Departamento de Matemáticas 1º Bachillerato



4 - Polinomios

1. p
012e03 - Dados los polinomios $A(x) = 2x^3 - 5x^2 + 6$, $B(x) = -\frac{1}{2}x^5 - x^4 + 6x$ halla:

(a)
$$A(x) + B(x)$$

Sol:
$$-\frac{x^5}{2} - x^4 + 2x^3 - 5x^2 + 6x + 6$$

(b)
$$A(x) - B(x)$$

Sol:
$$-\frac{x^5}{2} - x^4 + 2x^3 - 5x^2 + 6x + 6$$
 Sol: $\frac{x^5}{2} + x^4 + 2x^3 - 5x^2 - 6x + 6$

2. p012e04 - Dados los polinomios $A(x) = 3x^3 - 6x^2 + 2x - 1$, $B(x) = -x^4 + x^3 + x - 6$, $C(x) = -x^4 + x^3 + x - 6$ $x^4 - x^2 + x + \frac{1}{2}$ halla:

(a)
$$A(x) \cdot B(x)$$

Sol:
$$-3x^7 + 9x^6 - 8x^5 + 6x^4 - 25x^3 + 38x^2 - 13x + 6$$

(b)
$$A(x) - 3B(x) + 5C(x)$$
 (c) $x^2 \cdot A(x) + 3x \cdot B(x)$

Sol:
$$8x^4 - 11x^2 + 4x + \frac{39}{2}$$

(c)
$$x^2 \cdot A(x) + 3x \cdot B(x)$$

Sol:
$$-3x^4 + 2x^3 + 2x^2 - 18x$$

3. p012e07 - Halla el cociente y el resto de:

(a)
$$(5x^4 - 7x^2 + 6x + 1)$$

$$(x + 1)$$
 : (c) $(x - 1)$

$$(x^2 + 1)$$

Sol:
$$\left(\frac{5x^2}{3} - \frac{7}{3}, 6x + 1\right)$$

d)
$$(8x^6 - 5x^4 + 6) : (2x^2 - 6)$$

$$(x^9 - 7x + 1) \cdot (x^3 + x)$$

(b)
$$(7x^4 - 3x^2 + 6x - 1)$$

 $(x^2 - x + 3)$

Sol:
$$(7x^2 + 7x - 17,$$

Sol:
$$\left(4x^4 - \frac{x^2}{2} - \frac{1}{4},\right)$$

$$(3x^5 - 6x^2 + 9)$$

(a)
$$(5x^4 - 7x^2 + 6x + 1)$$
 : (c) $(x^6 - 5) : (x^2 - x)$ $(x^2 + 1)$ (3x²)

Sol: $(5x^4 - 7x^2 + 6x + 1)$: (d) $(8x^6 - 5x^4 + 6) : (2x^2 - (f))$ $(x^9 - 7x + 1) : (x^3 + x)$ (b) $(7x^4 - 3x^2 + 6x - 1)$: $(x^2 - x + 3)$ Sol: $(4x^4 - \frac{x^2}{2} - \frac{1}{4}, \frac{23}{4})$ Sol: $(7x^2 + 7x - 17, \frac{32x + 50}{6})$ (e) $(3x^5 - 6x^2 + 9)$:

4. p012e08 - Dados $A(x) = -x^3 + 2x^2 + 5$, $B(x) = 2x^4 + 3x + 6$ halla el valor numérico de ambos polinomios en:

(a)
$$x = 1$$

(c)
$$x = 2$$

(e)
$$x = \frac{1}{2}$$

Sol:
$$\frac{43}{8}$$
 y $\frac{61}{8}$

(b)
$$x = -1$$

(d)
$$x = -2$$

(f)
$$x = -\frac{1}{2}$$

Sol:
$$\frac{45}{8}$$
 $y \frac{37}{8}$

5. p012e09 - Halla, para cada uno de los siguientes polinomios, sus raíces:

(a)
$$x^2 - 1$$

Sol: $\{-1,1\}$

Sol: $\{-\sqrt{7}, \sqrt{7}\}$

Sol: $\{-2,2\}$

(b)
$$x^2 - 7$$

(c) $3x^2 - 12$

(d) $5x^2 - 25$

Sol: $\{-\sqrt{5}, \sqrt{5}\}$

6. p
012e10 - ¿Tiene el polinomio $A(x) = x^4 + 3$ alguna raíz real?

(a)
$$x^4 + 3$$

Sol:
$$\left\{-\frac{\sqrt{2}\sqrt[4]{3}}{2} - \frac{\sqrt{2}\sqrt[4]{3}i}{2}, -\frac{\sqrt{2}\sqrt[4]{3}i}{2} + \frac{\sqrt{2}\sqrt[4]{3}i}{2}, \frac{\sqrt{2}\sqrt[4]{3}i}{2} - \frac{\sqrt{2}\sqrt[4]{3}i}{2}, \frac{\sqrt{2}\sqrt[4]{3}i}{2} + \frac{\sqrt{2}\sqrt[4]{3}i}{2}\right\}$$