Departamento de Matemáticas $1^{\underline{0}}$ Bachillerato



5 - Fracciones Algebraicas

1. p014e01y3 - Comprueba si son equivalentes las siguientes fracciones algebraicas:

(a)
$$\frac{x^2-1}{x+3} y \frac{x^3+2x^2-x-2}{x^2+5x+6}$$

Sol: 0

(b)
$$\frac{x^2-4}{x^2-2x} y \frac{x+2}{x}$$

Sol: 0

2. p014e04 - Obtén la fracción irreducible (simplifica) equivalente a las fracciones algebraicas:

(a)
$$\frac{2x^3 - 5x^2 - 23x - 10}{x^3 + 3x^2 - 4x - 12}$$

Sol:
$$\frac{2x^2-9x-5}{x^2+x-6}$$

(c)
$$\frac{x^2+3x-4}{x^3-x}$$

Sol:
$$\frac{x+4}{x^2+x}$$

(b)
$$\frac{x^3-16x}{x^3+3x^2-4x}$$

Sol:
$$\frac{x-4}{x-1}$$

$$(d) \quad \frac{x^3 - 1}{x^2 - x}$$

Sol:
$$\frac{x^2 + x + 1}{x}$$

3. p014e05 - Simplifica las siguientes fracciones algebraicas:

(a)
$$\frac{x^2-9}{x+3}$$

Sol:
$$x - 3$$

Sol:
$$\frac{x-3}{x+2}$$

(b)
$$\frac{x^2-1}{x^3-x}$$

Sol:
$$\frac{1}{x}$$

(g)
$$\frac{2x-5}{2x^3-5x^2-2x+5}$$

Sol:
$$\frac{2}{2x^2-2}$$

(c)
$$\frac{x^4 - 4x^2 + 4}{x^4 - 4}$$

Sol:
$$\frac{x^2-2}{x^2+2}$$

(h)
$$\frac{x-2}{x^2-4}$$

Sol:
$$\frac{1}{x+2}$$

(d)
$$\frac{3x^2+x}{3x^3+x^2-12x-4}$$

Sol:
$$\frac{3x}{3x^2-12}$$

(i)
$$\frac{x^2-2}{x-\sqrt{2}}$$

Sol:
$$x + \sqrt{2}$$

(e)
$$\frac{2x^3+3x^2-8x+3}{2x^3-x^2-2x-1}$$

Sol:
$$\frac{2x^3+3x^2-8x+3}{2x^3-x^2-2x-1}$$

(j)
$$\frac{x^2+2x+1}{x^2-1}$$

Sol:
$$\frac{x+1}{x-1}$$

(k)
$$\frac{x^3 - 2x^2 - 5x + 6}{x^2 + x - 2}$$

Sol:
$$x - 3$$

(f) $\frac{x^3-5x^2+6}{x^3-4x}$

(l)
$$\frac{2}{x+7} + \frac{x+4}{x-7}$$

Sol:
$$\frac{x^2+13x+14}{x^2-49}$$

(m)
$$\frac{1}{x+5} + \frac{x}{x^2+10x+25}$$

Sol:
$$\frac{2x+5}{x^2+10x+25}$$

(n)
$$\frac{1}{x+5} - \frac{x}{x^2+10x+25}$$

Sol:
$$\frac{5}{x^2+10x+25}$$

$$(\tilde{\mathbf{n}}) \quad \frac{12}{x-3} + \frac{x+4}{2x+1} - \frac{x}{x^2 - 6x + 9}$$

Sol:
$$\frac{x^3 + 20x^2 - 76x}{2x^3 - 11x^2 + 12x + 9}$$

(o)
$$\frac{1}{x-1} \cdot \frac{x^2-1}{x+2} \cdot \frac{x+2}{x-3}$$

Sol:
$$\frac{x+1}{x-3}$$

(p)
$$\frac{2x+1}{x} \cdot \frac{x^2-3x}{4x^2-1}$$

Sol:
$$\frac{2x-6}{4x-2}$$

$$(\mathbf{q}) \quad \frac{3x-1}{x} \cdot \frac{x^2}{9x^2-1}$$

Sol:
$$\frac{3x}{9x+3}$$

(r)
$$7x : \frac{x^2 - 4x}{x - 2}$$

Sol:
$$\frac{7x-14}{x-4}$$

(s)
$$\frac{x-3}{x-1}$$
: $\frac{x^2-3x}{x^2-1}$

Sol:
$$\frac{x+1}{x}$$

(t)
$$\frac{x^2-3x-4}{x}$$
: $\frac{x+1}{x^2+2x}$

Sol:
$$x^2 - 2x - 8$$