

## **Parsing (part 3)**

Chapter 13 J&M'09

## **CKY** (or CYK)

Named after John Cocke, Daniel Younger and Tadao Kasami.

- Passive chart parser
- Very efficient (runs in polynomial time;  $n^3 \times |G|$ )
- Requires grammar transformation.

## CKY requires grammars in Chomsky Normal Form (CNF)

In CNF, all rules must be of one of the following forms:

$$X \rightarrow YZ$$

$$K \rightarrow w \text{ (where 'w' is a word token)}$$

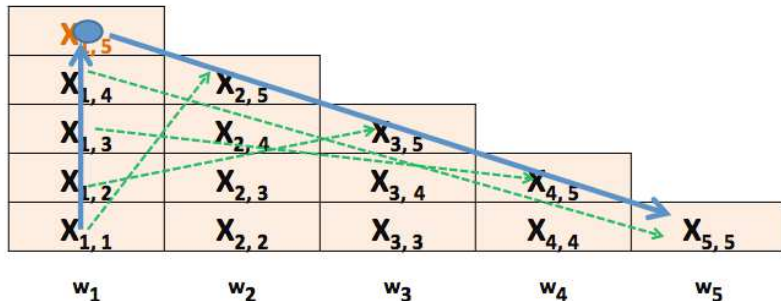
This **binarization** step is crucial for efficient parsing.

## Conversion to CNF

- Copy all conforming rules to new grammar
- Eliminate unit productions:  
Rules like **NP**  $\rightarrow$  **PN** and **PN**  $\rightarrow$  **Tom**  
become a single rule **NP**  $\rightarrow$  **Tom**
- Convert branching rules:  
Rules like **VP**  $\rightarrow$  **DTV NP NP** become  
**VP**  $\rightarrow$  **DVP NP**  
**DVP**  $\rightarrow$  **DTV NP**

# Parsing

For input  $w_1 \dots w_t$ , build parse triangle:



Each row corresponds to a string of ascending length.

Each cell corresponds to all of the possible categories for the corresponding span. For example, in

(1) Doves dove

Each cell of row 1 would be  $\{N, V\}$ .

# Parsing

Input: *Tom saw a friend from Australia*

Span length						
6	S					
5	–	VP				
4	S	–	NP			
3	–	VP	–	N		
2	–	–	NP	–	PP	
1	NP	TV, N	DT	N,TV	P	NP
	0 Tom	1 saw	2 a	3 friend	4 from	5 Australia 6

$S \rightarrow NP VP$

$NP \rightarrow DT N$

$NP \rightarrow Tom$

$NP \rightarrow Australia$

$N \rightarrow friend$

$VP \rightarrow TV NP$

$N \rightarrow N PP$

$TV \rightarrow saw$

$N \rightarrow saw$

$P \rightarrow from$

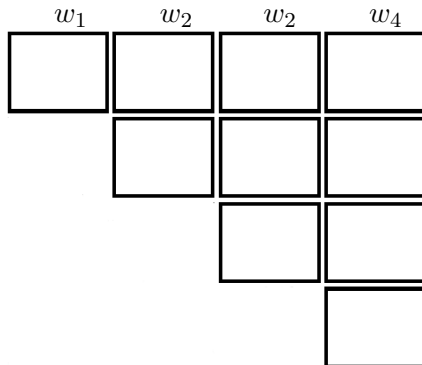
$VP \rightarrow VP PP$

$PP \rightarrow P NP$

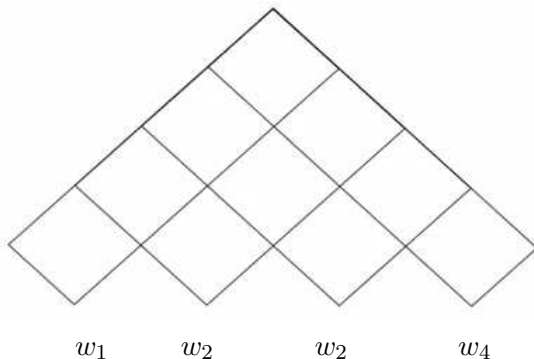
$DT \rightarrow a$

$TV \rightarrow friend$

Sometimes, the chart is shown as a parse triangle:



Sometimes, the chart is rotated:





**Exercise:**

Show that 'b a a b a' is parsed by CKY and the following grammar.

$$S \rightarrow A B$$
$$S \rightarrow B C$$
$$A \rightarrow B A$$
$$A \rightarrow a$$
$$B \rightarrow C C$$
$$B \rightarrow b$$
$$C \rightarrow A B$$
$$C \rightarrow a$$

## Probabilistic Context-free Grammar (PCFG)

Rules are augmented with a probability:

NP  $\rightarrow$  PN [0.35]

NP  $\rightarrow$  PRN [0.30]

NP  $\rightarrow$  DT N [0.20]

NP  $\rightarrow$  N [0.15]

DT  $\rightarrow$  *that* [0.10]

DT  $\rightarrow$  *a* [0.30]

DT  $\rightarrow$  *the* [0.60]

The total probability for rules with the same left-hand side is 1:

$$\sum_{\beta} P(X \rightarrow \beta) = 1$$

Where:

- $\beta$  is any sequence of (terminal/non-terminal) symbols.
- $P(X \rightarrow \beta)$  = probability of rule  $X \rightarrow \beta$

For example:  $P(\text{NP} \rightarrow \text{PN}) = 0.35$

## Statistical Parsing

$T$  is a parse tree and  $S = w_1 \dots w_n$  a token sequence. Bayes' rule:

$$P(T|w_1 \dots w_n) = \frac{P(w_1 \dots w_n|T) \times P(T)}{P(w_1 \dots w_n)}$$

But since  $P(w_1 \dots w_n|T)$  is always 1, then:

$$P(T|w_1 \dots w_n) = \frac{P(T)}{P(w_1 \dots w_n)}$$

In particular, we are interested in the most likely  $T$  for  $S$ :

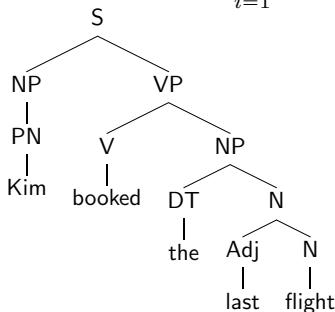
$$\hat{T} = \operatorname{argmax}_{T:S=\operatorname{yield}(T)} \frac{P(T)}{P(w_1 \dots w_n)}$$

But since  $P(w_1 \dots w_n)$  is constant over all  $T$ 's for a given  $S$  then:

$$\hat{T} \approx \operatorname{argmax}_{T:S=\operatorname{yield}(T)} P(T)$$

# Statistical Parsing

$$P(T) = \prod_{i=1}^n P(X_i \rightarrow Y_1 \dots Y_n)$$



Rule	P	Rule	P	Rule	P	Rule	P
$S \rightarrow NP VP$	0.8	$S \rightarrow VP$	0.2	$VP \rightarrow V$	0.3	$VP \rightarrow V NP$	0.5
$VP \rightarrow V NP NP$	0.2	$NP \rightarrow DT N$	0.2	$NP \rightarrow PN$	0.35	$NP \rightarrow PRN$	0.3
$NP \rightarrow N$	0.15	$N \rightarrow Adj N$	0.4	$N \rightarrow evening$	0.2	$N \rightarrow flight$	0.1
$PN \rightarrow Kim$	0.15	$V \rightarrow booked$	0.4	$Adj \rightarrow last$	0.1	$DT \rightarrow the$	0.4

$$P(T) = 0.8 \times 0.35 \times 0.15 \times 0.5 \times 0.4 \times 0.2 \times 0.4 \times 0.4 \times 0.1 \times 0.1 = 2.7 \times 10^{-6}$$

We can use Treebanks to estimate the probabilities for CFG rules:

$$P(X \rightarrow Y_1 \dots Y_n) = \frac{\text{Count}(X \rightarrow Y_1 \dots Y_n)}{\text{Count}(X)}$$

## Example:

[*S* [*NP* [*DT* This] [*N* text]] [*VP* [*V* is] [[*Adv* just ] [*NP* [*DT* an] [*N* example]]]]]. [*S* [*NP* [*PRN* I]] [*VP* [*V* made] [*NP* [*PRN* it]] [*RP* up]]].

$$P(\text{NP} \rightarrow \text{DT N}) = \frac{2}{4} = 0.5$$

## Penn Treebank:

```
1 (S (NP-SBJ-1 Jones)
2   (VP followed
3     (NP him)
4     (PP-DIR into
5       (NP the front room))))
```

## Treebanks

- Linguistic Data Consortium ([LDC](#))
- European Language Resources Association ([ELRA](#))
- [Stanford list](#)
- [NLTK data](#)
- [Others](#)

Or you can use a statistical parser to automatically parse a corpus you wish to use.

- **Stanford Parser:**

```
1 java -cp stanford-parser.jar:stanford-parser-3.4.1-models.jar  
2 edu.stanford.nlp.parser.lexparser.LexicalizedParser -outputFormat penn  
3 edu/stanford/nlp/models/lexparser/englishPCFG.ser.gz input.txt >  
4 output.txt
```

- **Berkeley Parser: (demo)**

```
1 java -jar berkeleyParser/BerkeleyParser-1.7.jar -gr  
2 berkeleyParser/eng_sm6.gr < input.txt > output.txt
```

- More [here](#)

## Parsing PCFG with the CKY parser

We need:

- A CNF grammar augmented with probabilities
- A way to resolve ambiguity:  
if there are two categories of the same type in the same span,  
then discard the less likely one.



S <sub>[.7 × .1 × .00001 = .0000007]</sub>						
S <sub>[.7 × .1 × .0001 = .000007]</sub>	VP <sub>[.5 × .2 × .0001 = .00001]</sub>					
	VP <sub>[.1 × .000 × .01 = .000000]</sub>					
–	VP <sub>[.5 × .2 × .001 = .0001]</sub>	NP <sub>[.5 × .4 × .0009 = .0001]</sub>				
	VP <sub>[.1 × .000 × .072 = .000004]</sub>					
S <sub>[.7 × .1 × .006 = .0004]</sub>	–	NP <sub>[.5 × .4 × .006 = .001]</sub>	N <sub>[.3 × .3 × .01 = .0009]</sub>			
–	VP <sub>[.5 × .2 × .06 = .006]</sub>	–	N <sub>[.3 × .3 × .072 = .006]</sub>	PP <sub>[.9 × .4 × .03 = .01]</sub>		
–	–	NP <sub>[.5 × .4 × .3 = .06]</sub>	–	PP <sub>[.9 × .4 × .2 = .072]</sub>	NP <sub>[.5 × .2 × .3 = .03]</sub>	
NP <sub>[.1]</sub>	Adj <sub>[.1]</sub> TV <sub>[.2]</sub>	DT <sub>[.4]</sub>	N <sub>[.3]</sub>	P <sub>[.4]</sub>	DT <sub>[.2]</sub> NP <sub>[.2]</sub>	TV <sub>[.05]</sub> N <sub>[.3]</sub>
Mary	attacked	a	farmer	with	her	axe

S → NP VP [.7]    VP → DVP NP [.3]    VP → VP PP [.1]  
 VP → TV NP [.5]    NP → DT N [.5]    NP → Mary [.1]  
 NP → her [.2]    DT → a [.4]    DT → her [.2]  
 N → Adj N [.1]    N → N PP [.3]    N → farmer [.3]  
 N → axe [.3]    Adj → attacked [.1]    PP → P NP [.9]  
 P → with [.4]    TV → attacked [.2]    TV → axe [.05]

## Evaluating PCFGS (PARSEVAL)

How do the constituents in the hypothesis parse tree match the constituents in a hand-labeled 'gold standard' (reference) parse tree?

$T_C$  = set of constituents for S according to reference

$T_G$  = set of constituents hypothesized for S

### 1 labeled precision

$$\frac{|T_C \cap T_G|}{|T_G|} = \frac{\text{\#of correctly identified constituents}}{\text{\#of constituents hypothesized}} = \frac{t_p}{t_p + f_p}$$

### 2 labeled recall

$$\frac{|T_C \cap T_G|}{|T_C|} = \frac{\text{\#of correctly identified constituents}}{\text{\#of constituents in reference}} = \frac{t_p}{t_p + f_n}$$

**Rule of thumb:** as precision increases, recall drops and vice versa.

Often precision and recall are reported as a single number:

$$\textbf{F-measure} : F_{\beta} = \frac{(\beta^2 + 1) \times P \times R}{\beta^2 \times P + R}$$

$\beta > 1$  favors Recall

$\beta < 1$  favors Precision

## PROBLEMS WITH PCFGs

### Poor independence assumption

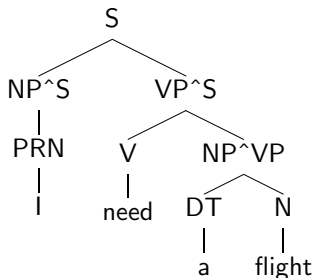
Linguistic structures are not independent from each other. For example, the distribution of  $NP \rightarrow PN$  is unbalanced:

91% of subject phrases are pronouns

34% of object phrases are pronouns

Solution: add information about the mother node in the daughters

*Parent annotation:*  $NP^S \rightarrow PRN$  [.91] vs.  $NP^{VP} \rightarrow PRN$  [.34]



## PROBLEMS WITH PCFGs (continued)

### **Lack of lexical conditioning**

Lexical items are important to resolve attachment ambiguities.

- (2) a. \*[Sam [dumped [the box into the bin]]].  
b. [Sam [dumped [the box] [into the bin]]].
- (3) a. [Sam [dumped [the box in the bin]]].  
b. [Sam [dumped [the box] [in the bin]]].
- (4) a. Sam likes [[green vegetables] and [music]].  
b. \*Sam likes [green [vegetables and music]].
- (5) a. \*I need some [fresh [air and sunshine]].  
b. I need some [[fresh air] and [sunshine]].

Solution: add information about the token in the mother node

## Dealing with the lack of lexical conditioning

*grammar lexicalization*

