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## What this code is about

The `c++` code `function.cpp` computes the highlighted term below appearing in the right-hand side of equation (4.39)

$$f(\kappa) = - \sum_{n=0}^{\infty} \frac{\mu_{-(2n+2)}}{\kappa^{n-1}} - \kappa \Lambda(\kappa) + \frac{i\pi}{2} \kappa^{3/2} \rho\left(\frac{1}{\sqrt{\kappa}}\right), \quad (1)$$

where

$$\Lambda(\kappa) = \frac{\sqrt{\kappa}}{2} \ln(\sqrt{\kappa}) \left( \rho\left(\frac{1}{\sqrt{\kappa}}\right) - \rho\left(-\frac{1}{\sqrt{\kappa}}\right) \right). \quad (2)$$

where

$$\rho(x) = xg(x) = xe^{-x/2} \sum_{m=0}^{\infty} c_m m! \sum_{k=0}^m \frac{(-x)^k}{(k!)^2 (m-k)!}. \quad (3)$$

The code requires the  $d + 1$  numbers  $c_m$ 's as inputs. These are read-in from the file `../Constant/Constants.txt`. The code outputs values for  $\kappa = 10^{-5} - 10^{23}$ , 0.2 and  $\kappa = 4$  and writes to the file `../results/FIFTH.txt`.

The file `run.sh` encapsulates commands to build and run the application using the `CMakeLists.txt` on a local machine running on Ubuntu 24.04.