



Reminder backtracking











Lup mănâncă capra

Capra mănâncă varza

Scop: mutarea unul câte unul pe mal opus fără să se mănânce











Lupul mănâncă capra













Capra mănâncă varza

































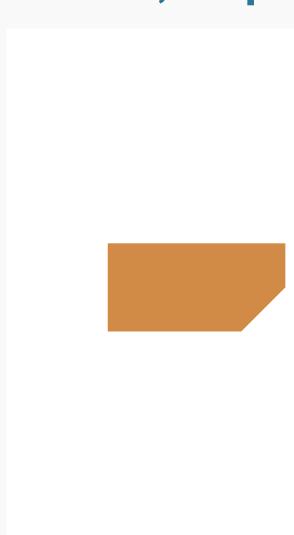






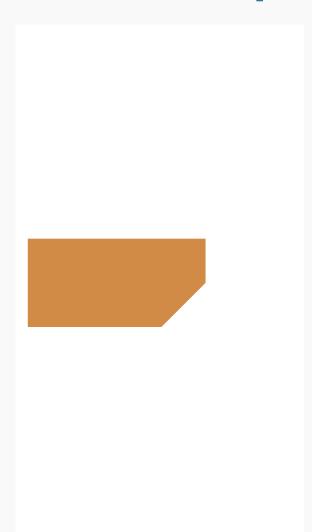








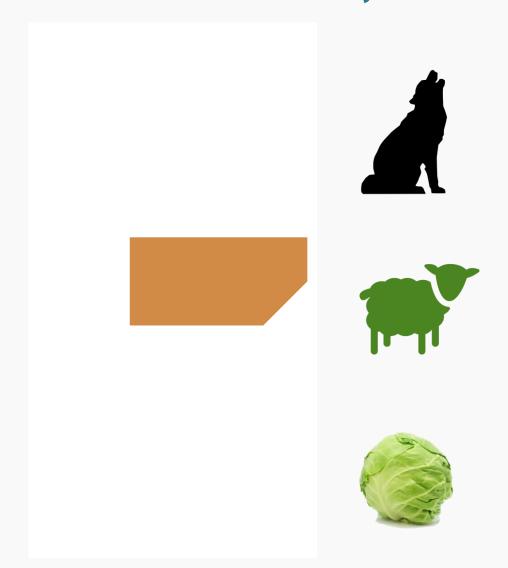




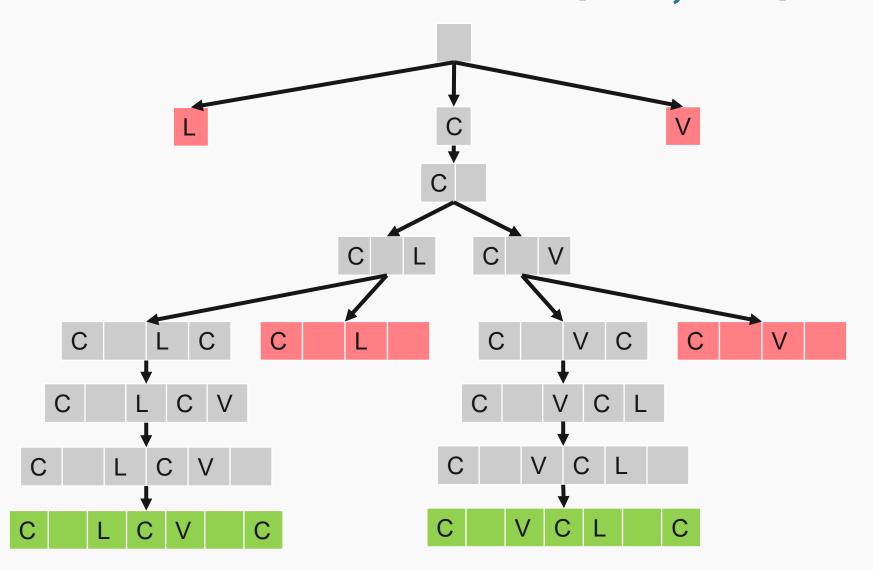














Abordarea Dijsktra – varză capră și lup

https://www.youtube.com/watch?v=0kXjl2e6qD0

Scoate toate detaliile nesemnificative din problemă

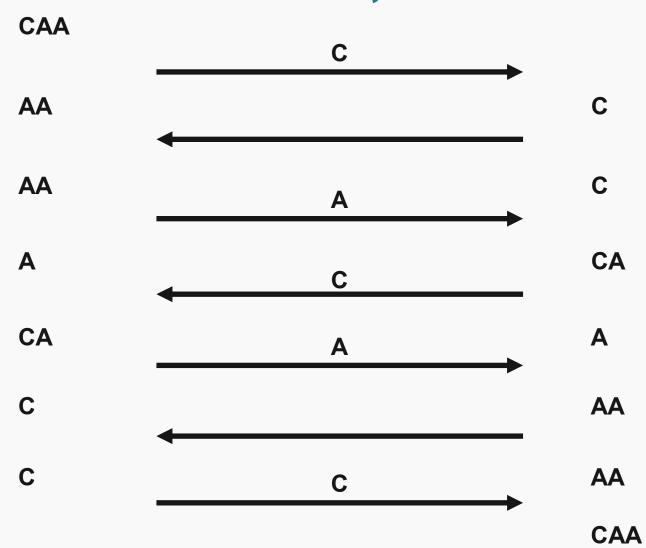
Contează dacă lupul mănâncă capra sau dacă invers capra mănâncă lupul?

Contează dacă capra mănâncă varză sau dacă invers lupul mănâncă capra?

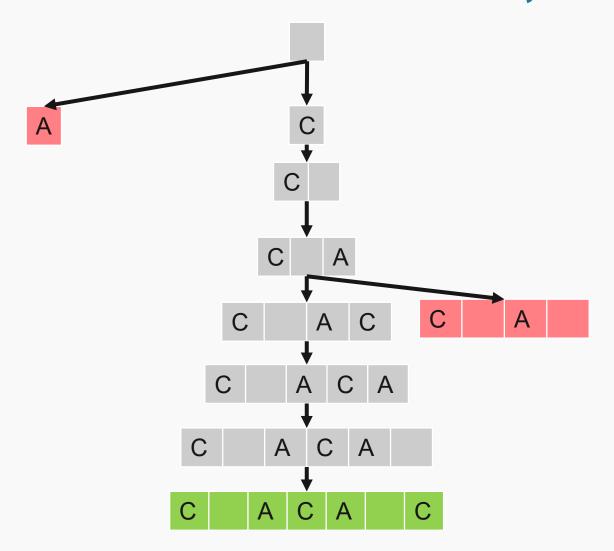
Dacă NU atunci nu e diferență între lup și varză.



Capră și restul









MinMax

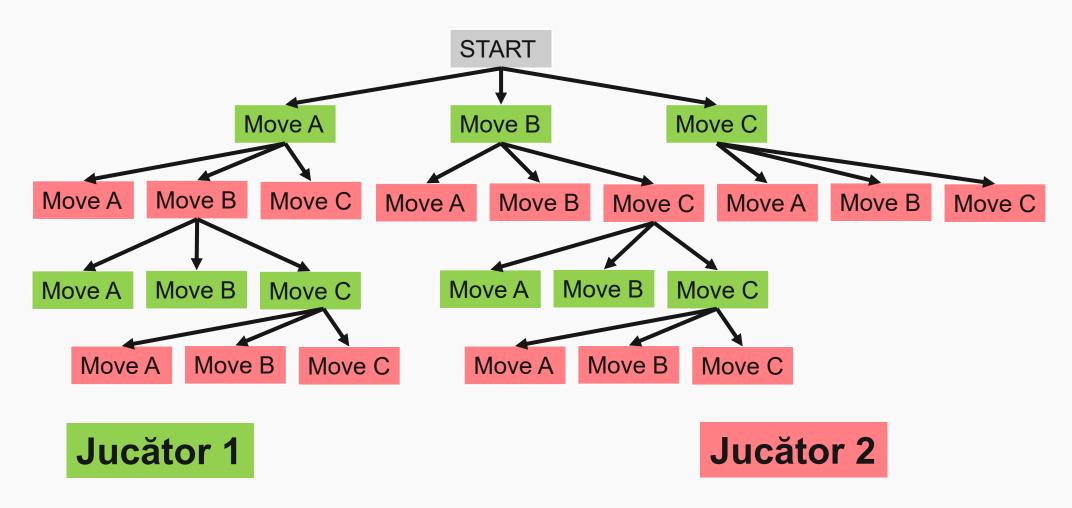
Ideea de la backtracking cu construcția arborelui de stări.

Jocuri competitive. – Vrem algoritm "Inteligență artigicială" care să câștige.

Ce face adversarul?

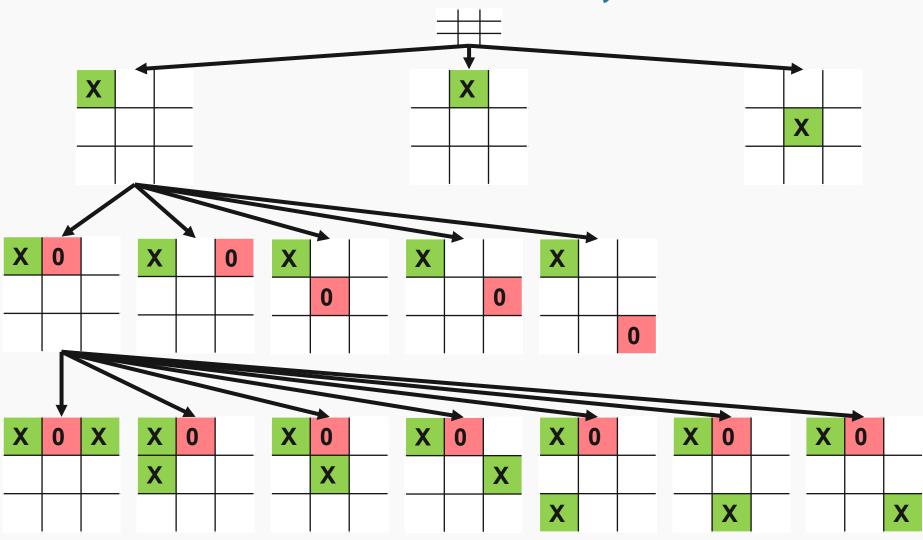


MinMax - Idee



Pe nivelele pare sunt mutări ale unui jucător. Pe nivele impare ale altui jucător.







MinMax

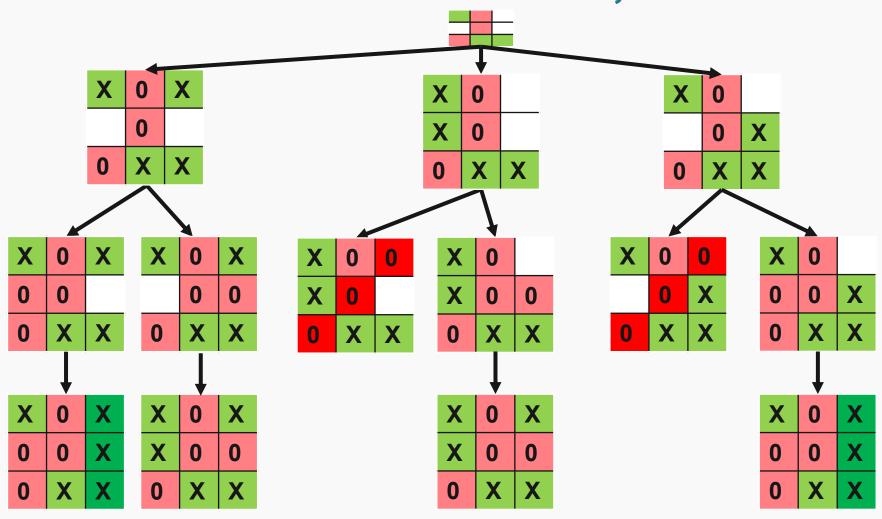
• Nu mai este suficient sa aplic backtracking.

 Chiar dacă găsesc un set de mutări prin care să câştig adversarul va alege mutări care să facă opusul.

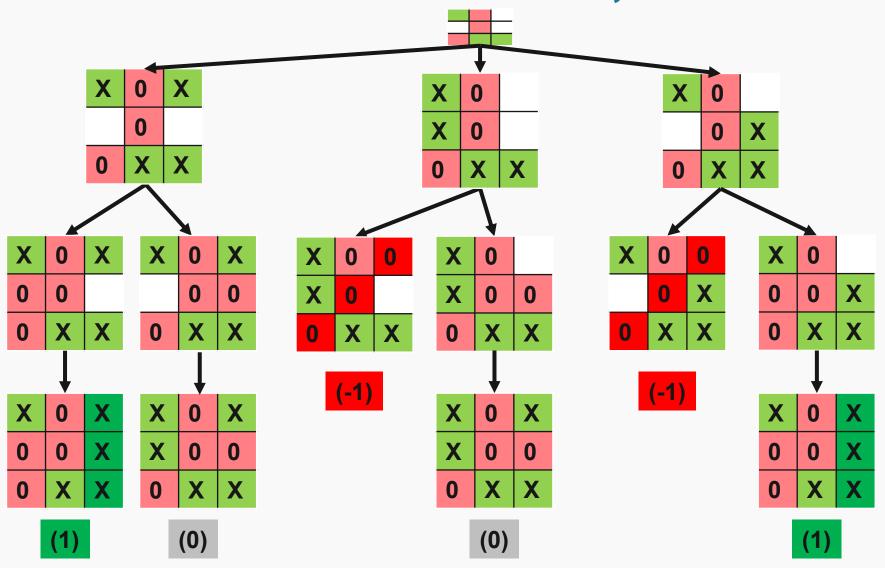
La nivelele unde eu aleg, fac mutări care să maximizeze șansele de câștig.

La nivelele unde alege adversarul, acesta probabil va încerca să îmi minimizeze șansele de câștig. Deci așa presupun că va face.

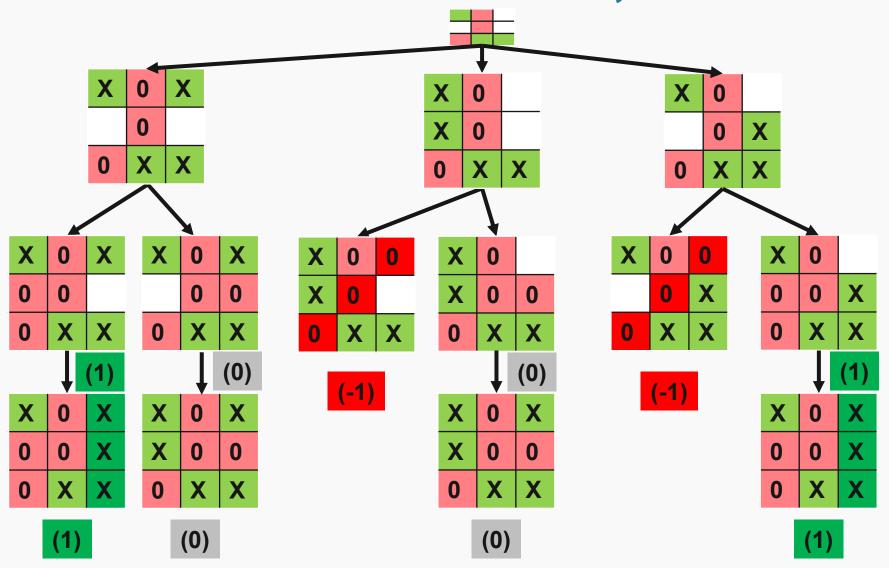




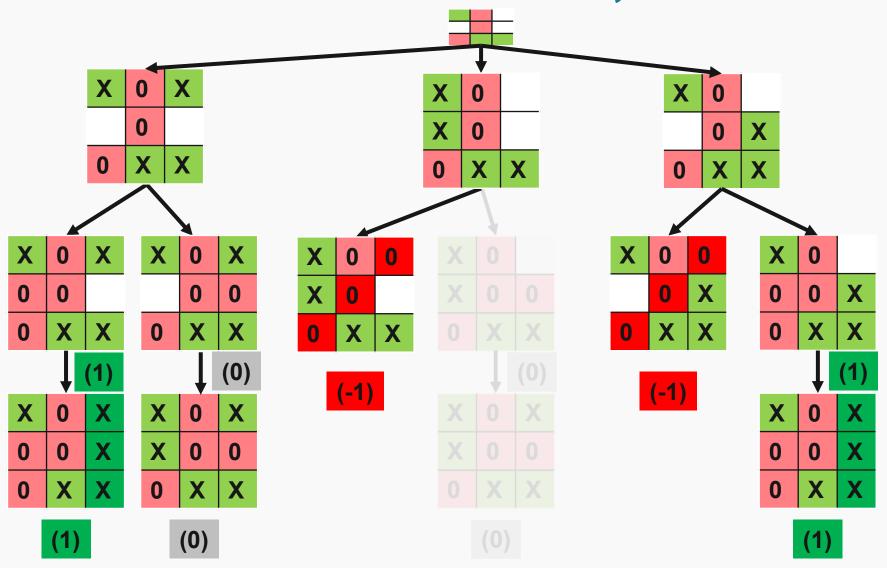




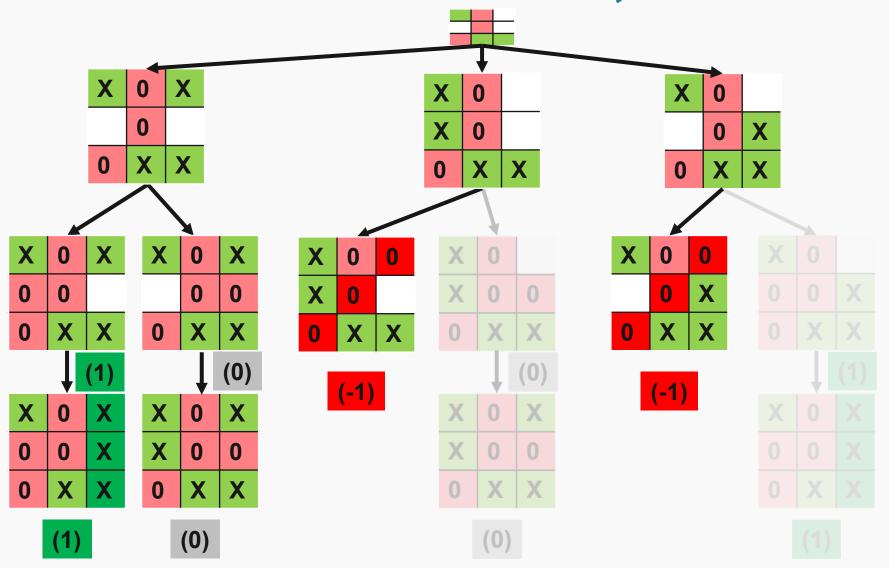




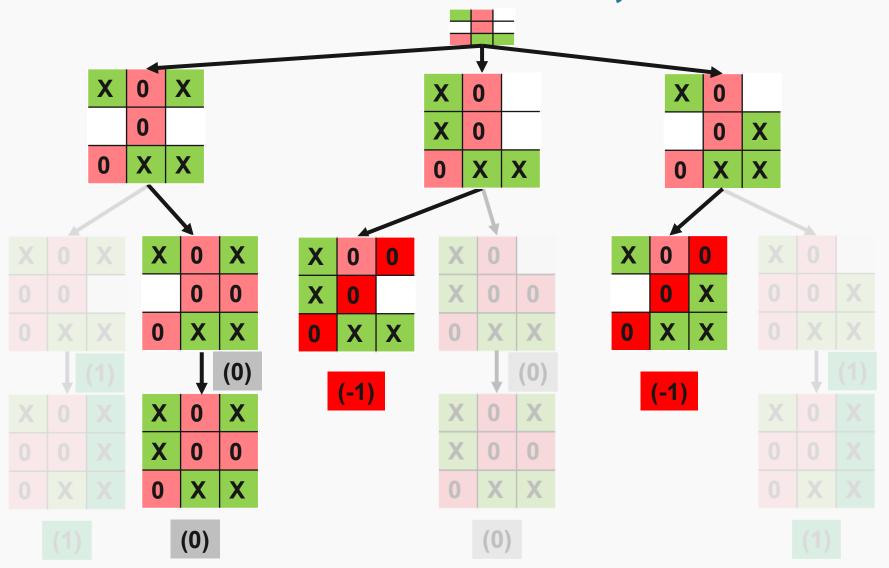




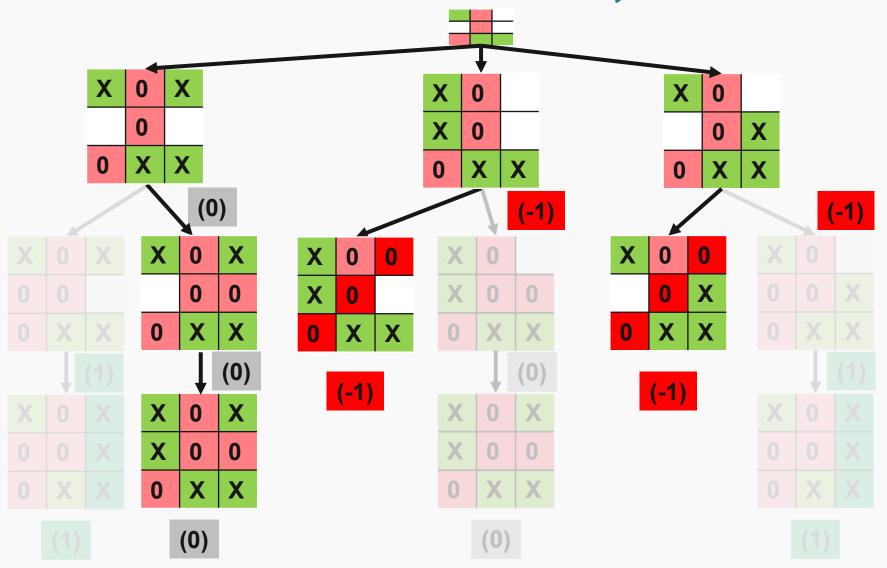




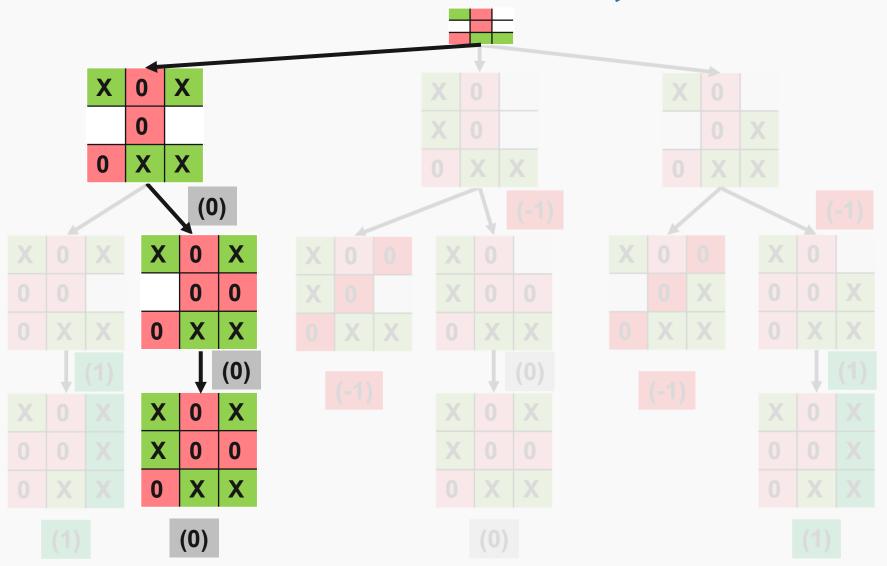














MinMax – Cât de mare este arborele?

X şi 0
Aproape
9*8*7*6*5*4*3*2*1 = 9! = 362,880 frunze
sub 1M, deci încape în memorie.

Dar şah?



MinMax – Cât de mare este arborele?

În general nu putem analiza tot arborele. Este prea mare.

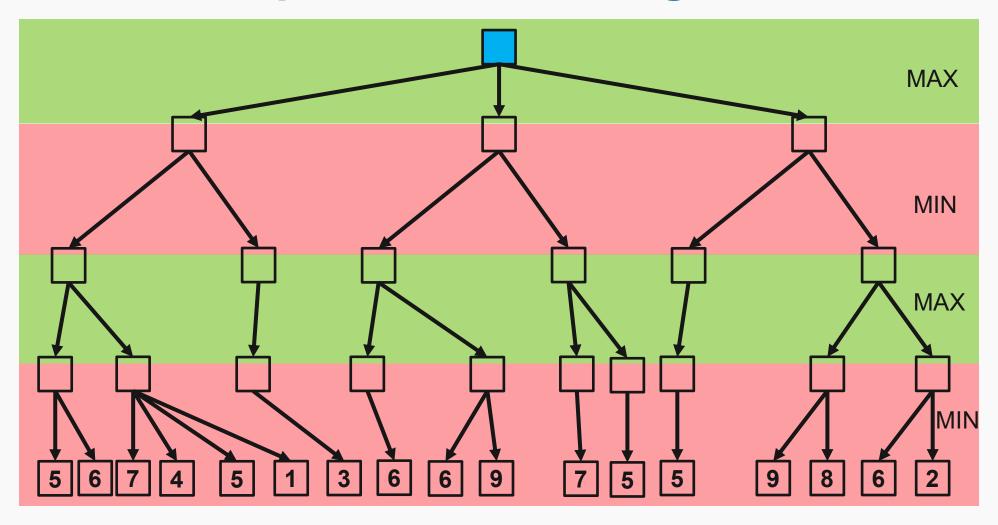
- Soluția: mergem până la o adâncime și încercăm să estimăm cât de avantajos sau dezavantajos este acea configurație a jocului.
- Estimăm -> Euristică (heuristic)



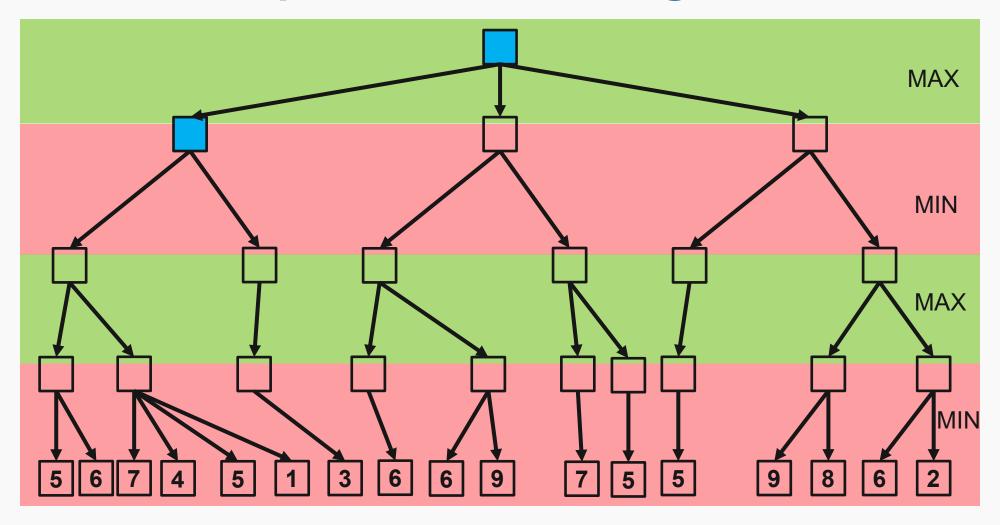
MinMax - Algoritm

```
int miniMax(gameNode node, int level, int maxDepth) {
 if (maxDepth = 0 | isEndGame(node))
       return heuristic(node);
 if (level % 2 == maximizingPlayer) {
   int value = -\infty;
   for each (child of node)
     value = max(value, miniMax(child, level + 1, maxDepth - 1));
   return value;
  } else {
   int value = +∞;
   for each (child of node)
     value = min(value, miniMax(child, level + 1, maxDepth - 1));
   return value;
```

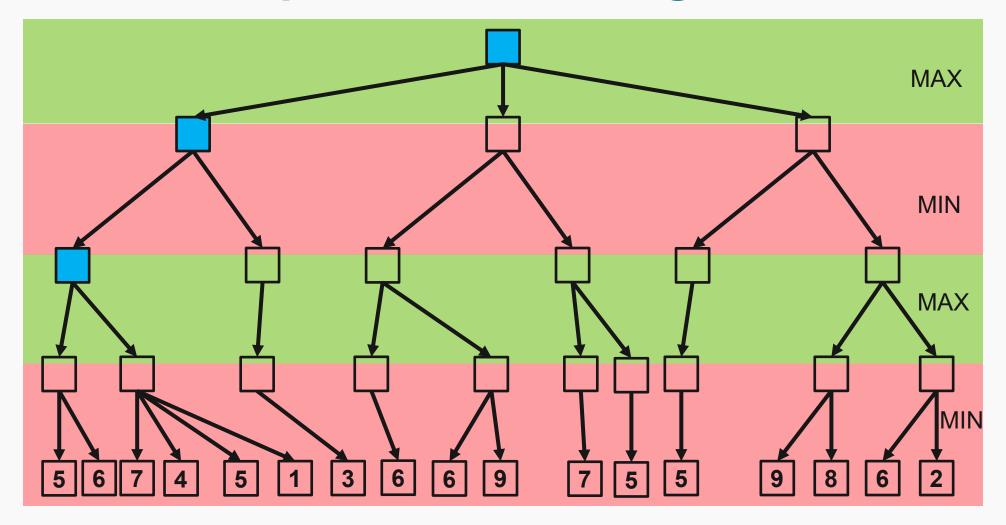




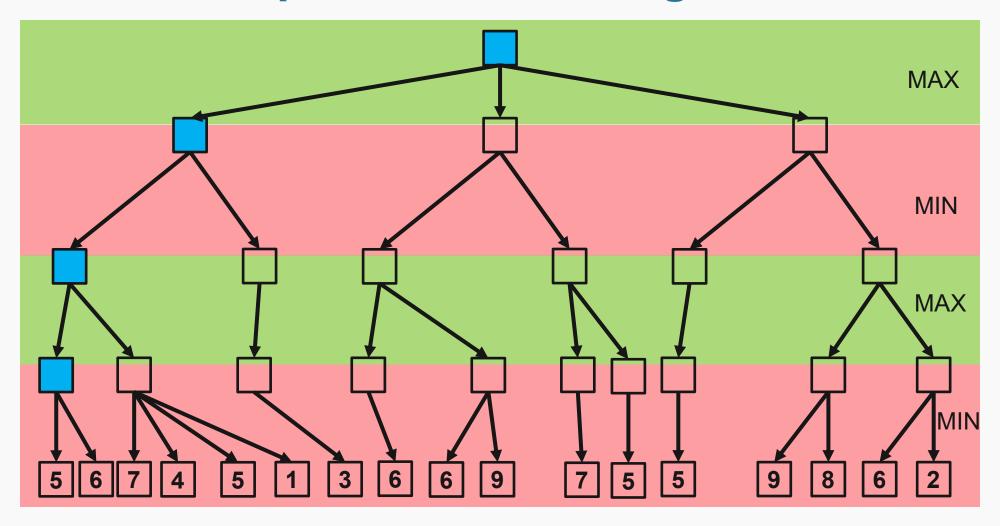




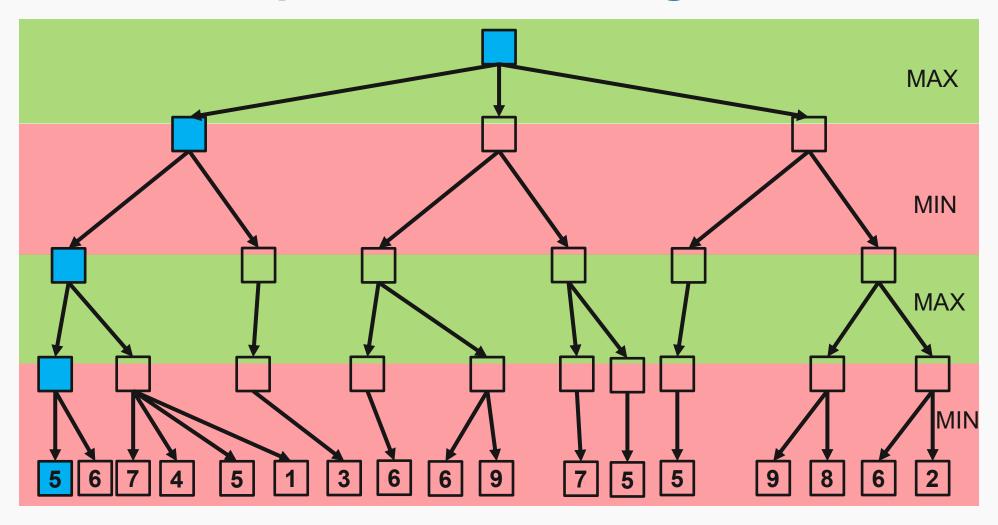




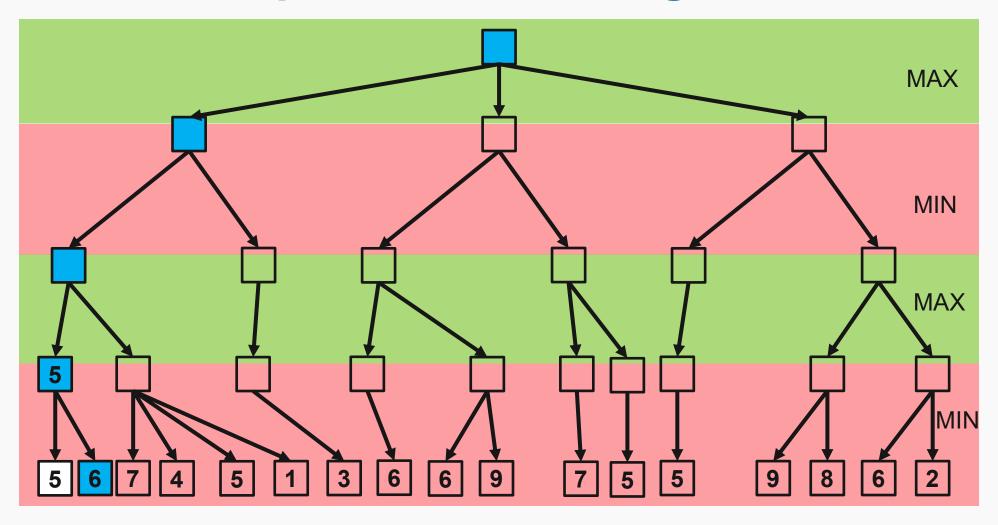




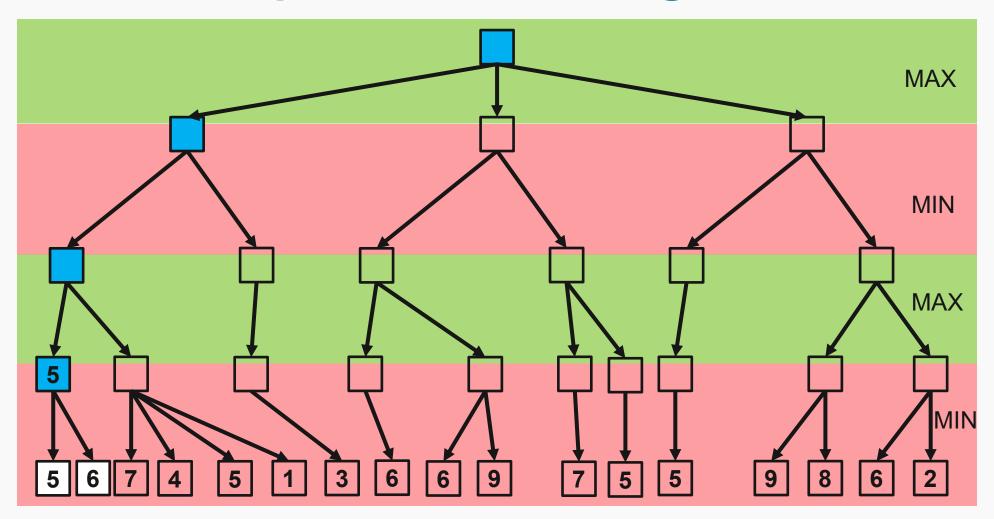




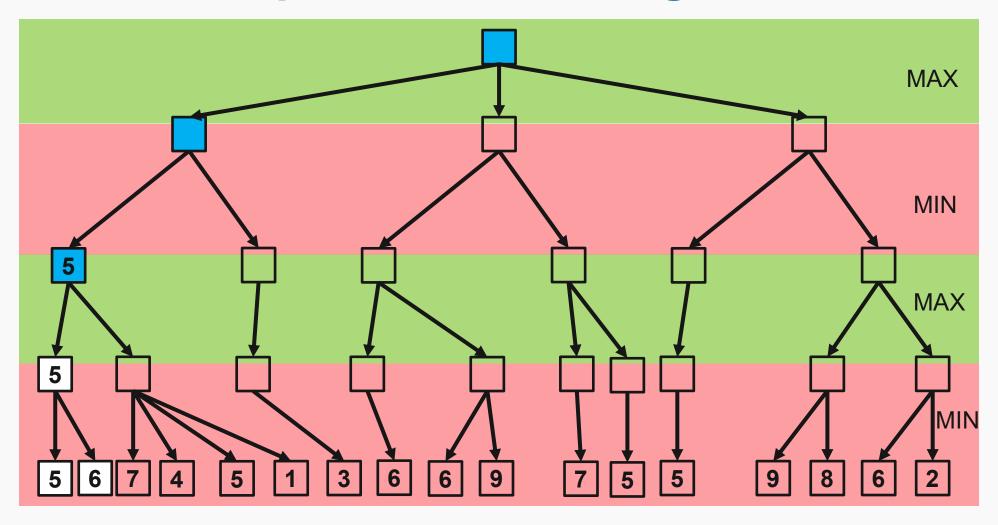




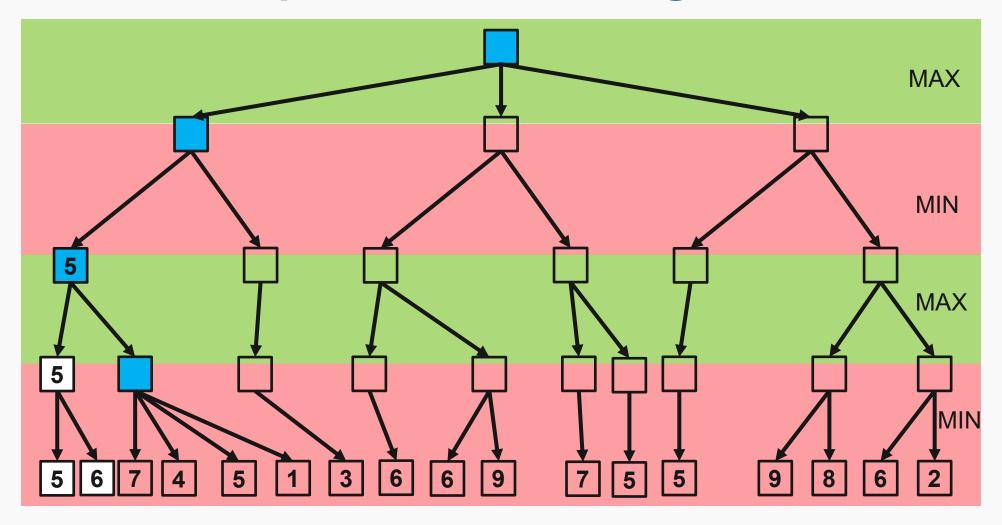




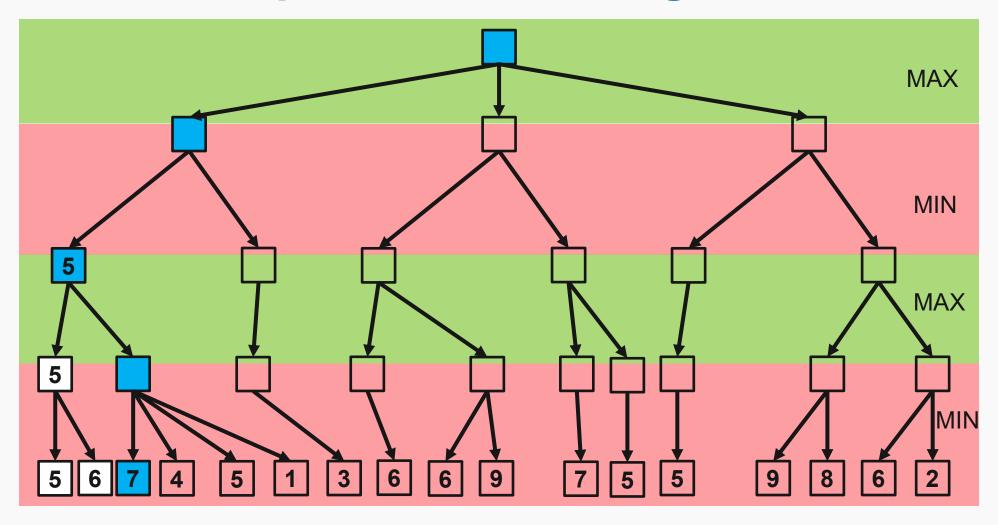




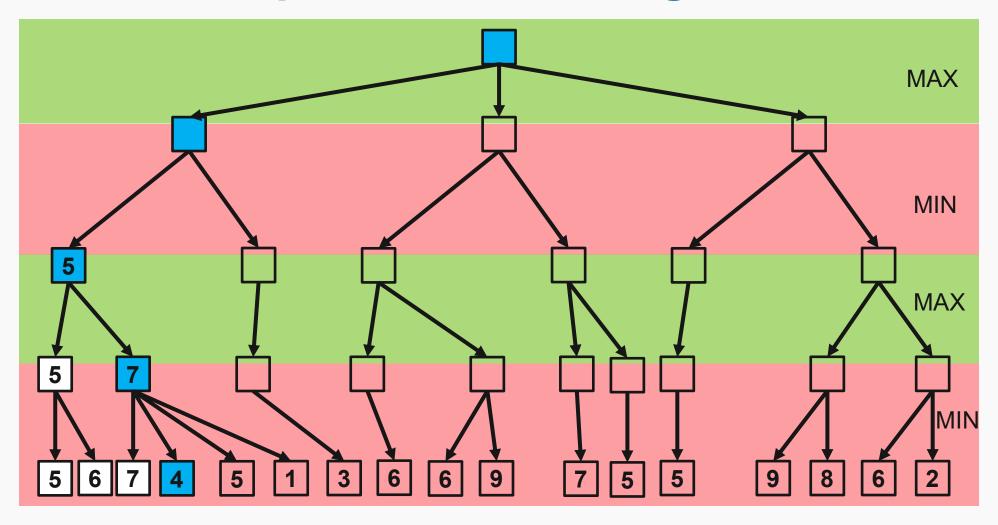




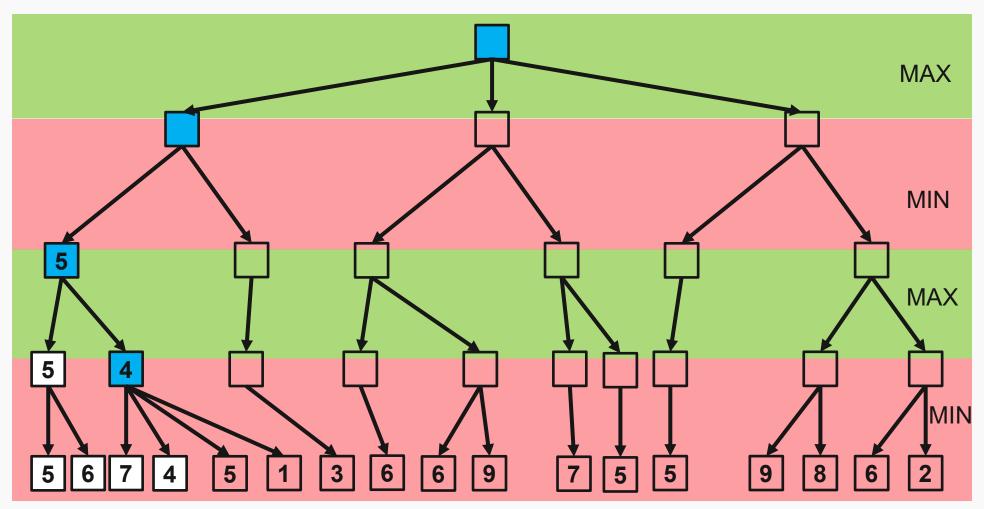






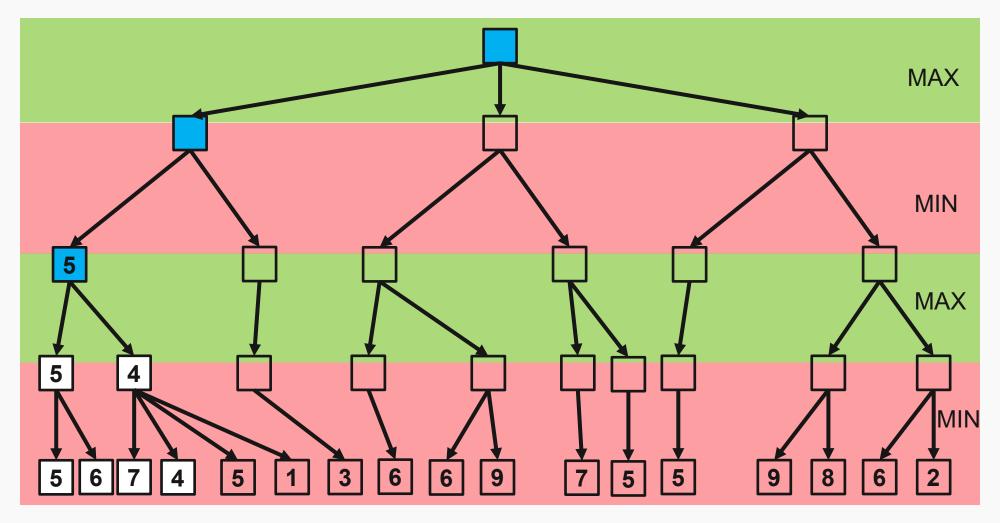




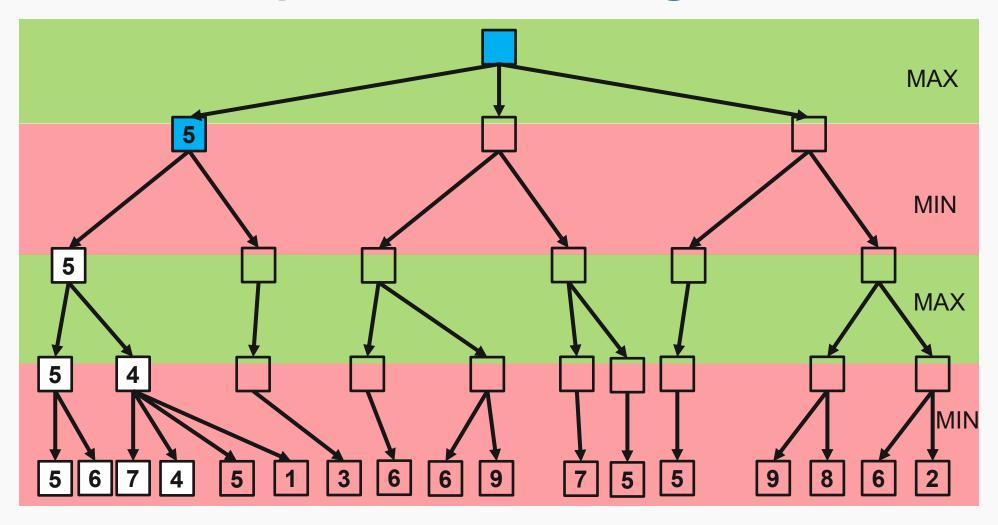


Suntem deja siguri că la acest nivel competitorul va alege 4 sau mai mic. Dar dacă el alege 4 sau mai mic, noi știm siguri că vom alege 5.

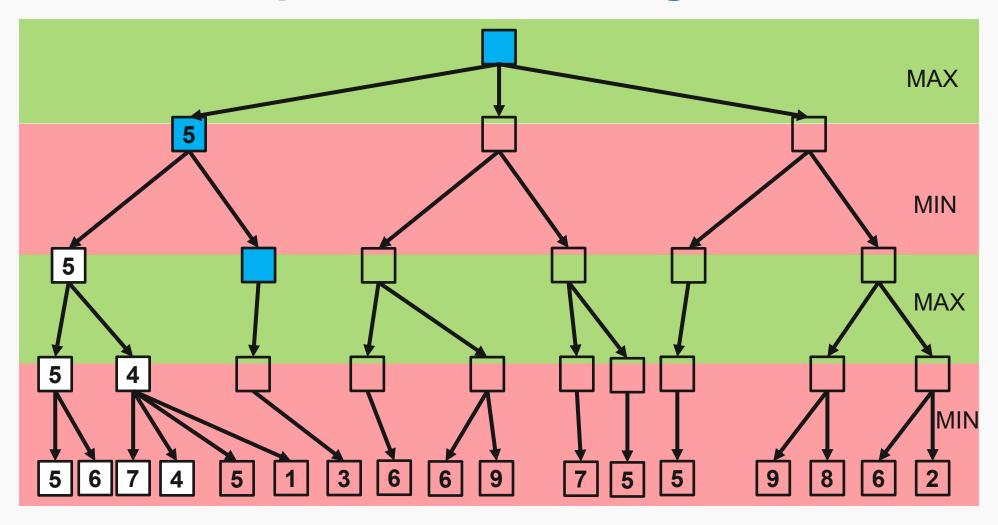




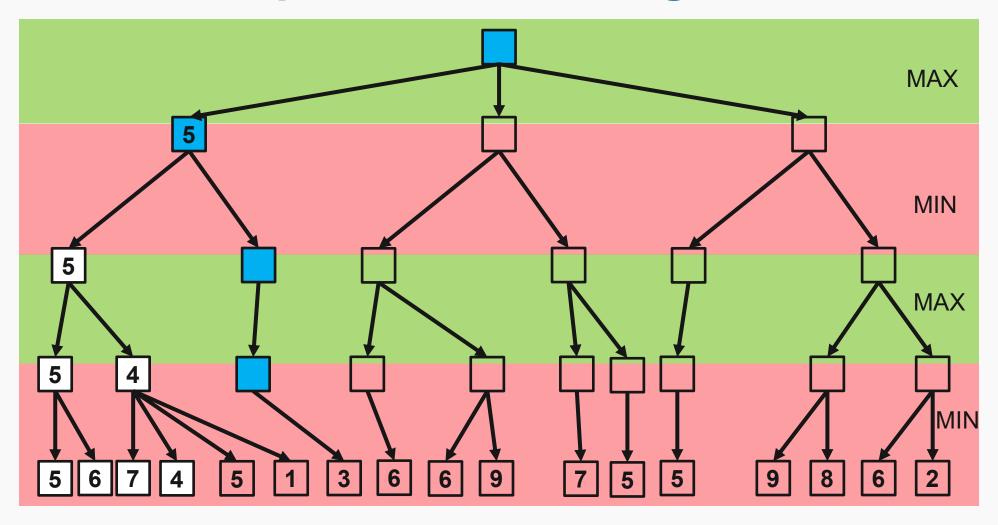




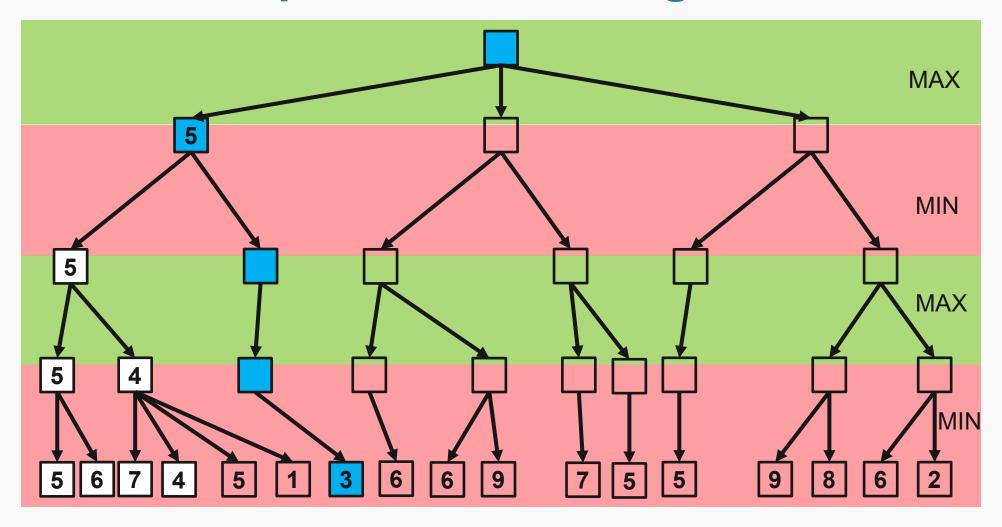




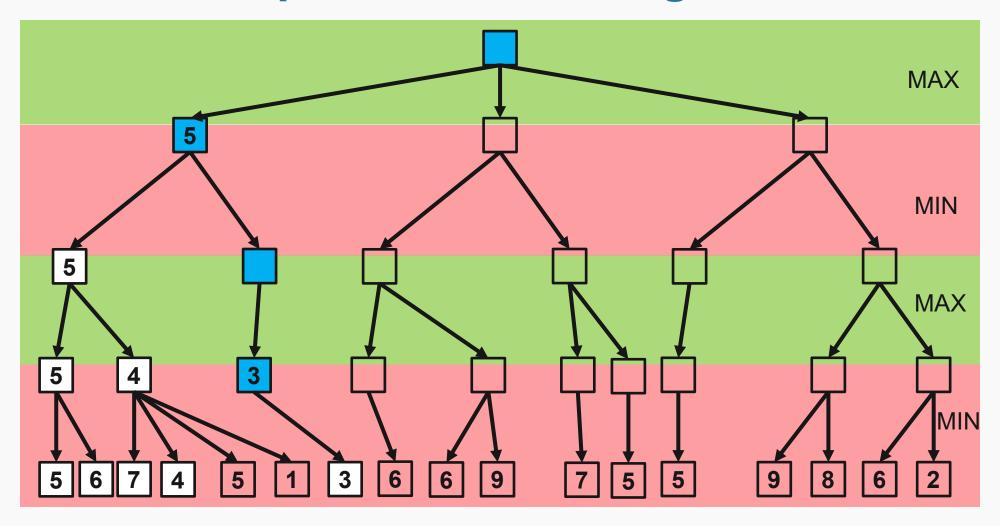




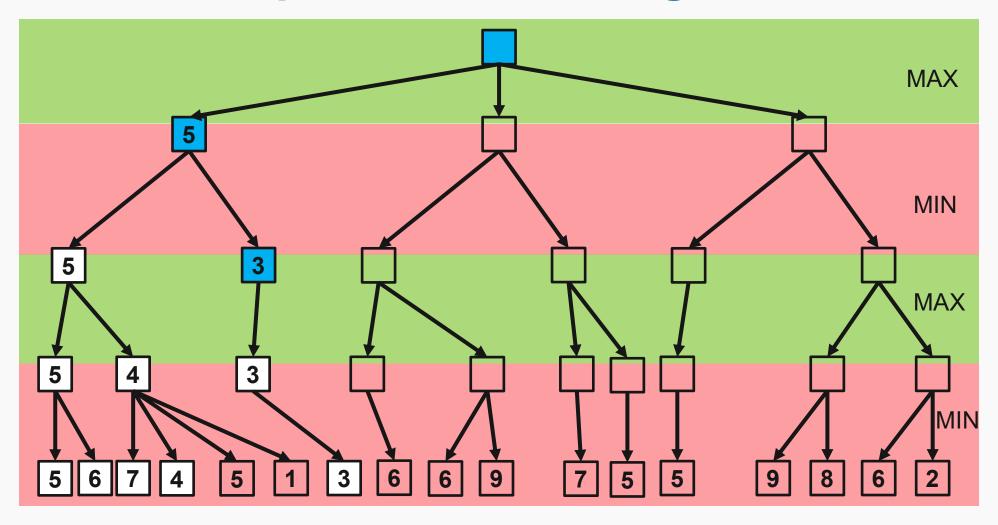




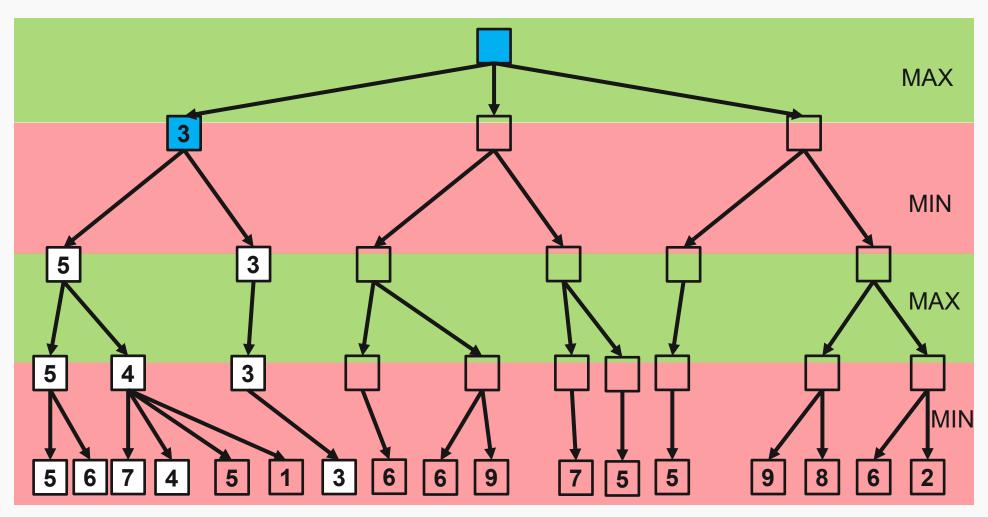




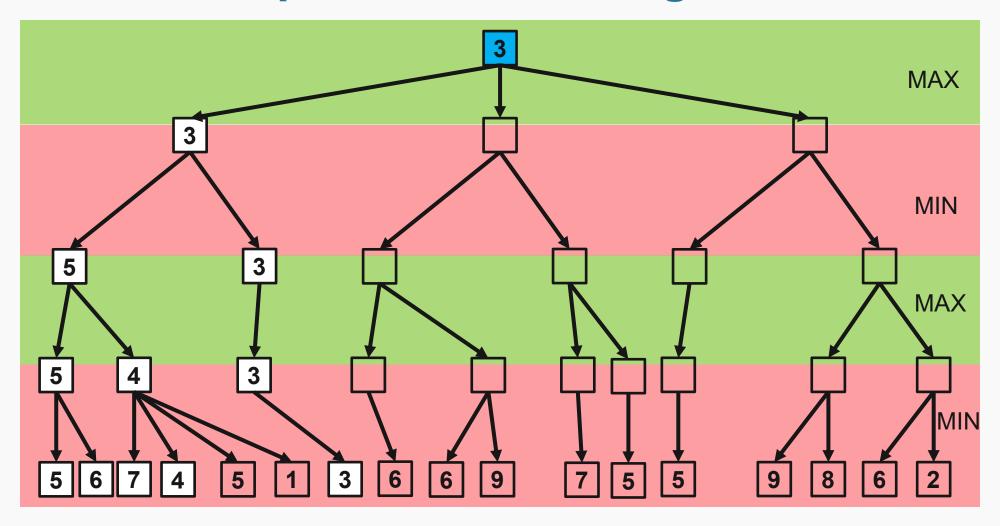




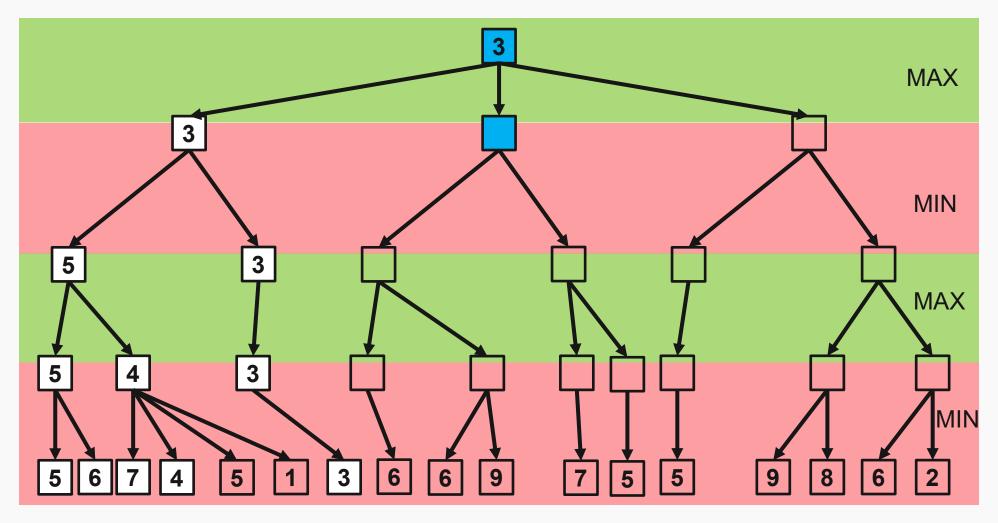




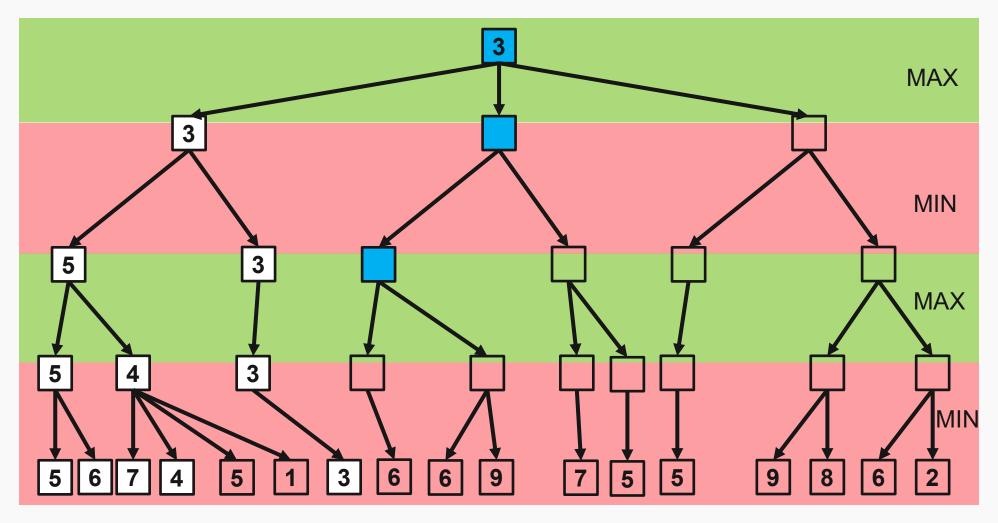




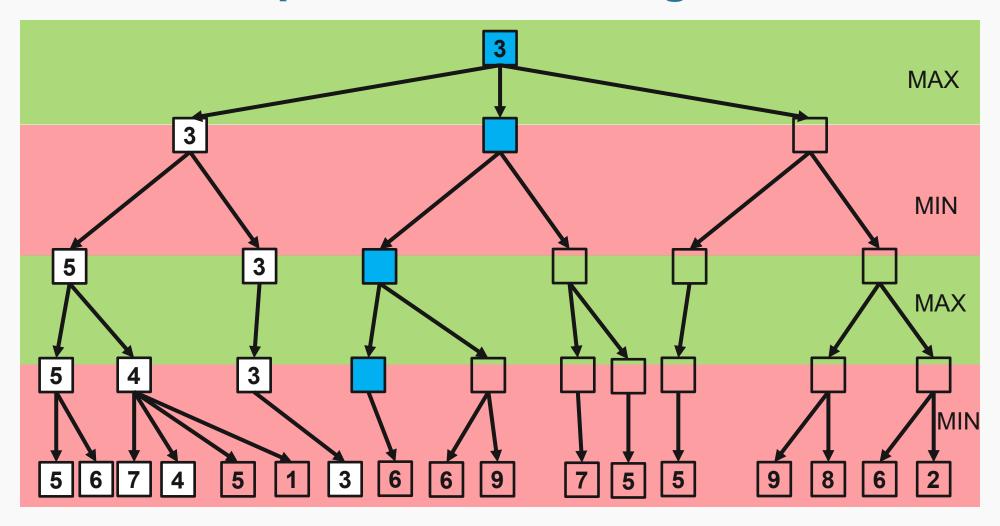




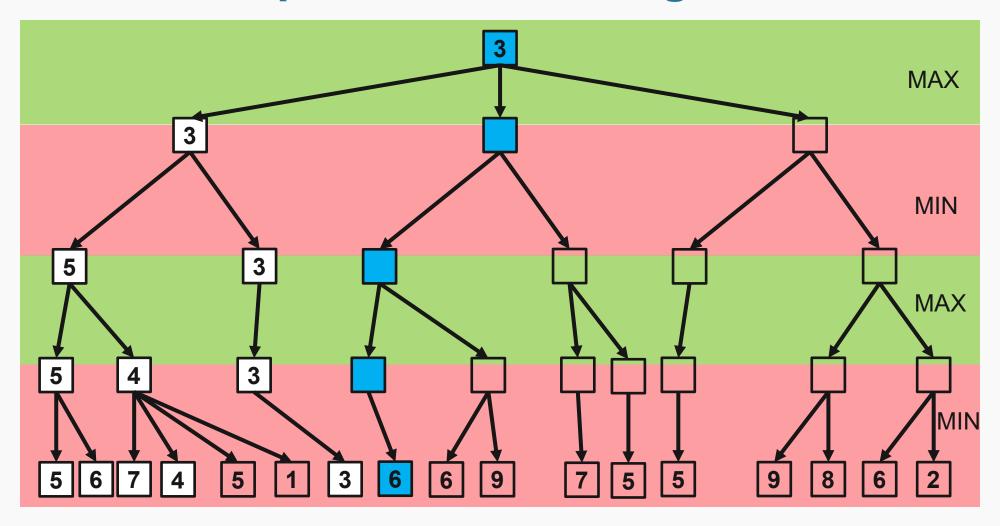




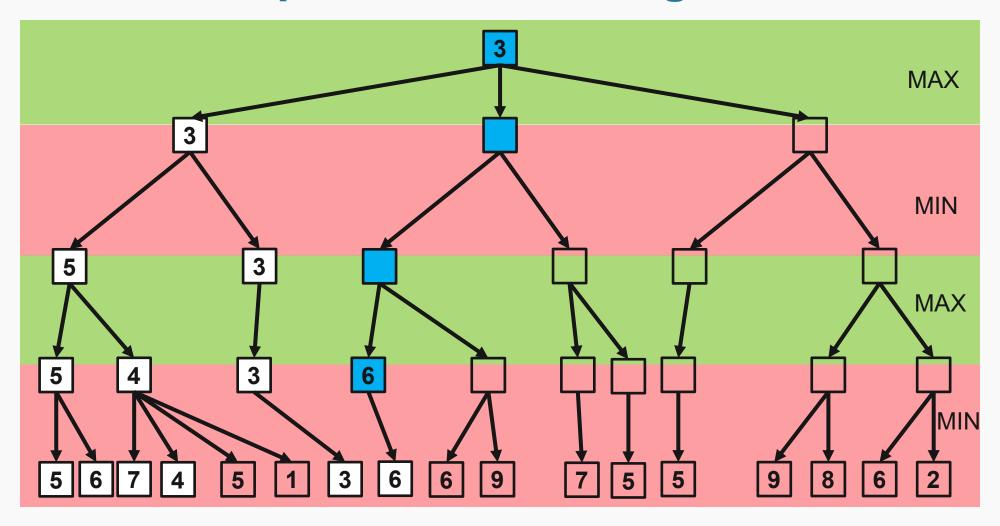




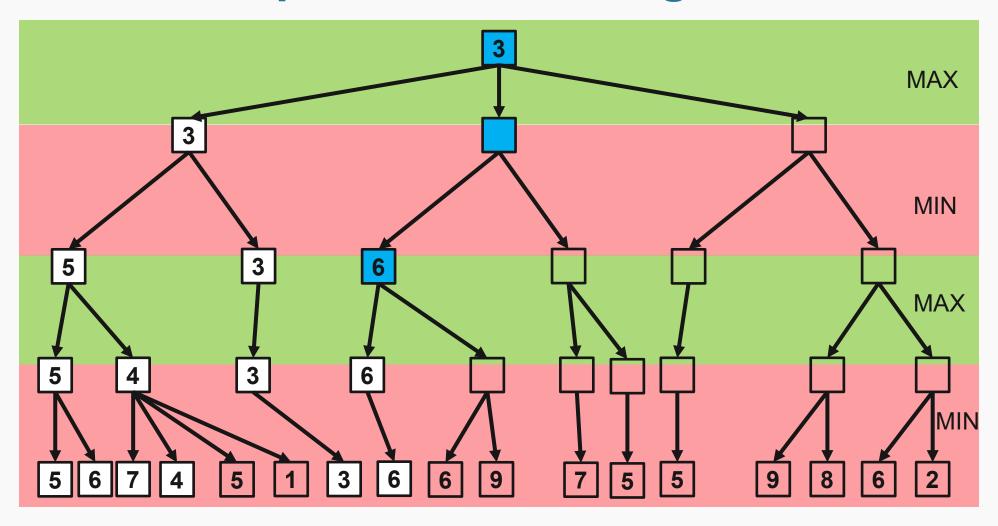




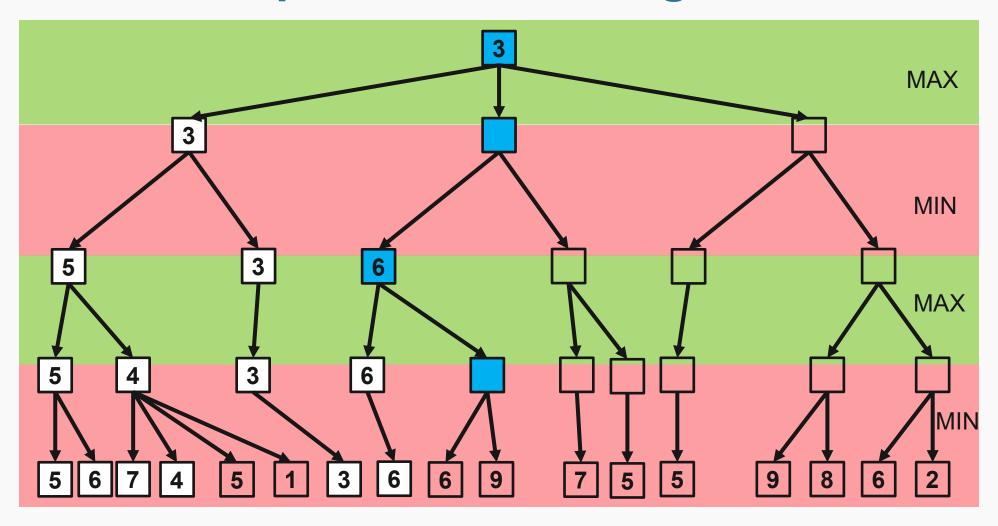




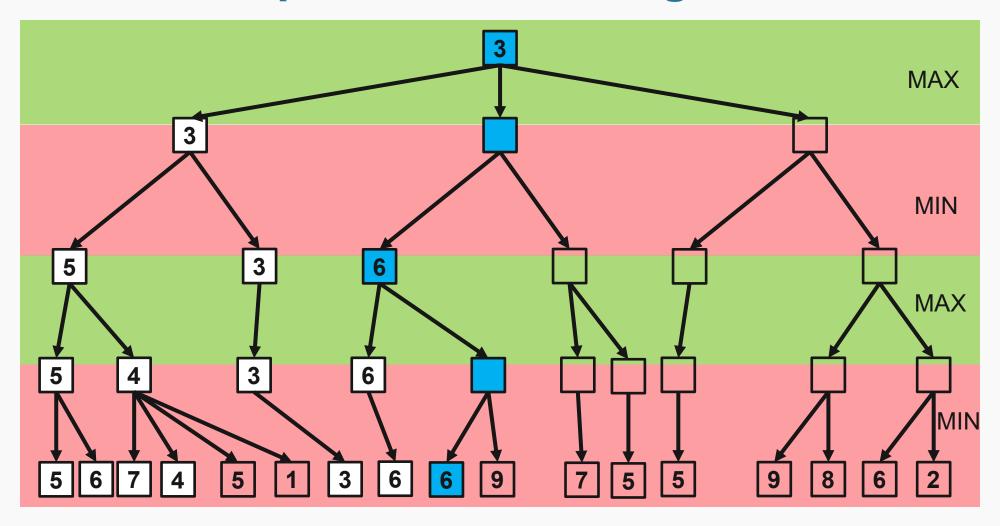




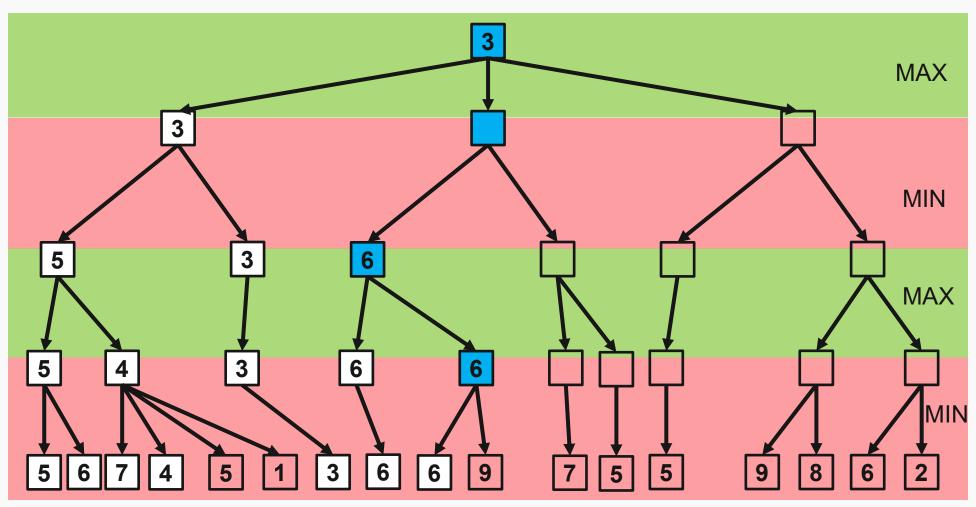






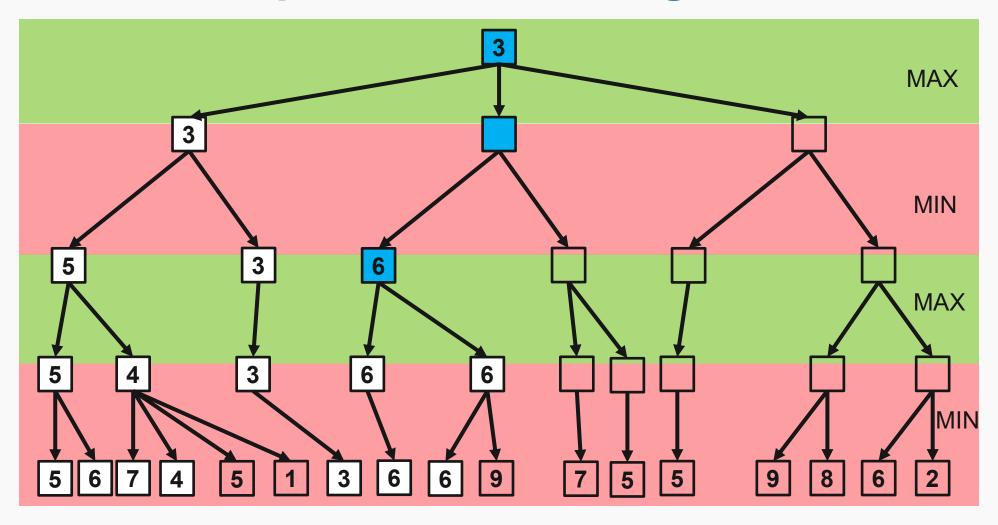




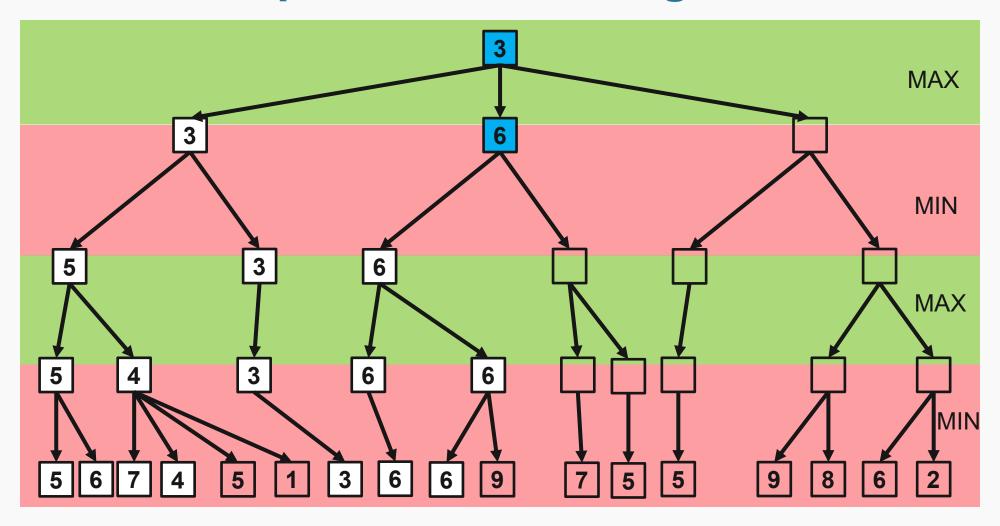


Suntem deja siguri că la acest nivel competitorul va alege 6 sau mai mic. Dar dacă el alege 6 sau mai mic, noi știm siguri că vom alege 6.

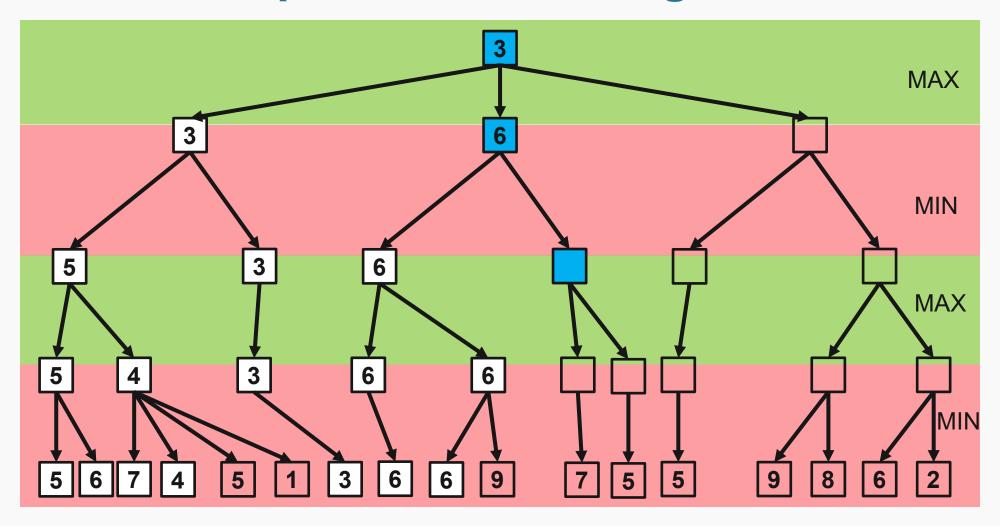




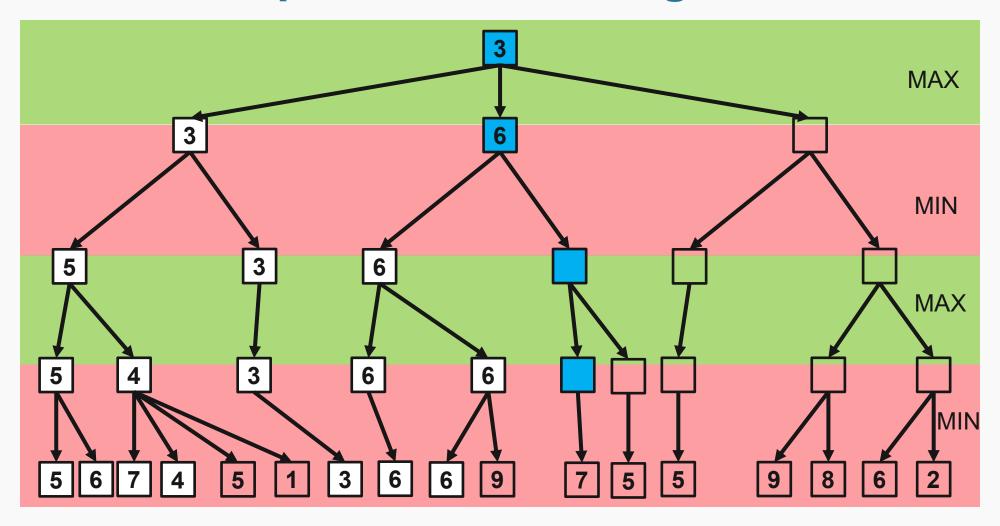




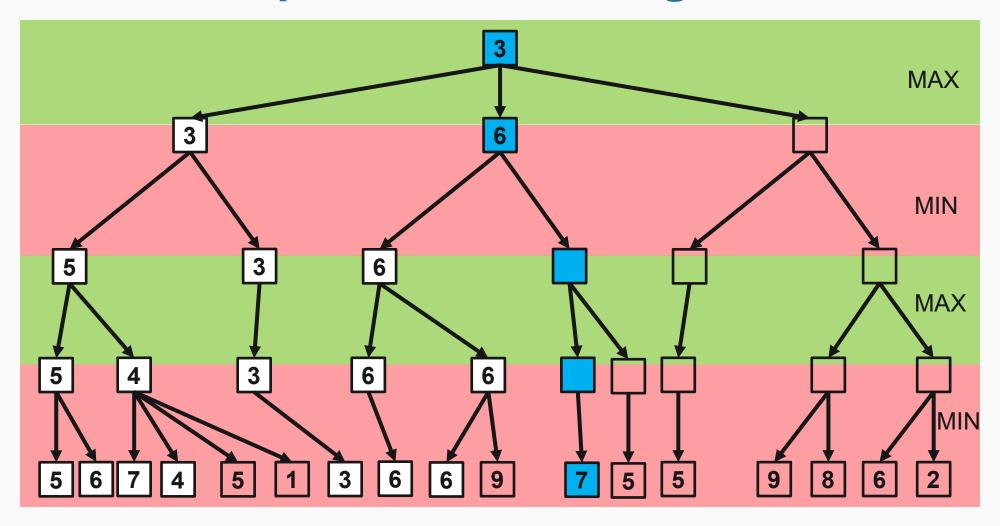




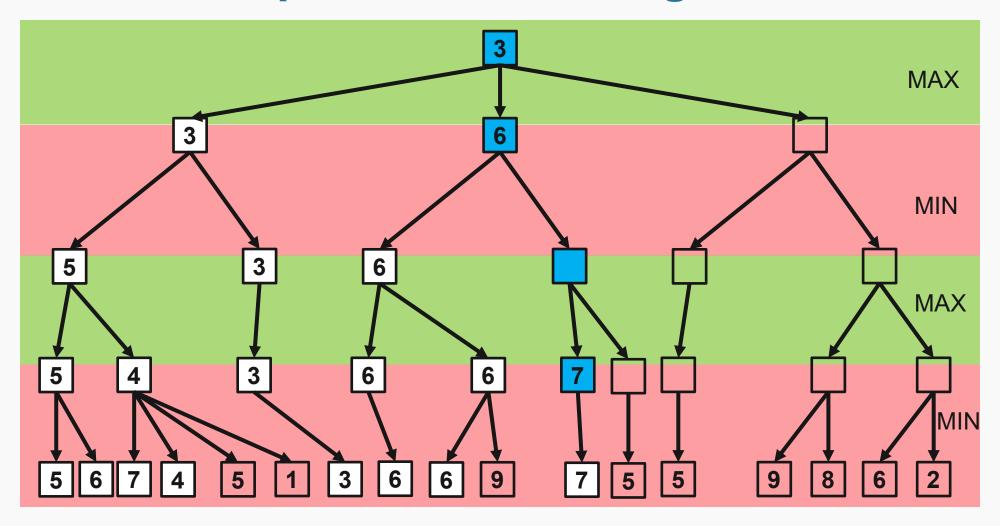




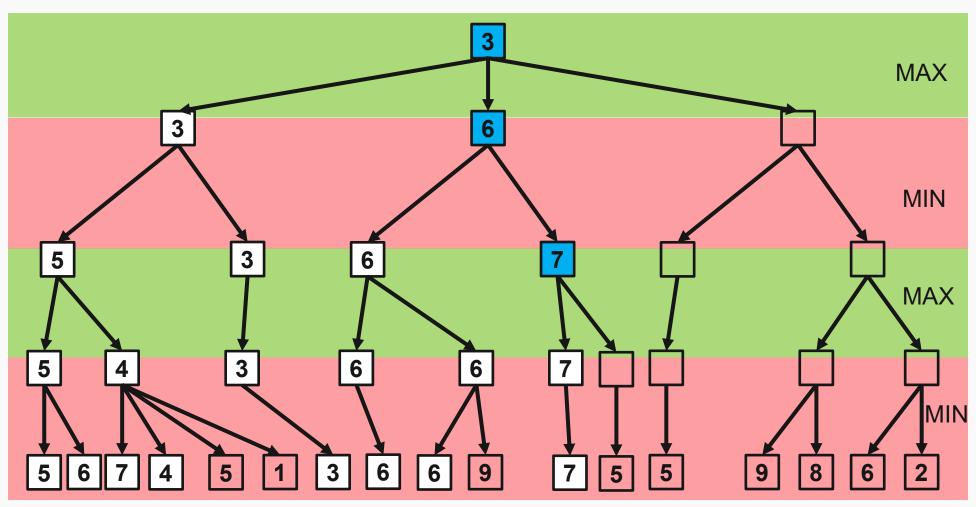






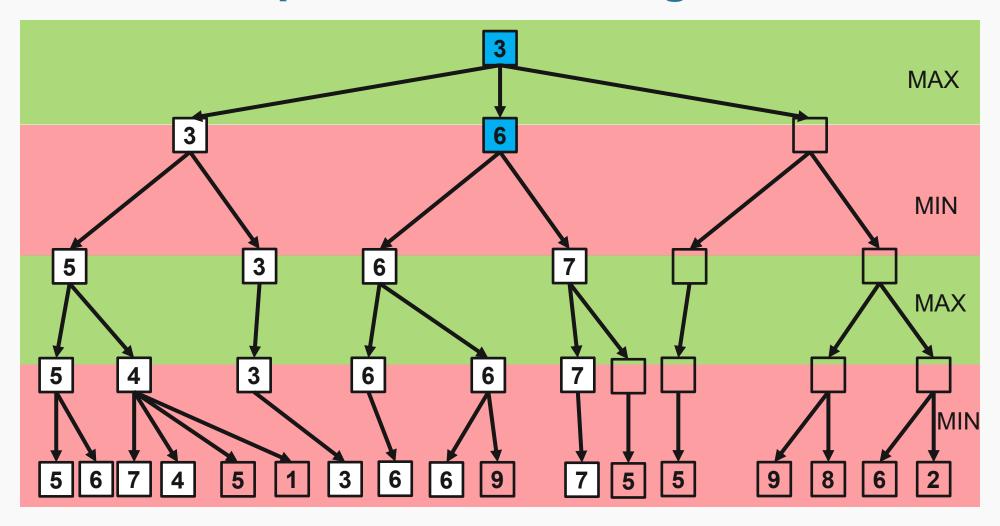




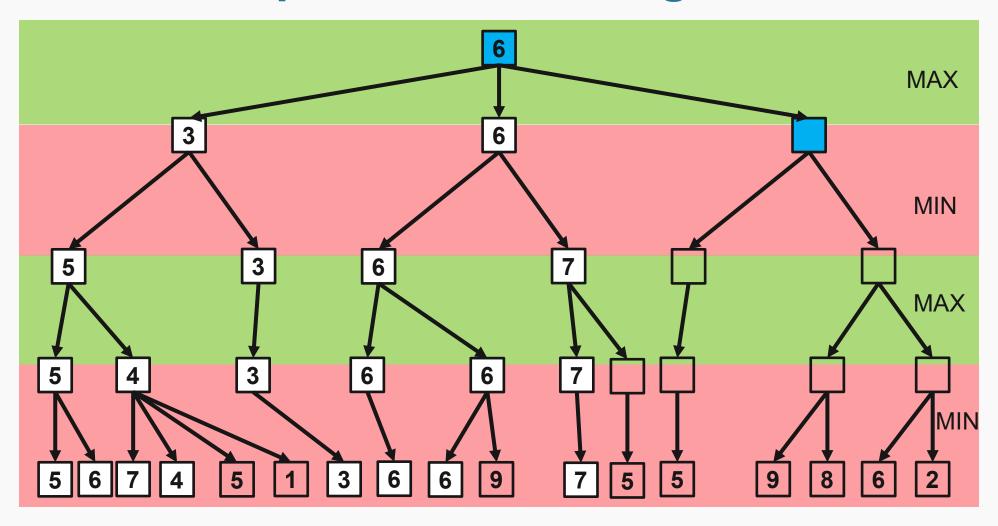


Suntem deja siguri că la acest nivel noi vom alege 7 sau mai mare. Dar dacă noi alegem 7 sau mai mare, știm că mai devreme competitorul alege 6.

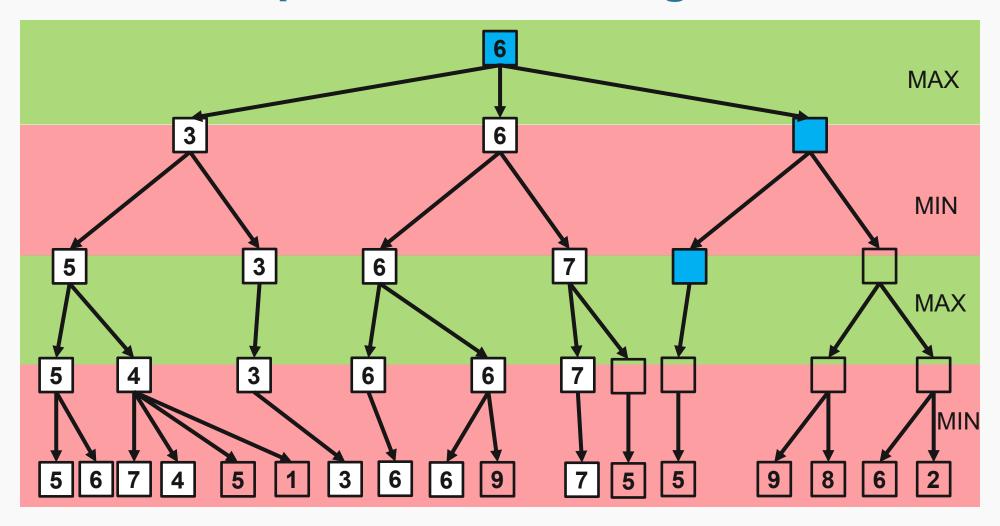




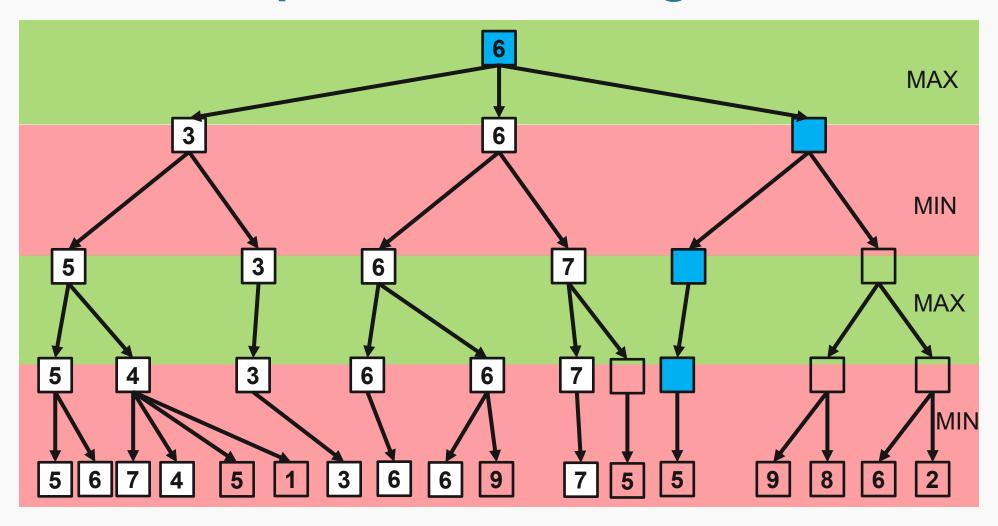




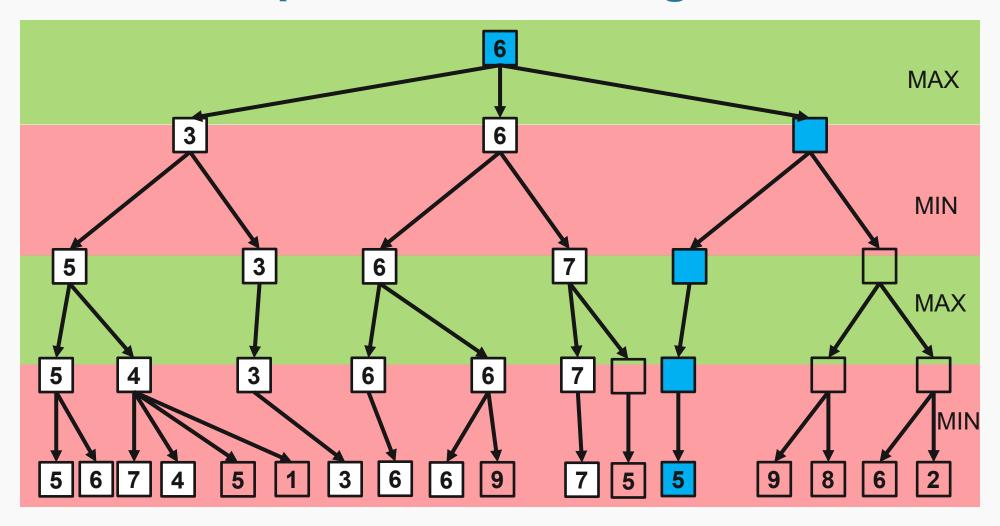




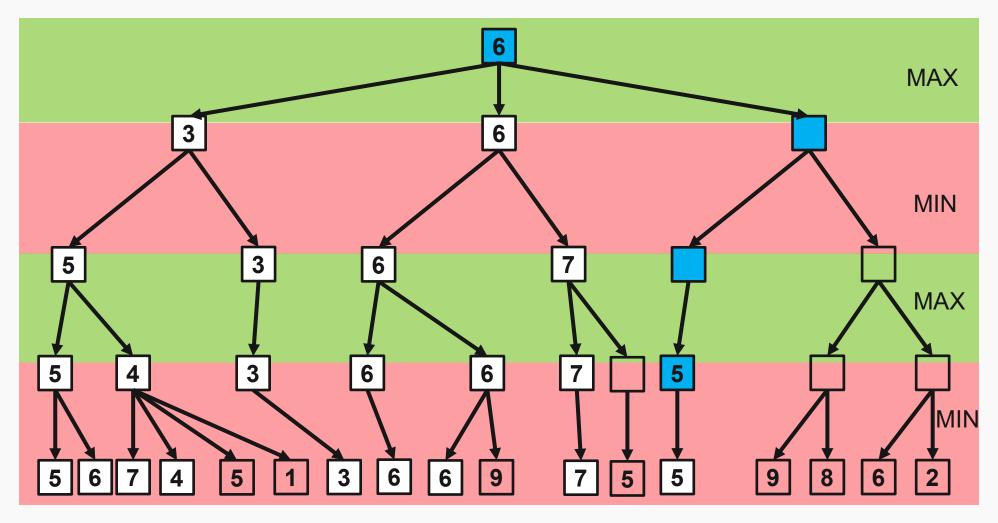




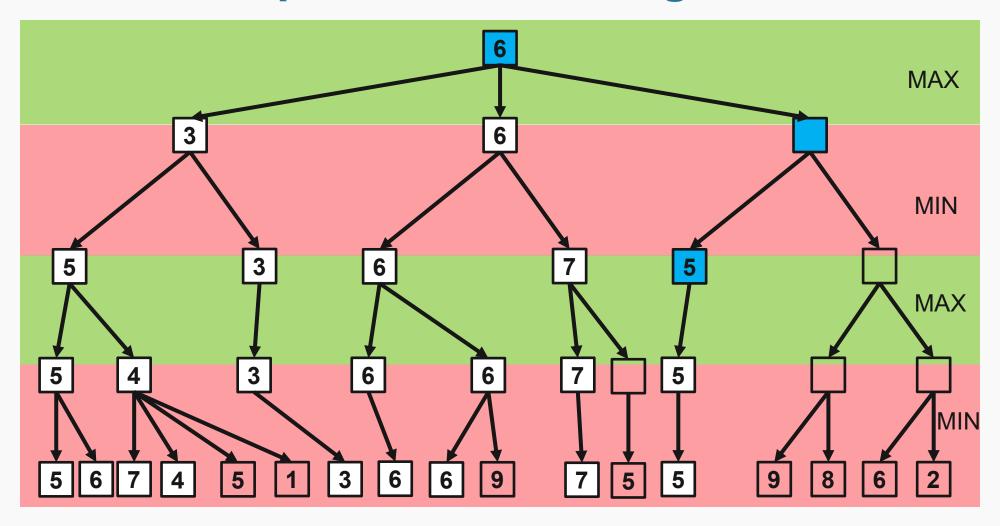




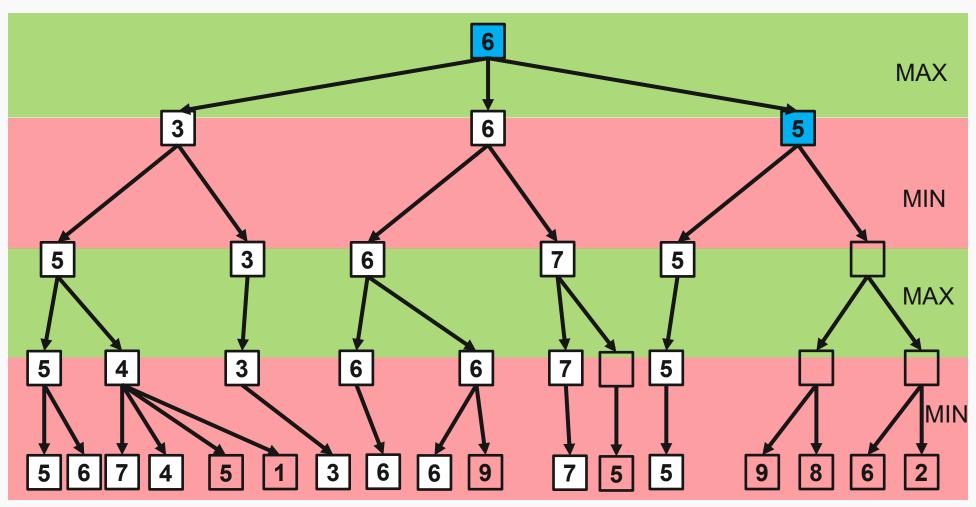






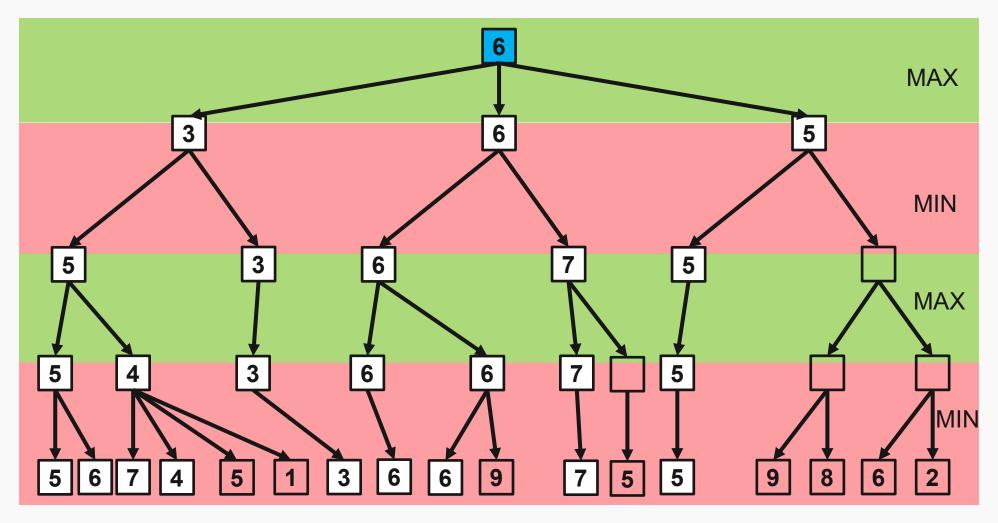




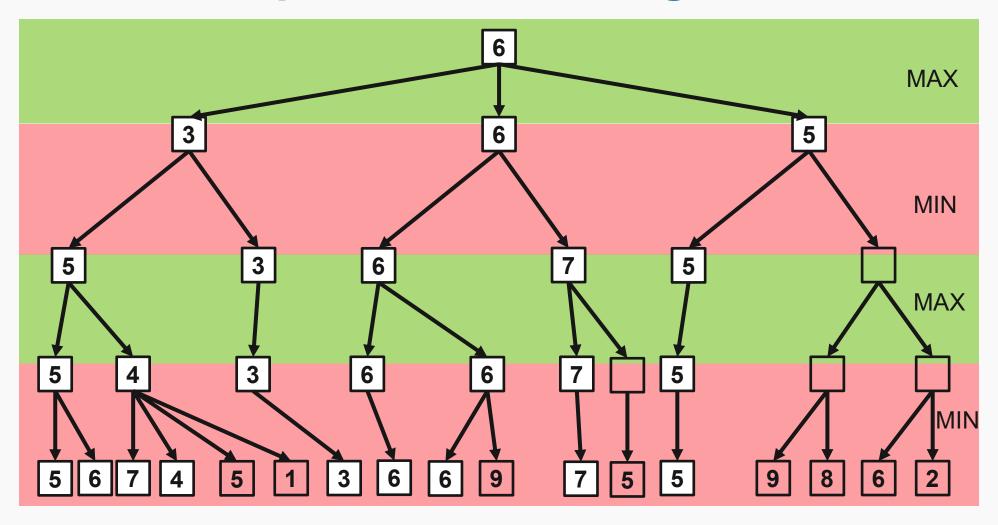


Suntem deja siguri că la acest nivel competitorul va alege 5 sau mai mic. Dar dacă el alege 5 sau mai mic, noi știm siguri că vom alege 6.









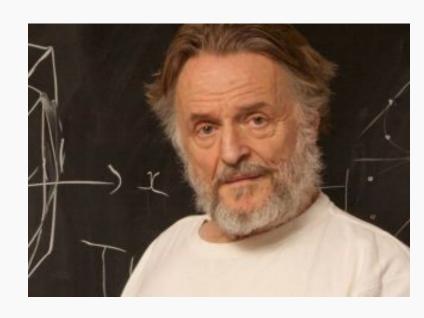


MinMax + AlphaBeta Pruning

```
int alphaBeta(gameNode node, int level, int maxDepth, int alpha, int beta) {
 if (maxDepth = 0 | isEndGame(node))
        return heuristic(node);
 if (level % 2 == maximizingPlayer) {
    int value = -\infty;
   for each (child of node) {
     value = max(value, alphaBeta(child, level + 1, maxDepth - 1, alpha, beta));
      alpha = max(alpha, value);
      if (alpha >= beta)
       break;
   return value;
 } else {
    int value = +∞;
    for each (child of node) {
     value = min(value, alphaBeta(child, level + 1, maxDepth - 1, alpha, beta));
      beta = max(beta, value);
      if (alpha >= beta)
       break;
    return value;
```



John Conway – game of life

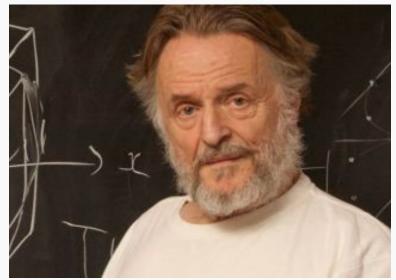


26-Decembrie-1937 -> 11-Aprilie-2020





John Conway – game of life



Celulele unei matrici pot avea valori 0 sau 1

Orice celulă 1 fără vecini devine 0

Orice celulă 1 cu 1 vecin devine 0

Orice celulă 1 cu 2 vecini rămâne 1

Orice celulă 1 cu 3 vecini rămâne 1

Orice celulă 1 cu 4+ vevini devine 0

Orice celulă 0 cu 3 vecini devine 1

26-Decembrie-1937 -> 11-Aprilie-2020

Cause of death: Coronavirus

https://bitstorm.org/gameoflife/



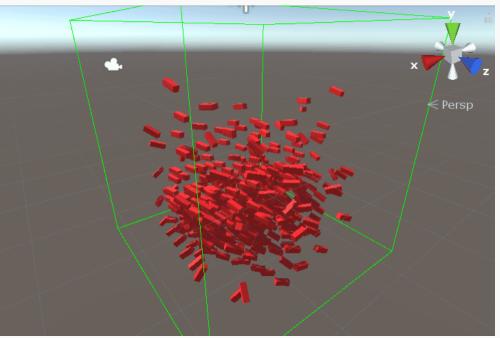
Pentru curioși – John Conway – surreal numbers

- https://en.wikipedia.org/wiki/Surreal_number
- https://www.youtube.com/watch?v=E8kUJL04ELA
- https://www.youtube.com/watch?v=1eAmxgINXrE
- https://www.youtube.com/watch?v=R9Plq-D1gEk



Boids - Craig Reynolds

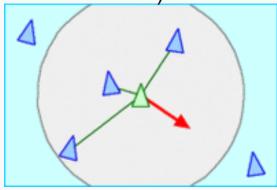




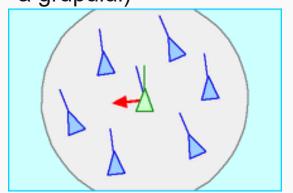


Boids – Reguli simple comportament complex

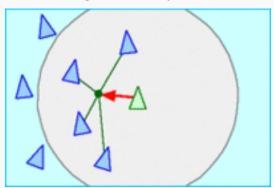
Separare (incearca sa evite coliziuni)



Aliniere (zboara in aceeasi directie cu directia generala a grupului)



Coeziune (sta aproape de centrul grupului)





Further discussion

- Nash equilibrium + Pareto Optimal
 - Prisoner's Dilema
 - Movie: A beautiful mind

Monte Carlo + Las Vegas (random algorithms)