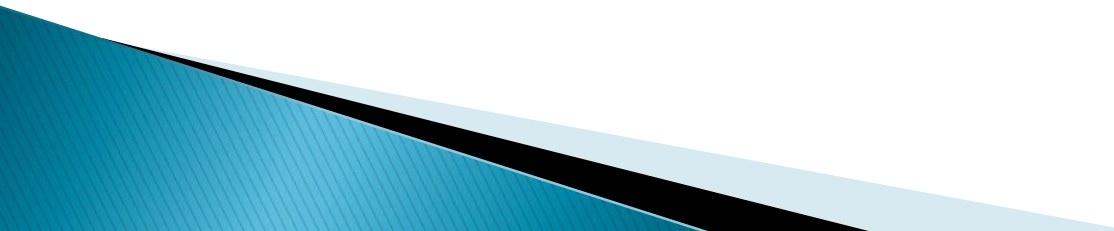


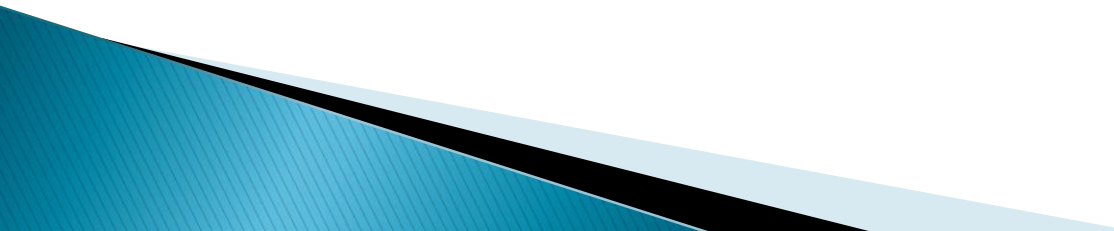
An Overview of Modern Data Analysis Strategies

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What's the plan ...

- ▶ We are going to scratch the surface in terms of modern issues related to data analysis in the behavioral sciences
 - ▶ There will be less of a focus on the actual methods used to conduct the analyses (i.e., less of the “how”, and more of a focus on the “why”), although we will also dabble in some applied work
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Day One

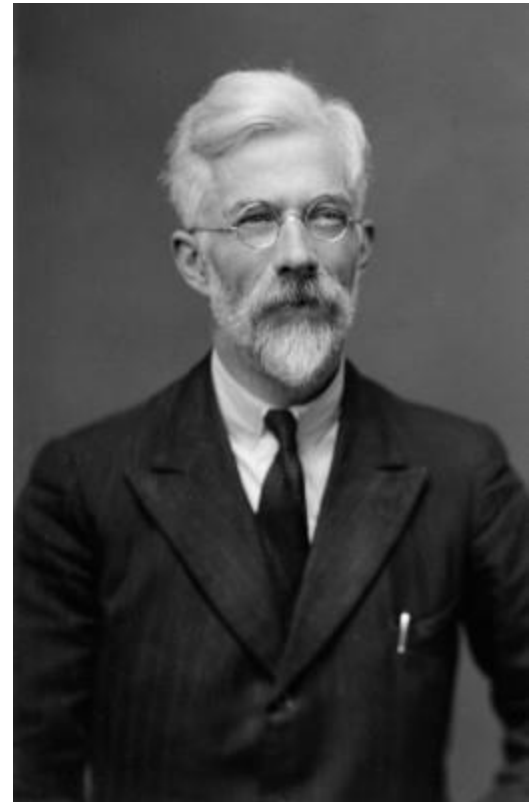
- ▶ Part 1: History of Null Hypothesis Significance Testing
 - ▶ Part 2: Problems with Null Hypothesis Significance Testing
 - ▶ Part 3: Multiplicity Issue and Null Hypothesis Significance Testing
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Part 1 : History of NHST

- ▶ Modern Null Hypothesis Significance Testing can be traced back to:
 - Fisher's Significance Testing
 - Neyman–Pearson Hypothesis Testing

Fisher's Significance Testing

- ▶ Ronald Aylmer Fisher was a biologist and statistician
- ▶ He was the main force behind tests of significance and can be considered the most influential figure in modern data analytic techniques



Main Goal of Fisherian Testing

- ▶ The primary motivation behind Fisher's approach to significance testing was to find the probability of the data, given the null hypothesis
 - This is our usual p -value
- ▶ Highlights
 - There is no alternative hypothesis
 - Power is of no interest
 - There is no alpha (α) level (a priori Type I error rate)

Steps Involved in Fisher's Approach to Significance Testing

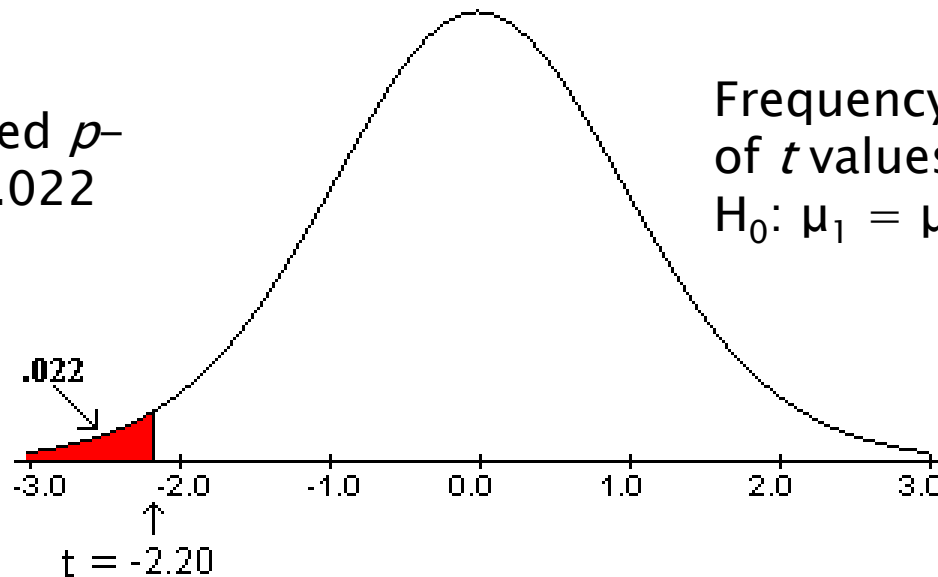
- ▶ Let's use as an example comparing two independent populations
 - Step 1: Select an appropriate test
 - Independent Samples t -test
 - Step 2: State H_0
 - $H_0: \mu_1 = \mu_2$
 - Could also be a directional hypothesis
 - E.g., $H_0: \mu_1 \geq \mu_2$
 - Could also test differences other than 0 (nil hypothesis)
 - E.g., $H_0: \mu_1 - \mu_2 = 5$ or $H_0: \mu_1 - \mu_2 \leq 5$

Steps Involved in Fisher's Approach to Significance Testing

- ▶ Step 3: Calculate the p -value, assuming H_0 is true
 - p -value: probability of finding a test statistic more extreme than that found, assuming H_0 is true

One-tailed p -value = .022

Frequency distribution of t values under $H_0: \mu_1 = \mu_2$ for $df = 15$



Steps Involved in Fisher's Approach to Significance Testing

▶ Step 4: Statistical Decision

- Is the p -value small enough to conclude that the results were highly unlikely if H_0 is true?
 - Typically made relative to some cutoff (e.g., .01, .05), however cutoffs need not be specified
 - What's important is that p -values of .049 and .051 are very similar probabilistically
 - Exact p -values are important since the magnitude of the probability is of utmost importance
 - The p -value provides information regarding the plausibility of H_0
 - Smaller p -values provide greater evidence against H_0

Steps Involved in Fisher's Approach to Significance Testing

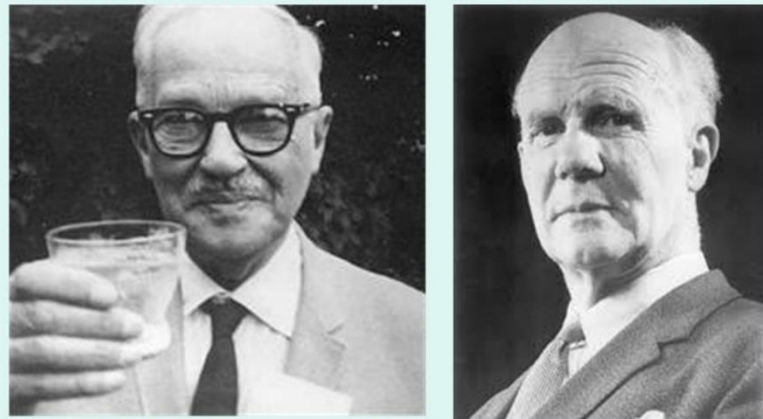
► Step 5: Interpret the Findings

- If a result is deemed statistically noteworthy, one of two statements is true
 - A rare mistake has occurred
 - H_0 does not accurately represent the true state of affairs
- Non-noteworthy results provide useful information, such as whether results were in the expected direction and the magnitude of the effects
 - Non-noteworthy results can even provide information that can be used to strengthen support for H_0

Neyman and Pearson's Hypothesis Testing Approach

- ▶ Jerzy Neyman and Egon Pearson sought to improve Fisher's approach to statistical significance testing
- ▶ Their approach greatly expanded on the principles and procedures outlined by Fisher

Jerzy Neyman and Egon Pearson



Steps Involved in Neyman and Pearson's Hypothesis Testing

- ▶ Step 1: State the Research Hypothesis
 - State what result is expected, including the minimally meaningful effect size (MMES)
 - This is used to establish appropriate hypotheses and conduct power analyses

- ▶ Step 2: Select an Appropriate Test Statistic
 - Note that since “power” is a concept in the Neyman and Pearson framework, tests can be compared based on differences in power (e.g., parametric vs nonparametric, one-tailed vs two-tailed)

Steps Involved in Neyman and Pearson's Hypothesis Testing

- ▶ Step 3: State the Main (Null) Hypothesis
 - Similar in nature to Fisher's H_0 (e.g., $H_0: \mu_1 = \mu_2$)
 - Also central to the Neyman–Pearson approach is the minimization of the risk of Type I errors (rejecting H_0 when it is true)
- ▶ Step 4: State the nominal Type I error rate (α)
 - A new concept is the idea of an α level
 - Under Neyman–Pearson only a single α level is chosen, where Fisher was more flexible (concern was the magnitude of p)

Steps Involved in Neyman and Pearson's Hypothesis Testing

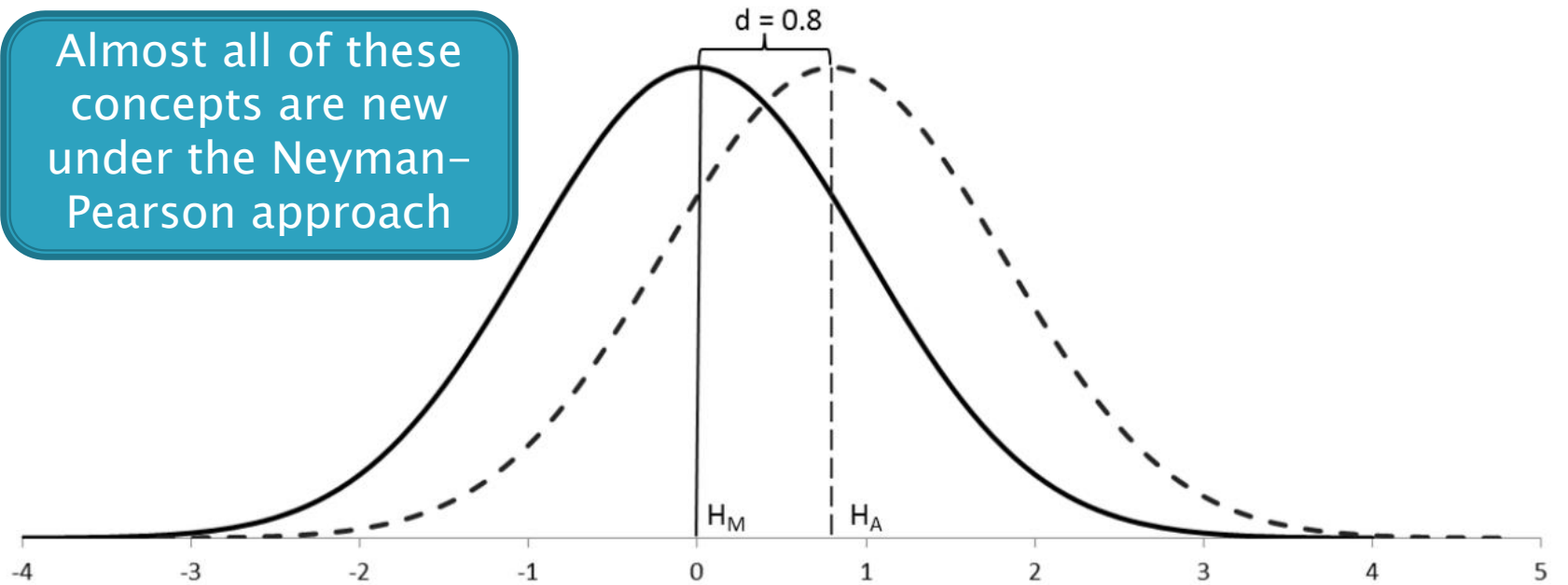
- ▶ Step 5: State the Alternate Hypothesis (H_A)
 - The concept of H_A is novel under the Neyman–Pearson approach
 - $H_A: \mu_1 \neq \mu_2$ could be used, but in the Neyman–Pearson framework we can also think of the alternate hypothesis with respect to the minimum meaningful effect size (e.g., $H_A: \mu_1 - \mu_2 = 3$)
 - The presence of H_A permits power analyses and introduces the concept of a Type II error (β , not rejecting H_0 when it is false)
 - Neyman and Pearson proposed 20% ($\beta = .20$) as an upper ceiling for β , and the value of alpha ($\beta = \alpha$) as its lower floor

Neyman–Pearson Hypothesis Testing

THE DECISION THE ANALYST MAKES	THE TRUTH	
	The null hypothesis (H_0) is true (H_a is false)	The null hypothesis (H_0) is not true (H_a is true)
	Reject H_0 (support H_a)	Correct Decision (1 - β) Power of the test
	TYPE I (α) error/ Alpha Risk/ p – value Overreacting (1 - α) = the Confidence level of the test	TYPE II (β) error/ Beta Risk Underreacting
	Fail to Reject H_0 (do not support H_a)	Correct Decision

Minimum Meaningful Effect Size, Power and the Alternate Hypothesis

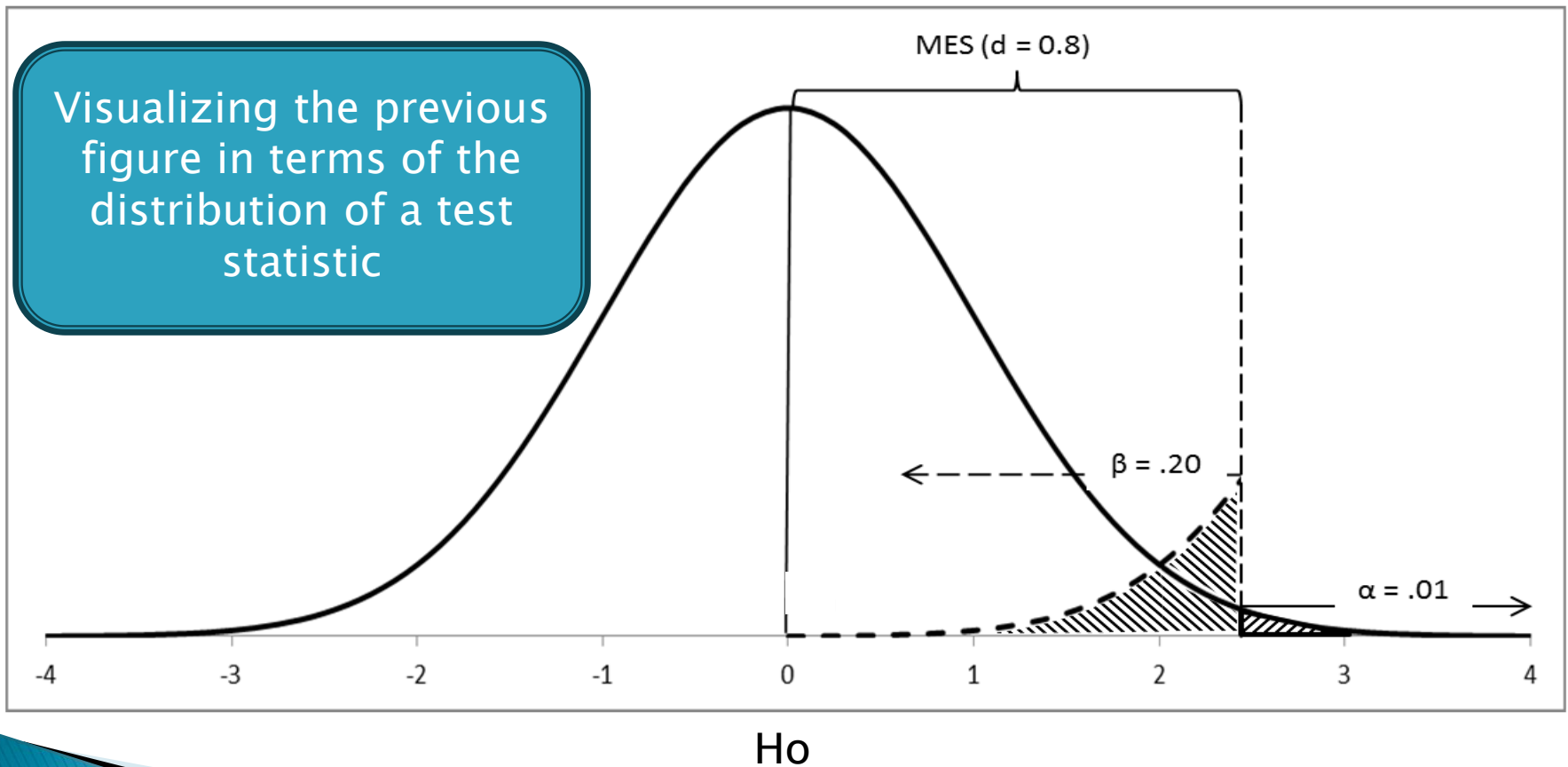
Almost all of these concepts are new under the Neyman-Pearson approach



Proposed distributions
under H_0/H_M and H_A

Minimum Meaningful Effect Size, Power and the Alternate Hypothesis

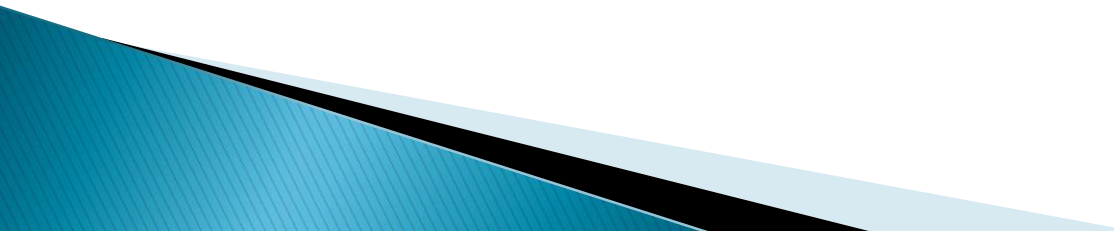
Visualizing the previous figure in terms of the distribution of a test statistic



Steps Involved in Neyman and Pearson's Hypothesis Testing

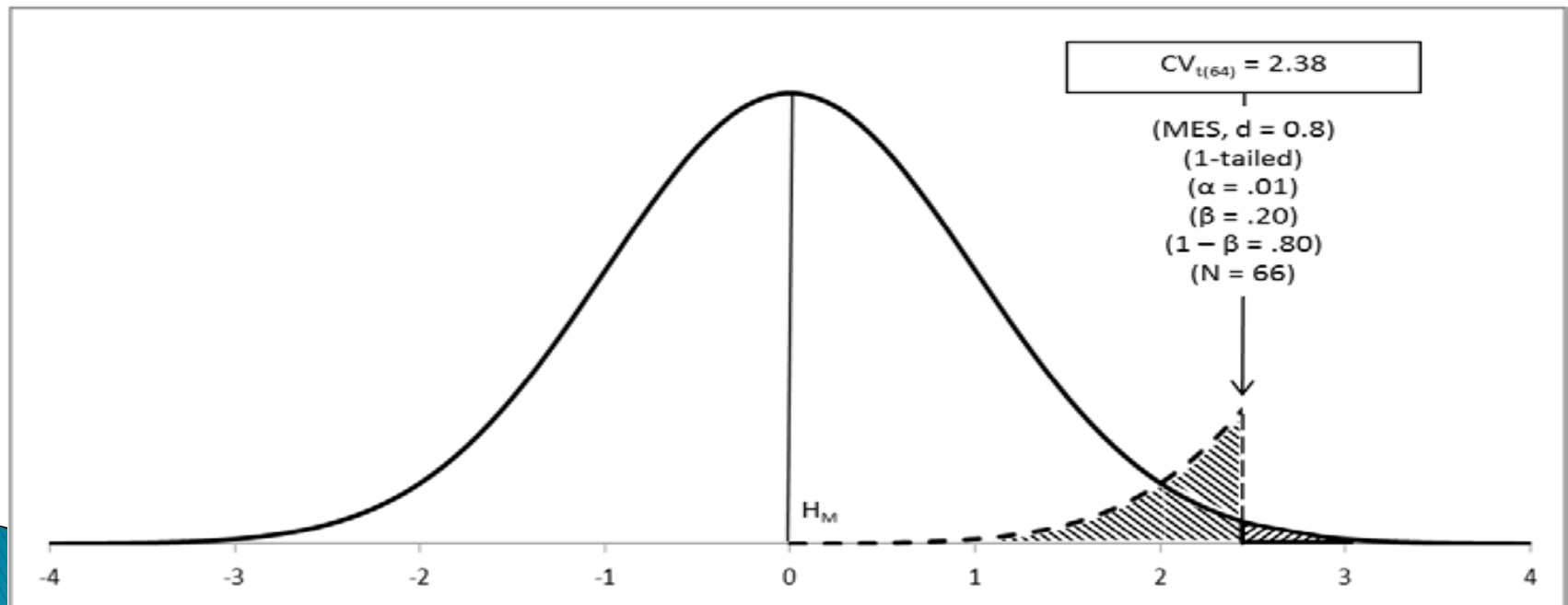
- ▶ Step 6: Conduct a Power Analysis
 - What sample size is required to ensure that $\beta < .20$ ($1 - \beta = .80$)?
 - There is no reason to conduct a low-power study (i.e., $1 - \beta < .80$)
 - β should fall between α and $.20$
 - *If it is desired to have β less than α , then the hypotheses should be reversed (N&P)*
 - Controlling for errors in the long run is very important!

Steps Involved in Neyman and Pearson's Hypothesis Testing

- ▶ Step 6: Conduct a Power Analysis
 - Power analyses based on the MMES were also to be conducted
 - In other words, from a power analysis perspective, important effects should be found with a high probability
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Steps Involved in Neyman and Pearson's Hypothesis Testing

- ▶ Step 7: Determine the Critical Value for the Test Statistic
 - The effect size ($d = .8$), along with α/β , determine N , N determines the df , and the df and α determine the CV



Steps Involved in Neyman and Pearson's Hypothesis Testing

- ▶ Step 8: Compare the test statistic to the critical value or the p -value to α
- ▶ Step 9: Make a decision regarding H_0/H_A
 - Reject or retain H_0
 - Unlike Fisher, the hypothesis decision is most important, not the magnitude of the p -value
- ▶ To summarize, the Neyman–Pearson approach emphasizes a priori decisions, including the MMES, error rates, power/sample size, etc., and focuses more on decisions regarding hypotheses than the magnitude of p -values

Modern NHST

- ▶ Modern null hypothesis significance testing borrows from both Fisher and Neyman–Pearson
 - Procedurally, most researchers follow Neyman–Pearson
 - Philosophically, however, many researchers are more in favour of Fisher’s approach in terms of evaluating evidence against H_0 through quantifying the magnitude of the p -value

Discussion Point

- ▶ What do you like or not like about either of the methods (Fisher vs Neyman–Pearson)?