

## Departamento de Matemáticas $4^{\underline{0}}$ Académicas

**Funciones** 



1. Calcular el dominio de las siguientes funciones:

(a) 
$$f(x) = \frac{x+13}{x^4 + x^3 - 3x^2 - 3x}$$

(b) 
$$f(x) = x^6 + x^2 - 2$$

(c) 
$$f(x) = \frac{7x+9}{x^3+8}$$

(d) 
$$f(x) = \sqrt{\frac{x-1}{x}}$$

(e) 
$$f(x) = \sqrt[3]{\frac{x-1}{x}}$$

(f) 
$$f(x) = \sqrt[4]{\frac{x(x+7)}{x^2+5x+6}}$$

(g) 
$$f(x) = \frac{x^3 - 6x^2 + 4x + 8}{x^3 - x^2 - 9x + 9}$$

(h) 
$$f(x) = \frac{1}{4x^2 - 1}$$

(i) 
$$f(x) = \frac{1}{\sqrt[4]{9 - x^2}}$$

(j) 
$$f(x) = \frac{2x+7}{\sqrt[3]{9-x}}$$

(k) 
$$f(x) = \frac{x^2 - 5x + 6}{\sqrt{x^4 - 1}}$$

(1) 
$$f(x) = \sqrt{-2x^2 + 5x - 3}$$

(m) 
$$f(x) = \frac{x^2 - 3}{x^3 - 2x^2 - x + 2}$$

(n) 
$$f(x) = \frac{5x^3 - 8}{1 + x + x^2}$$

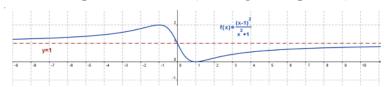
(n) 
$$f(x) = \frac{x-1}{x^4 - 7x^2 - 144}$$

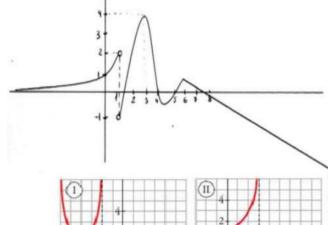
(o) 
$$f(x) = \frac{7x+9}{81x^4-16}$$

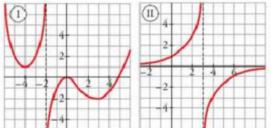
(p) 
$$f(x) = \sqrt[3]{\frac{x^6 - 5x + 1}{x^2 - 4x + 4}}$$

(q) 
$$f(x) = \frac{\sqrt{x^2 - 4x - 5}}{x^2 + 2x + 1}$$

2. Dadas las siguientes funciones, dadas por sus gráficas, obtén sus propiedades:







3. Representa las siguientes funciones, indicando sus propiedades:

(a) 
$$y = x^2 - 4x - 5$$

(b) 
$$y = -x^2 + 4x + 5$$

(c) 
$$y = -x^2 - 5x + 6$$

(c) 
$$y = -x^2 - 5x + 6$$
  
(d)  $f(x) = \begin{cases} 4 & \text{si} & x < -2 \\ -x^2 & \text{si} & -2 \le x < 4 \\ 2x - 3 & \text{si} & x \ge 4 \end{cases}$  (f)  $f(x) = \begin{cases} x + 1 & \text{si} & x \le 0 \\ x^2 - 4x + 3 & \text{si} & x > 0 \end{cases}$ 

(e) 
$$f(x) = \begin{cases} 2x & \text{si} & x < -3\\ x^2 - 2x - 8 & \text{si} & -3 \le x \le 3\\ 2x - 3 & \text{si} & x \ge 3 \end{cases}$$

(f) 
$$f(x) = \begin{cases} x+1 & \text{si } x \le 0 \\ x^2 - 4x + 3 & \text{si } x > 0 \end{cases}$$