
}
int m = (1 + r) / 2;
int val = st[i].f(x);
if (x < m) {
   val = max(val, res(i * 2 + 1, 1, m, x));
} else {
   val = max(val, res(i * 2 + 2, m, r, x));
}
return val;
};</pre>
```

3.3 SOS-dp

```
// dp initial fill, a[] is given array, mb extra zeros
for (int i = 0; i < (1 << N); i++) {</pre>
 dp[i] = a[i];
// Classic SOS-dp, goal: dp[mask] = \sum a[submasks of
    maskl
for (int i = 0; i < N; i++) {</pre>
 for (int mask = 0; mask < (1 << N); mask++) {</pre>
    if ((mask >> i) & 1) {
      dp[mask] += dp[mask ^ (1 << i)];
    }
 }
// Overmasks SOS-dp, goal: dp[mask] = \sum a[overmasks
    of maskl
for (int i = 0: i < N: i++) {</pre>
 for (int mask = (1 << N) - 1; mask >= 0; mask--) {
    if (((mask >> i) & 1) == 0) {
      dp[mask] += dp[mask ^ (1 << i)];
 }
// to inverse SOS-dp (restore original array by SOS-dp
// use same code, but -= instead of += in dp transitions
```

3.4 HB Π

```
// 0-indexation (\{a_0, ..., a_{n-1}\})
```

```
vector<int> lis(vector<int> a) {
 int n = (int) a.size();
 vector\langle int \rangle dp(n + 1, INF), ind(n + 1), par(n + 1); //
     INF > all a[i] required
 ind[0] = -INF;
 dp[0] = -INF;
 for (int i = 0; i < n; i++) {</pre>
   int 1 = upper_bound(dp.begin(), dp.end(), a[i]) - dp
    .begin();
   if (dp[l - 1] < a[i] && a[i] < dp[l]) {</pre>
     dp[1] = a[i];
     ind[1] = i;
      par[i] = ind[l - 1];
 vector<int> ans; // exact values
 for (int 1 = n: 1 >= 0: 1--) {
   if (dp[1] < INF) {</pre>
     int pi = ind[1];
      ans.resize(1);
     for (int i = 0; i < 1; i++) {</pre>
        ans[i] = a[pi]; // =pi if need indices
        pi = par[pi];
      reverse(ans.begin(), ans.end());
      return ans;
 return {};
```

$3.5 \quad HOB\Pi$

```
// 1-indexation ({0, a<sub>1</sub>,..., a<sub>n</sub>}, {0, b<sub>1</sub>,..., b<sub>m</sub>})
vector<int> lcis(vector<int> a, vector<int> b) {
  int n = (int) a.size() - 1, m = (int) b.size() - 1;
  vector<int> dp(m + 1), dp2(m + 1), par(m + 1);
  for (int i = 1; i <= n; i++) {
    int best = 0, best_idx = 0;
    for (int j = 1; j <= m; j++) {
        dp2[j] = dp[j];
        if (a[i] == b[j]) {
            dp2[j] = max(dp2[j], best + 1);
            par[j] = best_idx;
        }
        if (a[i] > b[j] && best < dp[j]) {
            best = dp[j];
            best_idx = j;
        }
</pre>
```

```
}
    swap(dp, dp2);
}
int pj = 0;
for (int j = 1; j <= m; j++) {
    if (dp[pj] < dp[j]) {
        pj = j;
    }
}
vector<int> ans; // exact values
while (pj > 0) {
    ans.push_back(b[pj]);
    pj = par[pj];
}
reverse(ans.begin(), ans.end());
return ans;
}
```

4 Деревья

4.1 Centroid

```
void sizes(int v, int p) {
  sz[v] = 1;
  for (auto u : g[v]) {
    if (u != p && !used[u]) {
      sizes(u, v);
      sz[v] += sz[u];
    }
  }
}
int centroid(int v, int p, int n) {
  for (int u : g[v]) {
    if (sz[u] > n / 2 && u != p && !used[u]) {
      return centroid(u, v, n);
    }
  }
  return v;
void dfs(int v, int p) {
  // code
  for (auto u : g[v]) {
    if (u != p && !used[u]) {
      dfs(u, v);
    }
```

```
}
void solve(int v) {
 sizes(v, -1);
 // code (?)
 for (auto u : g[v]) {
   if (!used[u]) {
     // code (?)
     dfs(u, v);
     // сохраняем результаты dfs
   }
 }
 // code (сливаем результаты dfs)
 used[v] = 1;
 for (int u : g[v]) {
   if (!used[u]) {
      solve(centroid(u, v, sz[u]));
   }
 }
signed main() {
 sizes(0, -1);
 solve(centroid(0, -1, n));
```

4.2 HLD

```
const int MAXN = 50500;
const int INF = (int) 1e15;
const int L = 20;
vector<int> g[MAXN];
int sz[MAXN];
int depth[MAXN];
vector<vector<int>> up(MAXN, vector<int>(L + 1));
void dfs(int v, int p) {
 up[v][0] = p;
 for (int i = 1; i <= L; i++) {
   up[v][i] = up[up[v][i - 1]][i - 1];
 for (int u : g[v]) {
   if (u != p) {
      dfs(u, v);
   }
 }
```

```
int lca(int u, int v) {
 if (u == v) {
    return u;
  int du = depth[u], dv = depth[v];
  if (du < dv) {
    swap(du, dv);
    swap(u, v);
  for (int i = L; i >= 0; i--) {
    if (du - (int) pow(2, i) >= dv) {
     u = up[u][i];
      du = (int) pow(2, i);
 }
  if (u == v) {
    return u;
 for (int i = L; i >= 0; i--) {
    if (up[u][i] != up[v][i]) {
     u = up[u][i];
     v = up[v][i];
 }
 return up[u][0];
void dfs1(int v, int p) {
  sz[v] = 1;
 for (int u : g[v]) {
   if (u != p) {
     dfs1(u, v);
      sz[v] += sz[u];
 }
int cnt = 0:
int nn[MAXN];
int pred[MAXN];
int rup[MAXN];
void dfs2(int v, int p, int root, int dep = 0) {
  depth[v] = dep;
 nn[v] = cnt++;
  pred[v] = p;
  rup[v] = root;
```

```
int mx = 0:
  int vert = -1;
  for (int u : g[v]) {
    if (u != p) {
      if (mx < sz[u]) {</pre>
        mx = sz[u];
        vert = u;
      }
    }
  }
  if (vert != -1) {
    dfs2(vert, v, root, dep + 1);
  for (int u : g[v]) {
    if (u != p && u != vert) {
      dfs2(u, v, u, dep + 1);
    }
  }
}
ST st({});
int n;
int mx_path_up(int u, int v) {
  if (depth[u] < depth[v]) {</pre>
    swap(u, v);
  int res = -INF;
  while (true) {
    int root = rup[u];
    if (depth[root] <= depth[v]) {</pre>
      res = \max(\text{res}, \text{st.rmq}(0, 0, n, nn[v], nn[u] + 1));}
      break;
    }
    res = max(res, st.rmq(0, 0, n, nn[root], nn[u] + 1))
    u = pred[rup[u]];
  return res;
int mx_path(int u, int v) {
  int vert = lca(u, v);
  return max(mx_path_up(u, vert), mx_path_up(v, vert));
}
void change(int u, int qd) {
  st.update(0, 0, n, nn[u], qd);
```

```
signed main() {
 cin >> n;
 vector<int> hs(n);
 for (auto &x : hs) {
   cin >> x;
 for (int i = 0; i < n - 1; i++) {
   cin >> u1 >> v1;
   g[u1].push_back(v1);
   g[v1].push_back(u1);
 dfs1(1, -1);
 dfs(1, 1);
 dfs2(1, -1, 1);
 vector<int> nhs(n);
 for (int i = 1; i <= n; i++) {
   nhs[nn[i]] = hs[i - 1];
 st = *new ST(nhs);
 char op;
 int q;
 cin >> q;
 while (q--) {
   cin >> op >> v1 >> u1;
   if (op == '?') {
      cout << mx_path(u1, v1) << endl;</pre>
   } else {
      change(v1, u1);
   }
```

4.3 Link-cut

```
struct Node {
  Node *ch[2];
  Node *p;
  bool rev;
  int sz;

  Node() {
    ch[0] = nullptr;
    ch[1] = nullptr;
    p = nullptr;
    rev = false;
    sz = 1;
```

```
};
int size(Node *v) {
 return (v ? v->sz : 0);
int chnum(Node *v) {
 return v \rightarrow p \rightarrow ch[1] == v;
bool isroot(Node *v) {
 return v->p == nullptr || v->p->ch[chnum(v)] != v;
void push(Node *v) {
 if (v->rev) {
    if (v->ch[0])
      v->ch[0]->rev ^= 1;
    if (v->ch[1])
      v->ch[1]->rev ^= 1;
    swap(v->ch[0], v->ch[1]);
    v->rev = false;
 }
void pull(Node *v) {
 v->sz = size(v->ch[1]) + size(v->ch[0]) + 1;
void attach(Node *v, Node *p, int num) {
 if (p)
    p->ch[num] = v;
  if (v)
    v - p = p;
void rotate(Node *v) {
  Node *p = v->p;
  push(p);
  push(v):
  int num = chnum(v);
  Node *u = v - > ch[1 - num];
  if (!isroot(v->p))
    attach(v, p->p, chnum(p));
  else
    v \rightarrow p = p \rightarrow p;
  attach(u, p, num);
  attach(p, v, 1 - num);
  pull(p);
```

```
pull(v);
void splay(Node *v) {
 push(v);
  while (!isroot(v)) {
   if (!isroot(v->p)) {
      if (chnum(v) == chnum(v->p))
        rotate(v->p);
      else
        rotate(v);
   }
    rotate(v);
}
void expose(Node *v) {
  splay(v);
  v->ch[1] = nullptr;
  pull(v);
  while (v->p != nullptr) {
   Node *p = v - p;
    splay(p);
    attach(v, p, 1);
    pull(p);
    splay(v);
}
void makeroot(Node *v) {
  expose(v);
  v->rev ^= 1;
  push(v);
}
void link(Node *v, Node *u) {
  makeroot(v):
  makeroot(u);
  u->p = v;
void cut(Node *v, Node *u) {
  makeroot(u);
  makeroot(v);
  v->ch[1] = nullptr;
  u->p = nullptr;
int get(Node *v, Node *u) {
```

```
makeroot(u);
 makeroot(v);
 Node *w = u;
 while (!isroot(w))
   y = y - y;
 return (w == v ? size(v) - 1 : -1);
const int MAXN = 100010;
Node *nodes[MAXN];
int main() {
 int n, q;
 cin >> n >> q;
 for (int i = 0; i < n; ++i)
   nodes[i] = new Node();
 while (q--) {
   string s;
   int a, b;
   cin >> s >> a >> b;
   a--, b--;
   if (s[0] == 'g')
      cout << get(nodes[a], nodes[b]) << '\n';</pre>
    else if (s[0] == '1')
     link(nodes[a], nodes[b]);
      cut(nodes[a], nodes[b]);
 }
```

5 Другое

5.1 Slope trick

```
// Дан массив a_n. Сделать минимальное кол-во \pm 1, чтобы a_n стал неубывающим.

void solve() {
   int n;
   cin >> n;
   vector<int> a(n);
   for (int i = 0; i < n; i++) {
      cin >> a[i];
   }
   int ans = 0;
   multiset<int> now;
   for (int i = 0; i < n; i++) {
      now.insert(a[i]);
```

```
ans += (*now.rbegin() - a[i]);
  now.erase(now.find(*now.rbegin()));
  now.insert(a[i]);
}
cout << ans << '\n';</pre>
```

5.2 attribute packed

```
struct Kek {
  int a;
  char b;
  // char[3]
  int c;
} __attribute__((packed));
// sizeof = 9 (instead of 12)
```

5.3 ordered set

5.4 pragma

5.5 Аллокатор Копелиовича

```
// Код вставить до инклюдов

#include <cassert>

const int MAX_MEM = 1e8; // ~100mb
int mpos = 0;
```

```
char mem[MAX_MEM];
inline void *operator new(std::size_t n) {
   assert((mpos += n) <= MAX_MEM);
   return (void *)(mem + mpos - n);
}
inline void operator delete(void *) noexcept {} // must
   have!
inline void operator delete(void *, std::size_t)
   noexcept {} // fix!!</pre>
```

6 Математика

6.1 FFT mod

```
const int MOD = 998244353; // 7 \cdot 17 \cdot 2^{23} + 1
const int GEN = 3;
//const int MOD = 7340033; // 7 \cdot 2^{20} + 1
//const int GEN = 5:
//const int MOD = 469762049; // 7 \cdot 2^{26} + 1
//const int GEN = 30;
const int LOG = 20;
const int MAXN = 1 << LOG;</pre>
int tail[MAXN + 1];
int OMEGA[MAXN + 1];
int binpow(int x, int p) {
  int res = 1;
  while (p > 0) {
    if (p & 1)
      res = res * 111 * x % MOD;
    x = x * 111 * x % MOD;
    p >>= 1;
  return res;
int omega(int n, int k) {
  return OMEGA[MAXN / n * k];
}
int gettail(int x, int lg) {
  return tail[x] >> (LOG - lg);
void calcomega() {
```

```
long long one = binpow(GEN, (MOD - 1) / MAXN);
  OMEGA[O] = 1;
 for (int i = 1; i < MAXN; ++i) {</pre>
    OMEGA[i] = OMEGA[i - 1] * one % MOD;
 }
void calctail() {
  int n = MAXN:
 for (int x = 0; x < n; ++x) {
    int res = 0:
    for (int i = 0; i < LOG; ++i) {</pre>
      res += ((x >> i) & 1) << (LOG - i - 1);
    }
    tail[x] = res;
// Without precalc, tail[], OMEGA[]
//long long omega(int n, int k) {
//
      return binpow(GEN, (MOD - 1) / n * k);
//}
//
//int gettail(int x, int lg) {
      int res = 0;
11
      for (int i = 0; i < lg; ++i)
11
          res += ((x >> i) & 1) << (lg - i - 1);
11
      return res:
//}
void fft(vector<int> &A, int lg) {
 int n = 1 << lg;</pre>
 for (int i = 0; i < n; ++i) {</pre>
    int j = gettail(i, lg);
    if (i < j)
      swap(A[i], A[j]);
 }
 for (int len = 2; len <= n; len *= 2) {
    for (int i = 0; i < n; i += len) {</pre>
      for (int j = 0; j < len / 2; ++j) {
        auto v = A[i + j];
        auto u = A[i + j + len / 2] * 111 * omega(len, j)
    ) % MOD;
        A[i + j] = (v + u) \% MOD;
        A[i + j + len / 2] = (v - u + MOD) \% MOD;
    }
 }
```

```
int inverse(int x) {
 return binpow(x, MOD - 2);
void invfft(vector<int> &A, int lg) {
  int n = 1 << lg;</pre>
 fft(A, lg);
 for (auto &el : A)
    el = el * 111 * inverse(n % MOD) % MOD;
  reverse(A.begin() + 1, A.end());
vector<int> mul(vector<int> A, vector<int> B) {
  int lg = 32 - __builtin_clz(A.size() + B.size() - 1);
  int n = 1 \ll lg:
  A.resize(n, 0);
  B.resize(n. 0):
  fft(A, lg);
  fft(B, lg);
  for (int i = 0; i < n; ++i)</pre>
   A[i] = A[i] * 111 * B[i] % MOD;
  invfft(A, lg);
 return A;
signed main() {
  calctail(); // HE 3AEWTb
  calcomega(); // HE 3AEWTb
  int n, m;
  cin >> n >> m;
  vector<int> A(n), B(m);
  for (int &el : A)
    cin >> el;
  for (int &el : B)
    cin >> el:
  auto C = mul(A, B);
 for (auto el : C)
    cout << el << ',,';
```

6.2 FFT

```
const double PI = acos(-1);
const int LOG = 20;
const int MAXN = 1 << LOG;</pre>
```

```
struct comp {
  double x, y;
  comp() : x(0), y(0) {}
  comp(double x, double y) : x(x), y(y) {}
  comp(int x) : x(x), y(0) {}
  comp operator+(const comp &o) const {
    return \{x + o.x, y + o.y\};
  comp operator-(const comp &o) const {
    return \{x - o.x, y - o.y\};
  comp operator*(const comp &o) const {
    return \{x * o.x - y * o.y, x * o.y + y * o.x\};
  comp operator/(const int k) const {
    return {x / k, y / k};
  comp conj() const {
    return {x, -y};
};
comp OMEGA[MAXN + 10];
int tail[MAXN + 10];
comp omega(int n, int k) {
  return OMEGA[MAXN / n * k];
void calcomega() {
  for (int i = 0; i < MAXN; ++i) {</pre>
    double x = 2 * PI * i / MAXN:
    OMEGA[i] = {cos(x), sin(x)};
  }
void calctail() {
  tail[0] = 0;
  for (int i = 1; i < MAXN; ++i) {</pre>
    tail[i] = (tail[i >> 1] >> 1) | ((i & 1) << (LOG -
    1));
  }
}
void fft(vector<comp> &A) {
  int n = A.size();
  for (int i = 0; i < n; ++i) {</pre>
    if (i < tail[i])</pre>
      swap(A[i], A[tail[i]]);
```

```
}
 for (int len = 2; len <= n; len *= 2) {
   for (int i = 0; i < n; i += len) {</pre>
     for (int j = 0; j < len / 2; ++j) {
        auto v = A[i + j];
        auto u = A[i + j + len / 2] * omega(len, j);
       A[i + j] = v + u;
        A[i + j + len / 2] = v - u;
     }
   }
 }
void fft2(vector<comp> &A, vector<comp> &B) {
 int n = A.size();
 vector<comp> C(n);
 for (int i = 0: i < n: ++i) {</pre>
   C[i].x = A[i].x;
   C[i].y = B[i].x;
 fft(C);
 C.push_back(C[0]);
 for (int i = 0; i < n; ++i) {</pre>
   A[i] = (C[i] + C[n - i].conj()) / 2;
   B[i] = (C[i] - C[n - i].conj()) / 2 * comp(0, -1);
void invfft(vector<comp> &A) {
 fft(A):
 for (auto &el : A)
    el = el / MAXN;
 reverse(A.begin() + 1, A.end());
vector<int> mul(vector<int> &a, vector<int> &b) {
 vector<comp> A(MAXN, 0), B(MAXN, 0);
 for (int i = 0; i < (int)a.size(); ++i)</pre>
   A[i] = a[i];
 for (int i = 0; i < (int)b.size(); ++i)</pre>
   B[i] = b[i]:
 fft2(A, B);
 for (int i = 0; i < MAXN; ++i)</pre>
   A[i] = A[i] * B[i];
 invfft(A);
 vector<int> c(MAXN);
 for (int i = 0; i < MAXN; ++i) {</pre>
   int x = round(A[i].x);
   c[i] = x;
 }
```

```
while (!c.empty() && c.back() == 0)
    c.pop_back();
 return c;
signed main() {
 calcomega(); // HE 3ABUTb
  calctail(); // HE 3AEWTE
 // your code here
```

6.3 Γaycc

```
vector<vector<int>> gauss(vector<vector<int>> &a) {
 int n = a.size():
 int m = a[0].size();
// int det = 1;
  for (int col = 0, row = 0; col < m && row < n; ++col)
    for (int i = row; i < n; ++i) {</pre>
      if (a[i][col]) {
        swap(a[i], a[row]);
        if (i != row) {
            det *= -1;
       }
        break;
    }
    if (!a[row][col])
      continue;
    for (int i = 0; i < n; ++i) {</pre>
      if (i != row && a[i][col]) {
        int val = a[i][col] * inv(a[row][col]) % mod;
        for (int j = col; j < m; ++j) {</pre>
          a[i][i] -= val * a[row][i];
          a[i][j] %= mod;
       }
     }
    }
    ++row;
// for (int i = 0; i < n; ++i) det = (det * a[i][i]) %
// det = (det % mod + mod) % mod:
// result in (-mod, mod)
 return a;
```

```
pair<int, vector<int>> sle(vector<vector<int>> a, vector
    <int> b) {
 int n = a.size();
 int m = a[0].size();
 assert(n == b.size());
 for (int i = 0; i < n; ++i) {</pre>
   a[i].push_back(b[i]);
 }
 a = gauss(a);
 vector<int> x(m, 0);
 for (int i = n - 1; i \ge 0; --i) {
   int leftmost = m;
   for (int j = 0; j < m; ++j) {
     if (a[i][j] != 0) {
       leftmost = j;
        break;
     }
   if (leftmost == m && a[i].back() != 0) return {-1.
   if (leftmost == m) continue;
   int val = a[i].back();
   for (int j = m - 1; j > leftmost; --j) {
     val -= a[i][j] * x[j];
     val %= mod;
   x[leftmost] = (val * inv(a[i][leftmost]) % mod + mod
   ) % mod;
 return {1, x};
vector<bitset<N>> gauss_bit(vector<bitset<N>> a, int m)
    {
 int n = a.size();
 for (int col = 0, row = 0; col < m && row < n; ++col)
   {
   for (int i = row; i < n; ++i) {</pre>
      if (a[i][col]) {
        swap(a[i], a[row]);
        break;
     }
   }
   if (!a[row][col])
      continue:
   for (int i = 0; i < n; ++i)</pre>
      if (i != row && a[i][col])
        a[i] ^= a[row];
   ++row;
```

```
}
return a;
```

6.4 Диофантовы уравнения

```
pair<int, int> ext_gcd(int a, int b) {
 int x1 = 1, y1 = 0, x2 = 0, y2 = 1;
 while (b) {
   int k = a / b:
   x1 = x1 - x2 * k;
   y1 = y1 - y2 * k;
   swap(x1, x2);
   swap(y1, y2);
   a %= b:
   swap(a, b);
 return {x1, y1};
bool cool_ext_gcd(int a, int b, int c, int &x, int &y) {
 if (b == 0) {
   y = 0;
   if (a == 0) {
     x = 0:
     return c == 0:
   } else {
     x = c / a:
     return c % a == 0;
   }
 auto [x0, y0] = ext_gcd(a, b);
 int g = x0 * a + y0 * b;
 if (c % g != 0)
   return false;
 x0 *= c / g;
 y0 *= c / g;
 int t = b / g;
 int k = (-x0) / t;
 if (x0 + t * k < 0)
   k += t / abs(t):
 x = x0 + t * k;
 y = y0 - (a / g) * k;
 return true;
```

6.5 KTO

```
// x = a_i % p_i
vector<vector<int>> r(k, vector<int>(k));
for (int i = 0; i < k; ++i)
 for (int j = 0; j < k; ++j)
   if (i != j)
      r[i][j] = binpow(p[i] % p[j], p[j] - 2, p[j]);
vector<int> x(k);
for (int i = 0; i < k; ++i) {</pre>
 x[i] = a[i];
 for (int j = 0; j < i; ++j) {
    x[i] = r[j][i] * (x[i] - x[j]);
    x[i] = x[i] % p[i];
    if (x[i] < 0) x[i] += p[i];</pre>
 }
int ans = 0;
for (int i = 0; i < k; ++i) {</pre>
 int val = x[i];
 for (int j = 0; j < i; ++j) val *= p[j];</pre>
  ans += val:
```

6.6 Код Грея

```
for (int i = 0; i < (1 << n); i++) {
  gray[i] = i ^ (i >> 1);
}
```

6.7 Линейное решето

6.8 Миллер Рабин

```
// assuming '#define int long long' is ON (replace 'int'
     with 'long long' if not)
// works for all n < 2^64
const int MAGIC[7] = {2, 325, 9375, 28178, 450775,
    9780504, 1795265022};
int bpow(__int128 a, int x, int mod) {
 a \%= mod;
  _{\rm int128} ans = 1;
 while (x) {
   if (x % 2) {
      ans *= a:
      ans %= mod;
   a *= a;
   a %= mod;
   x /= 2;
 return (int) ans;
bool is_prime(int n) {
 if (n == 1) return false;
 if (n <= 3) return true;
 if (n % 2 == 0 || n % 3 == 0) return false;
 int s = __builtin_ctzll(n - 1), d = n >> s; //
    n-1=2^s\cdot d
 for (auto a : MAGIC) {
   if (a % n == 0) {
      continue;
   int x = bpow(a, d, n);
   for (int _ = 0; _ < s; _++) {
      int y = bpow(x, 2, n);
      if (y == 1 && x != 1 && x != n - 1) {
        return false;
      }
      x = y;
   if (x != 1) {
      return false;
   }
 }
 return true;
```

```
typedef long long 11;
11 mult(11 a, 11 b, 11 mod) {
 return (__int128)a * b % mod;
11 f(11 x, 11 c, 11 mod) {
 return (mult(x, x, mod) + c) % mod;
ll rho(ll n, ll x0=2, ll c=1) {
 11 x = x0:
 11 y = x0;
 11 g = 1;
 while (g == 1) {
    x = f(x, c, n);
    y = f(y, c, n);
   y = f(y, c, n);
    g = gcd(abs(x - y), n);
 return g;
mt19937_64 rnd(time(nullptr));
void factor(int n, vector<int> &pr) {
 if (n == 4) {
    factor(2, pr);
    factor(2, pr);
    return;
 if (n == 1) {
    return;
  if (is_prime(n)) {
    pr.push_back(n);
    return;
 }
  int d = rho(n, rnd() \% (n - 2) + 2, rnd() \% 3 + 1);
  factor(n / d, pr);
  factor(d, pr);
```

7 Строки

7.1 Z-функция

```
vector<int> z_func(string s) {
 int n = s.size();
 vector < int > z(n, 0);
 z[0] = n:
 int 1 = 0, r = 0;
 for (int i = 1; i < n; i++) {
   if (i < r) {
     z[i] = min(z[i - 1], r - i);
   while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])  {
     z[i]++;
   }
   if (i + z[i] > r) {
     l = i;
     r = i + z[i];
 }
 return z;
```

7.2 Ахо-Корасик

```
int go[MAXN][ALPH];
vector<int> term[MAXN];
int par[MAXN], suf[MAXN];
char par_c[MAXN];
vector<int> g[MAXN];
int cntv = 1:
void add(string &s) {
 static int cnt_s = 1;
  int v = 0;
 for (char el: s) {
   if (go[v][el - 'a'] == 0) {
      go[v][el - 'a'] = cntv;
      par[cntv] = v;
      par_c[cntv] = el;
      cntv++;
    v = go[v][el - 'a'];
  term[v].push_back(cnt_s++);
void bfs() {
  deque < int > q = \{0\};
  while (!q.empty()) {
```

```
int v = q.front();
q.pop_front();
if (v > 0) {
    if (par[v] == 0) {
        suf[v] = 0;
    } else {
        suf[v] = go[suf[par[v]]][par_c[v] - 'a'];
    }
    g[suf[v]].push_back(v);
}
for (int c = 0; c < 26; c++) {
    if (go[v][c] == 0) {
        go[v][c] = go[suf[v]][c];
    } else {
        q.push_back(go[v][c]);
    }
}</pre>
```

7.3 Муффиксный Сассив

```
vector<int> build_suff_arr(string s) {
 s.push_back('#');
 int n = s.size();
 vector<int> suf(n), c(n);
 vector<int> cnt(MAX);
 for (int i = 0; i < n; i++) {</pre>
   cnt[s[i] - '#']++:
 vector<int> pos(MAX);
 for (int i = 1; i < MAX; i++) {</pre>
   pos[i] = pos[i - 1] + cnt[i - 1];
 for (int i = 0; i < n; i++) {</pre>
    suf[pos[s[i] - '#']++] = i;
 int cls = -1;
 for (int i = 0; i < n; i++) {</pre>
   if (i == 0 || s[suf[i]] != s[suf[i - 1]]) {
      cls++;
   }
    c[suf[i]] = cls;
 for (int L = 1; L < n; L *= 2) {
   fill(cnt.begin(), cnt.end(), 0);
   for (int i = 0; i < n; i++) {</pre>
      cnt[c[i]]++;
```

```
}
   pos[0] = 0;
   for (int i = 1; i < n; i++) {</pre>
     pos[i] = pos[i - 1] + cnt[i - 1];
   }
   for (int i = 0; i < n; i++) {</pre>
     suf[i] = (suf[i] - L + n) % n;
   vector<int> new_suf(n), new_c(n);
   for (int i = 0; i < n; i++) {</pre>
     int where = pos[c[suf[i]]];
     new_suf[where] = suf[i];
     pos[c[suf[i]]]++;
   }
   cls = -1;
   for (int i = 0; i < n; i++) {</pre>
     if (i == 0) {
        cls++;
       new_c[new_suf[i]] = cls;
        continue:
     pair<int, int> prev = {c[new_suf[i - 1]], c[(
    new_suf[i - 1] + L) % n]};
     pair<int, int> now = {c[new_suf[i]], c[(new_suf[i])]
     + L) % n]};
     if (prev != now) {
        cls++;
     new_c[new_suf[i]] = cls;
   swap(c, new_c);
   swap(suf, new_suf);
 }
 vector<int> res;
 for (int i = 1; i < n; i++) {</pre>
   res.push_back(suf[i]);
 return res;
vector<int> kasai(string s, vector<int> sa) {
 int n = s.size(), k = 0;
 vector<int> lcp(n, 0);
 vector<int> rank(n, 0);
 for (int i = 0; i < n; i++) rank[sa[i]] = i;</pre>
 for (int i = 0; i < n; i++, k ? k-- : 0) {
   if (rank[i] == n - 1) {
     k = 0:
      continue;
```

```
}
int j = sa[rank[i] + 1];
while (i + k < n && j + k < n && s[i + k] == s[j + k
]) k++;
lcp[rank[i]] = k;
}
return lcp;
}</pre>
```

7.4 Префикс-функция

```
vector<int> prefix_func(string s) {
  int n = s.size();
  vector<int> pref(n, 0);
  int ans = 0;
  for (int i = 1; i < n; i++) {
    while (ans > 0 && s[ans] != s[i]) {
        ans = pref[ans - 1];
    }
    if (s[i] == s[ans]) {
        ans++;
    }
    pref[i] = ans;
}
return pref;
}
```

7.5 Суффиксный автомат

```
// Суфавтомат с подсчётом кол-ва различных подстрок

const int SIGMA = 26;
int ans = 0;

struct Node {
  int go[SIGMA];
  int s, p;
  int len;

Node() {
  fill(go, go + SIGMA, -1);
   s = -1, p = -1;
  len = 0;
  }
};

int add(int A, int ch, vector<Node> &sa) {
```

```
int B = sa.size();
  sa.emplace_back();
  sa[B].p = A;
  sa[B].s = 0;
  sa[B].len = sa[A].len + 1;
  for (; A != -1; A = sa[A].s) {
    if (sa[A].go[ch] == -1) {
      sa[A].go[ch] = B;
      continue;
    int C = sa[A].go[ch];
    if (sa[C].p == A) {
      sa[B].s = C;
      break;
    int D = sa.size();
    sa.emplace back():
    sa[D].s = sa[C].s;
    sa[D].p = A:
    sa[D].len = sa[A].len + 1;
    sa[C].s = D;
    sa[B].s = D:
    copy(sa[C].go, sa[C].go + SIGMA, sa[D].go);
    for (; A != -1 && sa[A].go[ch] == C; A = sa[A].s)
      sa[A].go[ch] = D;
    break;
  }
  ans += sa[B].len - sa[sa[B].s].len;
  return B:
}
signed main() {
  string s;
  cin >> s;
  vector<Node> sa(1);
  int A = 0;
  for (char c : s)
    A = add(A, c - 'a', sa);
  cout << ans;</pre>
```

8 Структуры данных

8.1 Disjoint Sparse Table

```
int tree[LOG][MAXN];
int floorlog2[MAXN]; // i ? (31 - __builtin_clz(i)) : 0
```

```
void build(vector<int> &a) {
 int n = a.size();
 copy(a.begin(), a.end(), tree[0]);
 for (int lg = 1; lg < LOG; ++lg) {</pre>
   int len = 1 << lg;</pre>
    auto &lvl = tree[lg];
    for (int m = len; m < n; m += len * 2) {</pre>
     lvl[m-1] = a[m-1]:
     lvl[m] = a[m]:
     for (int i = m - 2; i >= m - len; --i)
       lvl[i] = min(lvl[i + 1], a[i]);
     for (int i = m + 1; i < m + len && i < n; ++i)</pre>
        lvl[i] = min(lvl[i - 1], a[i]);
   }
 for (int i = 2; i <= n; ++i)</pre>
    floorlog2[i] = floorlog2[i / 2] + 1;
// a[l..r)
int get(int 1, int r) {
 r--:
 int i = floorlog2[l ^ r];
 return min(tree[i][l], tree[i][r]);
```

8.2 Segment Tree Beats

```
// min=. sum
struct ST {
 vector<int> st, mx, mx_cnt, sec_mx;
 ST(int n) {
    st.resize(n * 4. 0):
   mx.resize(n * 4, 0);
   mx_cnt.resize(n * 4, 0);
    sec_mx.resize(n * 4, 0);
    build(0, 0, n);
 }
 void upd_from_children(int v) {
    st[v] = st[v * 2 + 1] + st[v * 2 + 2]:
    mx[v] = max(mx[v * 2 + 1], mx[v * 2 + 2]);
   mx cnt[v] = 0:
    sec_mx[v] = max(sec_mx[v * 2 + 1], sec_mx[v * 2 +
    2]);
    if (mx[v * 2 + 1] == mx[v]) {
     mx_cnt[v] += mx_cnt[v * 2 + 1];
```

```
} else {
    sec_mx[v] = max(sec_mx[v], mx[v * 2 + 1]);
  if (mx[v * 2 + 2] == mx[v]) {
    mx_cnt[v] += mx_cnt[v * 2 + 2];
    sec_mx[v] = max(sec_mx[v], mx[v * 2 + 2]);
}
void build(int i, int l, int r) {
  if (1 + 1 == r) {
    st[i] = mx[i] = 0;
    mx cnt[i] = 1:
    sec_mx[i] = -INF;
    return:
  }
  int m = (r + 1) / 2:
  build(i * 2 + 1, 1, m):
  build(i * 2 + 2, m, r);
  upd_from_children(i);
}
void push_min_eq(int v, int val) {
  if (mx[v] > val) {
    st[v] -= (mx[v] - val) * mx_cnt[v];
    mx[v] = val:
}
void push(int i) {
  push_min_eq(i * 2 + 1, mx[i]);
  push_min_eq(i * 2 + 2, mx[i]);
}
void update(int i, int l, int r, int gl, int gr, int
  val) {
  if (mx[i] <= val) {</pre>
    return;
  if (ql == 1 && qr == r && sec_mx[i] < val) {</pre>
    push_min_eq(i, val);
    return;
  push(i);
  int m = (r + 1) / 2;
  if (qr <= m) {</pre>
    update(i * 2 + 1, 1, m, ql, qr, val);
  } else if (ql >= m) {
```

```
update(i * 2 + 2, m, r, ql, qr, val);
   } else {
      update(i * 2 + 1, 1, m, ql, m, val);
      update(i * 2 + 2, m, r, m, qr, val);
   upd_from_children(i);
 int sum(int i, int l, int r, int ql, int qr) {
   if (1 == q1 && r == qr) {
      return st[i];
   }
   push(i);
   int m = (r + 1) / 2;
   if (qr <= m) {</pre>
      return sum(i * 2 + 1, 1, m, ql, qr);
   }
   if (q1 >= m) {
      return sum(i * 2 + 2, m, r, ql, qr);
   return sum(i * 2 + 1, 1, m, ql, m) + sum(i * 2 + 2,
    m, r, m, qr);
};
```

8.3 ДД по неявному

```
pair<Node *, Node *> split(Node *t, int k) {
  if (!now)
    return {nullptr, nullptr};
  int szl = size(t->1);
  if (k <= szl) {</pre>
    auto [l, r] = split(t->l, k);
    t \rightarrow 1 = r:
    pull(t);
    return {1, t};
  } else {
    auto [1, r] = split(t->r, k - szl - 1);
    t->r = 1:
    pull(t);
    return {t, r};
}
Node *merge(Node *1, Node *r) {
  if (!1)
    return r;
  if (!r)
```

```
return 1:
  if (1->y < r->y) {
    1->r = merge(1->r, r);
    pull(1);
    return 1;
 } else {
    r->1 = merge(1, r->1);
    pull(r);
    return r;
}
void insert(Node *&root, int pos, int val) {
 Node *new_v = new Node(val);
 auto [1, r] = split(root, pos);
 root = merge(merge(1, new_v), r);
void erase(Node *&root, int pos) {
  auto [lm, r] = split(root, pos + 1);
  auto [1, m] = split(lm, pos);
 root = merge(1, r);
int sum(Node *v) {
 return v ? v->sm : 0;
// query [1, r)
int query(Node *&root, int ql, int qr) {
 auto [lm, r] = split(root, qr);
  auto [1, m] = split(lm, ql);
 int res = sum(m):
 root = merge(merge(1, m), r);
  return res;
```

8.4 ДД

```
pair<Node *, Node *> split(Node *t, int x) {
   if (!t)
     return {nullptr, nullptr};
   if (x <= t->x) {
     auto [1, r] = split(t->1, x);
     t->1 = r;
   pull(t);
   return {1, t};
```

```
} else {
    auto [1, r] = split(t->r, x);
    t->r = 1:
    pull(t);
    return {t, r};
 }
Node *merge(Node *1, Node *r) {
 if (!1)
    return r;
 if (!r)
    return 1;
  if (1->y < r->y) {
   1->r = merge(1->r, r);
   pull(1);
   return 1:
 } else {
   r->1 = merge(1, r->1);
    pull(r);
    return r;
 }
void insert(Node *&root, int val) {
 Node *new_v = new Node(val);
 auto [l, r] = split(root, val);
 root = merge(merge(1, new_v), r);
void erase(Node *&root, int val) {
  auto [lm, r] = split(root, val + 1);
 auto [1, m] = split(lm, val);
 root = merge(1, r);
int sum(Node *v) {
 return v ? v->sm : 0;
// query [1, r)
int query(Node *&root, int ql, int qr) {
  auto [lm, r] = split(root, qr);
  auto [1, m] = split(lm, ql);
  int res = sum(m);
 root = merge(merge(1, m), r);
 return res;
```

8.5 Персистентное ДД по неявному

```
mt19937 rnd(228):
struct Node;
int size(Node *);
int sum(Node *);
struct Node {
  Node *1, *r;
  int val, sz, sm;
  Node(int val) : val(val), sz(1), sm(val) {
   1 = r = nullptr;
  Node(int val, Node *1, Node *r) : val(val), 1(1), r(r)
    sz = 1 + size(1) + size(r);
    sm = val + sum(1) + sum(r);
};
int size(Node *v) {
  return v ? v->sz : 0;
int sum(Node *v) {
  return v ? v->sm : 0;
pair<Node *, Node *> split(Node *t, int x) {
  if (!t)
    return {nullptr, nullptr};
  int lsz = size(t->1);
  if (lsz >= x) {
    auto [1, r] = split(t->1, x);
   auto v = new Node(t->val, r, t->r);
   return {1, v};
  } else {
    auto [1, r] = split(t->r, x - lsz - 1);
    auto v = new Node(t->val, t->l, l);
   return {v, r};
 }
}
bool chooseleft(int lsz, int rsz) {
  return rnd() % (lsz + rsz) < lsz;</pre>
```

```
Node *merge(Node *1, Node *r) {
 if (!1)
    return r;
 if (!r)
    return 1;
 if (chooseleft(l->sz, r->sz)) {
    auto rr = merge(1->r, r);
    auto v = new Node(1->val, 1->l, rr);
    return v:
 } else {
    auto ll = merge(1, r->1);
    auto v = new Node(r->val, ll, r->r);
    return v;
 }
Node *insert(Node *root, int pos, int val) {
 Node *new_v = new Node(val);
 auto [1, r] = split(root, pos);
 return merge(merge(1, new_v), r);
Node *erase(Node *root, int pos) {
 auto [lm, r] = split(root, pos + 1);
 auto [1, m] = split(lm, pos);
 return merge(1, r);
// query [1, r)
pair<int, Node *> query(Node *root, int ql, int qr) {
 auto [lm, r] = split(root, qr);
 auto [1, m] = split(lm, ql);
 int res = sum(m);
 auto new_root = merge(merge(1, m), r);
 return {res, new_root};
```

8.6 Персистентное ДО

```
// left: v ? v->l : nullptr (same for right)
// sum: v ? v->sm : 0

// v can be nullptr. returns new root of subtree
Node *update(Node *v, int l, int r, int qi, int qx) {
   if (qi < l || r <= qi)
      return v;
   if (l + 1 == r)
    return new Node(qx);</pre>
```

```
int m = (1 + r) / 2;
Node *u = new Node();
u->1 = update(left(v), 1, m, qi, qx);
u->r = update(right(v), m, r, qi, qx);
u->sm = sum(u->1) + sum(u->r);
return u;
}

int get(Node *v, int 1, int r, int ql, int qr) {
   if (!v || qr <= 1 || r <= ql)
      return 0;
   if (ql <= 1 && r <= qr)
      return v->sm;
   int m = (1 + r) / 2;
   auto a = get(v->1, 1, m, ql, qr);
   auto b = get(v->r, m, r, ql, qr);
   return a + b;
}
```

8.7 Спарсы

```
int tree[LOG][MAXN];
int floorlog2[MAXN]; // i ? (31 - __builtin_clz(i)) : 0
void build(vector<int> &a) {
 int n = a.size();
  copy(a.begin(), a.end(), tree[0]);
  for (int i = 1; i < LOG; ++i) {</pre>
   int len = 1 << (i - 1);</pre>
   for (int j = 0; j + len < n; ++j)
     tree[i][j] = min(tree[i - 1][j], tree[i - 1][j +
    len]):
 }
 for (int i = 2; i <= n; ++i)</pre>
    floorlog2[i] = floorlog2[i / 2] + 1;
// min a[1..r)
int get(int 1, int r) {
 int i = floorlog2[r - 1];
 return min(tree[i][1], tree[i][r - (1 << i)]);</pre>
```

8.8 Фенвик (+ на отрезке)

```
// a[l..r) += x
void update(int l, int r, int x) {
```

```
T1.add(1, x);
T1.add(r, -x);
T2.add(1, -x * 1);
T2.add(r, x * r);
}

// sum a[0..pos)
int rsq(int pos) {
  return T1.rsq(pos) * pos + T2.rsq(pos);
}

// sum a[1..r)
int sum(int 1, int r) {
  return rsq(r) - rsq(1);
}
```

8.9 Фенвик

```
// Нумерация с 0
struct FenwickTree {
  int n;
  vector<vector<int>>> ft;
  FenwickTree(int n) : n(n) {
   ft.resize(n + 1, vector<vector<int>>(n + 1, vector<
    int>(n + 1)));
 }
  // a[x][y][z] += d
  void upd(int x, int y, int z, int d) {
   x++, y++, z++;
   for (int x1 = x; x1 \le n; x1 += x1 & -x1) {
      for (int y1 = y; y1 <= n; y1 += y1 & -y1) {
        for (int z1 = z; z1 <= n; z1 += z1 & -z1) {</pre>
         ft[x1][y1][z1] += d;
       }
     }
   }
  // sum a[0..x)[0..y)[0..z)
  int rsq(int x, int y, int z) {
   int ans = 0;
   for (int x1 = x; x1 > 0; x1 -= x1 & -x1) {
      for (int y1 = y; y1 > 0; y1 -= y1 & -y1) {
        for (int z1 = z; z1 > 0; z1 -= z1 & -z1) {
          ans += ft[x1][y1][z1];
```