

1. p019e01 - Resuelve los sistemas:

(a)
$$\begin{cases} 3x - 2y = 1 \\ x + 6y = 7 \end{cases}$$

Sol:
$$\begin{bmatrix} 3 & -2 & 1 \\ 0 & \frac{20}{3} & \frac{20}{3} \end{bmatrix} \rightarrow$$

 $\{x : 1, \quad y : 1\}$

(b)
$$\begin{cases} 6x - 2y = 14 \\ 3x - y = 7 \end{cases}$$

Sol:
$$\begin{bmatrix} 6 & -2 & 14 \\ 0 & 0 & 0 \end{bmatrix} \rightarrow$$

 $\{x : \frac{y}{3} + \frac{7}{3}\}$

(c)
$$\begin{cases} 6x - 2y = 9 \\ 3x - y = 10 \end{cases}$$

Sol:
$$\begin{bmatrix} 6 & -2 & 9 \\ 0 & 0 & \frac{11}{2} \end{bmatrix} \rightarrow$$

 \emptyset

(d)
$$\begin{cases} 4x + 7y = -3 \\ 7x + 4y = 36 \end{cases}$$

Sol:
$$\begin{bmatrix} 4 & 7 & -3 \\ 0 & -\frac{33}{4} & \frac{165}{4} \end{bmatrix} \rightarrow$$

 $\{x : 8, \quad y : -5\}$

(e)
$$\begin{cases} 4x + 16 = 5y \\ 5y - 19 = 3x \end{cases}$$

Sol:
$$\begin{bmatrix} -5 & 4 & -16 \\ 0 & 1 & 3 \end{bmatrix} \rightarrow$$

 $\{x : 3, \quad y : \frac{28}{5}\}$

(f)
$$\begin{cases} x - 5 = y + 2 \\ 1 + 3x + 2y = x - 4 \end{cases}$$

Sol:
$$\begin{bmatrix} 1 & -1 & 7 \\ 0 & 4 & -19 \end{bmatrix} \rightarrow$$

 $\{x : \frac{9}{4}, \quad y : -\frac{19}{4}\}$

(g)
$$\begin{cases} x - 5 = y + 2 \\ 3x - 2y = x - 5 \end{cases}$$

Sol:
$$\begin{bmatrix} 1 & -1 & 7 \\ 0 & 0 & -19 \end{bmatrix} \rightarrow$$

 \emptyset

(h)
$$\begin{cases} x + 3y = 6 \\ 6y - 5 = 7 - 2x \end{cases}$$

Sol:
$$\begin{bmatrix} 3 & 1 & 6 \\ 0 & 0 & 0 \end{bmatrix} \rightarrow$$

 $\{x : -3y + 6\}$

(i)
$$\begin{cases} x - y = 8 \\ x + y = 24 \end{cases}$$

Sol:
$$\begin{bmatrix} 1 & -1 & 8 \\ 0 & 2 & 16 \end{bmatrix} \rightarrow$$

 $\{x : 16, \quad y : 8\}$

(j)
$$\begin{cases} x + 2y = 11 \\ 2x - y = 2 \end{cases}$$

Sol:
$$\begin{bmatrix} 1 & 2 & 11 \\ 0 & -5 & -20 \end{bmatrix} \rightarrow$$

 $\{x : 3, \quad y : 4\}$

(k)
$$\begin{cases} 3x - 4y = -9 \\ 2x + y = 5 \end{cases}$$

Sol:
$$\begin{bmatrix} 3 & -4 & -9 \\ 0 & \frac{11}{3} & 11 \end{bmatrix} \rightarrow$$

 $\{x : 1, \quad y : 3\}$

(l)
$$\begin{cases} 10(x - 2) + y = 1 \\ x + 3(x - y) = 5 \end{cases}$$

Sol:
$$\begin{bmatrix} 1 & 0 & 5 \\ 0 & 1 & 1 \end{bmatrix} \rightarrow$$

 $\{x : 2, \quad y : 1\}$

(m)
$$\begin{cases} \frac{x-y}{2} + \frac{x-y}{3} = 5 \\ \frac{x+y}{4} + y = 3 \end{cases}$$

Sol:
$$\begin{bmatrix} 0 & 1 & 3 \\ 0 & 0 & 5 \end{bmatrix} \rightarrow$$

 $\{x : \frac{29}{5}, \quad y : -\frac{1}{5}\}$

$$(n) \quad \begin{cases} \frac{3(y+2x+2)}{4} = \frac{4x+y-1}{3} \\ \frac{1}{3}(x+y) - \frac{1}{6}(x-y) = \frac{y-1}{6} \end{cases}$$

$$\text{Sol: } \begin{bmatrix} -\frac{4}{3} & -\frac{1}{3} & -\frac{1}{3} \\ 0 & \frac{1}{24} & -\frac{1}{8} \end{bmatrix} \rightarrow \{x : 39, \quad y : -20\}$$

$$(o) \quad \begin{cases} \frac{3-2y}{4} - \frac{1}{4} = \frac{1-2x}{6} \\ \frac{25}{8} - 1 = \frac{x+3}{2} - \frac{3(1+y)}{8} \end{cases}$$

$$\text{Sol: } \begin{bmatrix} \frac{3}{8} & \frac{x}{2} - \frac{25}{8} + \frac{17}{8} \\ 0 & -\frac{x}{3} + \frac{5}{12} \end{bmatrix} \rightarrow \{x : 5, \quad y : 4\}$$

$$(\tilde{n}) \quad \begin{cases} x - 2(x+y) = 3y - 2 \\ \frac{x}{3} + \frac{y}{2} = 3 \end{cases}$$

$$\text{Sol: } \begin{bmatrix} 1 & -3 & -2 \\ 0 & \frac{3}{2} & \frac{11}{3} \end{bmatrix} \rightarrow \{x : 12, \quad y : -2\}$$

$$(p) \quad \begin{cases} \frac{4y-5x}{6} + \frac{3x-2y}{2} = 1 - \frac{2}{9}(x+y) \\ \frac{4y+x-8}{8} - x = \frac{2(y-2x)}{3} \end{cases}$$

$$\text{Sol: } \begin{bmatrix} \frac{2}{9} & \frac{2}{9} & 1 \\ 0 & 1 & 3 \end{bmatrix} \rightarrow \{x : \frac{4}{7}, \quad y : -\frac{31}{7}\}$$

2. p021e23 - Resuelve los sistemas:

$$(a) \quad \begin{cases} x - 2y + 5z = 13 \\ 2x - 5y + z = 19 \\ x + 3y - 2z = -4 \end{cases}$$

$$\text{Sol: } \begin{bmatrix} -2 & 5 & 1 & 13 \\ 0 & -\frac{23}{2} & -\frac{1}{2} & -\frac{27}{2} \\ 0 & 0 & \frac{52}{23} & \frac{208}{23} \end{bmatrix} \rightarrow \{x : 4, \quad y : -2, \quad z : 1\}$$

$$(b) \quad \begin{cases} x - y + z = 7 \\ x + y - 3z = 1 \\ 2x + y - 4z = 5 \end{cases}$$

$$\text{Sol: } \begin{bmatrix} -1 & 1 & 1 & 7 \\ 0 & -2 & 2 & 8 \\ 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \{x : z + 4, \quad y : 2z - 3\}$$

$$(c) \quad \begin{cases} x - 2y + z = 13 \\ 3x - 4y + 2z = 1 \\ 2x - 2y + z = 0 \end{cases}$$

$$\text{Sol: } \begin{bmatrix} -2 & 1 & 1 & 13 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -25 \end{bmatrix} \rightarrow \emptyset$$

$$(d) \quad \begin{cases} x - y + z = 1 \\ x + z = 4 \\ y - 3z = -15 \end{cases}$$

$$\text{Sol: } \begin{bmatrix} -1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 4 \\ 0 & 0 & 3 & -6 \end{bmatrix} \rightarrow \{x : -2, \quad y : 3, \quad z : 6\}$$

$$(e) \quad \begin{cases} 2x - y + z = 6 \\ x + y - 2z = 1 \\ x - 2y + 3z = 0 \end{cases}$$

$$\text{Sol: } \begin{bmatrix} -1 & 1 & 2 & 6 \\ 0 & -1 & 3 & 7 \\ 0 & 0 & 9 & 21 \end{bmatrix} \rightarrow \emptyset$$

$$(f) \quad \begin{cases} x + 2y - 3z = 9 \\ 2x - y = 6 \\ 4x + 3y - 6z = 24 \end{cases}$$

$$\text{Sol: } \begin{bmatrix} 2 & -3 & 1 & 9 \\ 0 & -\frac{3}{2} & \frac{5}{2} & \frac{21}{2} \\ 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow \{x : \frac{3z}{5} + \frac{21}{5}, \quad y : \frac{6z}{5} + \frac{12}{5}\}$$

$$(g) \quad \begin{cases} 4x - 2y = 2 \\ 6y - 3z = 1 \\ 3z - 4x = -1 \end{cases}$$

$$\text{Sol: } \begin{bmatrix} -2 & 0 & 4 & 2 \\ 0 & -3 & 12 & 7 \\ 0 & 0 & 8 & 6 \end{bmatrix} \rightarrow$$

$$\{x : \frac{3}{4}, \quad y : \frac{1}{2}, \quad z : \frac{2}{3}\}$$

$$(h) \quad \begin{cases} x + 2y = 5 \\ 2x + y = -1 \\ -x + 3y = 6 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} 1 & 2 & 5 \\ 0 & -3 & -11 \\ 0 & 0 & -\frac{22}{3} \end{bmatrix} \rightarrow$$

□

$$(i) \quad \begin{cases} x - 3y = 1 \\ 4y - z = 1 \\ 2x - z = 1 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} -3 & 0 & 1 & 1 \\ 0 & -1 & \frac{4}{3} & \frac{7}{3} \\ 0 & 0 & \frac{2}{3} & -\frac{4}{3} \end{bmatrix} \rightarrow$$

$$\{x : -2, \quad y : -1, \quad z : -5\}$$

$$(j) \quad \begin{cases} x + 2 = -y \\ -y + 3 = 2x \\ 4x - y = 6 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} 1 & 1 & -2 \\ 0 & 1 & -7 \\ 0 & 0 & -21 \end{bmatrix} \rightarrow$$

□

$$(k) \quad \begin{cases} x - 2y + 3z = 2 \\ 2x - 3y + z = 1 \\ 3x - y + 2z = 9 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} -2 & 3 & 1 & 2 \\ 0 & -\frac{7}{2} & \frac{1}{2} & -2 \\ 0 & 0 & \frac{18}{7} & \frac{54}{7} \end{bmatrix} \rightarrow$$

$$\{x : 3, \quad y : 2, \quad z : 1\}$$

$$(l) \quad \begin{cases} x - 6 + y = 0 \\ -3y + x - 2 = 0 \\ 5x - 26 + y = 0 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 2 \\ 0 & 0 & 0 \end{bmatrix} \rightarrow$$

$$\{x : 5, \quad y : 1\}$$

$$(m) \quad \begin{cases} 2x + 2y = -2 \\ x + 6 = y \\ 3x + 5y = 1 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} 2 & 2 & -2 \\ 0 & -2 & -5 \\ 0 & 0 & -1 \end{bmatrix} \rightarrow$$

□

$$(n) \quad \begin{cases} x + y + z = 4 \\ x - 2y + 3z = 13 \\ x + 3y + 4z = 11 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} 1 & 1 & 1 & 4 \\ 0 & 5 & 3 & 21 \\ 0 & 0 & -\frac{13}{5} & -\frac{26}{5} \end{bmatrix} \rightarrow$$

$$\{x : 2, \quad y : -1, \quad z : 3\}$$

$$(\tilde{n}) \quad \begin{cases} z - 2(x + y) = -9 \\ 3x - y = 3 \\ 3y - z = 9 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} -1 & 0 & 3 & 3 \\ 0 & 1 & 0 & -9 \\ 0 & 0 & 9 & 9 \end{bmatrix} \rightarrow$$

$$\{x : 3, \quad y : 6, \quad z : 9\}$$

$$(o) \quad \begin{cases} \frac{x}{2} + \frac{y}{3} + z = 7 \\ x - \frac{y}{2} + \frac{z}{3} = 11 \\ \frac{x}{3} - y - \frac{z}{2} = 5 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} \frac{1}{3} & 1 & \frac{1}{2} & 7 \\ 0 & \frac{11}{6} & \frac{7}{4} & \frac{43}{2} \\ 0 & 0 & -\frac{73}{132} & -\frac{73}{22} \end{bmatrix} \rightarrow$$

$$\{x : 6, \quad y : -6, \quad z : 6\}$$

$$(p) \quad \begin{cases} \frac{x}{2} + \frac{y}{3} + \frac{z}{3} = 9 \\ \frac{x}{3} - \frac{y}{9} + \frac{z}{3} = 6 \\ \frac{x}{6} + \frac{y}{2} + \frac{z}{2} = 13 \end{cases}$$

$$\text{Sol:} \quad \begin{bmatrix} \frac{1}{3} & \frac{1}{3} & \frac{1}{2} & 9 \\ 0 & \frac{4}{9} & \frac{1}{2} & 9 \\ 0 & 0 & -\frac{7}{12} & -\frac{1}{2} \end{bmatrix} \rightarrow$$

$$\{x : \frac{6}{7}, \quad y : \frac{45}{7}, \quad z : \frac{135}{7}\}$$

$$(q) \quad \begin{cases} x - y + z = 5 \\ \frac{x-1}{2} + \frac{y}{3} = 1 \\ \frac{2x+y}{6} - \frac{3z+y}{8} = 4 \end{cases}$$

$$\text{Sol: } \begin{bmatrix} -1 & 1 & 1 & 5 \\ 0 & \frac{1}{3} & \frac{1}{3} & \frac{8}{3} \\ 0 & 0 & \frac{3}{8} & \frac{59}{8} \end{bmatrix} \rightarrow \left\{ x : \frac{177}{29}, \quad y : -\frac{135}{29}, \quad z : -\frac{167}{29} \right\}$$