

Departamento de Matemáticas $2^{\underline{0}}$ Bachillerato



Integral indefinida

1. p37e01 - Calcula las siguientes integrales inmediatas:

(a)
$$\int 4x^6 \cdot dx$$

Sol:
$$\frac{4x^7}{7} + K$$

(b)
$$\int 6x^3 + 8x^2 + 3 \cdot dx$$

Sol:
$$\frac{3x^4}{2} + \frac{8x^3}{3} + 3x + K$$

(c)
$$\int \sqrt{2}\sqrt{x} \cdot dx$$

Sol:
$$\frac{2\sqrt{2}x^{\frac{3}{2}}}{3} + K$$

(d)
$$\int \frac{1}{\sqrt[5]{x}} \cdot dx$$

Sol:
$$\frac{5x^{\frac{4}{5}}}{4} + K$$

(e)
$$\int \frac{\sqrt[3]{5}\sqrt[3]{x^2} + \sqrt{3}\sqrt{x^3}}{\sqrt{2}\sqrt{x}} \cdot dx$$

Sol:
$$\frac{\sqrt{2}\left(\frac{6\sqrt[3]{5}\sqrt{x}\sqrt[3]{x^2}}{7} + \frac{\sqrt{3}\sqrt{x}\sqrt{x^3}}{2}\right)}{2} + K$$

(f)
$$\int \frac{1}{x-1} \cdot dx$$

Sol:
$$\log(x-1) + K$$

(g)
$$\int \frac{5}{4x^2+1} \cdot dx$$

Sol:
$$\frac{5 \tan{(2x)}}{2} + K$$

(h)
$$\int \frac{2}{9x^2+1} \cdot dx$$

Sol:
$$\frac{2 \tan{(3x)}}{3} + K$$

(i)
$$\int \frac{1}{1-4x^2} \cdot dx$$

Sol:
$$-\frac{\log\left(x-\frac{1}{2}\right)}{4} + \frac{\log\left(x+\frac{1}{2}\right)}{4} + K$$

$$(j) \quad \int \frac{1}{x^2+4} \cdot dx$$

Sol:
$$\frac{\operatorname{atan}\left(\frac{x}{2}\right)}{2} + K$$

(k)
$$\int \frac{2x-3}{x^2-3x+9} \cdot dx$$

Sol:
$$\log(x^2 - 3x + 9) + K$$

(1)
$$\int 2e^{x^2}x \cdot dx$$

Sol:
$$e^{x^2} + K$$

(m)
$$\int \frac{1}{x-4} \cdot dx$$

Sol:
$$\log(x-4) + K$$

(n)
$$\int \frac{1}{(x-4)^3} \cdot dx$$

Sol:
$$-\frac{1}{2x^2-16x+32}+K$$

(
$$\tilde{\mathbf{n}}$$
) $\int e^{5x} \cdot dx$

Sol:
$$\frac{e^{5x}}{5} + K$$

(o)
$$\int \frac{\sqrt{x}+x}{x^2} \cdot dx$$

Sol:
$$\log(x) - \frac{2}{\sqrt{x}} + K$$

(p)
$$\int \frac{\log(x)^3}{x} \cdot dx$$

Sol:
$$\frac{\log(x)^4}{4} + K$$

(q)
$$\int \frac{\sin(\sqrt{x})}{\sqrt{x}} \cdot dx$$

Sol:
$$-2\cos(\sqrt{x}) + K$$

(r)
$$\int e^{9+(-2)x} \cdot dx$$

Sol:
$$-\frac{e^{9-2x}}{2} + K$$

2. p37e01cont - Calcula las siguientes integrales inmediatas:

(a)
$$\int 3^x - x^3 \cdot dx$$

Sol:
$$\frac{3^x}{\log(3)} - \frac{x^4}{4} + K$$

(b)
$$\int \frac{3x^2 + 2e^{2x} + \cos(x)}{x^3 + e^{2x} + \sin(x)} \cdot dx$$

Sol:
$$\log (x^3 + e^{2x} + \sin (x)) + K$$

(c)
$$\int 6\cos(2x-1)\cdot dx$$

Sol:
$$3\sin(2x-1) + K$$

(d)
$$\int \frac{x+1}{x^2+2x+3} \cdot dx$$

Sol:
$$\frac{\log(x^2+2x+3)}{2} + K$$

(e)
$$\int \sin(x) \cos(x) \cdot dx$$

Sol:
$$\frac{\sin^2(x)}{2} + K$$

(f)
$$\int e^{4x-3} \cdot dx$$

Sol:
$$\frac{e^{4x-3}}{4} + K$$

(g)
$$\int \frac{4}{x^2+3} \cdot dx$$

Sol:
$$\frac{4\sqrt{3} \operatorname{atan}\left(\frac{\sqrt{3}x}{3}\right)}{3} + K$$

(h)
$$\int \sqrt{(x+3)^3} \cdot dx$$

Sol:
$$\int \sqrt{(x+3)^3} \, dx + K$$

(i)
$$\int \frac{\sin(x)}{\cos(x)} \cdot dx$$

Sol:
$$-\log(\cos(x)) + K$$

3. p37e02 - Calcula las siguientes integrales, por cambio de variable:

(a)
$$\int x \sin(x^2) \cdot dx$$

Sol:
$$-\frac{\cos(x^2)}{2} + K$$

(b)
$$\int \frac{x}{\sqrt{x^2+5}} \cdot dx$$

Sol:
$$\sqrt{x^2 + 5} + K$$

(c)
$$\int \frac{\sin(x)}{\cos^5(x)} \cdot dx$$

Sol:
$$\frac{1}{4\cos^4(x)} + K$$

(d)
$$\int \frac{x}{(x^2+3)^5} \cdot dx$$

Sol:
$$-\frac{1}{8x^8+96x^6+432x^4+864x^2+648}+K$$

(e)
$$\int \frac{\tan^2(x)+1}{\sqrt{\tan(x)}} \cdot dx$$

Sol:
$$2\sqrt{\tan(x)} + K$$

(f)
$$\int (x-1)\sqrt{x^2-2x}\cdot dx$$

Sol:
$$\frac{x^2\sqrt{x^2-2x}}{3} - \frac{2x\sqrt{x^2-2x}}{3} + K$$

(g)
$$\int \sin(x) \sin(\cos(x)) \cdot dx$$

Sol:
$$\cos(\cos(x)) + K$$

(h)
$$\int \frac{\log(x)^2 + 1}{x} \cdot dx$$

Sol:
$$\frac{\log(x)^3}{3} + \log(x) + K$$

(i)
$$\int \sqrt{(\cos(x) + 1)^3} \sin(x) \cdot dx$$

Sol:
$$\int \sqrt{(\cos(x)+1)^3} \sin(x) \, dx + K$$

4. p37e03 - Calcula las siguientes integrales, por partes:

(a)
$$\int e^x x \cdot dx$$

Sol:
$$(x-1)e^x + K$$

(b)
$$\int \log(x) \cdot dx$$

Sol:
$$x \log(x) - x + K$$

(c)
$$\int x^3 \log(x) \cdot dx$$

Sol:
$$\frac{x^4 \log(x)}{4} - \frac{x^4}{16} + K$$

(d)
$$\int x \sin(x) \cdot dx$$

Sol:
$$-x\cos(x) + \sin(x) + K$$

(e)
$$\int \operatorname{atan}(x) \cdot dx$$

Sol:
$$x \arctan(x) - \frac{\log(x^2+1)}{2} + K$$

(f)
$$\int a\sin(x) \cdot dx$$

Sol:
$$x \sin(x) + \sqrt{1 - x^2} + K$$

(g)
$$\int x \cos(3x) \cdot dx$$

Sol:
$$\frac{x\sin(3x)}{3} + \frac{\cos(3x)}{9} + K$$

(h)
$$\int e^{2x}x^2 \cdot dx$$

Sol:
$$\frac{(2x^2-2x+1)e^{2x}}{4} + K$$

(i)
$$\int \frac{x}{e^x} \cdot dx$$

Sol:
$$(-x-1)e^{-x} + K$$

(j)
$$\int \frac{\log(x)}{x^2} \cdot dx$$

Sol:
$$-\frac{\log(x)}{x} - \frac{1}{x} + K$$

5. p37e04 - Resuelve las siguientes integrales, que luego aparecerán al integrar funciones racionales:

(a)
$$\int \frac{3}{2x-1} \cdot dx$$

Sol:
$$\frac{3\log(2x-1)}{2} + K$$

(b)
$$\int \frac{2}{(x+2)^3} \cdot dx$$

Sol:
$$-\frac{1}{x^2+4x+4}+K$$

(c) $\int \frac{7x-5}{x^2+4} \cdot dx$

Sol:
$$\frac{7 \log (x^2+4)}{2} - \frac{5 \arctan (\frac{x}{2})}{2} + K$$

(d) $\int \frac{x+2}{x^2+x+1} \cdot dx$

Sol:
$$\frac{\log(x^2+x+1)}{2} + \sqrt{3} \operatorname{atan}\left(\frac{\sqrt{3}(2x+1)}{3}\right) + K$$

(e)
$$\int \frac{1}{3x-4} \cdot dx$$

Sol:
$$\frac{\log(3x-4)}{3} + K$$

(f)
$$\int \frac{7}{(2x-3)^2} \cdot dx$$

Sol:
$$-\frac{7}{4x-6} + K$$

(g)
$$\int \frac{3x+4}{x^2+2} \cdot dx$$

Sol:
$$\frac{3\log(x^2+2)}{2} + 2\sqrt{2} \operatorname{atan}\left(\frac{\sqrt{2}x}{2}\right) + K$$

(h)
$$\int \frac{x-1}{x^2+2x+3} \cdot dx$$

Sol:
$$\frac{\log(x^2+2x+3)}{2} - \sqrt{2} \operatorname{atan}\left(\frac{\sqrt{2}(x+1)}{2}\right) + K$$

6. p37e05 - Calcula las siguientes integrales racionales:

(a)
$$\int \frac{x-2}{x^2+x} \cdot dx$$

Sol:
$$-2\log(x) + 3\log(x+1) + K$$

(b)
$$\int \frac{x^3 + 4x^2 - 10x + 7}{x^3 - 7x - 6} \cdot dx$$

Sol:
$$x + 2 \log(x - 3) - 5 \log(x + 1) + 7 \log(x + 2) + K$$

(c)
$$\int \frac{2x^2+5x-1}{x^3+x^2-2x} \cdot dx$$

Sol:
$$\frac{\log(x)}{2} + 2\log(x-1) - \frac{\log(x+2)}{2} + K$$

(d)
$$\int \frac{2x+3}{x^2+3x-10} \cdot dx$$

Sol:
$$\log(x^2 + 3x - 10) + K$$

(e)
$$\int \frac{1}{x^3 + x^2 - 6x} \cdot dx$$

Sol:
$$-\frac{\log(x)}{6} + \frac{\log(x-2)}{10} + \frac{\log(x+3)}{15} + K$$

(f)
$$\int \frac{x^2 + 2x}{x^2 - 1} \cdot dx$$

Sol:
$$x + \frac{3\log(x-1)}{2} + \frac{\log(x+1)}{2} + K$$

(g)
$$\int \frac{2x^2 + 7x - 1}{x^3 + x^2 - x - 1} \cdot dx$$

Sol:
$$\frac{2(x+1)\log(x-1)-3}{x+1} + K$$

(h)
$$\int \frac{2x-4}{(x-1)^2(x+3)} \cdot dx$$

Sol:
$$\frac{5(x-1)(\log(x-1)-\log(x+3))+4}{8(x-1)} + K$$

(i)
$$\int \frac{x^2+x}{x^4+2x^3-3x^2-4x+4} \cdot dx$$

Sol:
$$\frac{-12x+5(\log{(x-1)}-\log{(x+2)})(x^2+x-2)-6}{27(x^2+x-2)} +$$

$$(j) \quad \int \frac{x+2}{x^3 - 2x^2 + x} \cdot dx$$

Sol:
$$\frac{2(x-1)(\log(x)-\log(x-1))-3}{x-1}+K$$

(k)
$$\int \frac{8x^2 - 2x - 1}{x^3 - x^2 + 4x - 4} \cdot dx$$

Sol:
$$\log(x-1) + \frac{7\log(x^2+4)}{2} + \frac{5\tan(\frac{x}{2})}{2} + K$$

(l)
$$\int \frac{6x+8}{x^2+2x+5} \cdot dx$$

Sol:
$$3 \log (x^2 + 2x + 5) + \operatorname{atan} (\frac{x}{2} + \frac{1}{2}) + K$$

(m)
$$\int \frac{3x-2}{x^3-3x^2+12x-10} \cdot dx$$

Sol:
$$\frac{\log(x-1)}{9} - \frac{\log(x^2-2x+10)}{18} + \tan(\frac{x}{3} - \frac{1}{3}) + K$$

7. p
37e
06 - Calcula las siguientes integrales trigonométricas:

(a)
$$\int \cos^3(x) dx$$

Sol:
$$-\frac{\sin^3(x)}{3} + \sin(x) + K$$

(b)
$$\int \sin^3(x) dx$$

Sol:
$$\frac{\cos^3(x)}{3} - \cos(x) + K$$

(c)
$$\int \sin^3(x) \cos(x) dx$$

Sol:
$$\frac{\sin^4(x)}{4} + K$$

(d)
$$\int \sin(x) \cos^4(x) dx$$

Sol:
$$-\frac{\cos^5(x)}{5} + K$$

(e)
$$\int \cos^2(x) dx$$

Sol:
$$\frac{x}{2} + \frac{\sin(2x)}{4} + K$$

(f) $\int \sin^2(x) dx$

Sol:
$$\frac{x}{2} - \frac{\sin(2x)}{4} + K$$

(g) $\int \sin^2(x) \cos^2(x) dx$

Sol:
$$\frac{x}{8} - \frac{\sin(4x)}{32} + K$$

(h) $\int \cos^4(x) dx$

Sol:
$$\frac{3x}{8} + \frac{\sin(2x)}{4} + \frac{\sin(4x)}{32} + K$$

(i) $\int \frac{\sin(x) + \tan(x)}{\cos(x)} dx$

Sol:
$$-\log(\cos(x)) + \frac{1}{\cos(x)} + K$$

 $(j) \int \frac{\sin(x)}{(\cos^2(x)+1)\cos(x)} dx$

Sol:
$$\frac{\log (\cos^2 (x)+1)}{2} - \log (\cos (x)) + K$$

(k) $\int \frac{\sin(x)\cos(x)}{1-\cos(x)} dx$

Sol:
$$\log(\cos(x) - 1) + \cos(x) + K$$

(l) $\int \frac{\sin^3(x)}{1-\cos(x)} dx$

Sol:
$$-\frac{\cos^2(x)}{2} - \cos(x) + \frac{1}{6} + K$$

(m) $\int \frac{1}{\cos(x)+2} dx$

Sol:
$$\frac{2\sqrt{3}\left(\operatorname{atan}\left(\frac{\sqrt{3}\tan\left(\frac{x}{2}\right)}{3}\right) + \pi\left\lfloor\frac{x}{2\pi} - \frac{1}{2}\right\rfloor\right)}{3} + K$$

(n) $\int \frac{1}{\cos(x)+2} \, dx$

Sol:
$$\frac{2\sqrt{3}\left(\operatorname{atan}\left(\frac{\sqrt{3}\tan\left(\frac{x}{2}\right)}{3}\right) + \pi\left\lfloor\frac{x}{2\pi} - \frac{1}{2}\right\rfloor\right)}{3} + K$$

(\tilde{n}) $\int \frac{1}{\sin(x) + \cos(x) + 1} dx$

Sol:
$$\log (\tan (\frac{x}{2}) + 1) + K$$

(o) $\int \frac{\cos^2(x)}{\sin^2(x)} dx$

Sol:
$$-x - \frac{1}{\tan{(x)}} + K$$

8. p37e07 - Calcula las siguientes integrales irracionales:

(a) $\int \frac{\sqrt{x}}{\sqrt[4]{x} + \sqrt{x}} dx$

Sol:
$$-\frac{4x^{\frac{3}{4}}}{3} - 4\sqrt[4]{x} + 2\sqrt{x} + x + 4\log(\sqrt[4]{x} + 1) + K$$

(b) $\int \frac{\sqrt[4]{x} + \sqrt{x}}{-\sqrt[4]{x} + \sqrt{x}} dx$

Sol:
$$\frac{8x^{\frac{3}{4}}}{3} + 8\sqrt[4]{x} + 4\sqrt{x} + x + 8\log(\sqrt[4]{x} - 1) + K$$

(c) $\int \frac{\sqrt{x}}{x+1} dx$

Sol:
$$2\sqrt{x} - 2 \operatorname{atan}(\sqrt{x}) + K$$

(d) $\int \frac{x}{\sqrt{x}+x} dx$

Sol:
$$-2\sqrt{x} + x + 2\log(\sqrt{x} + 1) + K$$

(e) $\int \frac{1}{-\sqrt[4]{x} + \sqrt{x}} dx$

Sol:
$$4\sqrt[4]{x} + 2\sqrt{x} + 4\log(\sqrt[4]{x} - 1) + K$$

(f) $\int \frac{1}{x\sqrt{1-x^2}} dx$

Sol:
$$\begin{cases} -\cosh\left(\frac{1}{x}\right) & \text{for } \left|\frac{1}{x^2}\right| > 1\\ i\sin\left(\frac{1}{x}\right) & \text{otherwise} \end{cases} + K$$

(g)
$$\int \sqrt{x^2 + 1} \, dx$$

Sol:
$$\frac{x\sqrt{x^2+1}}{2} + \frac{\sinh(x)}{2} + K$$

- 9. p38e08 Calcula las siguientes integrales, por el método que creas conveniente:
 - (a) $\int e^x \cos(e^x) dx$

Sol:
$$\sin(e^x) + K$$

(b)
$$\int (x-1) \sqrt[3]{x^2-2x} \, dx$$

Sol:
$$\frac{3(x(x-2))^{\frac{4}{3}}}{8} + K$$

(c)
$$\int \frac{e^x}{(e^x+4)^2} dx$$

Sol:
$$-\frac{1}{e^x+4} + K$$

(d)
$$\int \frac{\tan^3(x) + \tan(x)}{1 - 2\tan(x)} dx$$

Sol:
$$-\frac{\log(\tan(x)-\frac{1}{2})}{4} - \frac{\tan(x)}{2} + K$$

(e)
$$\int \frac{1}{\sqrt{16-x^2}} \, dx$$

Sol:
$$a\sin\left(\frac{x}{4}\right) + K$$

(f)
$$\int \frac{6x^2 - 9x + 5}{(x-1)^2(x+2)} dx$$

Sol:
$$\frac{(x-1)(7\log(x-1)+47\log(x+2))-6}{9(x-1)}+K$$

(g)
$$\int \left(6x^5 + \sqrt[3]{x^4} - \frac{5}{\sqrt[7]{x^5}}\right) dx$$

Sol:
$$x^6 + \frac{3x\sqrt[3]{x^4}}{7} - \frac{35x}{2\sqrt[7]{x^5}} + K$$

(h)
$$\int (x^2 - 2x + 3) \log(x) dx$$

Sol:
$$\frac{x(-2x^2+9x+6(x^2-3x+9)\log(x)-54)}{18} + K$$

(i)
$$\int \frac{1}{\left(\sqrt{x}\cos(x)\right)^2} dx$$

Sol:
$$\int \frac{1}{x \cos^2(x)} dx + K$$

(j)
$$\int \frac{e^x+1}{e^x-1} dx$$

Sol:
$$-x + 2\log(e^x - 1) + K$$

(k)
$$\int \frac{\sqrt[3]{x}}{\sqrt{x^3} \sqrt[3]{x^4}} dx$$

Sol:
$$-\frac{2x^{\frac{4}{3}}}{3\sqrt{x^3}\sqrt[3]{x^4}} + K$$

(l)
$$\int e^{\cos(x)} \sin(x) dx$$

Sol:
$$-e^{\cos{(x)}} + K$$

(m)
$$\int \frac{x^2-1}{x^3-x^2} dx$$

Sol:
$$\log(x) - \frac{1}{x} + K$$

(n)
$$\int \frac{1}{\sqrt{x-1}+\sqrt{x+1}} dx$$

Sol:
$$\frac{2(2x+\sqrt{x-1}\sqrt{x+1})}{3(\sqrt{x-1}+\sqrt{x+1})} + K$$

10. p38e08cont - Calcula las siguientes integrales, por el método que creas conveniente:

(a)
$$\int \sin^4(x) \cos^3(x) dx$$

Sol:
$$-\frac{\sin^7(x)}{7} + \frac{\sin^5(x)}{5} + K$$

(b)
$$\int \frac{1}{\sqrt{x+1}+1} \, dx$$

Sol:
$$2\sqrt{x+1} - 2\log(\sqrt{x+1} + 1) + K$$

(c)
$$\int \frac{e^{2x}}{\sqrt{e^x+1}} dx$$

Sol:
$$\frac{2(e^x-2)\sqrt{e^x+1}}{3} + K$$

(d)
$$\int \left(-4x + 5 + \frac{1}{x^2}\right) dx$$

Sol:
$$\frac{x^2(5-2x)-1}{x} + K$$

(e)
$$\int \frac{e^x}{e^{2x}+1} dx$$

Sol: RootSum
$$(4z^2 + 1, (i \mapsto i \log (2i + e^x))) +$$
 Sol: $-\frac{3e^{2x}}{2} + 3e^x - 2 \log (e^x + 1) + K$

(f)
$$\int \sqrt{x} \log(x) dx$$

Sol:
$$\begin{cases} \frac{2x^{\frac{3}{2}}(3\log(x)-2)}{9} \\ -\frac{2x^{\frac{3}{2}}(3\log\left(\frac{1}{x}\right)+2)}{9} \\ -G_{3,3}^{2,1}\begin{pmatrix} 1 & \frac{5}{2}, \frac{5}{2} \\ \frac{3}{2}, \frac{3}{2} & 0 \end{pmatrix} x + G_{3,3}^{0,3}\begin{pmatrix} \frac{5}{2}, \frac{5}{2}, 1 \\ \frac{3}{2}, \frac{3}{2}, 0 \end{pmatrix} x \end{pmatrix} \text{ otherwise} \end{cases}$$

(g)
$$\int \frac{1 - \log(x)}{x \log(x)} dx$$

Sol:
$$-\log(x) + \log(\log(x)) + K$$

$$\text{(h)} \quad \int \frac{\sqrt[5]{x^3} + \sqrt[4]{x^5}}{\sqrt{x}} \, dx$$

Sol:
$$\frac{2\sqrt{x}\left(35\sqrt[5]{x^3}+22\sqrt[4]{x^5}\right)}{77}+K$$

(i)
$$\int \frac{1}{x^2 - 4x + 13} \, dx$$

Sol:
$$\frac{\tan(\frac{x}{3} - \frac{2}{3})}{3} + K$$

$$(j) \quad \int \frac{e^x - 3e^{3x}}{e^x + 1} \, dx$$

(k)
$$\int \frac{1}{\cos(x)+1} dx$$

Sol:
$$\tan\left(\frac{x}{R}\right) + K < 1$$

for
$$\left|\frac{1}{x}\right| < 1_+$$

$$\frac{3}{2}, \frac{3}{2}, 0$$
 otherwise

11. p38e09 - Calcula las siguientes integrales, por el método que creas conveniente:

(a)
$$\int \frac{1}{\sqrt{x}(\sqrt{x}+1)^2} dx$$

Sol:
$$-\frac{2}{\sqrt{x+1}} + K$$

(b)
$$\int \frac{x^4}{\sqrt[4]{x^5 + 1}} \, dx$$

Sol:
$$\frac{4(x^5+1)^{\frac{3}{4}}}{15} + K$$

(c)
$$\int x \log(x+1) dx$$

Sol:
$$\frac{x^2 \log(x+1)}{2} - \frac{x^2}{4} + \frac{x}{2} - \frac{\log(x+1)}{2} + K$$

(d)
$$\int \frac{x^3 + 2x - 4}{x^4 + x^3 + 4x^2 + 4x} dx$$

Sol:
$$-\log(x) + \frac{7\log(x+1)}{5} + \frac{3\log(x^2+4)}{10} + \frac{\tan(\frac{x}{2})}{5} + K$$

(e)
$$\int 3\sin^4(2x)\cos(2x)\,dx$$

Sol:
$$\frac{3\sin^5(2x)}{10} + K$$

(f)
$$\int \frac{x^3 - 3x^2 + 1}{\sqrt{x}} dx$$

Sol:
$$\frac{2\sqrt{x}(5x^3-21x^2+35)}{35}+K$$

(g)
$$\int \frac{e^x}{9e^{2x}+4} dx$$

Sol: RootSum $(144z^2 + 1, (i \mapsto i \log(8i + e^x))) + \frac{(\tilde{n}) \int \frac{2x^3 - 11x^2 + 18x - 5}{x^2 - 5x + 6} dx}{K}$

(h) $\int x \operatorname{atan}(x) dx$

Sol:
$$\frac{x^2 \operatorname{atan}(x)}{2} - \frac{x}{2} + \frac{\operatorname{atan}(x)}{2} + K$$

(i) $\int x^2 \sqrt{x+1} \, dx$

Sol:
$$\frac{2\sqrt{x+1}\left(15x^3+3x^2-4x+8\right)}{105}+K$$

(j) $\int \cos^4(3x) dx$

Sol:
$$\frac{3x}{8} + \frac{\sin(6x)}{12} + \frac{\sin(12x)}{96} + K$$

(k) $\int \frac{\sqrt[3]{x}-1}{\sqrt{x}+1} dx$

Sol:
$$\frac{6x^{\frac{5}{6}}}{5} - 3\sqrt[3]{x} - 2\sqrt{x} + 2\log(\sqrt{x}+1) + 2\sqrt[3]{-1}\log\left(-\sqrt[6]{x}e^{\frac{i\pi}{3}} + 1\right) - 2\log\left(-\sqrt[6]{x}e^{i\pi} + 1\right) - 2(-1)^{\frac{2}{3}}\log\left(-\sqrt[6]{x}e^{\frac{i\pi}{3}} + 1\right) + \sqrt{\log(x)^{3} - 2\log(x)^{2} - \log(x) + 2}dx$$

$$K$$

 $\int \frac{\sin(x)}{\cos^2(x) - 4} \, dx$ (l)

Sol:
$$-\frac{\log(\cos(x)-2)}{4} + \frac{\log(\cos(x)+2)}{4} + K$$

 $\int \frac{2^{\tan(x)}}{\cos^2(x)} \, dx$ (m)

Sol:
$$\int \frac{2^{\tan{(x)}}}{\cos^2{(x)}} dx + K$$

(n) $\int x^2 \cos(2x) \, dx$

Sol:
$$\frac{x^2 \sin(2x)}{2} + \frac{x \cos(2x)}{2} - \frac{\sin(2x)}{4} + K$$

Sol:
$$x^2 - x + 4\log(x-3) - 3\log(x-2) + K$$

(o) $\int \frac{\sin^2(x)+1}{\sin(x)\cos(x)} dx$

Sol:
$$\log \left(\frac{2}{\cos(x)+1}\right) - 2\log\left(\tan\left(\frac{x}{2}\right) - 1\right) - 2\log\left(\tan\left(\frac{x}{2}\right) + 1\right) + \log\left(\tan\left(\frac{x}{2}\right)\right) + K$$

(p) $\int e^x (x-1) dx$

Sol:
$$(x-2)e^x + K$$

(q) $\int \frac{\log(x)^3}{x} \, dx$

Sol:
$$\frac{\log(x)^4}{4} + K$$

Sol:
$$\frac{\log(\log(x)-2)}{3} - \frac{\log(\log(x)-1)}{2} + \frac{\log(\log(x)+1)}{6} + K$$

(s) $\int \frac{\cos(x)}{1-\cos(x)} dx$

Sol:
$$-x - \frac{1}{\tan(\frac{x}{2})} + K$$

 $\int \frac{6x+8}{x^2+2x+5} dx$ (t)

Sol:
$$3 \log (x^2 + 2x + 5) + \operatorname{atan} (\frac{x}{2} + \frac{1}{2}) + K$$