

PRACTICAL - 07

Code:

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// Ashwin Navange A-38 CSE
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
typedef long long int dlong;
typedef struct {
    dlong x, y;
} epnt;
typedef struct {
    long a, b;
    dlong N;
    epnt G;
    dlong r;
} curve;
typedef struct {
    long a, b;
} pair;

const long mxN = 1073741789;
const long mxr = 1073807325;
const long inf = -2147483647;
curve e;
epnt zerO;
int inverr;
long exgcd (long v, long u)
{
    register long q, t;
    long r = 0, s = 1;
    if (v < 0) v += u;

    while (v) {
        q = u / v;
        t = u - q * v;
        u = v; v = t;
        t = r - q * s;
        r = s; s = t;
    }
    if (u != 1) {
        printf ("impossible inverse mod N, gcd = %d\n", u);
        inverr = 1;
    }
    return r;
}
static inline dlong modn (dlong a)
{
    a %= e.N;
    if (a < 0) a += e.N;
    return a;
}
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dlong modr (dlong a)
{
    a %= e.r;
    if (a < 0) a += e.r;
    return a;
}

long disc (void)
{
    dlong c, a = e.a, b = e.b;
    c = 4 * modn(a * modn(a * a));
    return modn(-16 * (c + 27 * modn(b * b)));
}

int isO (epnt p)
{
    return (p.x == inf) && (p.y == 0);
}

int ison (epnt p)
{
    long r, s;
    if (! isO (p)) {
        r = modn(e.b + p.x * modn(e.a + p.x * p.x));
        s = modn(p.y * p.y);
    }
    return (r == s);
}

void padd (epnt *r, epnt p, epnt q)
{
    dlong la, t;

    if (isO(p)) {*r = q; return;}
    if (isO(q)) {*r = p; return;}

    if (p.x != q.x) {
        t = p.y - q.y;
        la = modn(t * exgcd(p.x - q.x, e.N));
    }
    else
        if ((p.y == q.y) && (p.y != 0)) {
            t = modn(3 * modn(p.x * p.x) + e.a);
            la = modn(t * exgcd (2 * p.y, e.N));
        }
    else
        {*r = zerO; return;}

    t = modn(la * la - p.x - q.x);
    r->y = modn(la * (p.x - t) - p.y);
    r->x = t; if (inverr) *r = zerO;
}

void pmul (epnt *r, epnt p, long k)
{
    epnt s = zerO, q = p;

    for (; k; k >>= 1) {

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        if (k & 1) padd(&s, s, q);
        if (inverr) {s = zerO; break;}
        padd(&q, q, q);
    }
    *r = s;
}
void pprint (char *f, epnt p)
{
    dlong y = p.y;

    if (isO (p))
        printf ("%s (0)\n", f);

    else {
        if (y > e.N - y) y -= e.N;
        printf ("%s (%lld, %lld)\n", f, p.x, y);
    }
}
int ellinit (long i[])
{
    long a = i[0], b = i[1];
    e.N = i[2]; inverr = 0;

    if ((e.N < 5) || (e.N > mxN)) return 0;

    e.a = modn(a);
    e.b = modn(b);
    e.G.x = modn(i[3]);
    e.G.y = modn(i[4]);
    e.r = i[5];

    if ((e.r < 5) || (e.r > mxr)) return 0;

    printf ("\nE: y^2 = x^3 + %dx + %d", a, b);
    printf (" (mod %lld)\n", e.N);
    pprint ("base point G", e.G);
    printf ("order(G, E) = %lld\n", e.r);

    return 1;
}
double rnd(void)
{
    return rand() / ((double)RAND_MAX + 1);
}
pair signature (dlong s, long f)
{
    long c, d, u, u1;
    pair sg;
    epnt V;

    printf ("\nsignature computation\n");
    do {
        do {

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    u = 1 + (long)(rnd() * (e.r - 1));
    pmul (&V, e.G, u);
    c = modr(V.x);
}
while (c == 0);

u1 = exgcd (u, e.r);
d = modr(u1 * (f + modr(s * c)));
}
while (d == 0);
printf ("one-time u = %d\n", u);
pprint ("V = uG", V);

sg.a = c; sg.b = d;
return sg;
}
int verify (epnt W, long f, pair sg)
{
    long c = sg.a, d = sg.b;
    long t, c1, h1, h2;
    dlong h;
    epnt V, V2;

    t = (c > 0) && (c < e.r);
    t &= (d > 0) && (d < e.r);
    if (! t) return 0;

    printf ("\nsignature verification\n");
    h = exgcd (d, e.r);
    h1 = modr(f * h);
    h2 = modr(c * h);
    printf ("h1,h2 = %d, %d\n", h1,h2);
    pmul (&V, e.G, h1);
    pmul (&V2, W, h2);
    pprint ("h1G", V);
    pprint ("h2W", V2);
    padd (&V, V, V2);
    pprint ("+ =", V);
    if (isO (V)) return 0;
    c1 = modr(V.x);
    printf ("c' = %d\n", c1);

    return (c1 == c);
}

void ec_dsa (long f, long d)
{
    long i, s, t;
    pair sg;
    epnt W;
    t = (disc() == 0);
    t |= isO (e.G);
    pmul (&W, e.G, e.r);

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t |= ! isO (W);
t |= ! ison (e.G);
if (t) goto errmsg;

printf ("\nkey generation\n");
s = 1 + (long)(rnd() * (e.r - 1));
pmul (&W, e.G, s);
printf ("private key s = %d\n", s);
pprint ("public key W = sG", W);
t = e.r;
for (i = 1; i < 32; i <= 1)
    t |= t >> i;
while (f > t) f >>= 1;
printf ("\naligned hash %x\n", f);

sg = signature (s, f);
if (inverr) goto errmsg;
printf ("signature c,d = %d, %d\n", sg.a, sg.b);

if (d > 0) {
    while (d > t) d >>= 1;
    f ^= d;
    printf ("\ncorrupted hash %x\n", f);
}

t = verify (W, f, sg);
if (inverr) goto errmsg;
if (t)
    printf ("Valid\n_____\n");
else
    printf ("invalid\n_____\n");

return;

errmsg:
printf ("invalid parameter set\n");
printf ("_____ \n");
}

int main (void)
{
printf("Ashwin Navange A-38 CSE\n");
typedef long eparm[6];
long d, f;
zerO.x = inf; zerO.y = 0;
srand(time(NULL));
eparm *sp, sets[3] = {
    {355, 671, 1073741789, 13693, 10088, 1073807281},
    { 3, 2,    5,  2,  1,    5},
    //{ 0, 7, 67096021, 6580, 779, 67079644},
};
f = 0x789abcde; d = 0;

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for (sp = sets; ; sp++) {
    if (ellinit (*sp))
        ec_dsa (f, d);

    else
        break;
}
}

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Output:

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"E:\College\Sem7\CSS Prac\P7\P7.exe"
Ashwin Navange A-38 CSE

E:  $y^2 = x^3 + 355x + 671 \pmod{1073741789}$ 
base point G (13693, 10088)
order(G, E) = 1073807281

key generation
private key s = 698000948
public key W = sG (538599244, 255633302)

aligned hash 789abcde

signature computation
one-time u = 609325335
V = uG (160496876, 510945367)
signature c,d = 160496876, 1028509288

signature verification
h1,h2 = 692711864, 301400238
h1G (145664034, 102797322)
h2W (21812882, 252928926)
+ = (160496876, 510945367)
c' = 160496876
Valid

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E:  $y^2 = x^3 + 3x + 2 \pmod{5}$ 
base point G (2, 1)
order(G, E) = 5

key generation
private key s = 2
public key W = sG (1, -1)

aligned hash 7

signature computation
one-time u = 2
V = uG (1, -1)
signature c,d = 1, 2

signature verification
h1,h2 = 1, 3
h1G (2, 1)
h2W (2, 1)
+ = (1, -1)
c' = 1
Valid

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