

Workshop 3 demonstrates how to write programs using Prolog, a programming language that was specifically designed for Artificial Intelligence. Prolog uses Predicate Calculus. We discussed Predicate Calculus in Workshop 1 for performing logical reasoning and inference.

### Learning Outcomes On completing this section and related learning activities, you should be able to: Define • The terms: fact, rule, goal and question Construct • Simple Prolog programs • The closed-world assumption and understand its implication for Prolog Describe • How Prolog programs are executed

### **Prolog**

- Logic Programming
  - ▶ Invented by Colmerauer & Kowalski
  - Implements Predicate Calculus
  - Goal Driven: searches for goals using Depth-First Search
  - Can return multiple answers



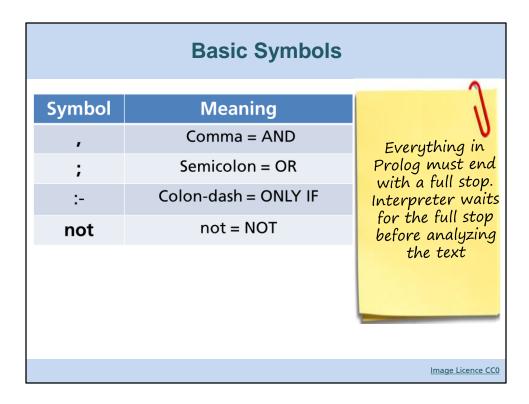




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Prolog is a widely used Al language. It is particularly useful as it allows fast-prototyping of systems. This is due to the nature of the programming language, which removes the requirement from the programmer of having to tell the computer how to solve a problem. Instead, the programmer essentially describes the problem to be solved, and the Prolog environment takes care of the rest.

Prolog is essentially an implementation of Predicate Calculus (we met Predicate Calculus in Workshop 1 Section 2). It is goal-driven, which means that when running a Prolog program, we simply state what we want to try and deduce (the goal), and Prolog tries to see if it can satisfy our goal. It uses Depth-First Search, so if it needs to prove more than one thing, it works the first one out completely, before moving onto the rest. It is also capable of returning multiple answers, so we can ask questions and find all possible answers to them.



Before looking at any code, we'll cover the basic constructs used in Prolog.

There are only really four symbols used in Prolog:

```
"," represents "and"
```

We'll see examples of these shortly.

The other main symbol used in Prolog is the full stop ".". ALL programming constructs in Prolog (rules, facts and questions) MUST end with a full stop. The Prolog interpreter relies on the presence of the full stop to detect the end of each programming construct. If you ask Prolog a question and it appears to do nothing, it is possible that you have missed the full stop. The interpreter won't start to answer your question until it encounters the full stop.

<sup>&</sup>quot;;" represents "or"

<sup>&</sup>quot;:-" represents "only if" and "not" simply represents "not"

### **Variables and Constants**

- Use the same convention we used for Predicate Calculus
  - Constants must start with lowercase letter
  - Variables must start with uppercase letter

There are no data types in Prolog, only *variables* and *constants*. Variables can be assigned ANY kind of value, as we'll see later in the workshop.

The same convention is used in Prolog as in Predicate Calculus, so variables MUST start with an uppercase letter and constants MUST start with a lowercase letter.

# Closed-World Assumption 1. All true facts are known 2. If something is not known, it's assumed to be false 3. Only need to give 'true' facts 4. Effectively states "if I do not know something it must be false"

One of the common problems with reasoning systems is deciding what knowledge to represent. Prolog makes the assumption that it knows everything that is true, therefore, anything that it doesn't know, or can't deduce, must be false. This has a big effect on how you formulate Prolog programs, as we only need to tell it what it needs to know. This is called the *Closed World Assumption*, as we have effectively defined the 'world' we are considering by the data we have given the program.

### **Facts**

- Represent things that are known to be true
- ► The knowledge in the system is represented by facts
- ▶ Syntax: relationship name(obj1, obj2,...,objn).
- obj1, obj2,...,objn are connected by the relation called relationship name

The simplest programming construct in Prolog is the *fact*. Facts are used to state things that are known to be true, and essentially provide a way of creating a database of knowledge that the program can use.

Facts have a simple structure, the name of the fact, with a list of 'arguments' enclosed in brackets.

Note that the facts MUST end with a full stop.

# likes (mary, john). Mary likes John Owns (john, gold). John owns gold Each occurrence of the same name is assumed to refer to the same object Programmer must decide on meanings

This slide shows some simple examples of facts.

They all start with the name of the fact (**likes**, **valuable or owns**) and relate the values in brackets in some way.

Notice that all of the fact names and the arguments start with a lowercase letter, so they are all constants.

There is no meaning to any of these constants, apart from the meaning that the programmer intended them to have.

Where a constant appears more than once in a program, it is assumed to refer to the same object (or entity).

### **Questions**

Once Prolog has a 'database' of facts the user can ask questions at the prompt:

Prompt	Meaning
?-	Prolog is waiting for a question

- Questions have a similar format to facts
- Variables can be used to match values

The interaction with a Prolog program is via *questions*, so these are the way that we tell the Prolog program what we want it to do.

When you are using Prolog and encounter the prompt:

?-

It tells you that Prolog is waiting for you to ask it a question.

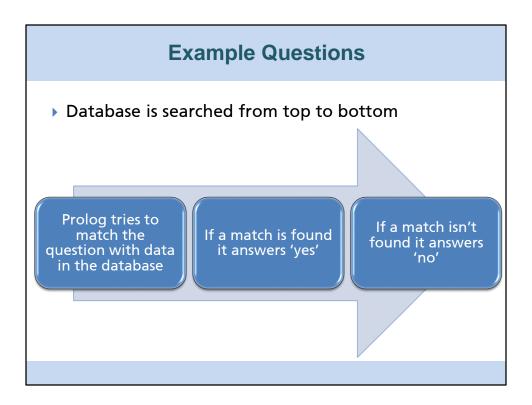
The simplest form of a question is just the same as that of a fact, as we'll see on the next slide.

### Consider the following database: likes( joe , fish ). likes( joe , mary ). likes( mary , book ). likes( john , book ). likes( john , book ).

The examples on the next few slides are questions that are asked of the database on this slide.

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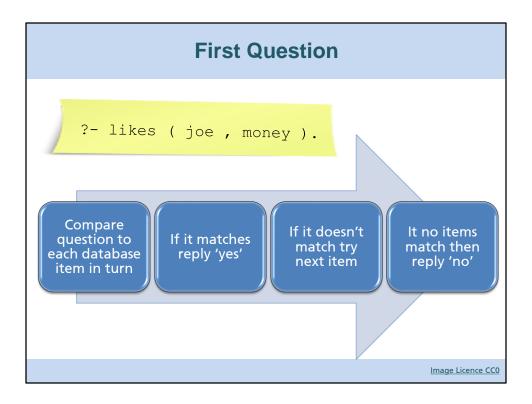
This simple database, contains 4 facts, each of which represents the relation likes. The last line shows a convention for commenting facts, namely a statement of the meaning of a fact. So in this case, likes(X, Y). states that object X likes object Y.



When you ask Prolog a question, it tries to match your question with the facts in the database. It does this in a systematic way, by looking at the contents of the database, one at a time, starting with the first element in the database, and working its way down the database until it either finds a match, or reaches the end of the database.

If a match is found it displays the word "yes" and then the prompt. If a match isn't found, it displays the word "no" and then the prompt.

It is important that you understand how Prolog tries to answer questions, as the order that the facts (and other constructs) are entered can have an effect on the way the program behaves.



The first question we'll look at is:

?- likes ( joe , money).

The **?**- is Prolog's prompt, so what we are asking is "does joe like money?". Note the full stop at the end of the question.

To attempt to answer this question, Prolog compares it to each of the facts in the database in turn. If it finds a match it replies "yes", otherwise it moves onto the next fact. If the end of the database is reached without finding a match, the "no" is returned.

For this question, Prolog achieves a partial matching for each fact in the database, as they are all **likes** facts. The first two facts also match the first argument, as the first arguments are the same. In these two cases, the second argument is also examined, but in neither case does it match. As the fact **likes(joe,money)**. is not in the database, Prolog returns the answer no.

### Video: Programming In Prolog Part 1 - Facts, Rules and Queries



Take a look at this short demo outlining Programming In Prolog Part 1 - Facts, Rules and Queries.

YouTube link: <a href="https://www.youtube.com/watch?v=gJOZZvYijqk">https://www.youtube.com/watch?v=gJOZZvYijqk</a>

```
Other Questions

likes(joe, fish).
likes(joe, mary).
likes(mary, book).
likes(john, book).

likes(X,Y). % X likes Y

?- likes (mary, joe).

?- likes (mary, book).
```

Using the same database as previously, what are the answers to these questions?

For the first question, the third element partially matches, but not completely, so the answer is "no".

For the second question, the third element matches exactly, so the answer is "yes".

### How Useful is This?

- Not very! Just looking up a database
- More interesting:We can use variables to look for answers
- Remember, a variable starts with an UPPERCASE letter

So far we've seen how we can define some facts and ask simple questions. This is not very useful, as all we are doing is checking to see whether a particular fact is in the database or not.

By using variables, we'll be able to ask more interesting questions.

Remember, the difference between a variable and a constant is that a variable starts with an uppercase letter.

### **Variables**

- Suppose we want to find out what John likes
- Could ask ALL possible questions but Not really feasible

```
?- likes ( john , coffee).
?- likes ( john , cars).
?- likes ( john , books).
....
```

Better to use a variable

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If we wanted to ask a more general question than those we have seen so far, such as "What does John like?", we could simply ask repeated questions, with different values for the second argument, which isn't really very practical.

It is far simpler to use a variable.

### **Using Variable to Ask Questions**

Question now becomes:

```
?- likes ( john , X).

where X is a variable
```

- ▶ This question asks "what does John like?"
- How are such queries handled?
- What happens if John likes more than one thing?

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By using a variable, our question becomes:

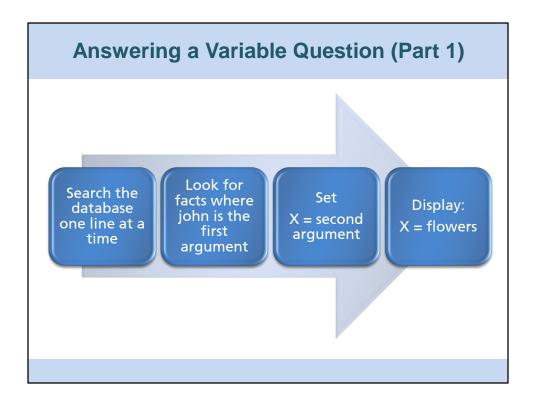
?- likes (john, X).

The only difference between this question and those that we have seen before is that the second argument is a variable. So unlike previous questions, we are asking something general, rather than something specific. In this case the question is "What does John like?".

We'll see how this question is handled over the next few slides.

## likes ( john , flowers ). likes ( john , mary ). likes ( paul , mary ). ?- likes ( john , X ).

So given this simple database, and the question ( ?- likes ( john , X ). ), how does Prolog try to answer this question? It is handled in essentially the same way as the previous questions.



Essentially the same approach that we have already seen is applied. The database is searched from top to bottom, until either a match is found, or the end of the database is reached.

In this case, the first fact has the same name as the question (likes), so that matches. The first arguments are then compared, in this case they are both john so again we have a match. Prolog now looks at the last argument, in the question we have a variable (X), whilst in the fact we have a value (flowers).

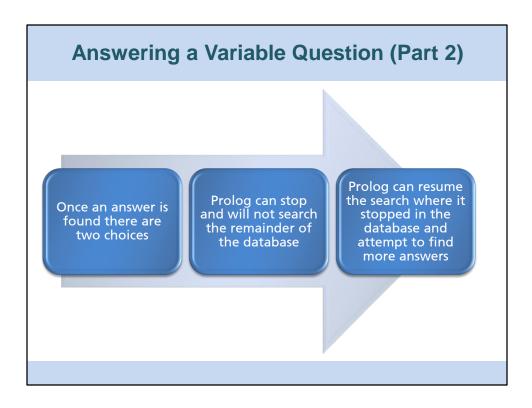
For these to match, we need to assign the variable X a value, so it is given the value flowers, to match the value in the database. This assigning of a value to a variable is called *instantiation*.

Once this has happened, Prolog has matched all of the values in the question with an element in the database, so it has answered the question. To tell the user the answer, it displays the following:

$$X = flowers$$

to show the value it has found for the variable X. Remember in our previous questions the answer was simply "yes".

At this point the prompt does not appear, as Prolog is waiting for us to tell it what to do next.

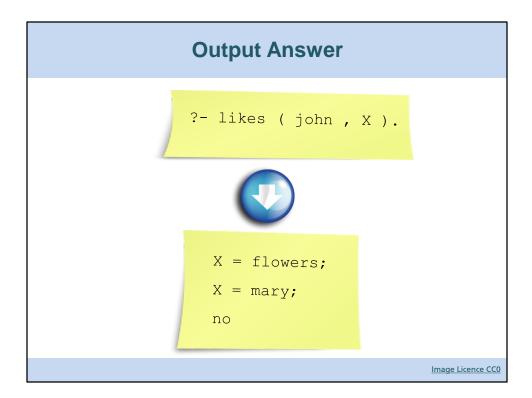


Once Prolog has found an answer to our question, we have two choices; we can either look for more answers or stop.

To stop, we just press the return key, at which point the prompt reappears and Prolog is ready for our next question.

If we want to look for more answers, we type a semi-colon ";" and then return.

Prolog now resumes its search from where it stopped to try and find other answers. If it finds another answer it displays it as before, otherwise it returns "no". Note that we could keep searching for as many answers as there are in the database.



This slide shows the answers we get to the question:

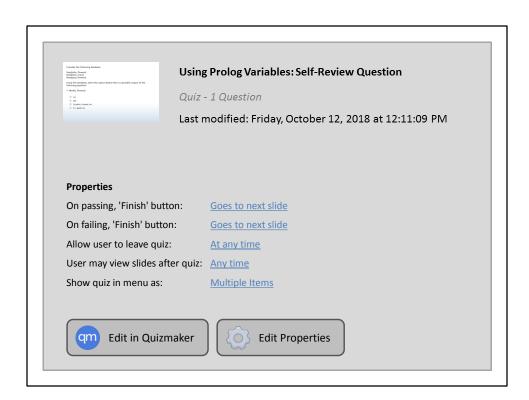
```
?- likes ( john , X ) .
```

### It initially returns:

X = flowers

On us typing a ";" and then return, it then resumes it search and then returns: X = mary

Once again we type ";" and return, to look for more answers. This time there are no more answers, so it returns "no".

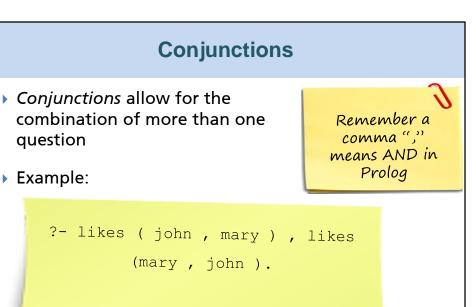


### **Using Variables In Prolog**

### **Using Variables**

- Using variables makes the process more powerful
- Still limited to basic pattern matching
- Need to be able to construct more complex questions

We now are able to ask more complex questions, but they are still fairly limited. We are still just matching our questions to a fact in the database. It would be useful to be able to ask more complex questions.



Does John like Mary and Mary like John? Image Licence CC0

question

Example:

The simplest way to ask more complex questions is to use conjunctions. A conjunction is a mathematical term for the logical AND operator. So we can ask two questions in one, and look for an answer that satisfies both. Recall that the comma symbol, is used to represent "and". So to ask two

questions we simply separate them by a comma. So the question shown in this slides asks "Does John like Mary AND does Mary like John?"

Such questions are handled in the same way as we've seen, except that the second question will only be examined if an answer can be found to the first question. Both of them need to be true for the conjunction to be true, in the same way as logical expressions are evaluated in 'C'.

### **Conjunctions and Variables**

- Suppose we had a question like:
  - " Is there anything that both John and Mary like?"
- ▶ How would this question be asked?

```
?- likes ( mary , X ) , likes ( john , X ).
```

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We can extend our conjoined questions to include variables, just like we did with other questions.

We saw before that **likes ( mary , X ).** asks the question "What does Mary like?".

By conjoining two similar questions, such as: ?- likes ( mary , X ) , likes ( john , X ).

our question is now "What does Mary like AND what does John like?".

But as we've used the same variable in both questions, we need to find something that they both like, so the question is actually "What do BOTH Mary AND John like?"

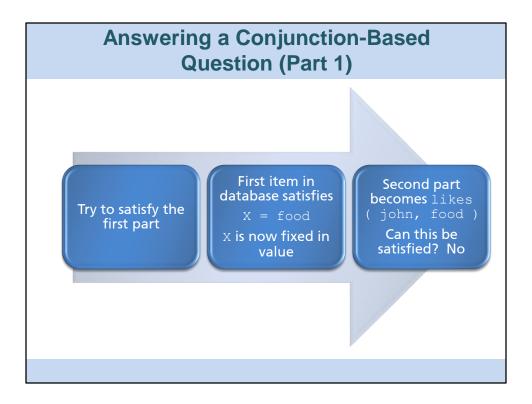
```
Conjunctions Example

likes ( mary , food ).
likes ( mary , wine ).
likes ( john , wine ).
likes ( john , mary ).

?- likes ( mary , X ) , likes ( john , X ).
```

This slide has a simple database that will be used to show how conjoined questions are answered.

The question we are going to ask is also shown on the slide, and it is the one we met in the last slide, namely "What do Mary and John both like?".



Prolog tries to satisfy the questions individually, so it will try to satisfy the first question and only if this succeeds will it try to satisfy the second question.

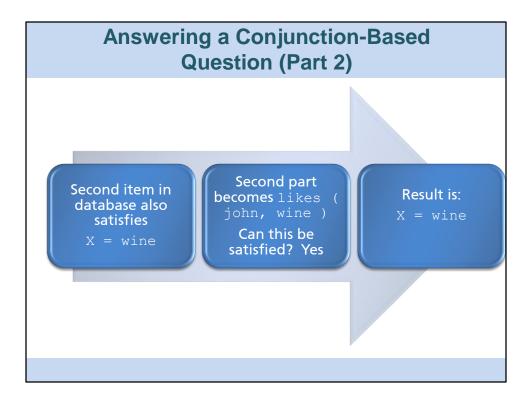
So the first question, likes ( mary , X ) is considered first. This question is dealt with in the way we've already seen. Prolog searches down through the database to find a fact that matches the fact name and the first argument. If it does it instantiates the variable to the second argument. In this case the first fact in our database matches our first question and so X is instantiated to 'food'.

Prolog now tries to answer the second question. As X has now been instantiated, the second question is now:

```
likes ( john , food )
```

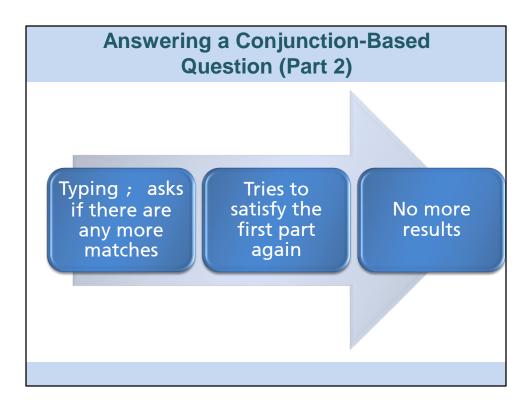
So Prolog searches the database for a match, which it cannot find, so the second question fails.

What Prolog does now is to try and find another answer to the first question.

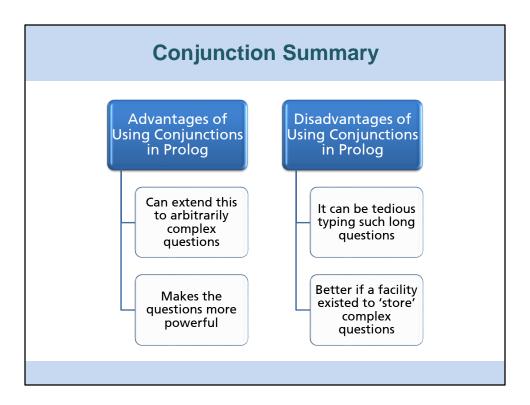


On searching further down through the database, Prolog now finds that the second fact in the database also matches the first question and so X is now instantiated to 'wine'.

Prolog now tries to answer the second question, which is now likes ( john , wine ) so Prolog searches the database for this fact and finds it. The second question has now been answered, and so our conjoined question has also been satisfied. Prolog responds in the usual way by displaying the value of the variable that satisfies both questions, namely  $\mathtt{X} = \mathtt{wine}$ .



As before, we can now ask for more answers by typing ";" Prolog will now try to find other answers to our question but can't so the answer "no" is returned.



We can now write fairly complex questions as we can extend this idea of conjoining questions to make as complicated a query as we need.

The drawback with this approach, is that it can be tedious having to type long questions, especially if we want to ask the same (or similar) question again.

It would therefore be very useful if we could record such questions and ask these stored questions. Prolog has just such a facility, the rule.

### Rules

- ▶ Rules can be used to define relationships
- Define rules as definitions:
  - X is a bird if:X is an animal, andX has feathers
- Prolog has just such a facility

Rules allow us to define relationships between objects, so that we do not need to define everything about an object explicitly.

For example we could define a relationship that birds are animals with feathers, or more formally:

X is a bird if:

X is an animal, and

X has feathers

So some entity X is a bird if it is an animal and it has feathers.

Fortunately, Prolog has just such a facility and the rest of this workshop will examine it.

# Defining a Rule Consider the previous example X is a bird if: X is an animal and X has feathers bird (X). % X is a bird animal (X). % X is an animal feathers (X). % X has feathers

Let's focus on the bird example.

# Defining More Complex Rules Symbol Meaning , Comma = AND :- Colon-dash = ONLY IF Nule thus becomes: bird (X):animal (X), feathers (X).

We know how to say "and". We just use a comma.

So the only thing we haven't seen how to represent yet is "if". To do this we use the symbol ":-"

By inserting these Prolog constructs into our rule we get:

```
bird (X):-
animal (X),
feathers (X).
```

This says, x is a bird if X is an animal and x has feathers. This is our first Prolog rule.

Note the full stop at the end of the rule.

### Rules : Example 1

```
male ( albert ).
male ( edward ).
female ( alice ).
female ( victoria ).
parents ( edward , victoria , albert ).
parents ( alice , victoria , albert ).
```

Write a rule that defines sister of ( X , Y )

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The rest of the examples will be based upon familial relationships as these should be familiar to you. Make sure that you do not assume that Prolog knows anything about such relationships. For example if we know that Bob's parents are Emily and Bill, and we know that Emily is female, then Prolog cannot deduce that Bob is male. Unless, of course, we explicitly tell it, or write a rule to deduce it.

In the database shown here, we define some basic facts about the gender of some people and who the parents of two of them are. For the parents facts, we assume that the fact parents (Child, Parent1, Parent2) means that Parent1 and Parent2 are the parents of Child.

What we want to do is write a rule that allows us to say that **X** is the sister of **Y**.

Rules : Example 1	
•	
	X is a sister of Y if:
	X is female and
-	X and Y have the same parents
	First line:
	▶ sister_of ( X , Y ) :-
	> Second line:
	▶ female ( X ),
5	
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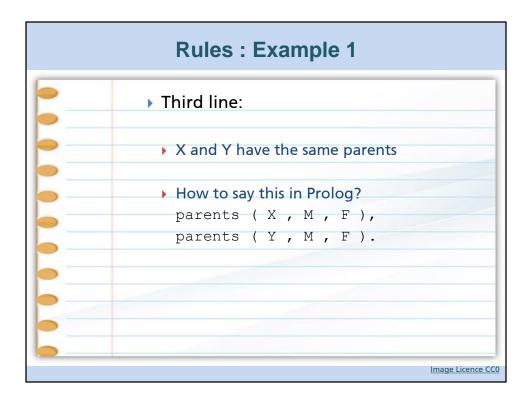
The first thing we need to do is decide what the relationship **sister of** means.

To simplify things we define a sister as someone who is female, and has the same parents as you. More formally we get:

X is a sister of Y if:

X is female and X and Y have the same parents

To convert this to Prolog, we simply replace each part with its Prolog equivalent. The first two lines are fairly straightforward and are shown in this slide. The third line is trickier and is covered in the next slide.



The final line of our rule is slightly more complex. The others can be defined by a simple factual relationship, but how do we say that two people have the same parents?

We know that we have the parents facts, which tell us who someone's parents' are. All we need to do is find out who the parents of X are and who the parents of Y are and check to see if they are the same. How can we check that they are the same?

To find the parents of X, we could say:

```
parents ( X , M , F )
```

so M and F would be the parents of X. When Prolog matches this in the database, M and F will be instantiated to the values that represent the parents of X. To check if Y has the same parents we can just say:

```
parents (Y, M, F)
```

As Y, M and F will all have values by this point, this effectively says "Are M and F the parents of Y?".

### Rules: Example 1

▶ Final Rule

```
sister_of ( X , Y ) :-
female ( X ),
parents ( X , M , F ),
parents ( Y , M , F ).
```

Note M and F (mother and father) do not appear in the head of the rule

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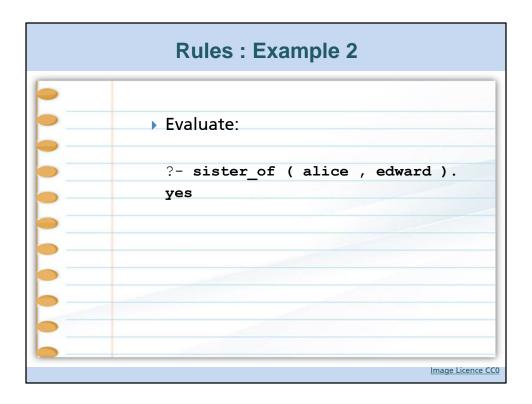
Now that we've written all of the rule we can see the final version.

An interesting aspect of this rule, is that the variables  $\mathbb{M}$  and  $\mathbb{F}$  only appear in the body of the rule, not in its head.  $\mathbb{M}$  and  $\mathbb{F}$  are effectively local variables to that rule, and so cease to exist once the rule has finished.

Rules contain *head* and *body* with the following syntax:

head :- body.

Read as "head is true if body is true



```
Suppose we ask the question:
```

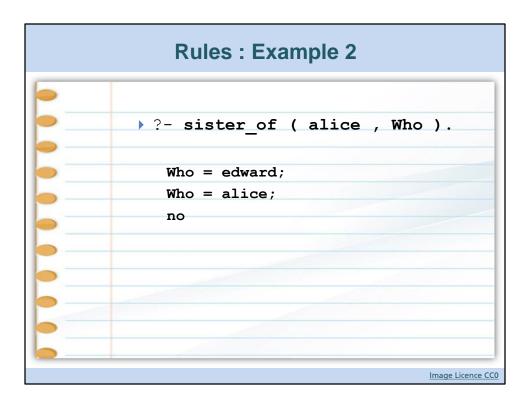
```
sister of ( alice , edward ).
```

Prolog starts by trying to find something in the database that matches the name of our question (sister\_of). It finds the rule that we have just written, which has two arguments, just like our question, so a match is found.

The heading of the rule (sister\_of(X,Y)) has two variables and our question has two constants (alice and edward). As the variables do not currently have any value, they are instantiated to the constants. So upon matching the question to our rule, X now has the value alice and Y now has the value edward. Our rule is now effectively:

Prolog now tries to satisfy each condition in turn (in exactly the same way as we've already seen). The first condition is shown to be true as the fact female (alice) is in the database. As the first condition is true, Prolog moves onto the second condition. It now tries to find out who Alice's parents are. By searching the database, it finds that they are Victoria and Albert. The variable M now has the value victoria and the variable F now has the value edward.

As a match for the second condition was found, the final condition is now tried. It now reads parents (edward, victoria, albert). This fact is in the database, so the condition is satisfied and the rule has shown that Alice is Edwards sister, so the value yes is returned.



In this question, a variable is used as well as a constant, so we are effectively asking, who is alice the sister of.

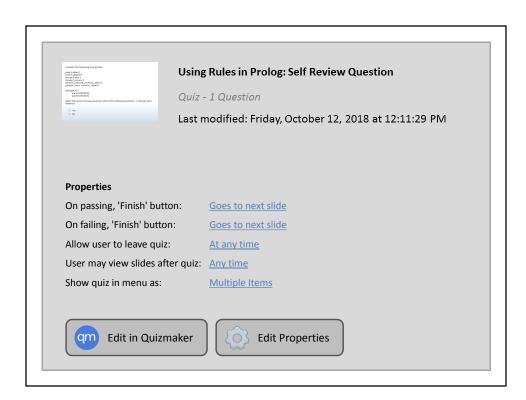
Prolog answers this question in a similar way to the last one. When it matches the question with the rule, the variable X is instantiated to alice, whilst Y is left uninstantiated. Y is effectively being used as a variable argument. This is a very powerful feature of Prolog, arguments can be used as both input and output parameters, we'll cover more of this later.

The first two conditions of the rule fire in exactly the same was as before (alice is still female and victoria and albert are still her parents). This time, however, the last condition is parents (Y, victoria, albert), effectively who has Victoria and Albert as parents.

Prolog searches through the database to try to find a match. It finds that the first parent's relation matches with the value of edward for Y. All of the conditions have now been met and edward is returned, giving Who = edward as the result. If we now type a ";", to ask for more answers, Prolog attempts to find another solution.

It does this by trying to resatisfy the last condition (if it can't it works back through the other conditions trying to resatisfy them). In this case it does find another match, the second instance of the fact parents, with a value for Y of alice.

So Prolog has deduced that Alice is her own sister. Clearly there is a problem with our rule. However this can be overcome by checking that X and Y are different. You'll see how to do this when you attempt the lab exercises.



Summary		
	<b></b>	
Introduced Prolog	Introduced basic Prolog symbols and core Prolog concepts such as rules, facts, goals and questions	
Closed World Assumption	Defined closed world assumption and examined its application to Prolog	
Prolog Programming	Constructed sample programs and examined how Prolog executes questions	

### References

ArsElectronica (2010) ASIMO [photo], (<u>CC BY-NC-ND 2.0</u>), available: https://www.flickr.com/photos/36085842@N06/4945217670/ [accessed 18 Apr 2019].

Fisher, L.M. (2017) Alain Colmerauer [photo], available: <a href="https://cacm.acm.org/news/217533-in-memoriam-alain-colmerauer-1941-2017/fulltext">https://cacm.acm.org/news/217533-in-memoriam-alain-colmerauer-1941-2017/fulltext</a> [accessed 26 Apr 2019].

Wilson, B. (2012) Robert Kowalski [photo], available: http://www.cse.unsw.edu.au/~billw/cs9414/notes/prolog/intro.html [accessed 26 Apr 2019].

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