



Journal of MONETARY ECONOMICS

www.elsevier.com/locate/jme

Journal of Monetary Economics 54 (2007) 346-368

# Modeling exchange rate passthrough after large devaluations ☆

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Received 15 March 2005; received in revised form 10 July 2005; accepted 4 August 2005 Available online 14 November 2006

## Abstract

Large devaluations are generally associated with large declines in real exchange rates. We develop a model which embodies two complementary forces that account for the large declines in the real exchange rate that occur in the aftermath of large devaluations. The first force is sticky nontradable-goods prices. The second force is the impact of real shocks that often accompany large devaluations. We argue that sticky nontradable goods prices generally play an important role in explaining post-devaluation movements in real exchange rates. However, real shocks can sometimes be primary drivers of real exchange-rate movements.

JEL classification: F31

Keywords: Exchange rate; Devaluations; Passthrough; Sticky prices

## 1. Introduction

Large devaluations are generally associated with large declines in the real exchange rate (RER). In an earlier paper (Burstein et al., 2005) we argue that the primary force causing

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<sup>&</sup>lt;sup>★</sup>We thank Miles Kimball and an anonymous referee for their suggestions, and Pierpaolo Benigno, Mario Crucini, Andrew Levin, Carlos Vegh, Jessica Wachter, Ivan Werning, and Michael Woodford for their comments. We gratefully acknowledge financial support from the National Science Foundation and the Searle Foundation.

these declines is a slow adjustment in the price of nontradable goods and services, not slow adjustment in the price of goods that are imported or exported. Our evidence suggests that the key puzzle about the post-devaluation behavior of inflation is, why do the prices of nontradable goods and services respond by so little in the aftermath of large devaluations? We develop a model that accounts for the negligible response of nontradable-goods prices in the aftermath of large devaluations.

Our model highlights two complementary forces that produce this result. The first force is sticky nontradable-goods prices. Instead of assuming that nontradable-goods prices are sticky, we develop conditions under which this phenomenon can emerge as an equilibrium outcome. The second force is the impact of real shocks associated with large devaluations that lead to a decline in the price of nontradable goods relative to traded goods. We study the importance of these two forces using three examples motivated by the devaluations in Korea (1997), Uruguay (2002), and the UK (1992).

In the Korean case, we find that to explain the large post-devaluation decline in the real exchange rate, we must allow for sticky nontradable-goods prices. Moreover, we argue that sticky nontradable-goods prices are sustainable as an equilibrium phenomenon. In the UK case, we find that the post-devaluation behavior of the real exchange rate can be explained solely as a result of sticky nontradable-goods prices. However, the Uruguayan case shows that it can be very misleading to assume that prices are sticky. In this case nontradable-goods prices cannot be sustained as an equilibrium phenomenon and real shocks alone account for the post-devaluation real exchange-rate depreciation.

To model sticky nontradable-goods prices, we build on the many studies that analyze price stickiness in closed economies. The closed-economy literature identifies a class of models in which the gains from adjusting prices in response to changes in monetary policy are very small. These gains can be so modest that when there are small costs of changing prices, price stickiness is an equilibrium phenomenon. We incorporate into our model the key feature emphasized by Ball and Romer (1990), a relatively flat marginal cost curve. In addition, we adopt Kimball's (1995) assumption that the elasticity of demand for the output of a monopolistic producer is increasing in its price relative to the prices of its competitors goods.

There are two key differences between our analysis of sticky prices and the analogue closed-economy literature. First, we consider large changes in monetary policy instead of small changes. Second, we focus on open economies and identify key features of the model economy that play an important role in making sticky nontradable-goods prices sustainable as an equilibrium phenomenon.

To model the direct impact of real shocks on inflation and the real exchange rate, we build on the literature that models the mechanisms through which large devaluations lead to contractions in economic activity. A common feature of these models is that devaluations are associated with negative wealth effects. We capture these effects by considering two alternative real shocks, a decline in export demand and a reduction in net foreign assets. The first shock is drawn from the experience of countries like Uruguay, whose devaluations were precipitated by large declines in export demand associated with recessions in countries with whom they trade. The second shock captures in a direct, albeit in a brute force manner, the decline in real wealth that is a hallmark of contractionary

<sup>&</sup>lt;sup>1</sup>See, for example, Aghion et al. (2001), Burnside et al. (2001), Caballero and Krishnamurthy (2001), Christiano et al. (2004), and Neumeyer and Perri (2005).

devaluations. Arguably, we can think of the fall in real wealth as a proxy for the balance-sheet effects emphasized by some authors.

We suppose that the model economy is initially in a fixed exchange-rate regime and that there is then a change in monetary policy that leads to a large, permanent devaluation. To simplify, we assume that if there is a real shock, it occurs at the same time as the devaluation. To assess whether or not sticky nontradable-goods prices are an equilibrium, we calculate the post-devaluation equilibrium assuming that nontradable-goods prices are constant. We then compute the benefits to a nontradable-goods producer of deviating from a symmetric equilibrium by changing his price. In our model, the nontradable-goods sector is monopolistically competitive. Firms in this sector set local currency prices as a mark-up on nominal marginal cost, which is proportional to the nominal wage rate. So the benefit of deviating from a symmetric sticky price equilibrium depends critically on the response of the mark-up and nominal wages to a devaluation. Since we measure the benefits of deviating relative to an equilibrium in which prices are constant forever, we are adopting a conservative strategy for rationalizing sticky prices.

Our model open economy incorporates four assumptions that mute this response. First, the share of tradable goods in the consumer price index (CPI) is small. Second, there are domestic distribution costs associated with the sale of traded goods. Third, there is a low elasticity of the demand for exports. Fourth, there is a moderate elasticity of substitution between tradable and nontradable goods.

Section 2 describes our model. Section 3 presents our basic results. Section 4 discusses the role played by different features of our model in accounting for sticky nontradable-goods prices. Section 5 uses our model to discuss the possibility of an overvalued currency. Section 6 concludes.

# 2. The model

Here we present our model of a small open economy.

## 2.1. The representative household

The household values streams of consumption services  $(C_t)$ , hours worked  $(N_t)$ , and real balances. Consumption services are produced by combining tradable  $(C_t^N)$  and nontradable  $(C_t^N)$  goods according to the CES technology

$$C_t = \left[ v^{1/\rho} (C_t^T)^{(\rho-1)/\rho} + (1-v)^{1/\rho} (C_t^N)^{(\rho-1)/\rho} \right]^{\rho/(\rho-1)}, \quad v \geqslant 0.$$
 (2.1)

The parameter  $\rho$  governs the elasticity of substitution between  $C_t^T$  and  $C_t^N$ . The price of consumption services,  $P_t$ , is given by

$$P_t = [v(P_t^T)^{1-\rho} + (1-v)(P_t^N)^{1-\rho}]^{1/(\rho-1)}.$$
(2.2)

The variables  $P_t^T$  and  $P_t^N$  denote the local currency prices of tradables and nontradable goods, respectively.

Lifetime utility (U) is given by

$$U = \sum_{t=0}^{\infty} \beta^{t} [u(C_{t}, N_{t}) + f(M_{t}/P_{t})], \quad 0 < \beta < 1.$$
(2.3)

The variable  $M_t$  represents beginning-of-period nominal money balances, and  $f(\cdot)$  is a strictly concave function. As in Greenwood et al. (1988), we assume that  $u(\cdot)$  takes the form

$$u(C_t, N_t) = \frac{1}{1 - \sigma} \left( C_t - B \frac{N_t^{1+\theta}}{1+\theta} \right)^{1-\sigma}, \tag{2.4}$$

where B > 0. Given this specification of  $u(\cdot)$ , there are no wealth effects on labor supply, so the uncompensated labor-supply elasticity,  $1/\theta$ , is equal to the Frisch elasticity.

The household can borrow and lend in international capital markets at a constant dollar interest rate, r. For simplicity, we assume that inflation in the U.S. is equal to zero. To abstract from trends in the current account, we also assume that  $\beta = 1/(1+r)$ . The household's flow budget constraint is given by

$$P_t^T C_t^T + P_t^N C_t^N + S_t a_{t+1} + M_{t+1} - M_t = W_t N_t + \Pi_t + (1+r)S_t a_t + T_t$$
 (2.5)

The variable  $a_t$  denotes the dollar value of the household's net foreign assets. The variables  $W_t$  and  $T_t$  represent the nominal wage rate and nominal government transfers to the household, respectively. Total nominal profits in the economy are given by  $\Pi_t$ . The variable  $S_t$  denotes the exchange rate expressed in units of local currency per dollar. We impose the no-Ponzi game condition

$$\lim_{t \to \infty} \frac{a_{t+1}}{(1+r)^t} = 0. \tag{2.6}$$

# 2.2. The import sector

We assume that the tradable consumption good is imported. The dollar price of this good,  $\bar{P}_t^*$ , is set in international markets and is invariant to the level of domestic consumption. We assume that purchasing power parity (PPP) holds for prices "at the dock", i.e., the price of imports exclusive of distribution costs is

$$\bar{P}_t^T = S_t \bar{P}_t^*.$$

For convenience, we normalize  $\bar{P}_t^*$  to one. The variable  $\bar{P}_t^T$  denotes the domestic producer price of imports. Burstein et al. (2005) argue that relative PPP is a reasonable approximation for the behavior of import prices at the dock after large devaluations.

As in Burstein et al. (2003) and Erceg and Levin (1996), we assume that selling a unit of a tradable consumption good requires  $\phi$  units of the final nontradable good. Perfect competition in the distribution sector implies that the retail price of imported goods is equal to

$$P_t^T = S_t + \phi P_t^N. \tag{2.7}$$

The domestic distribution margin, which we define as the fraction of the final price accounted for by distribution costs, is equal to  $\phi P_t^N/P_t^T$ .

## 2.3. The export sector

Exports are produced by a continuum of monopolistically competitive producers indexed by i. The size of this sector has measure one. Firm i uses labor  $(N_{it}^X)$  to produce  $X_{it}$ 

units of exportable good i using the technology

$$X_{it} = A^X N_{it}^X.$$

For simplicity, we assume that the representative household does not consume the export good. Demand for this good in the world market is given by

$$X_{it} = \xi(P_{it}^*)^{-\gamma}. \tag{2.8}$$

The variable  $P_{it}^*$  denotes the dollar retail price of export good *i*. The price elasticity of demand for the export good is given by  $\gamma > 1$ .

As in Corsetti and Dedola (2004), we assume that to sell a unit of the exported good to foreign consumers, foreign retailers must add  $\phi^*$  units of foreign distribution services. We normalize the dollar price of these services to one and assume that the distribution industry is competitive. It follows that  $P_{it}^*$  is given by

$$P_{it}^* = \bar{P}_{it}^X / S_t + \phi^*. \tag{2.9}$$

The variable  $\bar{P}_{ii}^X$  denotes the producer price of the exported good. Under these assumptions, distribution costs affect the elasticity of demand for exports with respect to producer prices (d log( $X_{ii}$ )/d log( $\bar{P}_{ii}^X$ )). The higher the distribution margin, the lower is the effective elasticity of demand.

Producer i maximizes profits, given by

$$\Pi_{it}^X = (\bar{P}_{it}^X - W_t/A^X)X_{it}.$$

The first-order conditions for this problem imply that all exporters charge the same price

$$\bar{P}_{t}^{X}/S_{t} = \frac{\gamma(W_{t}/S_{t})/A^{X} + \phi^{*}}{\gamma - 1}.$$
(2.10)

Total profits in the export sector are given by

$$\Pi_t^X = \int_0^1 \Pi_{it}^X \, \mathrm{d}i.$$

## 2.4. The final nontradable good

The final nontradable good  $(Y_t^N)$  is produced by competitive firms using a continuum of differentiated inputs,  $y_{it}^N$ , that are produced by the intermediate nontradable-goods sector. As in Kimball (1995), we assume that the production technology for  $Y_t^N$  is given by the implicit function

$$1 = \int_0^1 G(y_{it}^N / Y_t^N) \, \mathrm{d}i. \tag{2.11}$$

The function  $G(\cdot)$  satisfies: G(1) = 1 and G'(1) = 1. The standard Dixit–Stiglitz specification corresponds to the following specification for  $G(\cdot)$ ,

$$G(y_{it}^N/Y_t^N) = (y_{it}^N/Y_t^N)^{(\mu-1)/\mu}.$$
(2.12)

The representative firm maximizes profits,

$$\Pi_t^N = P_t^N Y_t^N - \int_0^1 p_{it} y_{it}^N \, \mathrm{d}i, \tag{2.13}$$

subject to the production technology (2.11). The first-order condition for this problem is

$$p_{it} = \lambda G'(y_{it}^{N}/Y_{t}^{N})(1/Y_{t}^{N}).$$

Here,  $\lambda$  is the Lagrange multiplier associated with Eq. (2.11).

Since the sector is competitive, equilibrium profits are zero and the price of the final nontradable good is

$$P_t^N = \frac{\int_0^1 p_{it} y_{it}^N \, \mathrm{d}i}{Y_t^N}.$$

In a symmetric equilibrium where all intermediate good firms charge the same price,  $p_{it} = p_t$ , the price of the final nontradable good is

$$P_t^N = p_t. (2.14)$$

## 2.5. The intermediate nontradable good

The nontradable intermediate good i is produced by monopolist i according to the technology

$$y_{it}^N = A^N N_{it}^N$$
.

Monopolist i chooses a price  $p_{it}$  to maximize profits given by

$$\Pi_t^i = p_{it} y_{it}^N - W_t y_{it}^N / A^N,$$

and commits to satisfy demand at this price. The first-order condition for the monopolist's problem implies that

$$p_{it} = \left[\frac{\varepsilon(z_{it})}{\varepsilon(z_{it}) - 1}\right] \frac{W_t}{A^N}.$$

Here,  $z_{it} = y_{it}^N/Y_t^N$  denotes the market share of the *i*th producer and  $\varepsilon(z_{it})$  is the elasticity of demand for intermediate nontradable good *i* 

$$\varepsilon(z_{it}) = -\frac{G'(z_{it})}{z_{it}G''(z_{it})}.$$

We adopt the following functional form for  $\varepsilon(z_{it})^2$ :

$$\varepsilon(z_{ii}) = \begin{cases} \varepsilon^{L} & \text{if } z_{ii} \geqslant 1 + \bar{z}, \\ \varepsilon^{H} & \text{if } z_{ii} \leqslant 1 - \bar{z}, \\ \frac{1}{2\bar{z}} [(1 + \bar{z} - z_{ii})\varepsilon^{H} + (z_{ii} - 1 + \bar{z})\varepsilon^{L}] & \text{if } 1 - \bar{z} \leqslant z_{ii} \leqslant 1 + \bar{z}. \end{cases}$$
(2.15)

This specification implies that in a symmetric equilibrium ( $z_{it} = 1$ ), the elasticity common to all the monopolists is

$$\varepsilon(1) = \frac{\varepsilon^H + \varepsilon^L}{2}.$$

<sup>&</sup>lt;sup>2</sup>We thank Miles Kimball for suggesting this functional form.

The optimal mark-up is

$$\mu = \frac{\varepsilon(1)}{\varepsilon(1) - 1}.$$

Once  $\bar{z}$  is specified, the parameters  $\varepsilon^L$  and  $\varepsilon^H$  jointly determine the average mark-up and the local slope of the mark-up around the point  $z_{ii} = 1$ . Given a value for  $\varepsilon^H$ , we choose  $\varepsilon^L$  so that  $\mu$  is equal to the calibrated steady-state mark-up. With these assumptions, the symmetric equilibrium is the same as the one in which  $G(\cdot)$  takes the Dixit–Stiglitz form, (2.12), so

$$p_{it} = p_t = \mu \frac{W_t}{A^N}. (2.16)$$

In practice, we set  $\bar{z}$  to a very small number (0.0001) so that  $\varepsilon(z_{it})$  is close to a step function. Therefore, a firm that deviates from a symmetric equilibrium by raising its price faces a discrete increase in the elasticity of demand for its product. In the standard Dixit–Stiglitz case  $\varepsilon(z_{it}) = \mu$  and  $p_{it}$  is a constant mark-up over marginal cost. Relative to the Dixit–Stiglitz case, firms in our model have less of an incentive to raise prices.

#### 2.6. Government

The government chooses a money supply sequence,  $\{M_t^s\}_{t=1}^{\infty}$ , and rebates any seignorage revenue to the household via lump-sum transfers:

$$M_{t+1}^s - M_t^s = T_t. (2.17)$$

## 2.7. Equilibrium and definition of the RER

A perfect-foresight, competitive equilibrium for this economy is a set of paths for quantities  $\{X_{it}, N_{it}^X, y_{it}^N, Y_t^N, N_{it}^N, C_t, C_t^N, C_t^T, N_t, a_{t+1}, M_{t+1}\}$  and prices  $\{P_{it}^*, \bar{P}_{it}^X, W_t, S_t, p_{it}, P_t^N, \bar{P}_t^T, P_t^T\}$  such that households maximize their utility and firms maximize profits; the government's budget constraint holds; and the goods, labor, money, and foreign exchange markets clear. We restrict our attention to symmetric equilibria in which all nontradable-goods producers choose the same price and quantity.

We define the RER as

$$RER = \frac{P_t}{S_t P_t^*}. (2.18)$$

Here,  $P_t^*$  denotes the foreign CPI. In our empirical measures of the RER, we compute both  $S_t$  and  $P_t^*$  as trade-weighted averages of exchange rates and foreign CPIs. With the exception of Uruguay, movements in  $P_t^*$  are quite small relative to the size of the devaluation. So, to simplify, we normalize  $P_t^*$  to one in the model.

## 3. Basic results

Here we study the quantitative properties of our model. We consider three numerical examples motivated by different devaluation episodes: Korea (1997), Uruguay (2002), and

the UK (1992). Korea and Uruguay experienced large devaluations that were followed by contractions in aggregate economic activity.

In Korea, inflation remained stable after the devaluation. In contrast, in Uruguay, inflation rose substantially after the devaluation. The UK devaluation was relatively small and was followed by a mild expansion and stable inflation.

In the Korean example, we generate a recession by assuming that net foreign assets,  $a_0$ , decline at the time of the devaluation. We calibrate the change in  $a_0$  so that our benchmark model generates a fall in real consumption consistent with that observed in Korea in the first year after the devaluation. We assume that the decline in  $a_0$  coincides with a 37% unanticipated, permanent devaluation. This devaluation coincides with the change in the trade-weighted exchange rate for the won in the first year after the devaluation. For expositional purposes we also consider the impact of a devaluation in the Korean example when there is no coincident decline in real wealth.

The Uruguayan devaluation coincided with a large decline in the demand for their exports, which stemmed from the 2001 Argentina currency crisis. Drawing on this observation, we assume in our Uruguayan example that the devaluation coincides with a fall in  $\xi$ , the level parameter in the export demand (2.8). We choose the devaluation rate in our example, 42%, to coincide with the cumulative devaluation in the trade-weighted peso exchange rate from January 2002 to June 2003. We note that the Uruguayan devaluation occurred in June 2002, but the trade-weighted nominal exchange rate changed substantially before June 2002 due to the Argentinean January 2002 devaluation. For this reason we choose January 2002 as our reference point.

For our UK example, we abstract from real shocks and consider a pure devaluation of 11%. This devaluation coincides with the trade-weighted change in the exchange rate for the pound sterling in the first year after the UK devaluation.

In all of the examples, we assume that prior to time zero agents anticipate that the exchange rate is fixed at  $S_t = S$  and that the economy is in a steady state with constant prices and quantities. At time zero, there is an unanticipated change in monetary policy that leads to a one-time permanent exchange-rate devaluation. Depending on the example, there can be a real shock that coincides with the devaluation.

We summarize the parameter values for our benchmark model in Table 1. Our results are independent of the function f(.), which controls the utility of real balances (see Eq. (2.3)). We set the elasticity of substitution between tradables and nontradables ( $\rho$ ) to 0.40. This value is consistent with estimates in the literature.<sup>3</sup> For each country, we set v, the share parameter in the CES consumption aggregator in Eq. (2.1), so that given  $\phi$ , the pre-devaluation share of import goods in consumption, exclusive of distribution costs, coincides with the data reported in Burstein et al. (2005). We assume that  $\theta = 0.25$ . This value implies a labor supply elasticity of four which coincides with the standard value of the Frisch labor supply elasticity used in the real-business-cycle literature (see Christiano and Eichenbaum, 1992; King and Rebelo (2000)). We choose B, the level parameter that controls the disutility of labor, so that the price of nontradables in the pre-devaluation steady state is equal to one.

We set  $\phi$  and  $\phi^*$  so that the pre-devaluation distribution margin is 50% in both the domestic and foreign markets. This value is consistent with the evidence in Burstein et al. (2003).

<sup>&</sup>lt;sup>3</sup>See, for example, Stockman and Tesar (1995), Lorenzo et al. (2003), and Gonzalez-Rozada and Neumeyer (2003).

Table 1 Benchmark calibration, parameter values

Common parameters			
Distribution margin (%)	$50, \phi = 1$		
Elasticity of labor supply	$4, \theta = 0.25$		
Elasticity of subst. in consumpt.	$0.4, \rho = 0.4$		
between tradables and nontradables			
Pre-devaluation markup	$20, \mu = 1.2$		
Country specific parameters	Korea	Uruguay	UK
Share of tradable goods in CPI	40, v = 0.31	40, v = 0.31	40, v = 0.31
(inclusive of distribution costs) (%)			
Foreign distribution margin (%)	$50, \phi^* = 0.21$	$50, \phi^* = 0.43$	$50, \phi^* = 0.24$
Elasticity of demand for exports	y = 2.53	y = 4.16	y = 2.67
Share of exports in GDP (%)	$32,(1+r)a_0=-0.93$	$18, (1+r)a_0 = 0.11$	$23, (1+r)a_0 = -0.27$
Level parameter, export production	$A^X = 19.6$	$A^X = 3.72$	$A^X = 13.62$
function			
Level parameter, disutility of labor	B = 0.44	B = 0.46	B = 0.41

We set the level parameter in the demand for exports,  $\xi$ , to one. The elasticity of demand for exports,  $\gamma$ , controls how much the export sector expands in the wake of the devaluation. For every country, we set  $\gamma$  so that the model replicates the expansion in exports that occurs in the year after the devaluation (see Table 1).

We require a relatively inelastic demand so that the model yields a plausible postdevaluation expansion of the export sector. This low elasticity is a simple way to mimic the frictions that limit in practice the expansion of the export sector, e.g. capacity constraints, financing constraints, or frictions to sectoral employment reallocation.

For every country, we set the level parameter in the production function of the export sector,  $A^X$ , and the initial level of net foreign assets  $(a_0)$  so that the share of exports in GDP in the model's steady state is equal to its value in the year prior to the devaluation.

We choose the intermediate demand aggregator parameters,  $\varepsilon^L$  and  $\varepsilon^H$ , so that the model has two properties. First, the steady-state mark-up is 20%. Second, the parameters are consistent with the calibration used by Kimball (1995) to generate sticky prices in a closed economy. This calibration has the property that when the relative market share  $(z_{it})$  decreases, the elasticity of demand increases from six to nine. Given how little information is available to calibrate the Kimball aggregator, we report the sensitivity of our results to alternative calibrations. We consider a calibration such that it is optimal for the deviator to change his price by 50% of the increase in marginal cost. This calibration is consistent with the symmetric translog specification of Bergin and Feenstra (2000). These two specifications of the demand aggregator encompass the calibration used by Dotsey and King (2005), which lies in between the Kimball and Bergin–Feenstra specifications. Finally, we also consider the standard Dixit–Stiglitz specification of demand in which the elasticity of demand is constant.

# 3.1. The Korean example

The first two columns of Table 2 report the response of the benchmark model to a single shock: a 37% devaluation. Columns 1 and 2 correspond to the case of flexible and sticky

Table 2
Prices and quantities in Korea one year after devaluation

	1	2	3	4	5
	Model			Data	
	No real shock		Negative real shock		Selected variables
	Flexible prices	Sticky prices	Flexible prices	Sticky prices	
Prices (log percent change)					
Nominal exchange rate	37.3	37.3	37.3	37.3	37.3
Real exchange rate	0.0	-28.6	-14.2	-28.6	-30.4
Consumer price index	37.3	8.7	23.1	8.7	6.6
Nontradable goods	37.3	0.0	19.3	0.0	5.1
Tradable goods	37.3	20.4	28.7	20.4	
Export prices (in local currency)	37.3	28.9	31.4	27.5	
Export prices (in U.S. dollars)	0.0	-8.4	-5.9	-9.8	
Nominal wage	37.3	10.9	19.3	5.9	
Quantities (log percent change)					
Total hours	0.0	9.9	-15.3	-10.1	
Hours worked in export sector	0.0	10.4	7.3	12.1	
Exports	0.0	10.4	7.3	12.1	12.0
Consumption	0.0	8.5	-19.0	-14.5	-14.4
Consumption of tradable goods	0.0	3.7	-21.2	-19.3	
Consumption of nontradable goods	0.0	9.9	-18.4	-13.1	
Incentives to change prices (levels)					
Post-devaluation markup, stayers		7.6		13.1	
Change in optimal price for deviator $(K)$		4.5		0.0	
Optimal markup for deviator $(K)$		12.5		13.1	
Percentage change in deviator profits $(K)$		9.9		0.0	

K—Results for the Kimball (1995) specification for the demand for nontradable goods.

nontradable-goods prices, respectively, when there is no real shock. Columns 3 and 4 report the impact of two simultaneous shocks: a 37% devaluation and a negative wealth shock for the flexible and sticky price case, respectively. We start with the case in which there is no real shock to build intuition that is useful for understanding the empirically relevant case of when there is a negative real shock.

## 3.1.1. No real shock

Column 1 of Table 2 indicates that when prices are flexible, the devaluation has no impact on quantities, whereas all prices, including the nominal wage, increase by 37%.

Column 2 of Table 2 shows that when nontradable-goods prices are sticky, the devaluation induces a low rate of CPI inflation (8.7%). Even though PPP holds for import

<sup>&</sup>lt;sup>4</sup>We also analyze the Korean example by assuming that the real shock is a decline in the demand for exports. Our results are similar to those obtained with the net foreign asset shock. The only difference is that exports rise by less when there is a negative shock to export demand.

prices at the dock, the presence of distribution costs implies that the retail price of imported goods rises by only 20.4%.

When nontradable-goods prices are sticky, the devaluation leads to a rise in hours worked (9.9%). To understand the expansion in hours worked we briefly discuss the response of output in the export and nontradable sectors.

The devaluation induces a fall in the dollar wage rate (W/S), which reduces the marginal cost of producing export goods. This reduction leads to a 8.4% decline in the dollar price of exports  $(\bar{P}^X/S)$  and a 10.4% rise in the volume of exports (see Table 2). To understand the behavior of  $\bar{P}^X/S$  and W/S, we note that the optimal response of export goods producers to a decline in marginal cost is to lower their dollar price and sell more units. Consistent with Eq. (2.10), absent foreign distribution costs  $(\phi^*=0)$ , the percentage declines in  $\bar{P}^X/S$  and W/S would be the same. However, as emphasized by Corsetti and Dedola (2004), when  $\phi^*>0$ , a 1% decline in the dollar price of exports  $(\bar{P}^X/S)$  induces a less than 1% decline in the retail dollar price of exports. Consequently, the price reduction induces a smaller rise in the demand for the product. Put differently, a positive value of  $\phi^*$  reduces the effective elasticity of demand with respect to  $\bar{P}^X/S$ . Therefore, the optimal response of the monopolist is to lower  $\bar{P}^X/S$  by less than when  $\phi^*=0$ .

According to Table 2 consumption of tradable goods rises by 3.7%. To understand this effect note that in equilibrium the following condition must hold:

$$ra_t = ra_0 = C_t^T - (\bar{P}_t^X/S_t)X_t.$$
 (3.1)

To derive this equation we start with (2.5) and rewrite profits as sales revenue minus labor costs. We then use Eqs. (2.17), (2.6), the market clearing condition for nontradable goods, and the intertemporal Euler equation for tradable consumption. The assumptions that  $\beta = 1/(1+r)$  and shocks are permanent imply that  $a_t$  is constant ( $a_t = a_0$ ). It follows from (3.1) that imports ( $C_t^T$ ) must rise to match export revenues.

To explain the response of hours worked in the nontradable-goods sector we note that the consumer's first-order conditions for  $C_t^T$  and  $C_t^N$  imply that

$$\frac{C_t^N}{C_t^T} = \left[\frac{P_t^T}{P_t^N}\right]^{\rho}.\tag{3.2}$$

We note that  $P_t^T/P_t^N$  rises, since  $P_t^N$  remains constant and  $P_t^T$  rises in response to the devaluation (see Eq. (2.7)). Since both  $C_t^T$  and the right-hand side of Eq. (3.2) rise, it follows that  $C_t^N$  must also rise. By assumption, nontradable-goods firms must satisfy demand at fixed prices, so hours worked in the nontradable sector rise. Since hours worked in both the export and nontradable-goods sectors increase so do the overall hours worked.

The wage rate that is relevant for labor supply decisions is the CPI-deflated real wage,  $W_t/P_t$ . Given our assumptions about preferences  $W_t/P_t$  must rise, because hours worked  $(N_t)$  increase. Since  $N_t$  rises by 9.9% and the elasticity of labor supply is four,  $W_t/P_t$  must rise by roughly 9.9/4%. The dollar-denominated wage falls by 26.4%, but this wage is not relevant for labor-supply decisions. Most of the worker's consumption basket is composed

<sup>&</sup>lt;sup>5</sup>The nominal wage rate reported in Table 2 rises by somewhat less than 9.9/4 because we compute the CPI reported in our tables as an arithmetic average of tradable and nontradable prices. The rate of change in the arithmetically averaged CPI is similar to the rate of change the theoretical price index that corresponds to the household's utility function (see Eq. (2.2)).

of nontradable goods whose prices have not changed. As a result, CPI and dollar-deflated real wages respond very differently to the devaluation.

The real-wage rate is constant in the flexible-price case and rises when prices are sticky. The increase in the nominal wage,  $W_t$ , is smaller in the sticky-price case because CPI inflation is much lower than in the flexible-price case.

Table 2 reports that the mark-up of nontradable-goods producers falls to 7.6% after the devaluation. A key question is, how great is the incentive of an individual nontradable-goods firm to deviate from the symmetric sticky price equilibrium? According to Table 2, the optimal mark-up for the deviator is 12.5% and the percentage increase in his profits is 9.9%. Consequently, the loss from keeping prices constant for a long period of time would be very great. We conclude that absent any real shocks, a large devaluation would lead firms to change prices and the economy would go to the flexible-price equilibrium.

## 3.1.2. Negative real shock

Column 3 of Table 2 shows that when prices are flexible, a devaluation of 37% leads to a 23.1% rise in the CPI. A devaluation also induces a fall in the dollar price of exports, an expansion of hours worked in the export sector, and an even greater drop in hours worked in the nontradable-goods sector. In addition, there is a decline in the dollar price of nontradable goods and in the dollar and CPI-deflated real wages.

These effects happen because when there is a negative real shock, the devaluation coincides with a decline in net foreign assets. According to Eq. (3.1) a decline in  $a_t$  must be accompanied by either an improvement in the trade balance  $(C_t^T - (\bar{P}_t^X/S_t)X_t)$ . In principle, this reduction can be accomplished by increasing exports or reducing imports. Exports can be increased either by raising aggregate hours worked or by reallocating workers from the nontradable-goods sector to the export sector.

Given our preference specification, it is not optimal to respond to a decline in  $a_0$  solely through a fall in  $C_t^T$ , so that  $X_t$  must rise. For exports to rise, the dollar price of exports must fall. Eq. (2.10) implies that the dollar wage must also fall. Under flexible prices (but not under sticky prices) whenever the dollar wage declines the CPI-deflated real wage also declines. To see this we note that the CPI-deflated real wage is

$$W_t/P_t = W_t/[v(P_t^T)^{1-\rho} + (1-v)(P_t^N)^{1-\rho}]^{1/(\rho-1)}.$$
(3.3)

Using Eqs. (2.14), (2.16), and (2.7) this expression can be rewritten as

$$W_t/P_t = 1/[v(S_t/W_t + \phi\mu/A^N)^{1-\rho} + (1-v)(\mu/A^N)^{1-\rho}]^{1/(\rho-1)}.$$
(3.4)

Our preference specification implies that aggregate hours worked depend only on the wage rate. Therefore aggregate hours worked fall. It follows that there must be a substantial decline in nontradable consumption to allow for a rise in the production of exports.

Since nontradable-goods prices are a mark-up on wages, the drop in dollar wages leads to a decline in the dollar price of nontradable goods. This decline creates a wedge between the devaluation rate (37%) and the CPI inflation rate (23%). However, even though the CPI inflation is lower than the change in the exchange rate, it is much higher than the actual rate of inflation in Korea (6.6%).

Column 4 of Table 2 shows that when nontradable-goods prices are sticky, the CPI inflation in the model (8.7%) is much closer to the actual rate of inflation (6.6%). Thus, the model does well in accounting for the post-devaluation decline in the RER.

Viewed as a whole, our results indicate that when nontradable-goods prices are sticky, the model successfully accounts for low post-devaluation rates of inflation. This result begs the question, is it reasonable to assume that nontradable-goods prices are sticky? To answer this question, we calculate the incentive of an individual nontradable-goods monopolist to deviate from a symmetric sticky-price equilibrium. The percentage change in profits of a deviator is equal to zero (see column 4 of Table 2). If there are any costs of changing prices, nontradable-goods producers will keep their prices constant, thus rationalizing the sticky-price equilibrium.<sup>6</sup> The gains to deviating from a sticky-price equilibrium are very small, when there is a negative real shock but large otherwise. This difference reflects the fact that nominal wages rise by much less when there is a negative real shock.

## 3.2. The Uruquay example

Table 3 reports the results of a 42% devaluation that coincides with a fall in  $\xi$ , the level parameter in the demand for exports (2.8), from 1 to 0.69. When nontradable-goods prices are flexible, the CPI inflation in the model (26%) is close to the actual rate of inflation (29%). This result suggests that sticky prices did not play a significant role in the Uruguayan case. Even though the model does well in accounting for the post-devaluation rate of inflation, it understates the post-devaluation decline in the RER (15.5% compared to 30.6%). This shortcoming is due to the fact that the model abstracts from changes in the international price of tradable goods,  $P_t^*$ . In the year after the Uruguayan devaluation there was a large rise in the CPI of Uruguay's major trading partners. This rise was associated primarily with a high rate of inflation in Uruguay's main trading partner, Argentina.

The CPI inflation is lower that the rate of devaluation because, other things equal, a negative shock to export demand induces a decline in export revenues. Given agents' preferences, it is not optimal to match this decline with only a fall in  $C_t^T$ , therefore  $\bar{P}_t^X/S_t$  must fall to mitigate the decline in  $X_t$ . It follows from (2.10) that the dollar wage must fall, so that nominal wages must rise by less than the rate of devaluation. Since nontradable-goods prices are a mark-up on nominal wages they also rise by less than the rate of devaluation. This result in turn implies that the rate of CPI inflation is lower than the rate of devaluation.

The previous results suggest that the flexible-price version of the model can account for post-devaluation inflation rates in Uruguay. This conclusion leads us to ask whether or not the sticky price equilibrium was sustainable in Uruguay. To answer this question, we compute the equilibrium of the model under the assumption that nontradable-goods prices are sticky. We then assess the gains to a nontradable firm from deviating from that equilibrium. According to column 2 of Table 3, the gains are equal to roughly one percent of a deviator's profits. These calculations indicate that a sticky-price equilibrium would not have been sustainable in Uruguay.

<sup>&</sup>lt;sup>6</sup>There is, of course, another equilibrium in which all nontradable goods producers change their prices. The existence of two equilibria, one in which prices are sticky and one in which all firms change prices, is a generic property of models that emphasize costs of changing prices.

Table 3
Prices and quantities in Uruguay one year after devaluation

	1	2	3	
	Model	Data		
	Negative real shoo	k	Selected variables	
	Flexible prices	Sticky prices		
Prices (log percent change)				
Nominal exchange rate	41.5	41.5	41.5	
Real exchange rate	-15.5	-31.7	-30.6	
Consumer price index	26.0	9.8	28.6	
Nontradable goods	21.7	0.0	0.0	
Tradable goods	32.1	22.9		
Export prices (in local currency)	28.4	19.9		
Export prices (in U.S. dollars)	-13.1	-21.6		
Nominal wage	21.7	8.1		
Quantities (log percent change)				
Total hours	-16.9	-5.8		
Hours worked in export sector	-11.1	5.1		
Exports	-11.1	5.1	-10.9	
Consumption	-18.4	-9.0	-18.5	
Consumption of tradable goods	-20.9	-14.3		
Consumption of nontradable goods	-17.7	-7.4		
Incentives to change prices (levels)				
Post-devaluation markup, stayers		10.7		
Change in optimal price for deviator (K)		1.6		
Optimal markup for deviator (K)		12.5		
Percentage change in deviator profits (K)		1.0		

K—Results for the Kimball (1995) specification for the demand for nontradable goods.

# 3.3. The UK example

Column 1 of Table 4 reports the response of our model economy to a permanent 11% devaluation when prices are flexible. In this case, there is no impact on real quantities, and prices increase by the rate of devaluation. This version of the model clearly cannot account for the low post-devaluation rate of inflation and mild expansion observed in the UK.

Column 2 of Table 4 reports results for the sticky-price case. The intuition behind these results is similar to that underlying the Korean case when there is no real shock. The key result here is that the CPI inflation is only 2.4%, which is roughly consistent with the CPI inflation in the data (1.7%). Also, consistent with the data, the model generates a mild expansion after the devaluation. We infer that the sticky nontradable-goods price model captures the salient features of the UK devaluation episode. As above, the key question is whether sticky prices are sustainable as an equilibrium phenomenon. Table 4 indicates that the answer to this question is yes. The gain to a nontradable-goods producer of deviating from a symmetric sticky price equilibrium is equal to zero under the Kimball (1995) specification of the nontradable-goods demand aggregator.

Table 4
Prices and quantities in UK one year after devaluation

	1	2	3
	Model		Data
	No real shock		Selected variables
	Flexible prices	Sticky prices	
Prices (log percent change)			
Nominal exchange rate	11.3	11.3	11.3
Real exchange rate	0.0	-9.0	-12.3
Consumer price index	11.3	2.4	1.7
Nontradable goods	11.3	0.0	4.8
Tradable goods	11.3	5.8	
Export prices (in local currency)	11.3	8.1	
Export prices (in U.S. dollars)	0.0	-3.2	
Nominal wage	11.3	3.1	
Quantities (log percent change)			
Total hours	0.0	3.1	
Hours worked in export sector	0.0	4.3	
Exports	0.0	4.3	4.3
Consumption	0.0	2.6	2.9
Consumption of tradable goods	0.0	1.2	
Consumption of nontradable goods	0.0	3.0	
Incentives to change prices (levels)			
Post-devaluation markup, stayers		16.3	
Change in optimal price for deviator (K)		0.0	
Optimal markup for deviator (K)		16.3	
Percentage change in deviator profits (K)		0.0	
Change in optimal price for deviator (BF)		1.6	
Optimal markup for deviator (BF)		18.2	
Percentage change in deviator profits (BF)		0.5	
Change in optimal price for deviator (DS)		3.1	
Optimal markup for deviator (DS)		20.0	
Percentage change in deviator profits (DS)		1.7	

*K*—Results for the Kimball (1995) specification for the demand for nontradable goods.

# 4. Isolating the key margins

Here, we use the UK example to discuss the mechanisms that enable our model to account for sticky nontradable-goods prices. We conduct this analysis by abstracting from real shocks, because the intuition is easier to convey when the only shock is a change in the exchange rate.

As noted, the optimal price for a nontradable-goods producer who chooses to deviate from a symmetric sticky nontradable-goods price equilibrium is given by

$$p_{it} = \mu \frac{W_t}{A^N}.$$

BF—Results for the Bergin–Feenstra (2000) specification for the demand for nontradable goods.

DS—Results for the Dixit-Stiglitz specification for the demand for nontradable goods.

The only way in which different specifications of the demand for nontradable goods affect  $p_{it}$  is through their impact on the gross mark-up,  $\mu$ . Other features of the model influence  $p_{it}$  because they affect the response of nominal wages to shocks.

To discuss the sensitivity of our results to our benchmark specification of the nontradable-goods demand aggregator, we consider two alternatives. First, we choose the parameters of the nontradable-goods demand aggregator (2.15) to be consistent with the specification proposed by Bergin and Feenstra (2000). Second, we consider the standard Dixit–Stiglitz demand specification. In both cases, we calibrate the demand aggregators so that the predevaluation values of all quantities and prices are the same as in our benchmark specification. Thus, different specifications of the aggregator only affect the benefit to a nontradable-goods producer of deviating from a symmetric sticky-price equilibrium.

Column 2 of Table 4 summarizes the benefit to a deviator for different specifications of the demand aggregator. As we have noted, the benefit is roughly zero for the Kimball case. With the Bergin–Feenstra calibration, the benefit is roughly 0.5% of profits. The present value of this gain is still moderate relative to the costs of changing prices estimated by Levy et al. (1997) and Zbaracki et al. (2004). With the Dixit–Stiglitz specification, the benefit to a deviator rises to 1.7% of profits. We conclude that our results are reasonably robust to modifications of the demand aggregator, as long as we do not go to the extreme of the Dixit–Stiglitz specification.

We also wish to explore the impact of other key parameters on the response of the nominal wage to the devaluation and on a firm's incentive to deviate from the sticky price equilibrium. For every change in a model parameter, we recalibrate the value of  $a_0$  so that the pre-devaluation share of exports in GDP remains constant. We use this procedure to facilitate comparisons across the different specifications. For a small devaluation, such as that of the UK, the benefits from deviating from the sticky-price equilibrium for the Kimball specification are always close to zero. Therefore, we focus our sensitivity analysis on the Bergin–Feenstra specification.

First, we consider the impact of foreign distribution costs. Column 2 of Table 5 reports results for the case in which the foreign distribution margin is zero instead of 50%. In this case, there is a smaller rise in the local currency price of exports (5.7% compared to 8.1%) and a larger fall in  $\bar{P}^X/S$  (-5.6% compared to -3.2%). As noted, a fall in  $\phi^*$  raises the effective demand elasticity faced by export-goods producers. This fall makes it optimal for producers to lower  $\bar{P}^X/S$  by more than they do when  $\phi^*$  is positive. Relative to the benchmark case, the associated increase in demand leads to a larger expansion in hours worked in the export sector and a greater rise in the nominal wage (5.7% compared to 3.1%). Consequently, the percentage increase in profits from deviating from the symmetric sticky-goods price equilibrium rises from 0.5% to 3.7%. We infer that the presence of foreign distribution costs helps rationalize the sticky-price equilibrium.

Column 3 reports the impact of changing the parameter v so that the share of traded goods (inclusive of distribution) in the CPI bundle falls from 40% to 25%. The devaluation now leads to a lower rate of CPI inflation (1.5% compared to 2.4%) and to smaller rise in nominal wages (2.6% compared to 3.1%). The benefit to the deviator falls from 0.5% to 0.2% of profits. We conclude that a small share of traded goods in the CPI bundle plays a positive role in rationalizing sticky nontradable-goods prices.

Column 4 reports the results we obtain by increasing the elasticity of substitution between tradables and nontradables from 0.4 to 1. This change implies that the demand for nontradable goods is more responsive to a change in the price of imported consumption

Table 5
The role of different margins in the model

	1	2	3	4	Domestic distribution margin = 0%
	Benchmark expansionary	Foreign distribution margin = 0%	Share of traded goods in CPI 25	ρ = 1	
Prices (log percent change)					
Nominal exchange rate	11.3	11.3	11.3	11.3	11.3
Real exchange rate	-9.0	-9.0	-9.8	-9.0	-6.6
Consumer price index	2.4	2.4	1.5	2.4	4.7
Nontradable goods	0.0	0.0	0.0	0.0	0.0
Tradable goods	5.8	5.8	5.8	5.8	11.3
Export prices (in local currency)	8.1	5.7	7.9	8.3	9.1
Export prices (in U.S. dollars)	-3.2	-5.6	-3.4	-3.0	-2.2
Nominal wage	3.1	5.7	2.6	3.7	5.8
Quantities (log percent change)					
Total hours	3.1	13.3	4.3	5.4	4.7
Hours worked in export sector	4.3	15.1	4.5	4.0	2.9
Exports	4.3	15.1	4.5	4.0	2.9
Consumption	2.6	12.6	4.0	4.7	3.0
Consumption of tradable goods	1.2	11.2	2.3	1.2	0.3
Consumption of nontradable goods	3.0	12.9	4.3	5.6	4.9
Incentives to change prices (levels)					
Post-devaluation markup, stayers	16.3	13.4	17.0	15.7	13.2
Change in optimal price for deviator (BF)	1.6	4.1	1.0	2.1	4.2
Optimal markup for deviator (BF)	18.2	18.2	18.2	18.2	18.2
Percentage change in deviator profits (BF)	0.5	3.7	0.2	0.9	3.9

	6	7	8
	Elasticity of demand for exports = 3.7	Share of exports in $GDP = 10\%$	Labor supply elasticity 1
Prices (log percent change)			
Nominalexchange rate	11.3	11.3	11.3
Real exchange rate	-9.0	-9.0	-9.0
Consumer price index	2.4	2.4	2.4
Nontradable goods	0.0	0.0	0.0
Tradable goods	5.8	5.8	5.8
Export prices (in local currency)	6.8	8.0	8.9
Export prices (in U.S. dollars)	-4.5	-3.3	-2.5
Nominal wage	4.0	2.9	5.1
Quantities (log percent change)			
Total hours	6.5	2.3	2.8
Hours worked in export sector	8.2	4.4	3.3
Exports	8.2	4.4	3.3
Consumption	5.8	1.9	2.3
Consumption of tradable goods	4.4	0.5	1.0
Consumption of nontradable goods	6.2	2.2	2.7
Incentives to change prices (levels)			
Post-devaluation markup, stayers	15.3	16.5	14.0
Change in optimal price for deviator (BF)	2.4	1.4	3.6
Optimal markup for deviator (BF)	18.2	18.2	18.2
Percentage change in deviator profits (BF)	1.2	0.4	2.7

BF—Results for the Bergin–Feenstra (2000) specification for the demand for nontradable goods.

goods relative to nontradable-goods. Relative to the benchmark specification, the devaluation induces larger rises in the demand for nontradable-goods, hours worked in the nontradable-goods sector, and nominal wages. The percentage change in profits for a deviator rises from 0.5% to 0.9% of profits. We conclude that a low degree of substitution between nontradable goods and imported goods helps rationalize sticky nontradable-goods prices.

Column 5 reports the results we obtain by eliminating domestic distribution costs. Setting  $\phi$  equal to zero increases the effective share of pure tradable goods in consumption and the effective elasticity of substitution between tradables and nontradables. For the reasons discussed above, both these effects imply that, after the devaluation, nominal wages rise by more than they do in the benchmark model. The incentive for nontradable goods firms to change their price is 3.9% compared to 0.5% of profits in the benchmark model. We conclude that sticky nontradable goods prices are easier to rationalize in the presence of domestic distribution costs.

Column 6 reports results of increasing the elasticity of demand for exports,  $\gamma$ , from 2.7 to 3.7. This change in  $\gamma$  increases the response of exports for two reasons. First, for a given drop in  $\bar{P}^X/S$ , there is a larger increase in exports. Second, the equilibrium fall in  $\bar{P}^X/S$  is actually larger. Raising  $\gamma$  has the same effect as lowering  $\phi^*$  on the elasticity of  $\bar{P}^X/S$  with respect to W/S. For the reasons discussed above,  $\bar{P}^X/S$  becomes more responsive to the drop in W/S. Therefore, the decline in  $\bar{P}^X/S$  is greater than in the benchmark model, which leads to a larger expansion in the export sector. There is also a larger increase in the nominal wage. The benefit of changing the price of nontradable goods increases from 0.5% to 1.2% of profits. A low elasticity of demand for exports helps to rationalize sticky prices in our model.

Column 7 summarizes the impact of lowering the share of exports in GDP from 23% to 10%. This value is closer to the pre-devaluation export shares in Argentina (10.9%) and Brazil (10.6%). In our model, a smaller export sector reduces the absolute value of the post-devaluation rise in hours worked in the export sector. Consequently, there is a smaller rise in nominal wages. The percentage change in profits for a deviator falls from 0.5% to 0.4% of profits. We conclude that a smaller share of exports in GDP helps rationalize the sticky-price equilibrium.

Column 8 reports the impact of lowering the labor supply elasticity from four to one. Relative to the benchmark model, there is a greater rise in the nominal wage and the CPI-deflated real wage. The greater impact on wages is a direct consequence of the lower labor-supply elasticity. These gains from deviating from the symmetric sticky nontradable-goods price equilibrium rise from 0.5% to 2.7% of profits. A high elasticity of labor supply is clearly critical in accounting for sticky prices.

## 5. An overvaluation experiment

A standard way of formalizing the notion that an exchange rate is overvalued is to assume that traded goods prices are sticky in domestic currency. Here, we discuss an

<sup>&</sup>lt;sup>7</sup>An offsetting effect results from the fact that the theoretical consumption deflator changes by less since the two goods are more substitutable. Other things equal, this effect leads to a smaller increase in the nominal wage.

<sup>&</sup>lt;sup>8</sup>This is consistent with evidence in Gupta et al. (2001) that suggests that the expansionary effect of a devaluation is stronger when the tradable sector is larger.

alternative, complementary mechanism through which exchange rates can become overvalued. We show that if nontradable-goods prices do not change after a real shock, the exchange rate becomes overvalued. By this we mean that the real exchange rate is higher than it would be under flexible prices.

We consider an economy that is in the steady state of a fixed exchange rate regime. For convenience, we normalize the foreign price level to one and define the real exchange rate as  $RER = P_t/S_t$ . For expositional purposes we consider the Korean example, where the economy suffers a decline in its net foreign assets,  $a_t$ . Qualitatively similar results obtain if there is a negative shock to export demand, as in our Uruguay example.

Table 6 reports the response of the economy to a decline in net foreign assets, the negative real shock considered in Table 2, under different scenarios. The numbers we report are rates of change relative to the pre-shock steady state.

Column 1 reports results for the case of flexible prices with no devaluation. Eq. (3.1) implies that a decline in net foreign assets requires an improvement in the trade balance. Given our assumptions about preferences, this improvement occurs via both a decline in imports and an increase in exports. The decline in imports is achieved through an increase in the retail price of imports relative to nontradables,  $P_t^T/P_t^N = S_t/P_t^N + \phi$  (see Eq. (3.2)). Since  $S_t$  is fixed, a rise in  $P_t^T/P_t^N$  requires a drop in  $P_t^N$ , which in turn induces a decline in  $P_t$  (see Eqs. (2.7) and (2.2)) and in the RER.

What are the consequences for wages and hours worked? Since the price of nontradables falls, the nominal wage,  $W_t$ , also falls (see Eq. (2.16)). The response of aggregate hours depends on the behavior of the CPI-deflated real wage,  $W_t/P_t$ . To see what happens to  $W_t/P_t$  we recall that to achieve an improvement in the trade balance, the quantity of exports must rise. This rise requires a fall in the dollar price of exports,  $\bar{P}_t^X/S_t$ . The drop in  $\bar{P}_t^X/S_t$  induces a decline in both the dollar-denominated wage,  $W_t/S_t$  and  $W_t/P_t$  (see Eqs. (2.10), (3.3), and (3.4)). The drop in  $W_t/P_t$  leads to a decrease in aggregate hours worked.

Column 2 reports the response of the economy to the negative real shock when nontradable-goods prices are sticky and there is no devaluation. The rate of CPI inflation is zero and the *RER* remains constant. When we compare columns one and two we see that the *RER* is 14.2% higher when nontradable-goods prices are sticky. In this sense, sticky nontradable-goods prices lead to an overvalued exchange rate after a negative real shock.

In the sticky-price equilibrium, the nominal wage falls by less than it does when nontradable-goods prices are flexible. This smaller wage decline implies that the dollar price of exports falls by less than when prices are flexible (-1.7% compared to -5.9%). As a result, there is a smaller expansion in exports when nontradable-goods prices are sticky (2.2% compared to 7.3%). Eq. (3.1) implies that consumption of imported goods must fall by more in the sticky-price equilibrium.

To explain the response of hours worked in the nontradable-goods sector we note that with a fixed exchange rate and sticky nontradable prices, the right-hand side of (3.2) is fixed. Consequently, the percentage declines in  $C_t^N$  and  $C_t^T$  are the same (23.6%). In contrast, under flexible prices, the negative real shock leads to a decline in  $P_t^N/P_t^T$  and a rise in  $C_t^N/C_t^T$ . This rise, together with the fact that  $C_t^T$  drops by less under flexible prices, implies that  $C_t^N$  also falls by less under flexible prices. Since the hours worked in the export sector rise by more in the flexible-price case, the previous argument establishes that the recession induced by the real shock is mitigated by flexible prices.

Given that nontradable-goods prices remain constant and the wage falls, the mark-up of nontradable-goods producers rises (from 20% to 26.3%). An individual producer could

Table 6 Overvaluation experiment

	1	2	3	
	Flexible prices	Sticky prices (no devaluation)	Sticky prices (with devaluation)	
Prices (log percent change)				
Nominal exchange rate	0.0	0.0	37.3	
Real exchange rate	-14.2	0.0	-28.6	
Consumer price index	-14.2	0.0	8.7	
Nontradable goods	-18.0	0.0	0.0	
Tradable goods	-8.6	0.0	20.4	
Export prices (in local currency)	-5.9	-1.7	27.5	
Export prices (in U.S. dollars)	-5.9	-1.7	-9.8	
Nominal wage	-18.0	-5.1	5.9	
Quantities (log percent change)				
Total hours	-15.3	-20.5	-10.1	
Hours worked in export sector	7.3	2.2	12.1	
Exports	7.3	2.2	12.1	
Consumption	-19.0	-23.6	-14.5	
Consumption of tradable goods	-21.2	-23.6	-19.3	
Consumption of nontradable goods	-18.4	-23.6	-13.1	
Incentives to change prices (levels)				
Post-devaluation markup, stayers	1.0	26.3	13.1	
Change in optimal price for deviator $(K)$	0.0	0.0	0.0	
Optimal markup for deviator (K)	0.0	26.3	13.1	
Percentage change in deviator profits (K)	0.0	0.0	0.0	

K—Results for the Kimball (1995) specification for the demand for nontradable goods.

increase his profits by lowering his price relative to the symmetric sticky-price equilibrium. As Table 6 shows, the resulting rise in profits is zero if we assume a Kimball demand aggregator. This rise in profits is very modest (0.7% of profits) for the Bergin–Feenstra aggregator.

The previous results show that if nontradable-goods prices are sticky, then the impact of a real shock to the economy leads to a smaller decline in the real exchange rate and a larger contraction than would be the case under flexible prices. In this sense, the negative real shock results in the exchange rate being overvalued. Under these circumstances, a devaluation leads to an expansion in economic activity and helps realign the real exchange rate.

Our model is consistent with the conventional wisdom that prices do not increase after a large devaluation, because they were too high before the devaluation. If we suppose that the exchange is overvalued in the sense just described above, then a devaluation that preserves the sticky nontradable-goods price equilibrium leads to a decline in the real exchange rate without a substantial amount of inflation (see column 3 of Table 6).

## 6. Conclusion

We propose an open economy, general equilibrium model that can account for the substantial drop in real exchange rates that occurs in the aftermath of large devaluations.

Our model embodies several elements that dampen wage pressures in the wake of a devaluation. If the nominal wage remains relatively stable in the aftermath of a large devaluation, this stability can eliminate the incentive for nontradable-goods producers to change their prices. If nontradable-goods prices remain stable, inflation is low, which is compatible with a stable nominal wage rate.

We conclude by noting an important shortcoming of our paper. To simplify our analysis, we focus on rationalizing a post-devaluation equilibrium in which nontradable-goods prices do not change at all. In reality, these prices do change, albeit by far less than the exchange rate, the price of imports and exportables, or the retail price of tradable goods. Modeling the detailed dynamics of nontradable-goods prices is a task that we leave for future research.

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