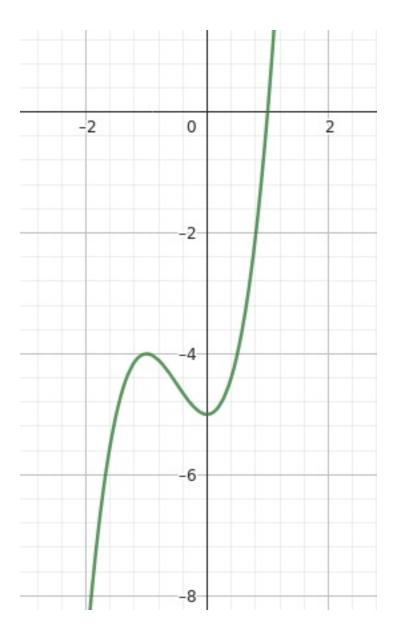
APLICACIONES DE LA DERIVADA

1. Calcula los intervalos de crecimiento y decrecimiento de las siguientes funciones:

i)
$$f(x) = 2x^3 + 3x^2 - 5$$

$$\int_{(x)}^{2} (x) = 6x^{2} + 6x = 6x (x + 1) = 3 \int_{(x)}^{2} (x) = 0 \quad \text{if } x = 6$$

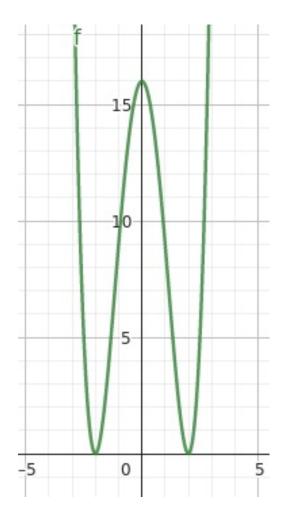
crevente Decrevente Crevente



ii)
$$f(x) = (x^2 - 4)^2$$

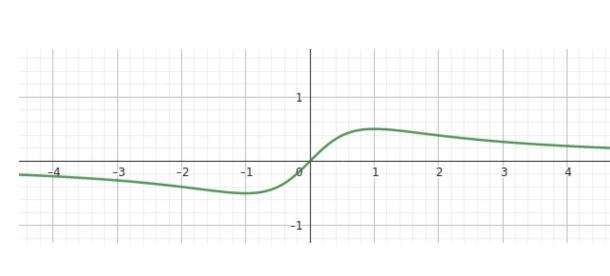
$$\int_{(x)}^{(x)} \int_{(x)}^{(x)} \int_$$

$$(-\infty, -2)$$
 $(-7, 0)$ $(0, 2)$ $(7, \infty)$
 $4x$ - + +
 $x-2$ - - +
 $x+2$ - + +
- +



$$v) \ f(x) = \frac{x}{x^2 + 1} \qquad \text{o} \qquad \text{for an } \mathbb{R}$$

$$(-\infty,-1), (=1,1), (1,+\infty)$$
 $(-1,-1), (=1,1), (=1,+\infty)$
 $(-1,+\infty)$
 $(-1,+\infty)$



vi)
$$f(x) = \frac{4x+5}{2x-3}$$
 $f(x) = \frac{4(2x-3)-2(4x+5)}{(2x-3)^2}$
 $f(x) = \frac{4(2x-3)-2(4x+5)}{(2x-3)^2}$
 $f(x) = \frac{4(2x-3)-2(4x+5)}{(2x-3)^2}$
 $f(x) = \frac{4(2x-3)-2(4x+5)}{(2x-3)^2}$
 $f(x) = \frac{2}{(2x-3)^2}$
 $f(x) = \frac{2}{(2x-3)^2}$

viii)
$$f(x) = x^2 e^x$$
 => (online en \mathbb{R} (g denouble) per suto en \mathbb{R} (g denouble) per suto en \mathbb{R} (g denouble) per suto en \mathbb{R} denouble \mathbb{R} (\mathbb{R}) = \mathbb{R} en \mathbb{R} denouble \mathbb{R} (\mathbb{R}) = \mathbb{R} en \mathbb{R} denouble \mathbb{R} (\mathbb{R}) = \mathbb{R} = \mathbb{R} (\mathbb{R}) = \mathbb{R} = \mathbb{R} (\mathbb{R}) = \mathbb{R} = \mathbb{R} (\mathbb{R}) = \mathbb{R} = \mathbb{R} = \mathbb{R} (\mathbb{R}) = \mathbb{R} =

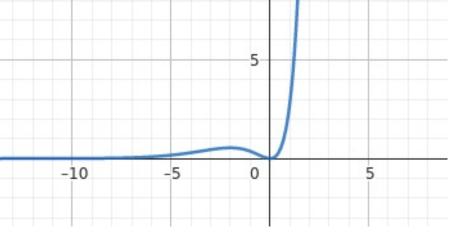
(g derivable) per sito
en en dominio

$$7 \times + \times^{2} = 0$$

$$2^{\times} > 0 \qquad \times (2 + \times) = 0$$

$$4 = 0, x = 2$$

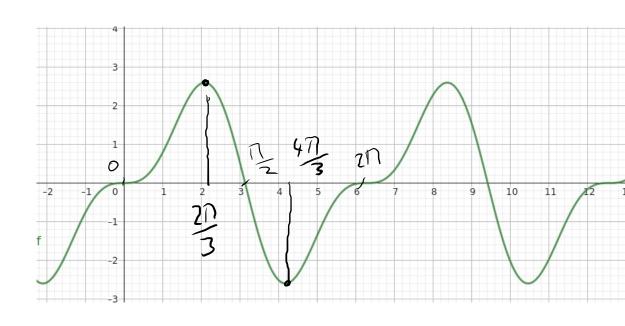
les verente en (-00, -2) y (6, +00) per decreviente en (-2, 0)



ix)
$$f(x) = \frac{e^x}{x^3}$$
 — I en contine en \mathbb{R}^-409 pr sulo en \mathbb{R}^-409 pr sulo en \mathbb{R}^-409 pr decisio \mathbb{R}^-409 \mathbb{R}^-409

tule 1° Vuetta y en calianes s'(x)=0 ni x=0, x-77, x4p 1(x) - 2(cos x - cos 2x)

$\left(0,\frac{21}{3}\right)$	$\left(\frac{2}{50},\frac{2}{50}\right)$	$\left(\frac{3}{3},50\right)$
2	+	+
Cosx-cos2x +	-	+
900	1800	27-0
0-(-1)	-/ - (+1)	0 - (-1)
(-2	+1
+		+
***		A



tu x= 27 => Maximo relation Eu x= 47 => Minimo relation

2. Halla los extremos relativos de las siguientes funciones:

i)
$$f(x) = -x^2 + 6x - 5$$

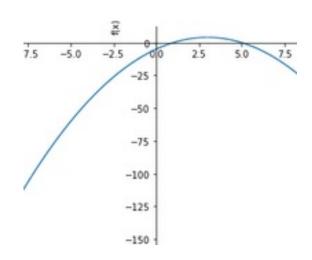
$$f(x) = -x^{2} + 6x - 5$$

$$f'(x) = 6 - 2x$$

$$f''(x) = -2$$

$$f''(3) = 0 \land f''(3) = -2$$

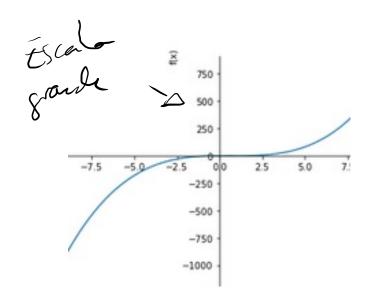
Hay un máximo relativo en (3, 4)

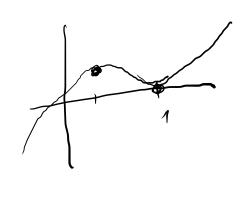


ii)
$$f(x) = x.(x-1)^2$$

$$f(x) = x(x-1)^2$$

 $f'(x) = (x-1)(3x-1)$
 $f''(x) = 6x - 4$
 $f'(\frac{1}{3}) = 0 \land f''(\frac{1}{3}) = -2$
Hay un máximo relativo en $(\frac{1}{3}, \frac{4}{27})$
 $f'(1) = 0 \land f''(1) = 2$
Hay un mínimo relativo en $(1, 0)$





iii)
$$f(x) = 2x^3-15x^2+36x-12$$

$$f(x) = 2x^3 - 15x^2 + 36x - 12$$

$$f'(x) = 6x^2 - 30x + 36$$

$$f''(x) = 12x - 30$$

$$f'(2) = 0 \land f''(2) = -6$$

Hay un máximo relativo en (2, 16)

$$f'(3) = 0 \land f''(3) = 6$$

Hay un mínimo relativo en (3, 15)

iv)
$$f(x) = \frac{2}{1+x^2}$$

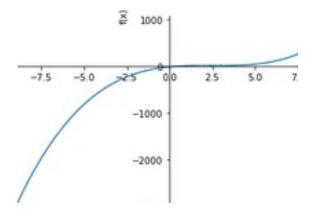
$$f'(x) = \frac{2}{x^2 + 1}$$

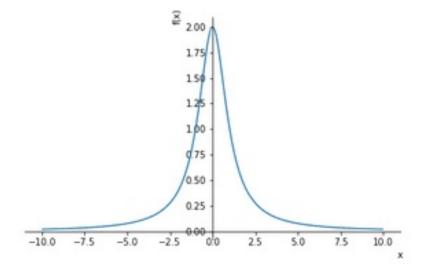
$$f'(x) = -\frac{4x}{(x^2 + 1)^2}$$

$$f''(x) = \frac{4(3x^2 - 1)}{(x^2 + 1)^3}$$

$$f'(0) = 0 \land f''(0) = -4$$

Hay un máximo relativo en (0, 2)





v)
$$f(x) = \frac{8x}{x^2 + 2}$$

$$f(x) = \frac{8x}{x^2 + 2}$$

$$f'(x) = \frac{8(2-x^2)}{x^4+4x^2+4}$$

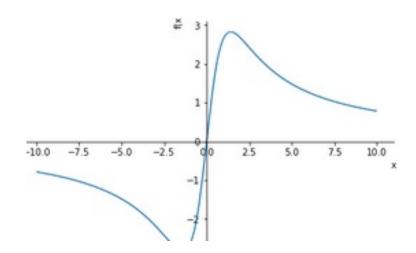
$$f''(x) = \frac{16x(x^2-6)}{(x^2+2)^3}$$

$$f'(-\sqrt{2})=0\wedge f''(-\sqrt{2})=\sqrt{2}$$

Hay un mínimo relativo en $(-\sqrt{2}, -2\sqrt{2})$

$$f'(\sqrt{2}) = 0 \wedge f''(\sqrt{2}) = -\sqrt{2}$$

Hay un máximo relativo en $(\sqrt{2},2\sqrt{2})$



vi)
$$f(x) = x.\ln x$$

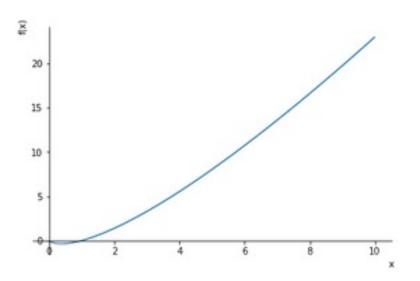
$$f'(x) = x \log(x)$$

$$f'(x) = \log(x) + 1$$

$$f''(x) = \frac{1}{x}$$

$$f'(e^{-1}) = 0 \land f''(e^{-1}) = e$$

Hay un mínimo relativo en $(e^{-1}, -\frac{1}{e})$



vii)
$$f(x) = x^2 e^x$$

$$f(x) = x^2 e^x$$

$$f'(x) = x(x+2)e^x$$

$$f''(x) = (x^2 + 4x + 2)e^x$$

$$f'(-2) = 0 \wedge f''(-2) = -\frac{2}{\epsilon^2}$$

Hay un máximo relativo en $(-2, \frac{4}{e^2})$

$$f'(0) = 0 \wedge f''(0) = 2$$

Hay un mínimo relativo en (0, 0)

viii)
$$f(x) = \frac{x}{\ln x}$$

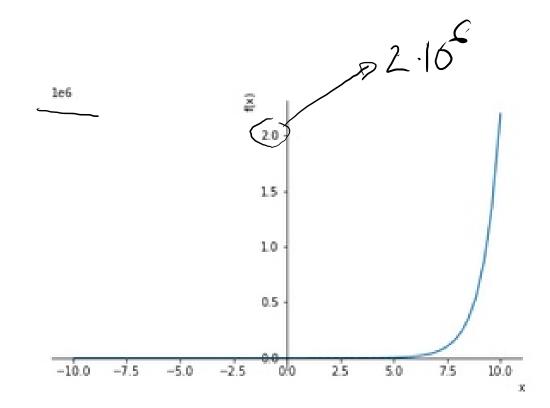
$$f(x) = \frac{x}{\log(x)}$$

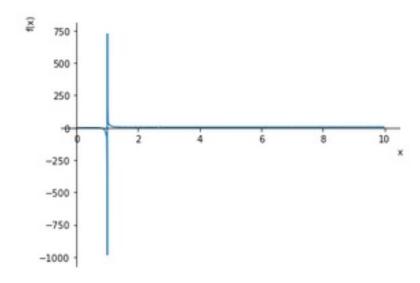
$$f'(x) = \frac{\log(x)-1}{\log(x)^2}$$

$$f''(x) = \frac{2 - \log(x)}{x \log(x)^3}$$

$$f'(e) = 0 \wedge f''(e) = e^{-1}$$

Hay un mínimo relativo en (e, e)





$$ix) f(x) = x - sen x$$

$$f(x) = x - \sin(x)$$

$$f'(x) = 1 - \cos(x)$$

$$f''(x) = \sin(x)$$

Candidely
$$\longrightarrow f'(0) = 0 \land f''(0) = 0$$

No hay mínimo ni máximo en (0,0)

$$\int^{\Lambda} \int_{\mathcal{U}} \int_{\mathcal{U}} f'(2\pi) = 0 \wedge f''(2\pi) = 0$$

No hay mínimo ni máximo en $(2\pi, 2\pi)$

$$x) f(x) = x + \cos x$$

$$f(x) = x + \cos(x)$$

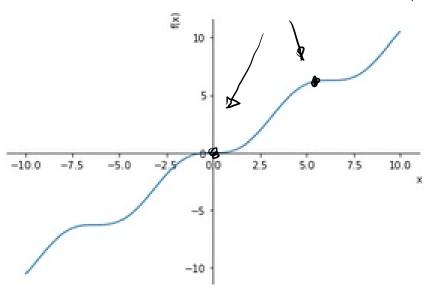
$$f'(x) = 1 - \sin(x)$$

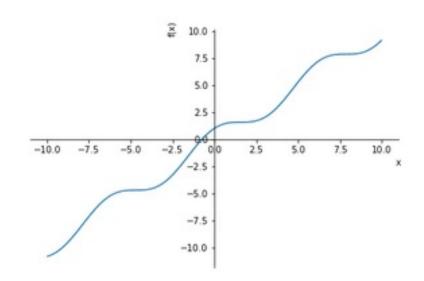
$$f''(x) = -\cos(x)$$

$$f'(\frac{\pi}{2}) = 0 \wedge f''(\frac{\pi}{2}) = 0$$

No hay mínimo ni máximo en $(\frac{\pi}{2}, \frac{\pi}{2})$

Pto de inflexión





xi) f(x) = 2.sen x - sen 2x

$$f(x) = 2\sin(x) - \sin(2x)$$

$$f'(x) = 2\cos(x) - 2\cos(2x)$$

$$f''(x) = 2(4\cos(x) - 1)\sin(x)$$

$$f'(0) = 0 \wedge f''(0) = 0$$

No hay mínimo ni máximo en (0,0)

$$f'(-\frac{4\pi}{3}) = 0 \wedge f''(-\frac{4\pi}{3}) = -3\sqrt{3}$$

Hay un máximo relativo en $\left(-\frac{4\pi}{3}, \frac{3\sqrt{3}}{2}\right)$

$$f'(-\frac{2\pi}{3}) = 0 \wedge f''(-\frac{2\pi}{3}) = 3\sqrt{3}$$

Hay un mínimo relativo en $\left(-\frac{2\pi}{3}, -\frac{3\sqrt{3}}{2}\right)$

$$f'(\frac{2\pi}{3}) = 0 \wedge f''(\frac{2\pi}{3}) = -3\sqrt{3}$$

Hay un máximo relativo en $(\frac{2\pi}{3}, \frac{3\sqrt{3}}{2})$

$$f'(\frac{4\pi}{3}) = 0 \wedge f''(\frac{4\pi}{3}) = 3\sqrt{3}$$

Hay un mínimo relativo en $(\frac{4\pi}{3}, -\frac{3\sqrt{3}}{2})$

$$f'(2\pi) = 0 \wedge f''(2\pi) = 0$$

No hay mínimo ni máximo en $(2\pi, 0)$

