## What this code is about

The c++ code function.cpp computes the second term in the right-hand side of equation (4.20) in the paper,

$$f(\beta) = \sum_{k=0}^{\infty} \frac{(-1)^k}{\beta^{k-1}} \mu_{-(2k+2)} + \frac{\beta \Delta(\beta)}{\beta}.$$
 (1)

where

$$\Delta(\beta) = \frac{\pi\sqrt{\beta}}{4} \left( \rho\left(\frac{i}{\sqrt{\beta}}\right) + \rho\left(\frac{-i}{\sqrt{\beta}}\right) \right) + \frac{\sqrt{\beta}\ln\beta}{4i} \left( \rho\left(\frac{i}{\sqrt{\beta}}\right) - \rho\left(\frac{-i}{\sqrt{\beta}}\right) \right), \tag{2}$$

and

$$\rho(x) = xe^{-x/2} \sum_{m=0}^{d} c_m m! \sum_{k=0}^{m} \frac{(-x)^k}{(k!)^2 (m-k)!}.$$
 (3)

The code requires the d+1 numbers  $c_m$ 's as inputs. These are read-in from the file ../Constant/Constants.txt. The code outputs values for for  $\beta = 10^{-5} - 10^{23}, 0.2$  and  $\beta = 4$  and writes to the file ../results/FIFTH.txt.

The file run.sh encapsulates commands to build and run the application using the CMakeLists.txt on local machine running on Ubuntu 24.04.