

---

## What this code is about

The C++ file `constant.cpp` solves the system of  $d + 1$  linear equations for the first  $d + 1$  expansion coefficients  $c_m$

$$\mu_n = \sum_{m=0}^d c_m P(n, m) \quad (1)$$

where the matrix  $P(n, m)$  is given by

$$P(n, m) = m! 2^{n-\nu+1} \sum_{k=0}^m \frac{(-2)^k \Gamma(n + k - \nu + 1)}{(k!)^2 (m - k)!}. \quad (2)$$

In the case of the funnel potential,

$$\epsilon_{k+1} = \mu_k = \int_0^\infty x^k \rho(x) dx, \quad k = 0, 1, \dots \quad (3)$$

for  $k = 0, 1, \dots$ , where  $\epsilon_{k+1}$  are the coefficients of the weak-coupling perturbation expansion for the ground-state energy,

$$E(\beta) = -\frac{1}{2} \sum_{k=0}^{\infty} \epsilon_k (-\beta)^k, \quad \epsilon_0 = 1. \quad (4)$$

The file `compile.job` is a SLURM script to compile the code in an HPC and generate an executable.

The file `together.job` is a SLURM script to run the executable in an HPC.