## What this code is about

The C++ code second.cpp computes the second term in equation (3.55)

$$\sum_{k=0}^{\infty} \frac{(-1)^k \mu_{-(2k+2)}}{\beta^k} = \sum_{k=0}^{\left\lfloor \frac{d}{2} \right\rfloor - 1} \frac{(-1)^k}{\beta^k} \left( A_{2k} + \frac{B_{2k}}{B_{2k}} + C_{2k} \right) + \sum_{k=\left\lfloor \frac{d}{2} \right\rfloor}^{\infty} \frac{(-1)^k}{\beta^k} D_{2k}, \quad (1)$$

where  $\lfloor x \rfloor$  is the floor function and the term  $A_k$  is given by

$$B_k = \sum_{m=k+1}^{d} c_m m! \sum_{l=0}^{k} \frac{(-1)^l}{(l!)^2 (m-l)!} \int_0^{\infty} \frac{e^{-x/2}}{x^{k+\nu+1-l}} dx,$$
 (2)

and

$$\int_{0}^{\infty} \frac{e^{-x/2}}{x^{k+\nu+1-l}} dx = \frac{(-1)^{k-l+1} \left(\frac{1}{2}\right)^{k-l+1+\nu} \pi}{\Gamma(k-l+1+\nu) \sin(\pi\nu)}.$$
(3)

The code requires the d+1 numbers  $c_m$ 's as inputs. These are read-in from the file Constant.txt. The code outputs values for for  $\beta = 10^{-5} - 10^{23}, 0.2$  and  $\beta = 4$  and writes to the file SECOND.txt.

The file compile.job is a SLURM script to compile the code in an HPC and generate an executable.

The file together job is a SLURM script to run the executable in an HPC.