

# PAUTA TAREA 1

## Pregunta 1

1.  $I_t = Y_t - C_t - G_t$

$$K_{t+1} = (1-\delta)K_t + (Y_t - C_t - G_t)$$

$$K_{t+1} - K_t = Y_t - C_t - G_t - \delta K_t \quad | \cdot 1/L_t$$

$$\frac{K_{t+1}}{L_t} - \frac{K_t}{L_t} = \frac{Y_t}{L_t} - \frac{C_t}{L_t} - \frac{G_t}{L_t} - \frac{\delta K_t}{L_t}$$

$$\frac{L_{t+1}}{L_t} \cdot \frac{K_{t+1}}{L_t} - K_t = Y_t - C_t - G_t - \delta K_t$$

$$\frac{L_{t+1}}{L_t} \cdot \frac{K_{t+1}}{L_{t+1}} - K_t = Y_t - C_t - G_t - \delta K_t$$

$$K_{t+1} - K_t = Y_t - C_t - G_t - \delta K_t$$

Ing. disponible del hogar:  $y_t - g_t = (1-\tau)y_t$

$$\therefore S_t = S \cdot \text{Ing. disponible} = s(1-\tau)y_t$$

$$C_t = (1-s) \cdot \text{Ing. disponible} = (1-s)(1-\tau)y_t$$

$$K_{t+1} - K_t = (y_t - g_t) - C_t - \delta K_t$$

$$= (1-\tau)y_t - (1-s)(1-\tau)y_t - \delta K_t$$

$$= s(1-\tau)y_t - \delta K_t$$

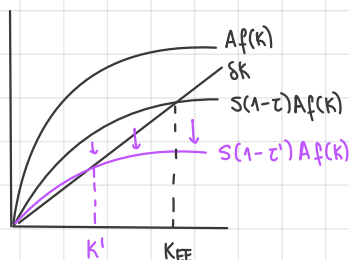
$$y_t = A_t \frac{F(K_t, L_t)}{L_t} = A_t F\left(\frac{K_t}{L_t}, \frac{L_t}{L_t}\right) = A_t f(k_t)$$

$$\Rightarrow K_{t+1} - K_t = s(1-\tau)A_t f(k_t) - \delta K_t$$

2. En EE:  $K_{t+1} = K_t = K^{EE}$ ,  $A_t = A$

$$0 = s(1-\tau)A f(k) - \delta K \Rightarrow \therefore K^{EE} \text{ satisface: } \delta K^{EE} = s(1-\tau)A f(K^{EE})$$

3.



- Como el gobierno no se puede endeudar, un aumento en  $g \Leftrightarrow$  aumento en  $\tau$ .
- Ante  $\uparrow \tau$ , cae la curva de inversión (y  $\therefore$  el  $K$ ), ya que los recursos que se usan para financiar la depreciación, ahora se usan para financiar  $g$ .
- Como el shock es transitorio, después  $g$  cae ( $\tau$  también) y  $K$  vuelve a su valor de EE.

4.  $y_t = C_t + i_t + g_t \Rightarrow K_t^\alpha g_t^\beta = C_t + i_t + g_t$

5.  $y_t = K_t^\alpha (\tau y_t)^\beta$   
 $y_t = K_t^\alpha \tau^\beta y_t^\beta$   $\rightarrow y_t^{1-\beta} = \tau^\beta K_t^\alpha \rightarrow y_t = [\tau^\beta K_t^\alpha]^{\frac{1}{1-\beta}}$

6. Ahora ya no tenemos  $A_t \therefore A_t f(k_t)$  pasa a ser solo  $f(k_t)$

$$K_{t+1} - K_t = s(1-\tau) f(k_t) - \delta K_t$$

$$K_{t+1} - K_t = s(1-\tau) \tau^{\beta/(1-\beta)} K_t^{\alpha/(1-\beta)} - \delta K_t$$

En EE:

$$\delta K^{EE} = s(1-\tau) \tau^{\beta/(1-\beta)} K^{EE \alpha/(1-\beta)}$$

$$\frac{\delta K^{EE \alpha/(1-\beta)}}{K^{EE \alpha/(1-\beta)}} = \frac{s(1-\tau) \tau^{\beta/(1-\beta)}}{\delta}$$

$$K^{EE \frac{1-\alpha-\beta}{1-\beta}} = \frac{s(1-\tau) \tau^{\beta/(1-\beta)}}{\delta}$$

$$K^{EE} = \left[ \frac{s(1-\tau) \tau^{\beta/(1-\beta)}}{\delta} \right]^{\frac{1-\alpha-\beta}{1-\beta}}$$

7.  $K^{EE} = \left( \frac{s}{\delta} \right)^{\frac{1-\alpha-\beta}{1-\beta}} \left[ \tau^{\beta/(1-\beta)} - \tau^{1/(1-\beta)} \right]^{\frac{1-\alpha-\beta}{1-\beta}}$

$$\frac{\partial KEE}{\partial \tau} = 0 \Rightarrow \frac{\partial KEE}{\partial \tau} = \left( \frac{s}{\delta} \right)^{\frac{1-\alpha}{1-\beta}} \left[ \left( \frac{1-\alpha}{1-\beta} \right) \left[ \tau^{\beta/(1-\beta)} - \tau^{1/(1-\beta)} \right]^{-\alpha/(1-\beta)} \left( \left( \frac{\beta}{1-\beta} \right) \tau^{-1/(1-\beta)} - \left( \frac{1}{1-\beta} \right) \tau^{-\beta/(1-\beta)} \right) \right] = 0$$

$$\left[ \tau^{\beta/(1-\beta)} - \tau^{1/(1-\beta)} \right]^{-\alpha/(1-\beta)} \left[ \beta \tau^{-1/(1-\beta)} - \tau^{-\beta/(1-\beta)} \right] = 0$$

Asumiendo que  $\left[ \tau^{\beta/(1-\beta)} - \tau^{1/(1-\beta)} \right]^{-\alpha/(1-\beta)} \neq 0$ :

$$\beta \tau^{-1/(1-\beta)} - \tau^{-\beta/(1-\beta)} = 0$$

$$\tau^{-\beta/(1-\beta) + 1/(1-\beta)} = \beta$$

$$\tau^* = \beta$$

→ corresponde a la participación del gasto de gobierno en la fn. de producción

## Pregunta 2

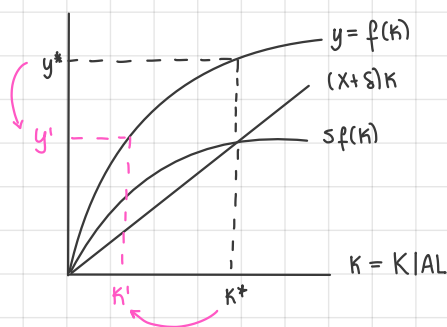
1.

•  $n = 0$ , estado estacionario

• ¿qué sucede con  $y = Y/AL$  si hay un aumento en  $L$ ?

- Un aumento en  $L$ , hace que  $k = K/AL$  caiga, es decir, cae el capital por trabajador efectivo. Un menor  $k$ , dado que,  $f'(k) > 0$ , también hace que  $y = f(k)$  sea menor, por lo tanto, el producto por trabajador efectivo también cae. Ahora bien, además del efecto directo sobre el producto, un  $k$  menor implica que este es más productivo (porque  $f''(k) < 0$ ), la economía va a invertir más en capital, haciendo que este aumente. Lo anterior, va acompañado de un mayor producto por trabajador efectivo.

El aumento continuo de  $k$  eventualmente se va a topar con los rendimientos decrecientes, llegando al punto donde se comienza a deprecian. En ese punto,  $k$  queda constante en su valor de estado estacionario, al igual que el producto.



$$\dot{K} = sf(k) - (s + x)k, \quad y = f(k), \quad k = K/AL$$

Etapas 1:  $\uparrow L \Rightarrow \downarrow k \Rightarrow k' < k^* \Rightarrow y' < y^*$  (debido a  $f'(k) > 0$ )

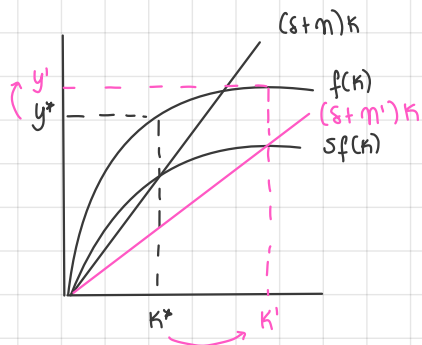
Etapas 2:  $k' < k^* \Rightarrow sf(k') > (s + x)k' \Rightarrow \uparrow k' \Rightarrow \uparrow y'$

Etapas 3:  $\uparrow k'$  hasta que  $sf(k') = (s + x)k' \Rightarrow k' = k^* \Rightarrow y' = y^*$

2.

•  $n > 0$ ,  $x = 0$ , estado estacionario

• ¿qué sucede con  $k$ ,  $y$ ,  $c$  si cae  $n$ ?



-  $\downarrow n$ , cae la pendiente de  $(s + m)k$

-  $\dot{K} = sf(k) - (s + m)k \rightarrow$  antes  $\dot{K} = 0$ , ahora  $\dot{K} > 0 \therefore k' > k^*$

-  $\uparrow k \Rightarrow \uparrow y$  ( $y' > y^*$ )

-  $c = (1 - s)y \Rightarrow \uparrow y \Rightarrow \uparrow c$

$\therefore$  sube el capital, producto y consumo

### 3. Economía centralizada (problema del planner)

$$- Y(t) = C(t) + I(t), \quad \dot{K}(t) = I(t) - \delta K(t), \quad I(t) = sY(t)$$

$$- \dot{K}(t) = sY(t) - \delta K(t) / \cdot 1/A(t)L(t) \rightarrow \text{fn. de producción es labor augmenting}$$

$$\frac{\dot{K}(t)}{A(t)L(t)} = \frac{sY(t)}{A(t)L(t)} - \frac{\delta K(t)}{A(t)L(t)}$$

$$- \dot{K}(t) = \frac{\partial K(t)/A(t)L(t)}{\partial t}$$

$$= \frac{\dot{K}(t)}{A(t)L(t)} - \frac{K(t)}{A(t)^2 L(t)^2} [A(t)\dot{L}(t) + A(t)L(t)\dot{A}(t)]$$

$$\dot{K}(t) = \frac{\dot{K}(t)}{A(t)L(t)} - K(t) \left[ \frac{\dot{A}(t)L(t)}{A(t)L(t)} + \frac{A(t)\dot{L}(t)}{A(t)L(t)} \right]$$

$$\dot{K}(t) = \frac{\dot{K}(t)}{A(t)L(t)} - K(t)(n+x)$$

$$- Y(t)/A(t)L(t) = (K(t)/A(t)L(t))^\alpha (A(t)L(t)/A(t)L(t))^{1-\alpha}$$

$$f(K(t)) = K(t)^\alpha$$

$$\text{En EE: } \dot{K}(t) = 0, \quad K(t) = K^{EE}$$

$$- \dot{K}(t) = \frac{\dot{K}(t)}{A(t)L(t)} - K(t)(n+x)$$

$$\dot{K}(t) = \frac{sY(t)}{A(t)L(t)} - \frac{\delta K(t)}{A(t)L(t)} - K(t)(n+x)$$

$$0 = sK^{EE\alpha} - K^{EE}(\delta+n+x)$$

$$sK^{EE\alpha} = K^{EE}(\delta+n+x)$$

$$K^{EE\alpha-1} = \frac{\delta+n+x}{s}$$

$$K^{EE} = \left[ \frac{\delta+n+x}{s} \right]^{1/\alpha-1}$$

$$\dot{K}(t) = sK(t)^\alpha - K(t)(\delta+n+x)$$

### Economía descentralizada (problema del hogar y la firma)

Hogares:

- acumulación de activos ( $A$ : tecnología,  $\bar{A}$ : activos):

$$\dot{\bar{A}}(t) = [r(t)\bar{A}(t) + w(t)L(t)] - C(t) / \cdot 1/A(t)L(t)$$

$$\frac{\dot{\bar{A}}(t)}{A(t)L(t)} = \frac{r(t)\bar{A}(t)}{A(t)L(t)} + \frac{w(t)L(t)}{A(t)L(t)} - \frac{C(t)}{A(t)L(t)}$$

$$\dot{\bar{A}}(t) = \frac{\partial (\bar{A}(t)/A(t)L(t))}{\partial t}$$

$$= \frac{\dot{\bar{A}}(t)}{A(t)L(t)} - \frac{\bar{A}(t)}{A(t)^2 L(t)^2} [A(t)\dot{L}(t) + A(t)L(t)\dot{A}(t)]$$

$$\dot{\bar{A}}(t) = \frac{\dot{\bar{A}}(t)}{A(t)L(t)} - \bar{A}(t) \left[ \frac{\dot{A}(t)L(t)}{A(t)L(t)} + \frac{A(t)\dot{L}(t)}{A(t)L(t)} \right]$$

$$\dot{\bar{A}}(t) = \frac{\dot{\bar{A}}(t)}{A(t)L(t)} - \bar{A}(t)(n+x)$$

$$\dot{\bar{A}}(t) = \frac{r(t)\bar{A}(t)}{A(t)L(t)} + \frac{w(t)L(t)}{A(t)L(t)} - \frac{C(t)}{A(t)L(t)} - \bar{A}(t)(n+x)$$

$$\dot{\bar{A}}(t) = r(t)\bar{A}(t) + \frac{w(t)}{A(t)} - C(t) - \bar{A}(t)(n+x)$$

Usaremos que  $A(t) = A(0) e^{xt}$  con  $A(0) = 1 \therefore A(t) = e^{xt}$

$$\dot{\bar{A}}(t) = (r(t) - n - x)\bar{A}(t) + \frac{w(t)}{A(t)} e^{-xt} - C(t)$$

Firmas:

- max. sus beneficios con  $R(t) = r(t) + \delta$

$$\pi(t) = F(K(t), A(t)L(t)) - R(t)K(t) - w(t)L(t)$$

$$\begin{aligned} & F(K(t), A(t)L(t)) - (r(t) + \delta)K(t) - w(t)L(t) \quad / \cdot A(t)L(t) / A(t)L(t) \\ & A(t)L(t) \left[ F\left(\frac{K(t)}{A(t)L(t)}, 1\right) - \frac{(r(t) + \delta)K(t)}{A(t)L(t)} - w(t)e^{-xt} \right] \\ & = A(t)L(t) [K(t)^\alpha - (r(t) + \delta)K(t) - w(t)e^{-xt}] \end{aligned}$$

$$\frac{\partial \pi}{\partial K} = 0 \rightarrow \alpha K(t)^{\alpha-1} - (r(t) + \delta) = 0 \rightarrow \boxed{r(t) = \alpha K(t)^{\alpha-1} - \delta}$$

$$\frac{\partial \pi}{\partial L} = 0 \rightarrow A(t) \left[ (K(t)^\alpha - (r(t) + \delta)K(t) - w(t)e^{-xt}) + L(t) \left( \alpha K(t)^{\alpha-1} \cdot (-1) \cdot \frac{K(t)}{L(t)^2} - (r(t) + \delta) \cdot (-1) \cdot \frac{K(t)}{L(t)^2} \right) \right] = 0$$

$$K(t)^\alpha - (r(t) + \delta)K(t) - w(t)e^{-xt} + \frac{L(t)}{L(t)} \left( -\alpha K(t)^{\alpha-1} K(t) + (r(t) + \delta)K(t) \right) = 0$$

$$K(t)^\alpha - \cancel{(r(t) + \delta)K(t)} - w(t)e^{-xt} - \alpha K(t)^{\alpha-1} K(t) + \cancel{(r(t) + \delta)K(t)} = 0$$

$$\boxed{w(t) = e^{xt} [K(t)^\alpha - \alpha K(t)^{\alpha-1} K(t)]} \Leftrightarrow w(t) = e^{xt} [f(K(t)) - K(t) f'(K(t))]$$

Equilibrio

- Tenemos:

$$\begin{aligned} \dot{a}(t) &= (r(t) - n - x) a(t) + w(t) e^{-xt} - c(t) \\ r(t) &= \alpha K(t)^{\alpha-1} - \delta \\ w(t) &= e^{xt} [K(t)^\alpha - \alpha K(t)^{\alpha-1} K(t)] \\ a(t) &= K(t) \rightarrow \text{en ec. cerrada} \end{aligned}$$

$$\begin{aligned} \therefore \dot{K}(t) &= (\alpha K(t)^{\alpha-1} - \delta - n - x) K(t) + \cancel{e^{-xt}} \cdot \cancel{e^{xt}} [K(t)^\alpha - \alpha K(t)^{\alpha-1} K(t)] - c(t) \\ &= -(\delta + n + x) K(t) + \cancel{\alpha K(t)^{\alpha-1} K(t)} + K(t)^\alpha - \cancel{\alpha K(t)^{\alpha-1} K(t)} - c(t) \\ &= K(t)^\alpha - c(t) - (\delta + n + x) K(t) \end{aligned}$$

recordando que  $K(t)^\alpha = f(K(t))$ ,  $f(K(t)) = c(t) + i(t)$ ,  $i(t) = s f(K(t))$

$$\begin{aligned} f(K(t)) - c(t) &= i(t) = s f(K(t)) \\ K(t)^\alpha - c(t) &= s K(t)^\alpha \end{aligned}$$

$$\therefore \boxed{\dot{K}(t) = s K(t)^\alpha - K(t)(\delta + n + x)}$$

→ Dado que no hay distorsiones, las dinámicas del capital son equivalentes en ambas economías, y  $\therefore$  el KEE también.

#### 4. Trayectoria analítica del capital

$$\begin{aligned} \dot{K}(t) &= s K(t)^\alpha - K(t)(\delta + n + x) \quad / \cdot K(t)^{1-\alpha} \\ \dot{K}(t) \cdot K(t)^{1-\alpha} &= s - K(t)^{1-\alpha} (\delta + n + x) \quad (1) \end{aligned}$$

Definimos  $v(t) = K(t)^{1-\alpha} \Rightarrow \ln(v(t)) = (1-\alpha) \ln(K(t))$

$$\ln(\dot{v}(t)) = (1-\alpha) \ln(K(t)) \Leftrightarrow \frac{\dot{v}(t)}{v(t)} = (1-\alpha) \cdot \frac{\dot{K}(t)}{K(t)} = \frac{\dot{K}(t)}{K(t)} = K(t) \cdot \frac{\dot{v}(t)}{v(t)} \cdot \left( \frac{1}{1-\alpha} \right)$$

Reemplazamos  $K(t) = K(t) \cdot \frac{\dot{V}(t)}{V(t)} \cdot \left(\frac{1}{1-\alpha}\right)$  en (1)

$$K(t) \cdot \frac{\dot{V}(t)}{V(t)} \cdot \left(\frac{1}{1-\alpha}\right) \cdot K(t)^{1-\alpha} = s - K(t)^{1-\alpha} (\delta + m + x)$$

$$s = K(t)^{1-\alpha} \cdot \frac{\dot{V}(t)}{V(t)} \left(\frac{1}{1-\alpha}\right) + K(t)^{1-\alpha} (\delta + m + x)$$

$$s = K(t)^{1-\alpha} \left[ \frac{\dot{V}(t)}{V(t)} \left(\frac{1}{1-\alpha}\right) + (\delta + m + x) \right]$$

Reemplazamos  $K(t)^{1-\alpha} = V(t)$

$$s = V(t) \left[ \frac{\dot{V}(t)}{V(t)} \left(\frac{1}{1-\alpha}\right) + (\delta + m + x) \right]$$

$$s = \left(\frac{1}{1-\alpha}\right) \dot{V}(t) + (\delta + m + x) V(t)$$

$$s(1-\alpha) = \dot{V}(t) + (1-\alpha)(\delta + m + x) V(t)$$

Dado que necesitamos trabajar con integrales, cambiemos el argumento de  $\dot{V}()$  y  $V()$  a  $b$ .

$$\begin{aligned} s(1-\alpha) &= \dot{V}(b) + (1-\alpha)(\delta + m + x) V(b) \quad / \quad e^{(1-\alpha)(\delta + m + x)b} \\ e^{(1-\alpha)(\delta + m + x)b} s(1-\alpha) &= e^{(1-\alpha)(\delta + m + x)b} [\dot{V}(b) + (1-\alpha)(\delta + m + x) V(b)] \quad / \quad \int_0^t () db \\ \int_0^t e^{(1-\alpha)(\delta + m + x)b} s(1-\alpha) db &= \int_0^t e^{(1-\alpha)(\delta + m + x)b} [\dot{V}(b) + (1-\alpha)(\delta + m + x) V(b)] db \\ s(1-\alpha) \left[ \frac{e^{(1-\alpha)(\delta + m + x)b}}{(1-\alpha)(\delta + m + x)} + C_1 \right] \Big|_0^t &= \left[ e^{(1-\alpha)(\delta + m + x)b} V(b) + C_2 \right] \Big|_0^t \end{aligned}$$

$$s(1-\alpha) \left[ \frac{e^{(1-\alpha)(\delta + m + x)t}}{(1-\alpha)(\delta + m + x)} + C_1 \right] - \frac{e^{(1-\alpha)(\delta + m + x)0}}{(1-\alpha)(\delta + m + x)} - C_1 = e^{(1-\alpha)(\delta + m + x)t} V(t) + C_2 - e^{(1-\alpha)(\delta + m + x)0} V(0) - C_2$$

$$\begin{aligned} \left(\frac{s}{\delta + m + x}\right) e^{(1-\alpha)(\delta + m + x)t} - \left(\frac{s}{\delta + m + x}\right) &= e^{(1-\alpha)(\delta + m + x)t} V(t) - V(0) \\ V(t) &= \left(\frac{s}{\delta + m + x}\right) - \left(\frac{s}{\delta + m + x}\right) e^{-(1-\alpha)(\delta + m + x)t} + V(0) e^{-(1-\alpha)(\delta + m + x)t} \end{aligned}$$

$$V(t) = \left(\frac{s}{\delta + m + x}\right) + e^{-(1-\alpha)(\delta + m + x)t} \left[ V(0) - \left(\frac{s}{\delta + m + x}\right) \right]$$

Reemplazamos  $V(t) = K(t)^{1-\alpha}$

$$K(t)^{1-\alpha} = \left(\frac{s}{\delta + m + x}\right) e^{-(1-\alpha)(\delta + m + x)t} \left[ K(0)^{1-\alpha} - \left(\frac{s}{\delta + m + x}\right) \right]$$

$$K(t) = \left[ \left(\frac{s}{\delta + m + x}\right) e^{-(1-\alpha)(\delta + m + x)t} \left[ K(0)^{1-\alpha} - \left(\frac{s}{\delta + m + x}\right) \right] \right]^{\frac{1}{1-\alpha}} \rightarrow \text{La brecha entre } K \text{ y su valor de EE se cierra a tasa } (1-\alpha)(\delta + m + x).$$

## 5. Ecuación de convergencia del producto. Velocidad de convergencia

$$\dot{K}(t) = sK(t)^\alpha - K(t)(\delta + n + x) \quad / \cdot 1/K(t)$$

$$\frac{\dot{K}(t)}{K(t)} = sK(t)^{\alpha-1} - (\delta + n + x)$$

$$\ln(\dot{K}(t)) = s \cdot e^{-(1-\alpha)\ln(K(t))} - (\delta + n + x)$$

Hacemos una expansión de Taylor en torno a su PE:

$$\ln(\dot{K}(t)) \approx \ln(\dot{K}^{EE}) + \left( \frac{\partial \ln(\dot{K}(t))}{\partial \ln(K(t))} \right) \bigg|_{\ln(K^{EE})} (\ln(K(t)) - \ln(K^{EE}))$$

$$\ln(\dot{K}(t)) \approx -s(1-\alpha)K^{EE}{}^{\alpha-1} (\ln(K(t)) - \ln(K^{EE}))$$

Calculamos  $K^{EE}$ .

$$0 = sK^{EE}{}^\alpha - K^{EE}(\delta + n + x)$$

$$sK^{EE}{}^\alpha = K^{EE}(\delta + n + x)$$

$$K^{EE}{}^{\alpha-1} = \left( \frac{\delta + n + x}{s} \right)$$

$$\therefore \ln(\dot{K}(t)) \approx -\cancel{s}(1-\alpha) \left( \frac{\delta + n + x}{\cancel{s}} \right) (\ln(K(t)) - \ln(K^{EE}))$$

$$\ln(\dot{K}(t)) \approx -(1-\alpha)(\delta + n + x)(\ln(K(t)) - \ln(K^{EE}))$$

$$\ln(\dot{K}(t)) + (1-\alpha)(\delta + n + x)\ln(K(t)) = (1-\alpha)(\delta + n + x)\ln(K^{EE})$$

Si  $y(t) = K(t)^\alpha \rightarrow K(t) = y(t)^{1/\alpha}$ :

$$\ln(y(t)^{1/\alpha}) + (1-\alpha)(\delta + n + x)\ln(y(t)^{1/\alpha}) = (1-\alpha)(\delta + n + x)\ln(y^{EE})$$

$$\cancel{1/\alpha} \ln(y(t)) + \cancel{1/\alpha} (1-\alpha)(\delta + n + x)\ln(y(t)) = \cancel{1/\alpha} (1-\alpha)(\delta + n + x)\ln(y^{EE})$$

$$\ln(y(t)) = -(1-\alpha)(\delta + n + x)[\ln(y(t)) - \ln(y^{EE})]$$

Dado que necesitamos trabajar con integrales cambiamos el argumento a b.

$$\ln(y(b)) = -(1-\alpha)(\delta + n + x)[\ln(y(b)) - \ln(y^{EE})] / e^{(1-\alpha)(\delta + n + x)b}$$

$$e^{(1-\alpha)(\delta + n + x)b} \ln(y(b)) = e^{(1-\alpha)(\delta + n + x)b} (1-\alpha)(\delta + n + x)\ln(y^{EE}) - e^{(1-\alpha)(\delta + n + x)b} (1-\alpha)(\delta + n + x)\ln(y(b)) / \int_0^t db$$

$$\int_0^t e^{(1-\alpha)(\delta + n + x)b} \ln(y(b)) db = \int_0^t [e^{(1-\alpha)(\delta + n + x)b} (1-\alpha)(\delta + n + x)\ln(y^{EE})] db - \int_0^t e^{(1-\alpha)(\delta + n + x)b} (1-\alpha)(\delta + n + x)\ln(y(b)) db$$

$$\int_0^t [e^{(1-\alpha)(\delta + n + x)b} \ln(y(b)) + e^{(1-\alpha)(\delta + n + x)b} (1-\alpha)(\delta + n + x)\ln(y(b))] db = (1-\alpha)(\delta + n + x)\ln(y^{EE}) \int_0^t e^{(1-\alpha)(\delta + n + x)b} db$$

$$\left[ e^{(1-\alpha)(\delta + n + x)b} \ln(y(b)) + C_1 \right]_0^t = (1-\alpha)(\delta + n + x)\ln(y^{EE}) \left[ \frac{e^{(1-\alpha)(\delta + n + x)b}}{(1-\alpha)(\delta + n + x)} + C_2 \right]_0^t$$

$$e^{(1-\alpha)(\delta + n + x)t} \ln(y(t)) - \ln(y(0)) = \ln(y^{EE})(e^{(1-\alpha)(\delta + n + x)t} - 1) / e^{-(1-\alpha)(\delta + n + x)t}$$

$$\ln(y(t)) - e^{-(1-\alpha)(s+m+x)t} \ln(y(0)) = \ln(y_{EE}) - e^{-(1-\alpha)(s+m+x)t} \ln(y_{EE})$$

$$\ln(y(t)) = \ln(y_{EE}) - e^{-(1-\alpha)(s+m+x)t} \ln(y_{EE}) + e^{-(1-\alpha)(s+m+x)t} \ln(y(0))$$

velocidad de convergencia:  $\beta = - \left. \frac{\partial \dot{k}/k}{\partial \ln(k)} \right|_{k=EE} = -(- (1-\alpha)(s+m+x)) = (1-\alpha)(s+m+x)$

$$\therefore \ln(y(t)) = \ln(y_{EE}) - e^{-\beta t} \ln(y_{EE}) + e^{-\beta t} \ln(y(0))$$

6. Respuesta libre pero es importante mencionar que la convergencia condicional depende de las condiciones iniciales, en este caso,  $\ln(y(0))$ .