

Departamento de Matemáticas 2º Bachillerato CCSS



Intervalos de confianza

1. Intervalo de confianza para la media, si la media muestral es: 200.8, la desviación típica: 15, tamaño de la muestra: 25 y el grado de confianza: 90.0 %.

Sol:
$$\alpha = 1 - 0.9 = 0.1 \rightarrow \frac{\alpha}{2} = 0.05$$

Valor crítico:

$$P(Z > z_{\alpha/2}) = 0.05 \rightarrow P(Z < z_{\alpha/2}) = 0.95 \rightarrow z_{\alpha/2} = 1.6449$$

 $[scale=0.8] = 0.9; = 1.6449; \bar{0}.05); [no markers, domain=-5:5, samples=100, axis lines=left,]$ height=5cm, width=12cm, xtick=0,, ytick=, xticklabels = 0, z_{α} =,enlargelimits=false, clip=false, axis on top [fill=cyan!20, draw=none, domain=-:] gauss(0,1); [very thick,cyan!50!black] gauss(0,1); [] at (5.2,1.5); [-] (+6.5,1)node[right] -(+5,6,0,1); Error cometido:

$$E=z_{\alpha/2}\cdot \frac{\sigma}{\sqrt{n}} \to E=1,6449\cdot \frac{15}{5,0}=4,9347$$

Por tanto el intervalo de confianza será:

$$(\overline{x} - E, \overline{x} + E) = (200.8 - 4.9347, 200.8 + 4.9347) = (195.8653, 205.7347)$$

[scale=0.4] = 10; = 10; = 1; = +1; = - = ()/2; [very thick] = (0) - (0); [draw=black,]fill=white (0,0) circle (2pt); [draw=black, fill=white] (0.0) circle (2pt); [latex-latex] (1.5,0) – (+1.5,0); [shift=(0),color=black] (0pt,3pt) - (0pt,-3pt); [shift=(0),color=black] (0pt,0pt) -(0pt,-3pt) node [below] 195,865300000000002; [shift=(,0),color=black] (0pt,3pt) - (0pt,-3pt); [shift=(.0),color=black] (0pt,0pt) - (0pt,-3pt) node[below] 200.8; [shift=(.0),color=black] (0pt,3pt) - (0pt,-3pt); [shift=(0,0),color=black] (0pt,0pt) - (0pt,-3pt) node [below] 205,7347; [decorate, decoration=brace, thick]((0.2)-((0.2)) node[above, midway] E = 4,9347;

2. Intervalo de confianza para la media, si la media muestral es: 1053, la desviación típica: 75, tamaño de la muestra: 150 y el grado de confianza: 98.0 %.

Sol:
$$\alpha = 1 - 0.98 = 0.02 \rightarrow \frac{\alpha}{2} = 0.01$$

Valor crítico:

$$P(Z > z_{\alpha/2}) = 0.01 \rightarrow P(Z < z_{\alpha/2}) = 0.99 \rightarrow z_{\alpha/2} = 2.3263$$

 $[scale=0.8] = 0.98; = 2.3263; \bar{0}.01); [no markers, domain=-5:5, samples=100, axis li$ nes=left, height=5cm, width=12cm, xtick=0,, ytick=, xticklabels=0, $z_{\frac{\alpha}{2}}$ =,enlargelimits=false, clip=false, axis on top] [fill=cyan!20, draw=none, domain=-:] gauss(0,1); [very thick,cyan!50!black] gauss(0,1); [] at (5.2,1.5); [-] (+6.5,1) node[right] - (+5,6,0,1);

$$E = z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}} \to E = 2,3263 \cdot \frac{75}{12,24744871391589} = 14,2456$$

Por tanto el intervalo de confianza será:

$$(\overline{x} - E, \overline{x} + E) = (1053 - 14,2456,1053 + 14,2456) = (1038,7544,1067,2456)$$