

HCMIU - Calculus I - Mid-term Test
 Semester 2 - Year: 2021 ~ 2022 - Duration : 90 minutes
 Date Modified : Thursday, June 26th, 2025

INSTRUCTIONS:

- Use of calculator is allowed. Each student is allowed one doubled-sized sheet of reference material (size A4 or similar). All other documents and electronic devices are forbidden
- You must explain your answers in detail; no points will be given for the answer alone.
- There are a total of 5 (five) questions. Each one carries 20 points

Question 1. Test the series for convergence or divergence:

$$(a) \sum_{n=1}^{\infty} \frac{9^n}{n!n} \quad (b) \sum_{n=1}^{\infty} \left(\frac{n}{n+1} \right)^{2n^2}$$

Question 2. Use the sum of the first 10 terms to approximate the sum of the series. Estimate error (find the remainder):

$$\sum_{n=1}^{\infty} \frac{1}{4^n + 1}$$

Question 3. Determine the radius of convergence of the following power series, then test the endpoints to determine the interval of convergence.

$$\sum_{n=0}^{\infty} \frac{(-2)^n (x+3)^n}{3^{n+1}}$$

Question 4. Do the following requests:

- Find both the parametric and the vector equations of the line through point $(1, -1, 0)$, that is parallel to the line $x = 3 + 4t, y = 5 - t, z = 7$.
- Find the distance between the given point $Q(-2, 5, 9)$ and the line: $x = 5t + 7, y = 2 - t, z = 12t + 4$.

Question 5. Do the following requests:

- Find

$$\lim_{t \rightarrow 0} \left(\frac{\sin(t)}{t} \mathbf{i} - \frac{e^t - t - 1}{t} \mathbf{j} + \frac{\cos(t) + \frac{t^2}{2}}{t^2} \mathbf{k} \right)$$

- Investigate the limit

$$\lim_{(x,y) \rightarrow (0,0)} \frac{(x+y)^2}{x^2 + y^2}$$

END OF TEST - BEST OF LUCK