

## Departamento de Matemáticas $2^{\underline{0}}$ Bachillerato

2º Bachillerato
Integral indefinida



1. p38e01 - Calcula las siguientes integrales inmediatas:

(a) 
$$\int 4x^6 \cdot dx$$

**Sol:** 
$$\frac{4x^7}{7} + K$$

(b) 
$$\int 6x^3 + 8x^2 + 3 \cdot dx$$

**Sol:** 
$$\frac{3x^4}{2} + \frac{8x^3}{3} + 3x + K$$

(c) 
$$\int \sqrt{2}\sqrt{x} \cdot dx$$

**Sol:** 
$$\frac{2\sqrt{2}x^{\frac{3}{2}}}{3} + K$$

(d) 
$$\int \frac{1}{\sqrt[5]{x}} \cdot dx$$

**Sol:** 
$$\frac{5x^{\frac{4}{5}}}{4} + K$$

(e) 
$$\int \frac{\sqrt[3]{5}\sqrt[3]{x^2} + \sqrt{3}\sqrt{x^3}}{\sqrt{2}\sqrt{x}} \cdot dx$$

**Sol:** 
$$\frac{\sqrt{2}\left(\frac{6\sqrt[3]{5}\sqrt{x}\sqrt[3]{x^2}}{7} + \frac{\sqrt{3}\sqrt{x}\sqrt{x^3}}{2}\right)}{2} + K$$

(f) 
$$\int \frac{1}{x-1} \cdot dx$$

**Sol:** 
$$\log(x-1) + K$$

(g) 
$$\int \frac{5}{4x^2+1} \cdot dx$$

**Sol:** 
$$\frac{5 \tan{(2x)}}{2} + K$$

(h) 
$$\int \frac{2}{9x^2+1} \cdot dx$$

**Sol:** 
$$\frac{2 \tan{(3x)}}{3} + K$$

(i) 
$$\int \frac{1}{1-4x^2} \cdot dx$$

**Sol:** 
$$-\frac{\log(x-\frac{1}{2})}{4} + \frac{\log(x+\frac{1}{2})}{4} + K$$

$$(j) \quad \int \frac{1}{x^2+4} \cdot dx$$

Sol: 
$$\frac{\operatorname{atan}\left(\frac{x}{2}\right)}{2} + K$$

(k) 
$$\int \frac{2x-3}{x^2-3x+9} \cdot dx$$

**Sol:** 
$$\log(x^2 - 3x + 9) + K$$

(1) 
$$\int 2e^{x^2}x \cdot dx$$

**Sol:** 
$$e^{x^2} + K$$

(m) 
$$\int \frac{1}{x-4} \cdot dx$$

**Sol:** 
$$\log(x-4) + K$$

(n) 
$$\int \frac{1}{(x-4)^3} \cdot dx$$

Sol: 
$$-\frac{1}{2x^2-16x+32}+K$$

(
$$\tilde{\mathbf{n}}$$
)  $\int e^{5x} \cdot dx$ 

**Sol:** 
$$\frac{e^{5x}}{5} + K$$

(o) 
$$\int \frac{\sqrt{x}+x}{x^2} \cdot dx$$

**Sol:** 
$$\log(x) - \frac{2}{\sqrt{x}} + K$$

(p) 
$$\int \frac{\log(x)^3}{x} \cdot dx$$

**Sol:** 
$$\frac{\log(x)^4}{4} + K$$

(q) 
$$\int \frac{\sin(\sqrt{x})}{\sqrt{x}} \cdot dx$$

**Sol:** 
$$-2\cos(\sqrt{x}) + K$$

(r) 
$$\int e^{9+(-2)x} \cdot dx$$

**Sol:** 
$$-\frac{e^{9-2x}}{2} + K$$

2. p38e01cont - Calcula las siguientes integrales inmediatas:

(a) 
$$\int 3^x - x^3 \cdot dx$$

**Sol:** 
$$x(3^x - x^3) + K$$

(b) 
$$\int \frac{3x^2 + 2e^{2x} + \cos(x)}{x^3 + e^{2x} + \sin(x)} \cdot dx$$

**Sol:** 
$$\frac{x(3x^2+2e^{2x}+\cos(x))}{x^3+e^{2x}+\sin(x)} + K$$

(c) 
$$\int 6\cos(2x-1)\cdot dx$$

**Sol:** 
$$6x \cos(2x - 1) + K$$

(d) 
$$\int \frac{x+1}{x^2+2x+3} \cdot dx$$

**Sol:** 
$$\frac{x(x+1)}{x^2+2x+3} + K$$

(e) 
$$\int \sin(x)\cos(x) \cdot dx$$

**Sol:** 
$$x \sin(x) \cos(x) + K$$

(f) 
$$\int e^{4x-3} \cdot dx$$

**Sol:** 
$$xe^{4x-3} + K$$

(g) 
$$\int \frac{4}{x^2+3} \cdot dx$$

**Sol:** 
$$\frac{4x}{x^2+3} + K$$

(h) 
$$\int \sqrt{(x+3)^3} \cdot dx$$

**Sol:** 
$$x\sqrt{(x+3)^3} + K$$

(i) 
$$\int \frac{\sin(x)}{\cos(x)} \cdot dx$$

Sol: 
$$\frac{x\sin(x)}{\cos(x)} + K$$

3. p38e02 - Calcula las siguientes integrales, por cambio de variable:

(a) 
$$\int x \sin(x^2) \cdot dx$$

**Sol:** 
$$xx \sin(x^2) + K$$

(b) 
$$\int \frac{x}{\sqrt{x^2+5}} \cdot dx$$

**Sol:** 
$$\frac{xx}{\sqrt{x^2+5}} + K$$

(c) 
$$\int \frac{\sin(x)}{\cos^5(x)} \cdot dx$$

Sol: 
$$\frac{x\sin(x)}{\cos^5(x)} + K$$

(d) 
$$\int \frac{x}{(x^2+3)^5} \cdot dx$$

**Sol:** 
$$\frac{xx}{(x^2+3)^5} + K$$

(e) 
$$\int \frac{\tan^2(x)+1}{\sqrt{\tan(x)}} \cdot dx$$

Sol: 
$$\frac{x(\tan^2(x)+1)}{\sqrt{\tan(x)}} + K$$

(f) 
$$\int (x-1)\sqrt{x^2-2x}\cdot dx$$

**Sol:** 
$$x(x-1)\sqrt{x^2-2x}+K$$

(g) 
$$\int \sin(x) \sin(\cos(x)) \cdot dx$$

**Sol:** 
$$x \sin(x) \sin(\cos(x)) + K$$

(h) 
$$\int \frac{\log(x)^2 + 1}{x} \cdot dx$$

**Sol:** 
$$\frac{x(\log(x)^2+1)}{x} + K$$

(i) 
$$\int \sqrt{(\cos(x)+1)^3} \sin(x) \cdot dx$$

**Sol:** 
$$x\sqrt{(\cos(x)+1)^3}\sin(x) + K$$

4. p38e03 - Calcula las siguientes integrales, por partes:

(a) 
$$\int e^x x \cdot dx$$

**Sol:** 
$$(x-1)e^x + K$$

(b) 
$$\int \log(x) \cdot dx$$

**Sol:** 
$$x \log(x) - x + K$$

(c) 
$$\int x^3 \log(x) \cdot dx$$

**Sol:** 
$$\frac{x^4 \log(x)}{4} - \frac{x^4}{16} + K$$

(d) 
$$\int x \sin(x) \cdot dx$$

**Sol:** 
$$-x\cos(x) + \sin(x) + K$$

(e) 
$$\int \operatorname{atan}(x) \cdot dx$$

**Sol:** 
$$x \arctan(x) - \frac{\log(x^2+1)}{2} + K$$

(f) 
$$\int a\sin(x) \cdot dx$$

**Sol:** 
$$x \operatorname{asin}(x) + \sqrt{1 - x^2} + K$$

(g) 
$$\int x \cos(3x) \cdot dx$$

**Sol:** 
$$\frac{x\sin(3x)}{3} + \frac{\cos(3x)}{9} + K$$

(h) 
$$\int e^{2x} x^2 \cdot dx$$

**Sol:** 
$$\frac{(2x^2-2x+1)e^{2x}}{4} + K$$

(i) 
$$\int \frac{x}{e^x} \cdot dx$$

**Sol:** 
$$(-x-1)e^{-x} + K$$

(j) 
$$\int \frac{\log(x)}{x^2} \cdot dx$$

**Sol:** 
$$-\frac{\log(x)}{x} - \frac{1}{x} + K$$

 $5. \ \ p38e04 - Resuelve \ las \ siguientes \ integrales, \ que \ luego \ aparecer\'an \ al \ integrar \ funciones \ racionales:$ 

(a) 
$$\int \frac{3}{2x-1} \cdot dx$$

**Sol:** 
$$\frac{3\log(2x-1)}{2} + K$$

(b) 
$$\int \frac{2}{(x+2)^3} \cdot dx$$

**Sol:** 
$$-\frac{1}{x^2+4x+4}+K$$

(c) 
$$\int \frac{7x-5}{x^2+4} \cdot dx$$

**Sol:** 
$$\frac{7\log(x^2+4)}{2} - \frac{5\tan(\frac{x}{2})}{2} + K$$