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HW6

Generate RSA key parameters where $p=7$ and $q=13$. $0 < e < 7$.

Identify the RSA public key and the RSA private key.

Generate d using the extended Euclidean algorithm. Show detailed work. Do all work by hand.

Only $e = 5$ is co-prime so we will use $e = 5$

$$e = 5$$

$$p = 7$$

$$q = 13$$

$$n = p * q = 91$$

$$\phi(n) = (p - 1) * (q - 1) = 72$$

$$\text{GDC}(72, 5)$$

$$72 / 5 = 14 \text{ r } 2 \Rightarrow 2 = 72(1) + 5(-14)$$

$$5 / 2 = 2 \text{ r } 1 \Rightarrow 1 = 5(1) + 2(-2)$$

$$2 / 1 = 2 \text{ r } 0 \Rightarrow 0 = 2(1) + 1(-2)$$

$$72 / 5 = 14 \text{ r } 2 \Rightarrow 2 = 72(1) + 5(-14)$$

$$\begin{aligned} 5 / 2 = 2 \text{ r } 1 &\Rightarrow 1 = 5(1) + [72(1) + 5(-14)](-2) \\ &= 5(1) + 72(-2) + 5(28) \\ &= 5(29) + 72(-2) \end{aligned}$$

$$2 / 1 = 2 \text{ r } 0 \Rightarrow 0 = 2(1) + 1(-2)$$

$$5(29) + 72(-2) = \text{GCD}(72, 5) = 1$$

$$d = 29$$