Departamento de Matemáticas 1º Bachillerato



5 - Fracciones Algebraicas

1. p014e01y3 - Comprueba si son equivalentes las siguientes fracciones algebraicas:

(a)
$$\frac{x^2-1}{x+3} y \frac{x^3+2x^2-x-2}{x^2+5x+6}$$

Sol:
$$\frac{\left(-x+\left(x^3+2x^2\right)\right)-2}{\left(x^2+5x\right)+6} - \frac{x^2-1}{x+3} = 0$$

(b)
$$\frac{x^2-4}{x^2-2x} y \frac{x+2}{x}$$

Sol:
$$-\frac{x^2-4}{x^2-2x} + \frac{x+2}{x} = 0$$

2. p014e04 - Obtén la fracción irreducible (simplifica) equivalente a las fracciones algebraicas:

(a)
$$\frac{2x^3 - 5x^2 - 23x - 10}{x^3 + 3x^2 - 4x - 12}$$

Sol:
$$\frac{2x^2-9x-5}{x^2+x-6}$$

(c)
$$\frac{x^2+3x-4}{x^3-x}$$

Sol:
$$\frac{x+4}{x^2+x}$$

(b)
$$\frac{x^3 - 16x}{x^3 + 3x^2 - 4x}$$

Sol:
$$\frac{x-4}{x-1}$$

$$(d) \quad \frac{x^3 - 1}{x^2 - x}$$

Sol:
$$\frac{x^2 + x + 1}{x}$$

3. p015e05 - Simplifica las siguientes fracciones algebraicas:

(a)
$$\frac{x^2-9}{x+3}$$

Sol:
$$x - 3$$

$$(x)$$
 $2x-5$

Sol: $\frac{x-3}{x+2}$

Sol: $\frac{2}{2x^2-2}$

(b)
$$\frac{x^2-1}{x^3-x}$$

Sol:
$$\frac{1}{x}$$

(g)
$$\frac{2x-5}{2x^3-5x^2-2x+5}$$

$$(h)$$
 $x-2$

(c)
$$\frac{x^4 - 4x^2 + 4x^2}{x^4 - 4}$$

Sol:
$$\frac{x^2-2}{x^2+2}$$

(h)
$$\frac{x-2}{x^2-4}$$

Sol:
$$\frac{1}{x+2}$$

(d)
$$\frac{3x^2+x}{3x^3+x^2-12x-4}$$

Sol:
$$\frac{3x}{3x^2-12}$$

$$(i) \quad \frac{x^2-2}{x-\sqrt{2}}$$

Sol:
$$x + \sqrt{2}$$

(e)
$$\frac{2x^3+3x^2-8x+3}{2x^3-x^2-2x-1}$$

Sol:
$$\frac{2x^3+3x^2-8x+3}{2x^3-x^2-2x-1}$$

(j)
$$\frac{x^2+2x+1}{x^2-1}$$

Sol:
$$\frac{x+1}{x-1}$$

(k)
$$\frac{x^3 - 2x^2 - 5x + 6}{x^2 + x - 2}$$

Sol:
$$x - 3$$

(f)

4. p015e07 - Calcula, simplificando el resultado:

(a)
$$\frac{2}{x+7} + \frac{x+4}{x-7}$$

Sol:
$$\frac{x^2+13x+14}{x^2-49}$$

(b)
$$\frac{1}{x+5} + \frac{x}{x^2+10x+25}$$

Sol:
$$\frac{2x+5}{x^2+10x+25}$$

(c)
$$\frac{1}{x+5} - \frac{x}{x^2+10x+25}$$

Sol:
$$\frac{5}{x^2+10x+25}$$

(d)
$$\frac{12}{x-3} + \frac{x+4}{2x+1} - \frac{x}{x^2-6x+9}$$

Sol:
$$\frac{x^3 + 20x^2 - 76x}{2x^3 - 11x^2 + 12x + 9}$$

(e)
$$\frac{1}{x-1} \cdot \frac{x^2-1}{x+2} \cdot \frac{x+2}{x-3}$$

Sol:
$$\frac{x+1}{x-3}$$

(f)
$$\frac{2x+1}{x} \cdot \frac{x^2-3x}{4x^2-1}$$

Sol:
$$\frac{2x-6}{4x-2}$$

$$(g) \quad \frac{3x-1}{x} \cdot \frac{x^2}{9x^2-1}$$

Sol:
$$\frac{3x}{9x+3}$$

(h)
$$7x : \frac{x^2 - 4x}{x - 2}$$

Sol:
$$\frac{7x-14}{x-4}$$

(i)
$$\frac{x-3}{x-1}$$
: $\frac{x^2-3x}{x^2-1}$

Sol:
$$\frac{x+1}{x}$$

(j)
$$\frac{x^2-3x-4}{x}$$
: $\frac{x+1}{x^2+2x}$

Sol:
$$x^2 - 2x - 8$$

5. p015e09 - Efectúa simplificando el resultado si es posible:

(a)
$$\frac{x}{x+1} + \frac{3x}{x^2-1} - \frac{1}{x-1}$$

Sol:
$$\frac{x^2+x-1}{x^2-1}$$

(b)
$$\frac{x}{x^2-5x+6} + \frac{2}{x-3} - \frac{3}{x-2}$$

Sol:
$$\frac{5}{x^2-5x+6}$$

(c)
$$\frac{2}{x-2} + \frac{1}{x+2} - \frac{x-1}{x^2-4}$$

Sol:
$$\frac{2x+3}{x^2-4}$$

(d)
$$\frac{x}{x^2-9x+20} - \frac{1}{x^2-11x+30} + \frac{2}{x^2-10x+24}$$

Sol:
$$\frac{x+1}{x^2-9x+20}$$

(e)
$$\frac{x^2+3x+2}{x^2-3x+2} \cdot \frac{x^2-1}{x^2-x-6}$$

Sol:
$$\frac{x^2+2x+1}{x^2-5x+6}$$

(f)
$$\frac{3x-2}{10x+4} \cdot \frac{4x}{6x-4}$$

Sol:
$$\frac{x}{5x+2}$$

(g)
$$\frac{3x^2+5x-2}{x^4+2x^2-15}$$
: $\frac{9x^2-6x+1}{x^4+5x^2}$

Sol:
$$\frac{3x^3+6x^2}{9x^3-3x^2-27x+9}$$

(h)
$$\frac{x}{x^2+5x+6} - \frac{2}{x+2} + \frac{3}{x+3}$$

Sol:
$$\frac{2x}{x^2+5x+6}$$

(i)
$$\frac{x^2-2x-3}{x^2-5x} \cdot \frac{x^2-4x-5}{x^2-4x+3}$$

Sol:
$$\frac{x^2+2x+1}{x^2-x}$$

(j)
$$\frac{x^2-4}{x^3-x^2+3x-3}$$
 : $\frac{x^2-3x+2}{x^3+3x}$

Sol:
$$\frac{x^2+2x}{x^2-2x+1}$$

(k)
$$\frac{x}{x^2-2x+1} - \frac{x-3}{x^2-x}$$

Sol:
$$\frac{4x-3}{x^3-2x^2+x}$$

(1)
$$\frac{x+1}{x^2-4} + \frac{2x-1}{x^2+2x} + \frac{3x-2}{x^2-2x}$$

Sol:
$$\frac{6x^2-2}{x^3-4x}$$

$$\left(\mathbf{m}\right) \quad \frac{\frac{x+1}{x^2}}{\frac{x^2-1}{x^3}}$$

Sol:
$$\frac{x}{x-1}$$

(n)
$$\left(\frac{1}{x^2-1}\right)$$
: $\frac{1}{\frac{1}{1+x^2} + \frac{2x^2}{1-x^4}}$

Sol:
$$-\frac{1}{x^4-2x^2+1}$$

$$\left(\tilde{\mathbf{n}}\right) \quad \frac{x}{1 + \frac{1}{1 + \frac{1}{x}}}$$

Sol:
$$\frac{x^2+x}{2x+1}$$

$$\text{(o)} \quad \frac{\frac{1}{x-2} - \frac{1}{x+2}}{1 - \frac{4}{x^2 - 4}}$$

Sol:
$$\frac{4}{x^2-8}$$

$$\left(\mathbf{p}\right) \quad \frac{1}{\frac{x+1}{x-1} - \frac{x-1}{x+1}}$$

Sol:
$$\frac{x^2-1}{4x}$$

(q)
$$(x^3 + x) : (1 - \frac{2x}{2x + \frac{2}{x}})$$

Sol:
$$x^5 + 2x^3 + x$$

(r)
$$(\frac{1}{x} - \frac{1}{x+1})(x - \frac{x+1}{x-1})$$

Sol:
$$\frac{x^2-2x-1}{x^3-x}$$

(s)
$$\frac{1}{x}(\frac{2}{x} - \frac{3}{x+1}) - \frac{x+1}{x}(3 - \frac{4}{x+1})$$

Sol:
$$-\frac{3x^3+2x^2-2}{x^3+x^2}$$

$$(t) \quad \frac{\frac{x-1}{x+2} - \frac{x+2}{x-1}}{1 - \frac{1}{x-1}}$$

Sol:
$$-\frac{6x+3}{x^2-4}$$