

1 Constraints of Participant Behaviors

1.1 The constraints for "park"

- (1) $\forall i \in (0, e], w_0^B.pos \in D, w_i^B.pos = w_{i-1}^B.pos$
- (2) $\forall i \in [0, e], spd_i = 0$

1.2 The constraints for "retrograde"

- (1) $w_e^B.pos \in D, w_0^B.pos \notin D, w_0^B.pos \in l_m$
- (2) $fd(w_e^B.pos, w_0^B.pos, l_m) = 1$
- (3) $e < p$
- (4) $(w_e^B.x - w_0^B.x) = DX(0, e), (w_e^B.y - w_0^B.y) = DY(0, e)$
- (5) $\forall i \in (0, e), \left| \frac{spd_i - spd_{i-1}}{\Delta t} \right| \leq ac^{max}, spd_i \leq spd^{max}$

1.3 The constraints for "follow vehicle"

- (1) $w_e^B.pos \in D \wedge w_0^B.pos \notin D$
- (2) $w_0^B.pos \in l_m \wedge l_m \in R_i, w_e^B.pos \in l_n \wedge l_n \in R_j, i = j, m = n$
- (3) $fd(w_0^B.pos, w_e^B.pos, l_m) = 1$
- (4) $\forall i \in (0, e], w_i^O.pos \in l_m, \sqrt{(w_i^B.x - w_i^O.x)^2 + (w_i^B.y - w_i^O.y)^2} \geq H$
- (5) $e < p$
- (6) $(w_0^B.x - w_e^B.x) = DX(0, e), (w_0^B.y - w_e^B.y) = DY(0, e)$
- (7) $\forall i \in (0, e), \left| \frac{spd_i - spd_{i-1}}{\Delta t} \right| \leq ac^{max}, spd_i \leq spd^{max}$

1.4 The constraints for "follow lane"

- (1) $w_e^B.pos \in D \wedge w_0^B.pos \notin D$
- (2) $w_0^B.pos \in l_m \wedge l_m \in R_i, w_e^B.pos \in l_n \wedge l_n \in R_j, i = j, m = n$
- (3) $fd(w_0^B.pos, w_e^B.pos, l_m) = 1$
- (4) $\nexists i \in (0, e], (w_i^O.pos \in l_m) \wedge (\sqrt{(w_i^B.x - w_i^O.x)^2 + (w_i^B.y - w_i^O.y)^2} \geq H)$
- (5) $e < p$
- (6) $(w_0^B.x - w_e^B.x) = DX(0, e), (w_0^B.y - w_e^B.y) = DY(0, e)$
- (7) $\forall i \in (0, e), \left| \frac{spd_i - spd_{i-1}}{\Delta t} \right| \leq ac^{max}, spd_i \leq spd^{max}$

1.5 The constraints for "cut in"

- (1) $w_e^B.pos \in D \wedge w_0^B.pos \notin D$
- (2) $w_0^B.pos \in l_m \wedge l_m \in R_i, w_e^B.pos \in l_n \wedge l_n \in R_j, i = j, m \neq n$
- (3) $fd(w_0^B.pos, w_e^B.pos, l_m) = 1$
- (4) $w_s^B.pos \in l_m, w_f^B.pos \in l_n, fd(w_0^B.pos, w_s^B.pos, l_m) = 1, fd(w_s^B.pos, w_f^B.pos, l_m) = 1, fd(w_f^B.pos, w_e^B.pos, l_n) = 1$
- (5) $w_s^O.pos \in l_n, fd(w_s^O.pos, w_s^B.pos, l_n) = 1, \sqrt{(w_s^B.x - w_s^O.x)^2 + (w_s^B.y - w_s^O.y)^2} \geq H$
- (6) $s = m;$
- (7) $m < f < n, f < e < p$
- (8) $(w_0^B.x - w_s^B.x) = DX(0, s), (w_0^B.y - w_s^B.y) = DY(0, s)$
- (9) $(w_s^B.x - w_f^B.x) = DX(s, f), (w_s^B.y - w_f^B.y) = DY(s, f)$

$$(10) (w_f^B.x - w_e^B.x) = DX(f, e), (w_s^B.y - w_f^B.y) = DY(s, f)$$

$$(11) \forall i \in (0, e), \left| \frac{spd_i - spd_{i-1}}{\Delta t} \right| \leq ac^{max}, spd_i \leq spd^{max}$$

1.6 The constraints for "change lane"

$$(1) w_e^B.pos \in D \wedge w_0^B.pos \notin D$$

$$(2) w_0^B.pos \in l_m \wedge l_m \in R_i, w_e^B.pos \in l_n \wedge l_n \in R_j, i = j, m \neq n$$

$$(3) fd(w_0^B.pos, w_e^B.pos, l_m) = 1$$

$$(4) w_s^B.pos \in l_m, w_f^B.pos \in l_n, fd(w_0^B.pos, w_s^B.pos, l_m) = 1, fd(w_s^B.pos, w_f^B.pos, l_m) = 1, fd(w_f^B.pos, w_e^B.pos, l_n) = 1$$

$$(5) \nexists i \in [s, f], (w_i^O.pos \in l_n) \wedge fd(w_i^O.pos, w_i^B.pos, l_n) = 1 \wedge (\sqrt{(w_i^B.x - w_i^O.x)^2 + (w_i^B.y - w_i^O.y)^2} \geq H)$$

$$(6) s = m$$

$$(7) m < f < n, f < e < p$$

$$(8) (w_0^B.x - w_s^B.x) = DX(0, s), (w_0^B.y - w_s^B.y) = DY(0, s)$$

$$(9) (w_s^B.x - w_f^B.x) = DX(s, f), (w_s^B.y - w_f^B.y) = DY(s, f)$$

$$(10) (w_f^B.x - w_e^B.x) = DX(f, e), (w_s^B.y - w_f^B.y) = DY(s, f)$$

$$(11) \forall i \in (0, e), \left| \frac{spd_i - spd_{i-1}}{\Delta t} \right| \leq ac^{max}, spd_i \leq spd^{max}$$

1.7 The constraints for "vehicle cross"

$$(1) w_e^B.pos \in D \wedge w_0^B.pos \notin D$$

$$(2) w_0^B.pos \in l_m \wedge l_m \in R_i, w_e^B.pos \in l_n \wedge l_n \in R_j, i \neq j$$

$$(3) fd(w_0^B, w_e^B, l_m) = 1$$

$$(3) \exists l_{ex}^m, l_{en}^m \in l_m, \exists l_{ex}^n, l_{en}^n \in l_n, \arctan|(k_1 - k_2)/(1 + k_1 k_2)| < \frac{\pi}{2}, k_1 = (l_{ex}^m.y - l_{en}^m.y)/(l_{ex}^m.x - l_{en}^m.x), k_2 = (l_{ex}^n.y - l_{en}^n.y)/(l_{ex}^n.x - l_{en}^n.x)$$

$$(4) \sqrt{(l_{en}^n.x - l_{ex}^m.x)^2 + (l_{en}^n.y - l_{ex}^m.y)^2} < \sqrt{(l_{ex}^n.x - l_{en}^m.x)^2 + (l_{ex}^n.y - l_{en}^m.y)^2}$$

$$(5) e < p$$

$$(6) (w_0^B.x - w_e^B.x) = DX(0, e), (w_0^B.y - w_e^B.y) = DY(0, e)$$

$$(7) \forall i \in (0, e), \left| \frac{spd_i - spd_{i-1}}{\Delta t} \right| \leq ac^{max}, spd_i \leq spd^{max}$$

1.8 The constraints for "turn around"

$$(1) w_e^B.pos \in D \wedge w_0^B.pos \notin D$$

$$(2) w_0^B.pos \in l_m \wedge l_m \in R_i, w_e^B.pos \in l_n \wedge l_n \in R_j, i \neq j$$

$$(3) fd(w_0^B, w_e^B, l_m) = 1$$

$$(3) \exists l_{ex}^m, l_{en}^m \in l_m, \exists l_{ex}^n, l_{en}^n \in l_n, \arctan|(k_1 - k_2)/(1 + k_1 k_2)| \geq \frac{\pi}{2}, k_1 = (l_{ex}^m.y - l_{en}^m.y)/(l_{ex}^m.x - l_{en}^m.x), k_2 = (l_{ex}^n.y - l_{en}^n.y)/(l_{ex}^n.x - l_{en}^n.x)$$

$$(4) \sqrt{(l_{en}^n.x - l_{ex}^m.x)^2 + (l_{en}^n.y - l_{ex}^m.y)^2} < \sqrt{(l_{ex}^n.x - l_{en}^m.x)^2 + (l_{ex}^n.y - l_{en}^m.y)^2}$$

$$(5) s < f < e, e < p$$

$$(6) (w_0^B.x - l_{ex}^m.x) = DX(0, s), (w_0^B.y - l_{ex}^m.y) = DY(0, s)$$

$$(7) (l_{ex}^m.x - l_{en}^n.x) = DX(s, f), (l_{ex}^m.y - l_{en}^n.y) = DY(s, f)$$

$$(8) (l_{ex}^n.x - l_{en}^m.x) = DX(s, f), (l_{ex}^n.y - l_{en}^m.y) = DY(f, e)$$

$$(9) \forall i \in (0, e), \left| \frac{spd_i - spd_{i-1}}{\Delta t} \right| \leq ac^{max}, spd_i \leq spd^{max}$$

1.9 The constraints for "pedestrian walk"

- (1) $w_e^B.pos \in D$
- (2) $\forall i \in [0, e], w_i^B.pos \notin R$
- (3) $(w_0^B.x - w_e^B.x) = DX(0, e), (w_0^B.y - w_e^B.y) = DY(0, e)$
- (4) $\forall i \in (0, e), spd_i \leq 5$

1.10 The constraints for "pedestrian cross"

- (1) $w_e^B.pos \in D$
- (2) $\exists i \in [0, e], w_i^B.pos \in R$
- (3) $(w_0^B.x - w_e^B.x) = DX(0, e), (w_0^B.y - w_e^B.y) = DY(0, e)$
- (4) $\forall i \in (0, e), spd_i \leq 5$