

1. **Teoría:** Reducción al primer cuadrante

- (a) Ángulos complementarios (suman  $90^\circ$ )      (c) Ángulos suplementarios (suman  $180^\circ$ )      (e) Ángulos cuya suma es  $360^\circ$

$$\operatorname{sen} (90^\circ - \alpha) = \cos \alpha$$

$$\cos (90^\circ - \alpha) = \operatorname{sen} \alpha$$

$$\operatorname{tg} (90^\circ - \alpha) = \operatorname{cotg} \alpha$$

$$\operatorname{sen} (180^\circ - \alpha) = \operatorname{sen} \alpha$$

$$\cos (180^\circ - \alpha) = -\cos \alpha$$

$$\operatorname{tg} (180^\circ - \alpha) = -\operatorname{tg} \alpha$$

$$\operatorname{sen} (360^\circ - \alpha) = -\operatorname{sen} \alpha$$

$$\cos (360^\circ - \alpha) = \cos \alpha$$

$$\operatorname{tg} (360^\circ - \alpha) = -\operatorname{tg} \alpha$$

- (b) Ángulos que difieren  $90^\circ$       (d) Ángulos que difieren  $90^\circ$

$$\operatorname{sen} (90^\circ + \alpha) = \cos \alpha$$

$$\cos (90^\circ + \alpha) = -\operatorname{sen} \alpha$$

$$\operatorname{tg} (90^\circ + \alpha) = -\operatorname{cotg} \alpha$$

$$\operatorname{sen} (180^\circ + \alpha) = -\operatorname{sen} \alpha$$

$$\cos (180^\circ + \alpha) = -\cos \alpha$$

$$\operatorname{tg} (180^\circ + \alpha) = \operatorname{tg} \alpha$$

2. Demostrar que para cualquier ángulo  $\alpha$ , se verifica:  $\sec^2 \alpha + \operatorname{cosec}^2 \alpha = \sec^2 \alpha \cdot \operatorname{cosec}^2 \alpha$

3. Demostrar si son verdaderas o falsas las siguientes ecuaciones:

(a)  $\frac{\operatorname{tg} \alpha + \operatorname{tg} \beta}{\operatorname{cotg} \alpha + \operatorname{cotg} \beta} = \operatorname{tg} \alpha \cdot \operatorname{tg} \beta$

(e)  $\operatorname{cotg}^2 \alpha - \cos^2 \alpha = \operatorname{cotg}^2 \alpha \cdot \cos^2 \alpha$

(b)  $\frac{\operatorname{sen} \alpha \cdot \cos \alpha}{\cos^2 \alpha - \operatorname{sen}^2 \alpha} = \frac{\operatorname{tg} \alpha}{1 - \operatorname{tg}^2 \alpha}$

(f)  $\operatorname{sen} \alpha \cdot \cos \alpha \cdot \operatorname{tg} \alpha \cdot \operatorname{cotg} \alpha \cdot \sec \alpha \cdot \operatorname{cosec} \alpha = 1$

(c)  $\operatorname{cotg} \alpha - \frac{\operatorname{cotg}^2 \alpha - 1}{\operatorname{cotg} \alpha} = \operatorname{tg} \alpha$

(g)  $\frac{1 + \operatorname{tg} \alpha}{1 - \operatorname{tg} \alpha} = \frac{\cos \alpha + \operatorname{sen} \alpha}{\cos \alpha - \operatorname{sen} \alpha}$

(d)  $\frac{\operatorname{sen} \alpha + \operatorname{cotg} \alpha}{\operatorname{tg} \alpha + \operatorname{cosec} \alpha} = \cos \alpha$

(h)  $\frac{1 + \operatorname{tg}^2 \alpha}{\operatorname{cotg} \alpha} = \frac{\operatorname{tg} \alpha}{\cos^2 \alpha}$

4. Simplificar las siguientes expresiones:

(a)  $\operatorname{sen} \alpha \cdot \frac{1}{\operatorname{tg} \alpha}$

(g)  $\frac{\cos^2 \alpha - \operatorname{sen}^2 \alpha}{\cos^4 \alpha - \operatorname{sen}^4 \alpha}$

(b)  $\operatorname{sen}^3 \alpha + \operatorname{sen} \alpha \cdot \cos^2 \alpha$

(h)  $\frac{\sec^2 \alpha + \cos^2 \alpha}{\sec^2 \alpha - \cos^2 \alpha}$

(c)  $\sqrt{1 - \operatorname{sen} \alpha} \cdot \sqrt{1 + \operatorname{sen} \alpha}$

(d)  $\operatorname{sen}^4 \alpha - \cos^4 \alpha$

(e)  $\frac{\cos^3 \alpha + \cos^2 \alpha \cdot \operatorname{sen} \alpha + \cos \alpha \cdot \operatorname{sen}^2 \alpha + \operatorname{sen}^3 \alpha}{\operatorname{sen}^3 \alpha}$

(i)  $\frac{\cos^2 \alpha}{1 - \operatorname{sen} \alpha}$

(f)  $\operatorname{sen} \alpha \cdot \cos \alpha \left( \operatorname{tg} \alpha + \frac{1}{\operatorname{tg} \alpha} \right)$

(j)  $\frac{\operatorname{cosec} \alpha}{1 + \operatorname{cotg}^2 \alpha}$

5. Calcular las restantes razones trigonométricas de  $\alpha$ , conocida:

(a)  $\cos \alpha = \frac{4}{5}$  y  $\alpha \in \text{I}$

(d)  $\sec \alpha = 2$  y  $\alpha \in \text{IV}$

(b)  $\operatorname{sen} \alpha = \frac{3}{5}$  y  $\alpha \in \text{II}$

(e)  $\operatorname{cosec} \alpha = -2$  y  $\alpha \in \text{III}$

(c)  $\operatorname{tg} \alpha = -\frac{3}{4}$  y  $\alpha \in \text{II}$

(f)  $\operatorname{cotg} \alpha = -2$  y  $\alpha \in \text{IV}$

6. Si  $\operatorname{tg} \alpha = \frac{3}{4}$ , halla el valor de las siguientes razones trigonométricas:

- |   |   |   |
|---|---|---|
| (a) $\operatorname{tg} \left( \frac{\pi}{2} - \alpha \right) =$ | (e) $\operatorname{cotg} \left( \frac{\pi}{2} + \alpha \right) =$ | (i) $\operatorname{sen}(\pi + \alpha) =$                      |
| (b) $\operatorname{sen}(\pi - \alpha) =$                        | (f) $\operatorname{sec}(\pi - \alpha) =$                          | (j) $\operatorname{tg} \left( \frac{\pi}{2} + \alpha \right)$ |
| (c) $\operatorname{cos}(\pi + \alpha) =$                        | (g) $\operatorname{cosec} \left( \frac{3\pi}{2} - \alpha \right)$ | (k) $\operatorname{cotg}(\pi + \alpha) =$                     |
| (d) $\operatorname{tg}(\pi - \alpha) =$                         | (h) $\operatorname{cos} \left( \frac{3\pi}{2} + \alpha \right) =$ | (l) $\operatorname{sec}(\pi - \alpha) =$                      |

7. Resolver las siguientes ecuaciones:

- |  |   |
|--|---|
| (a) $\operatorname{sen} 2x = \frac{1}{2}$                |   |
| (b) $\operatorname{tg} \frac{x}{2} = \frac{\sqrt{3}}{3}$ | (c) $\operatorname{sen} \left( 3x - \frac{\pi}{2} \right) = -\frac{1}{2}$ |

8. Resolver las siguientes ecuaciones:

- |   |  |
|---|--|
| (a) $2 \operatorname{sen} x + \operatorname{cosec} x = 2\sqrt{2}$ | (d) $\operatorname{sen} x \cdot \operatorname{cos} x = 2 \cdot \operatorname{sen} x$ |
| (b) $\operatorname{sen} x = \operatorname{cos}^2 x + 1$           | (e) $2 \operatorname{cos} x - 3 \operatorname{tg} x = 0$                             |
| (c) $\operatorname{tg} x - \operatorname{sen} x = 0$              | (f) $\operatorname{tg} x + 3 \cdot \operatorname{cotg} x = 4$                        |