

```
ops = { '+': lambda x,y: x+y,
        '-': lambda x,y: x-y,
        '*': lambda x,y: x*y,
        '/': lambda x,y: x//y }
```

```
def make_node(op, name):
    class node:
        def __init__(self, op1, op2):
            self.__operand1 = op1
            self.__operand2 = op2
        def eval(self):
            return op(self.__operand1.eval(), self.__operand2.eval())
        def combine(self):
            if isinstance(self.__operand1, leaf) and
                isinstance(self.__operand2, leaf):
                return leaf(str(self.eval()))
            else:
                self.__operand1 = self.__operand1.combine()
                self.__operand2 = self.__operand2.combine()
                return self
        def __str__(self): return "("+self.__operand1.__str__() +
                                    name + self.__operand2.__str__()+")"
    return node
```

```
class leaf:
    def __init__(self, value):
        self.__value = value
    def eval(self):
        return int(self.__value)
    def combine(self): return self
    def __str__(self): return self.__value
```

```
translator = {op:make_node(fop, op) for op, fop in ops.items()}
translator.update({str(x):leaf(str(x)) for x in range(10)})
```

```
class calculator:
    def __init__(self, expr):
        self.__root, dropped = self.__convert(expr, 0)
    def is_value(self): return isinstance(self.__root, leaf)
    def __convert(self, expr, n):
        if n < len(expr):
            if expr[n] in {'+', '*', '-', '/'}:
                op1,n1 = self.__convert(expr,n+1)
                op2,n2 = self.__convert(expr,n1+1)
                return translator[expr[n]](op1,op2),n2
            else: return translator[expr[n]],n
    def combine(self):
        self.__root = self.__root.combine()
        return self
    def eval(self): return self.__root.eval()
    def __str__(self): return self.__root.__str__()
```

```
def print_reduction(e):
    print(e)
    if not e.is_value(): print_reduction(e.combine())
```