

CIA62020 - DIA 05 DO CURSO DE CÁLCULO

DERIVADA

CIA62020 · DIA 05 DO CURSO DE CÁLCULO

DERIVADA - Taxa de variação
de $f(x)$

Sec 1 Sec 2
 $\in \mathbb{R}$

teoria teoria

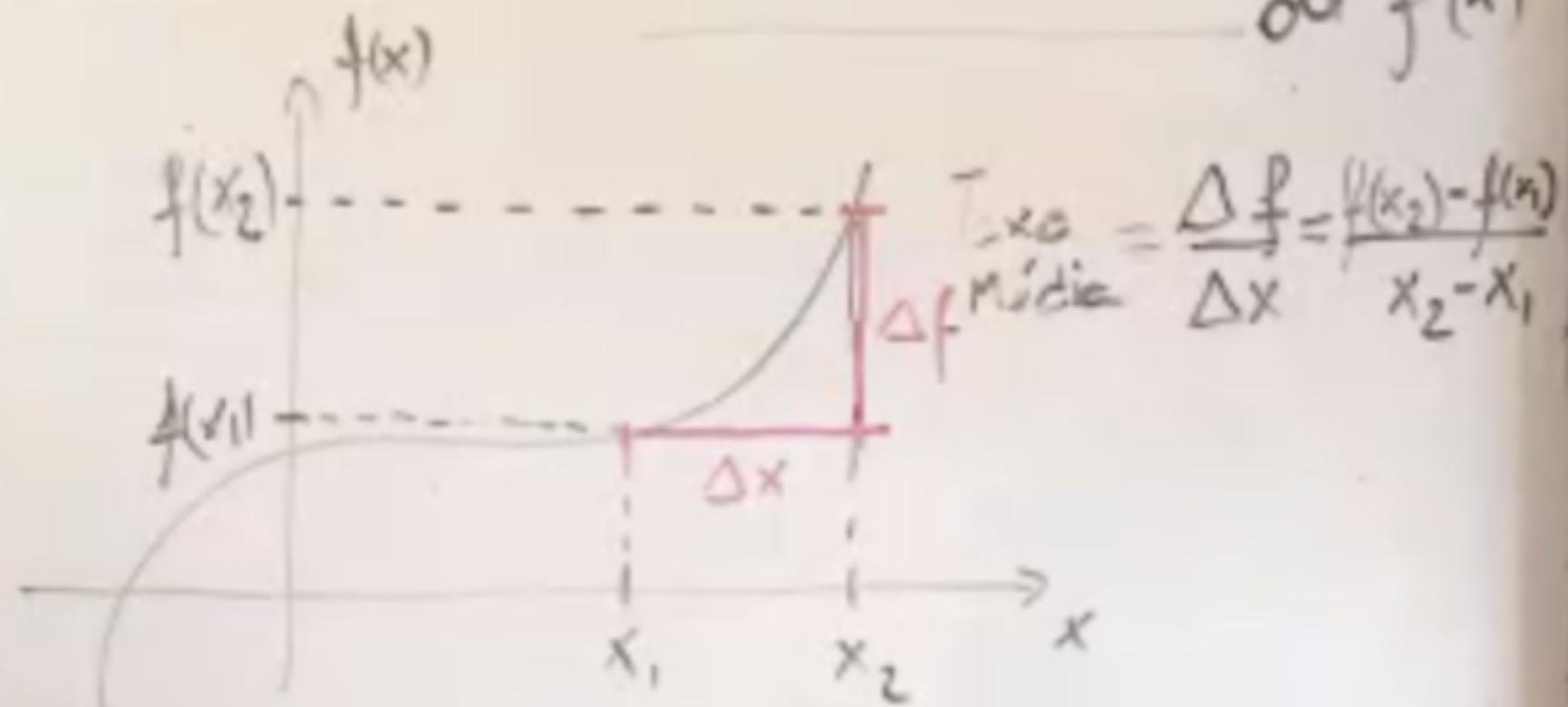
Sec 3 | $\cancel{S_{\text{ex}}^4}$
T | $\cancel{S_{\text{ex}}^4}$
ISh T

Exercícios
em grupo

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DERIVADA - Taxa de variação
de $f(x)$

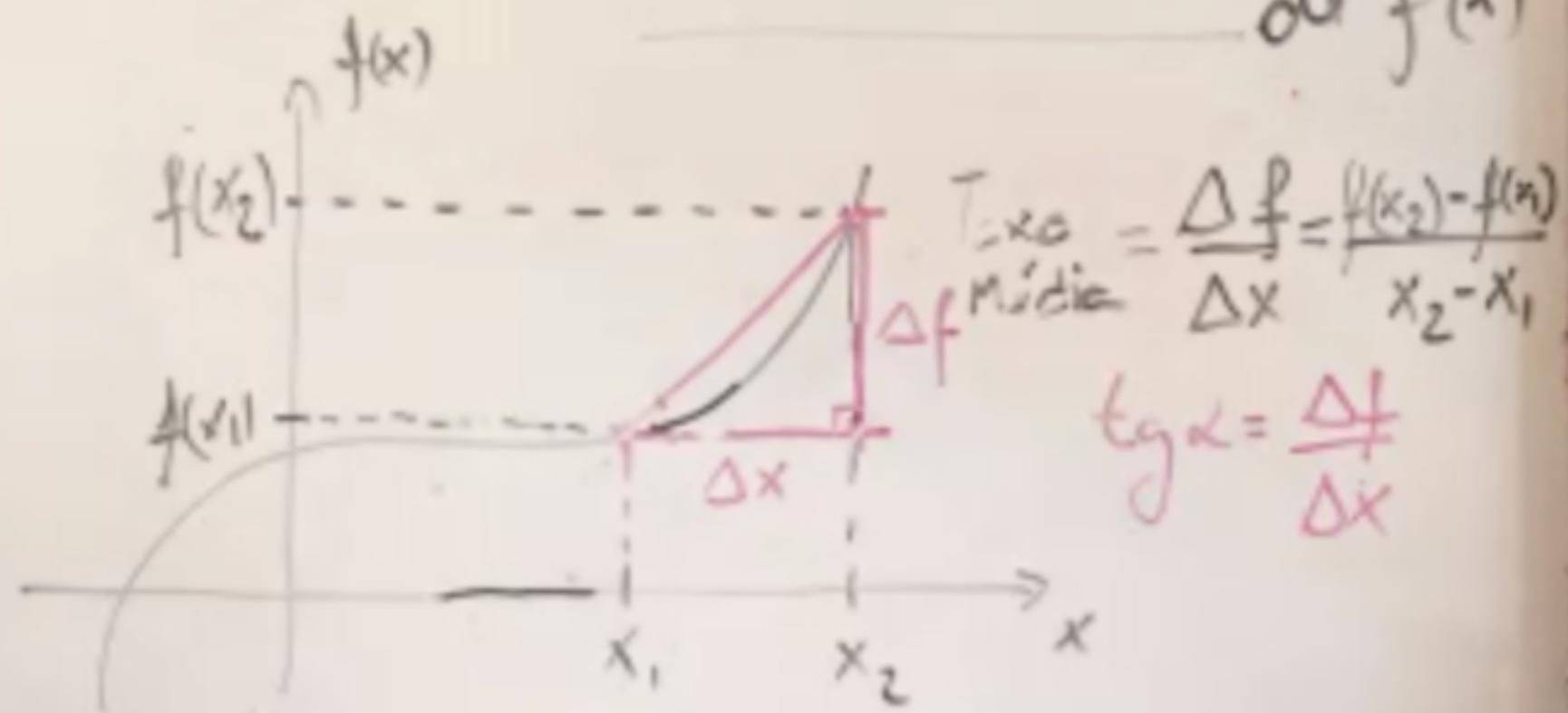


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DERIVADA - Taxa de variação

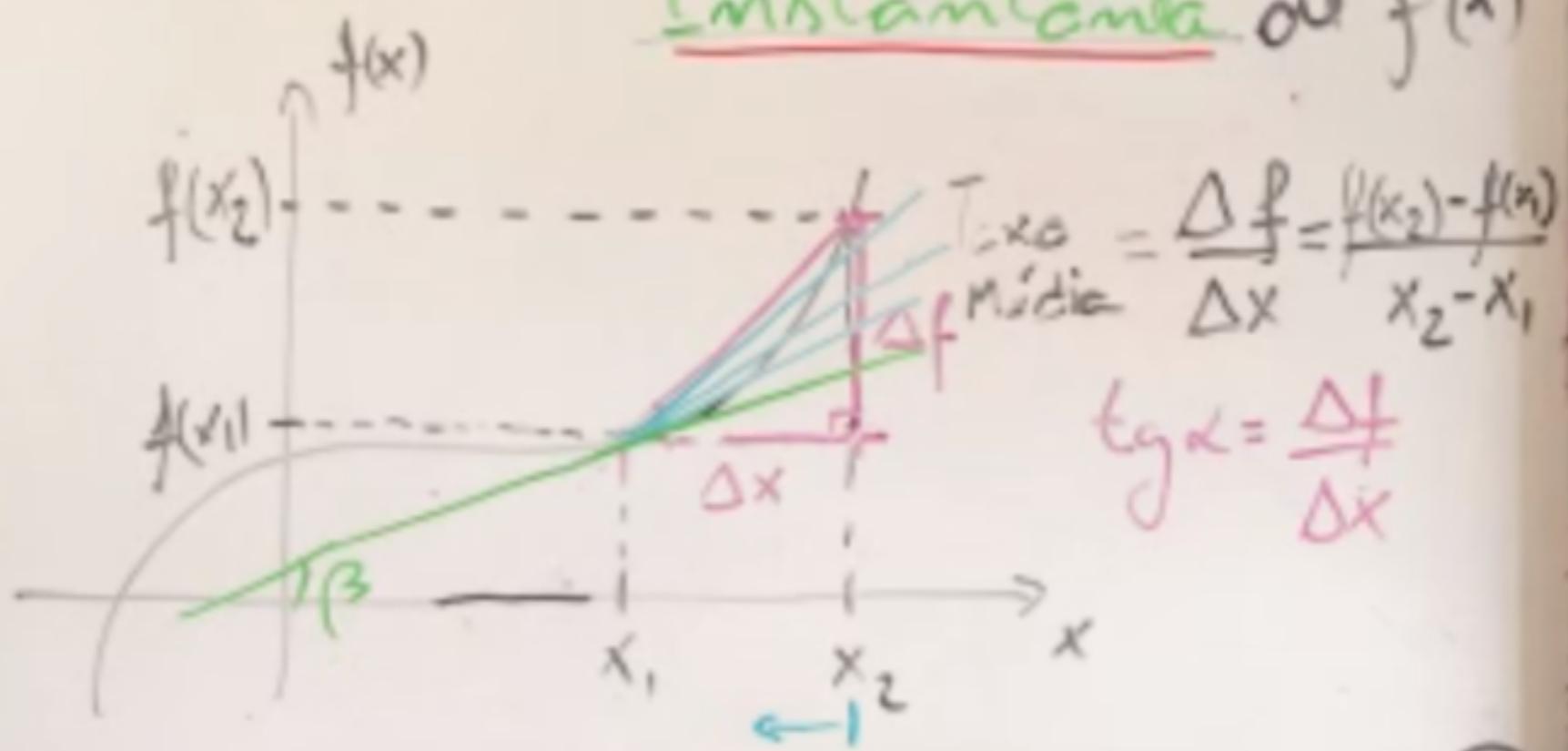
de $f(x)$



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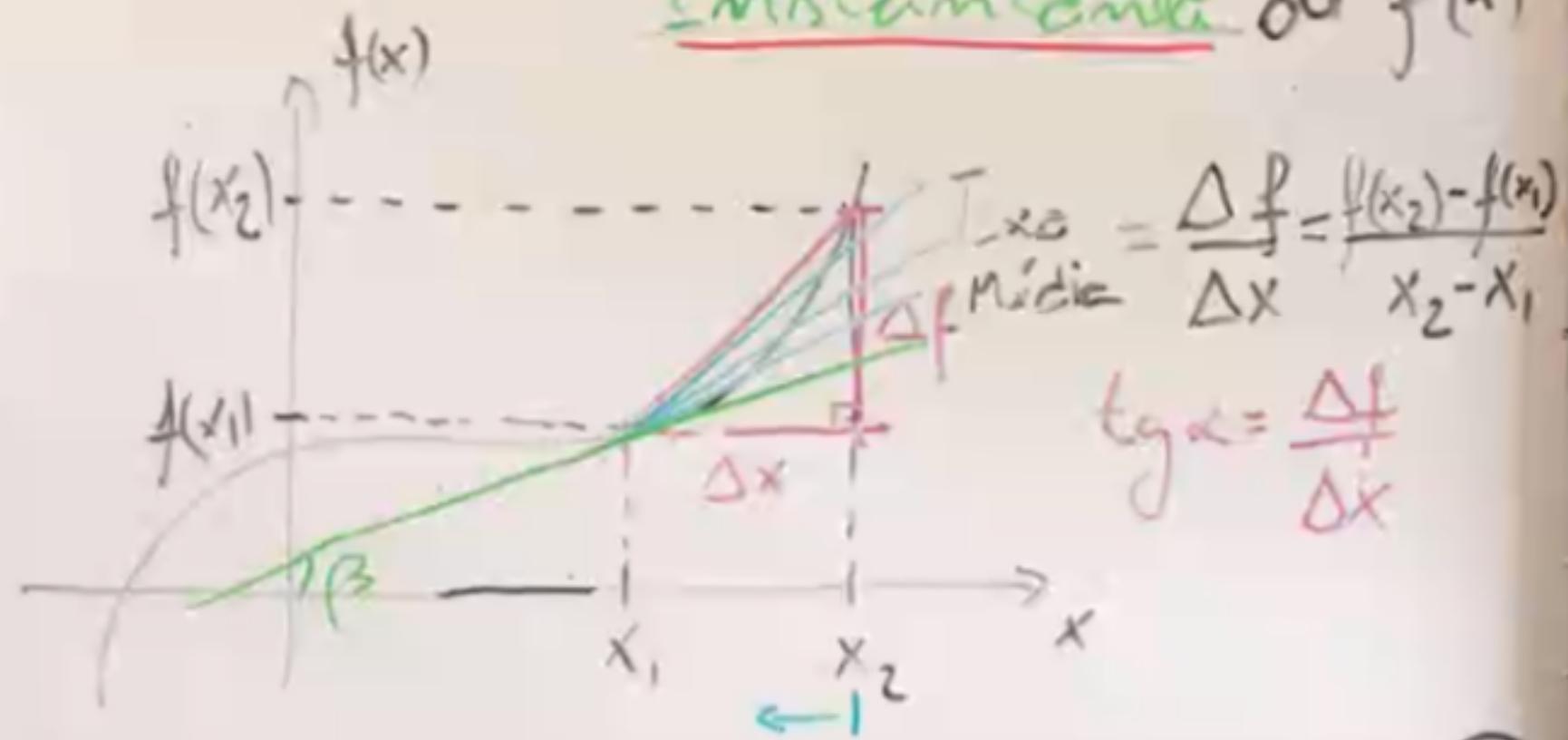
DERIVADA - Taxa de variação
Instantânea de $f(x)$



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CIA6 2020 - DIAS DO CURSO DE CÁLCULO

DERIVADA - Taxa de variação instantânea de $f(x)$

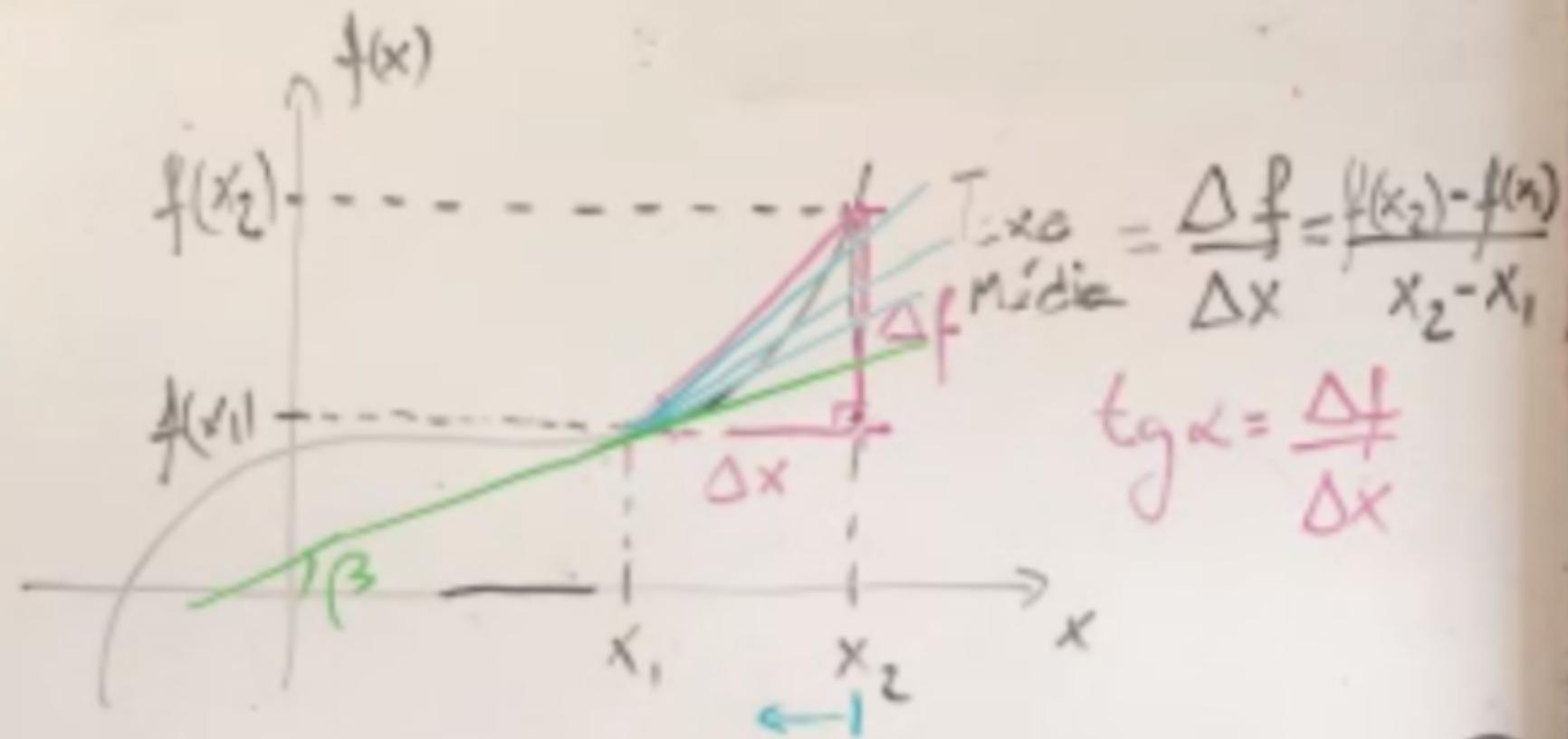


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$$\frac{df(x_1)}{dx} = f'(x_1) \equiv \lim_{x_2 \rightarrow x_1} \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \lim_{\Delta x \rightarrow 0} \frac{\Delta f}{\Delta x}$$

\downarrow

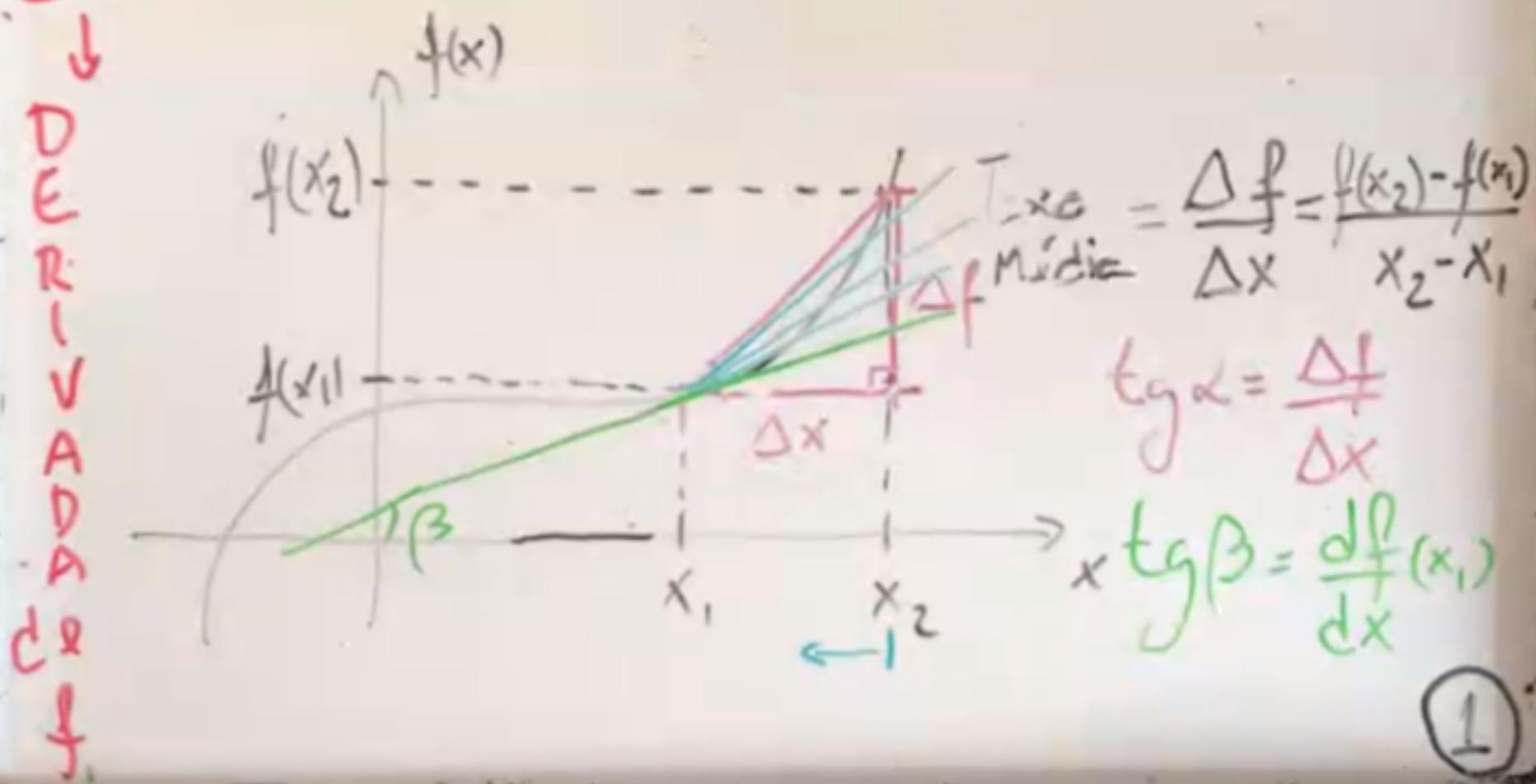
DERIVADA de f



$$\text{Tg } \alpha = \frac{\Delta f}{\Delta x}$$

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$$\frac{df(x_1)}{dx} = f'(x_1) \equiv \lim_{x_2 \rightarrow x_1} \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \lim_{\Delta x \rightarrow 0} \frac{\Delta f}{\Delta x}$$



$$\frac{df(x_1)}{dx} = f'(x_1) \equiv \lim_{x_2 \rightarrow x_1} \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \lim_{\Delta x \rightarrow 0} \frac{\Delta f}{\Delta x}$$

$$F_R = m a = m \frac{d\vec{v}}{dt} =$$

$$-\cancel{m \ddot{v}} = m \cancel{\frac{d\vec{v}}{dt}} = m \frac{d}{dt} \left(\frac{d\vec{s}}{dt} \right) =$$

$$= m \frac{d^2\vec{s}}{dt^2}$$

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REPERTÓRIO DE DERIVADAS

1) $f(x) = ax + b$

$$f'(x) = \frac{df}{dx}(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} =$$

$$= \lim_{h \rightarrow 0} \frac{a(x+h) + b - ax - b}{h} = \lim_{h \rightarrow 0} \frac{ah}{h}$$

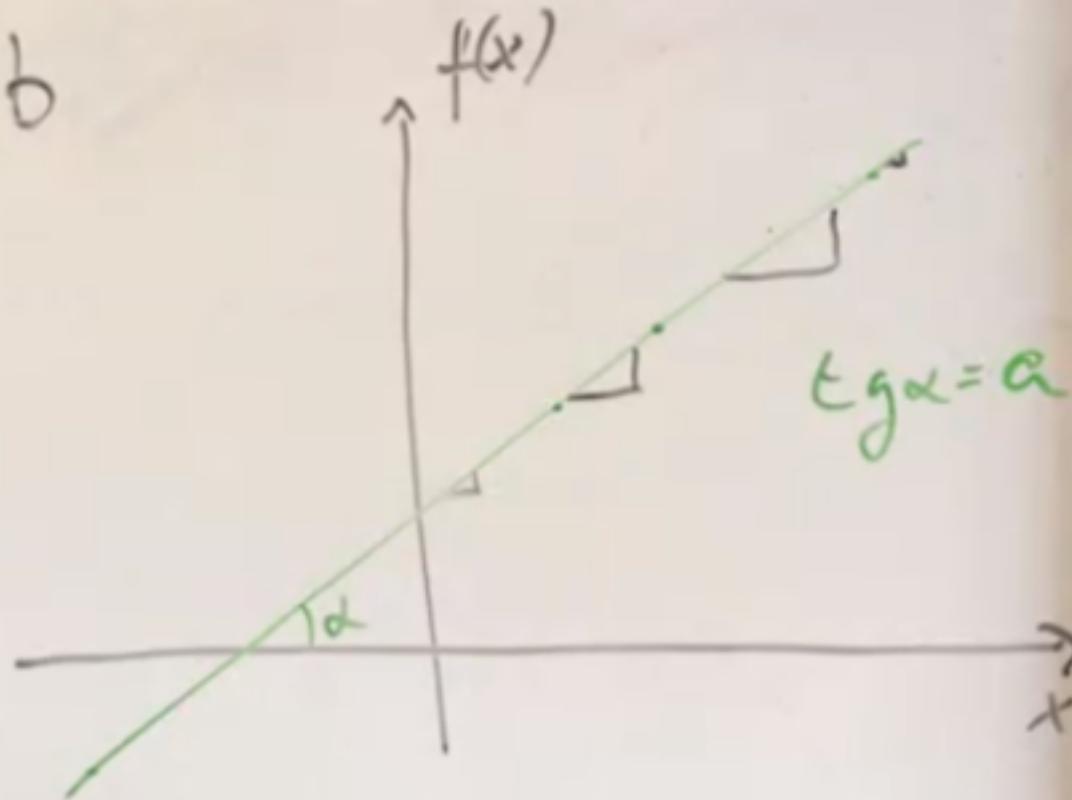
$$= \lim_{h \rightarrow 0} \frac{ah}{h} = \lim_{h \rightarrow 0} a = a$$

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REPERTÓRIO DE DERIVADAS

1) $f(x) = ax + b$

$$f'(x) = \frac{df}{dx} = a$$



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REPERTÓRIO DE DERIVADAS

$$2) f(x) = ax^2 + bx + c$$

$$f'(x) = \frac{df}{dx}(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} =$$

$$= \lim_{h \rightarrow 0} \frac{a(x+h)^2 + b(x+h) + c - ax^2 - bx - c}{h} =$$

$$= \lim_{h \rightarrow 0} \frac{ax^2 + 2axh + ah^2 + bx + bh - ax^2 - bx}{h} =$$

$$= \lim_{h \rightarrow 0} \frac{2axh + ah^2 + bh}{h} = \lim_{h \rightarrow 0} (2ax + b + ah) =$$

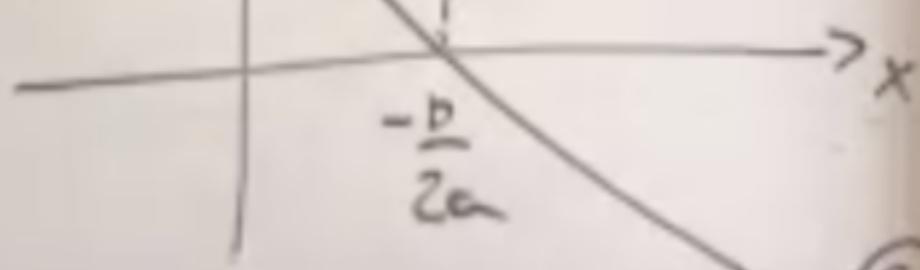
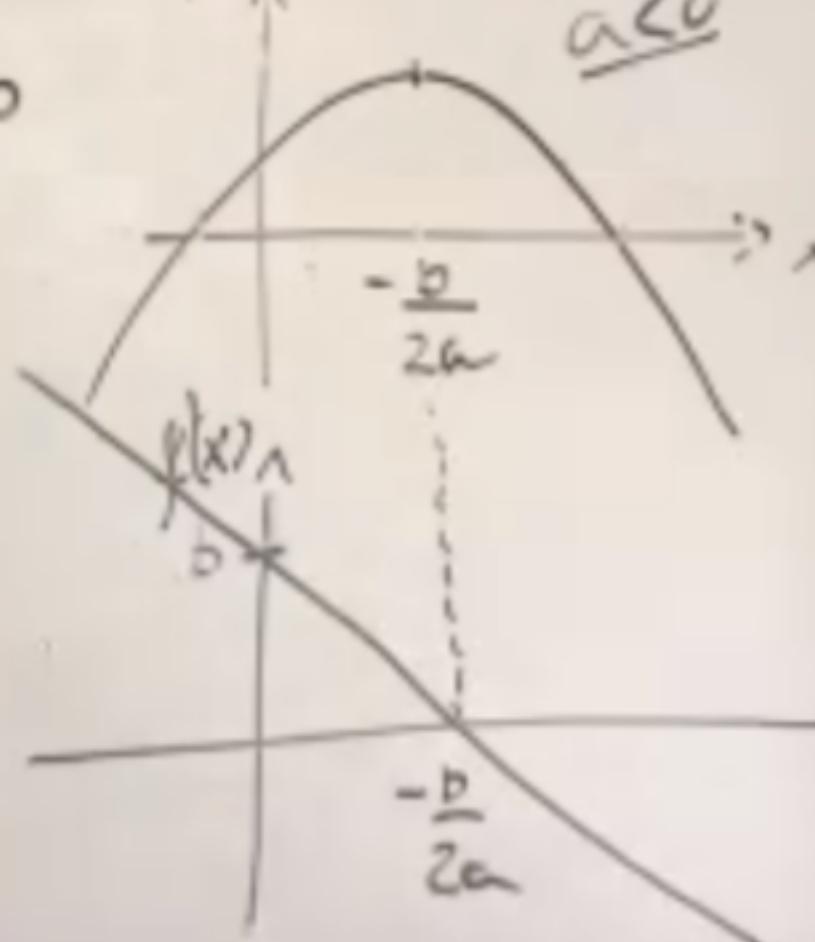
$$= 2ax + b$$

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REPERTÓRIO DE DERIVADAS

2) $f(x) = ax^2 + bx + c$ $f(x)$

$$f'(x) = \frac{d}{dx} f(x) = 2ax + b$$

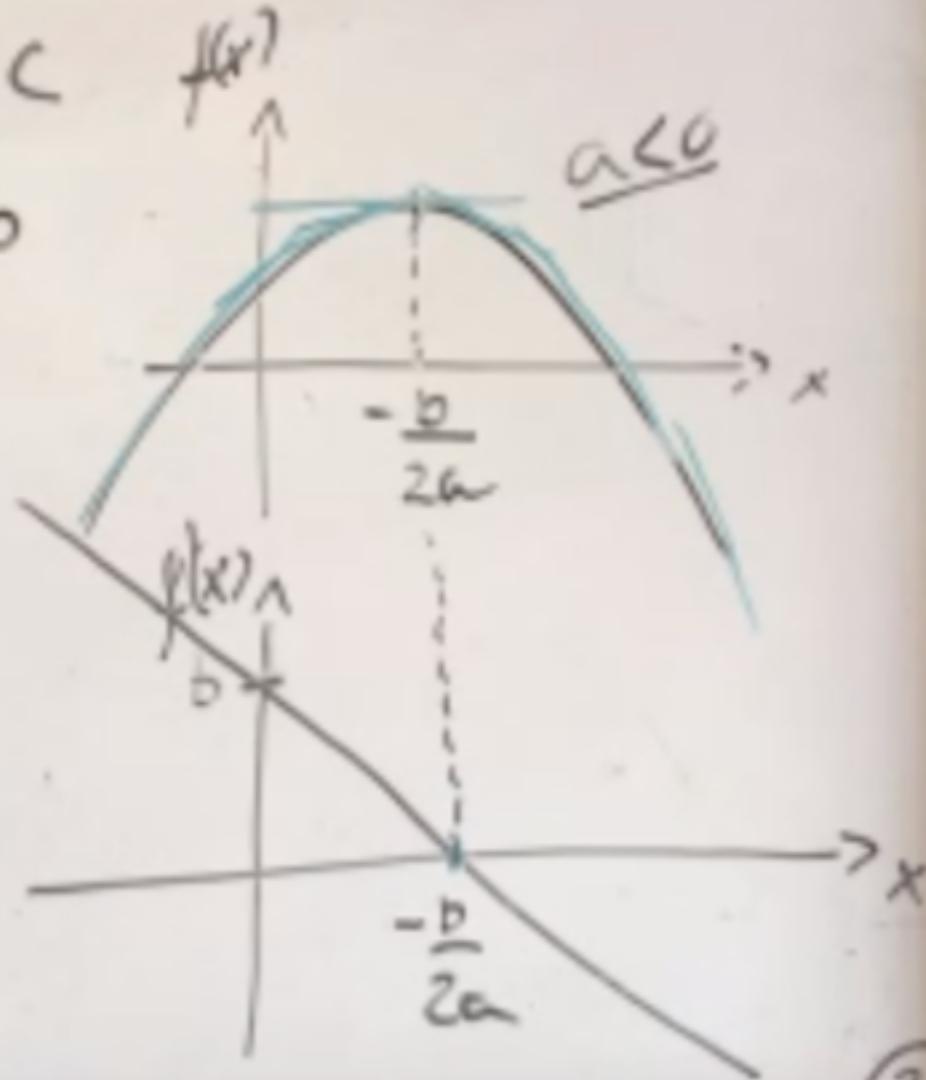


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REPERTÓRIO DE DERIVADAS

2) $f(x) = ax^2 + bx + c$ $f'(x)$

$$f'(x) = \frac{d}{dx} f(x) = 2ax + b$$



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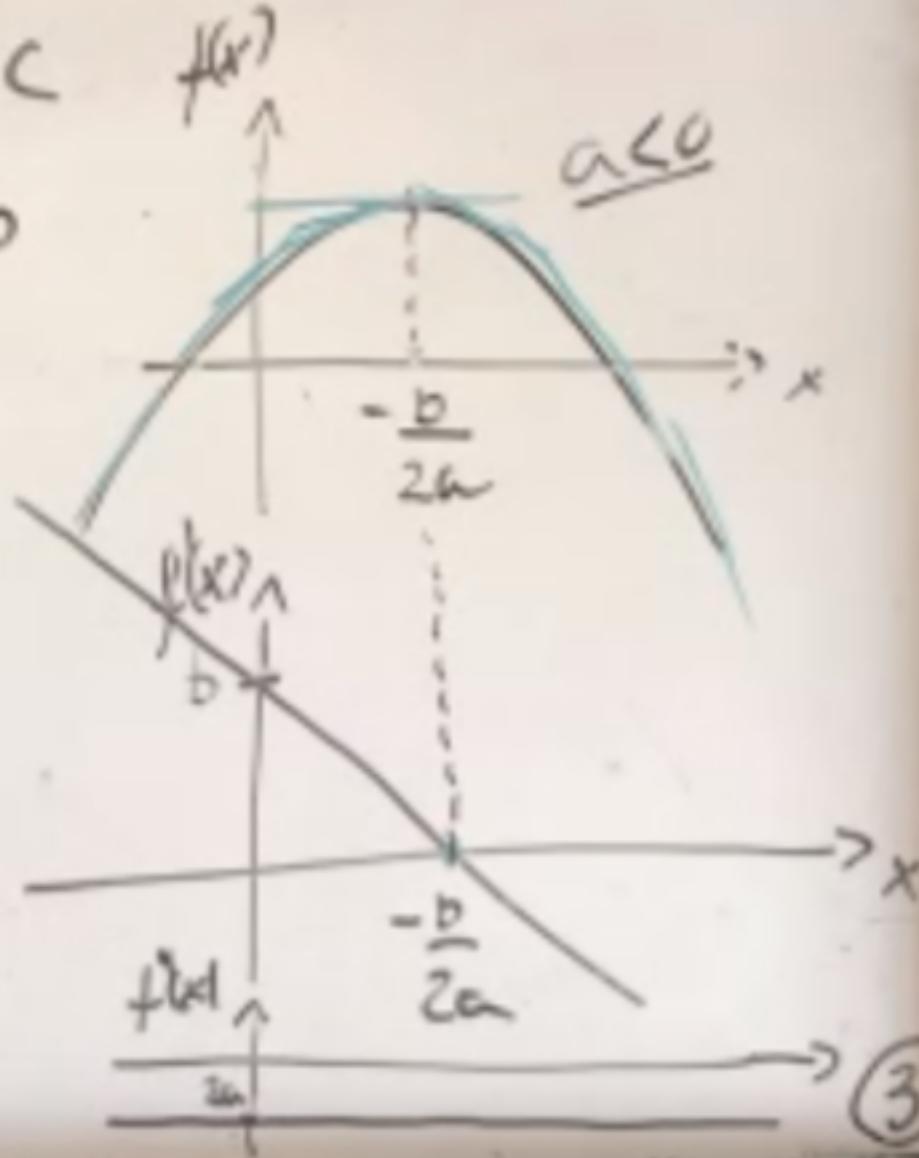
REPERTÓRIO DE DERIVADAS

2) $f(x) = ax^2 + bx + c$ $f(x)$

$$f'(x) = \frac{d}{dx} f(x) = 2ax + b$$

$$\frac{d}{dx} \left(\frac{d}{dx} f(x) \right) = 2a$$

$$f''(x) = \frac{d^2}{dx^2} f(x) = 2a$$



REPERTÓRIO DE DERIVADAS

$$2) f(x) = ax^2 + bx + c \quad s(t) = -\frac{g}{2}t^2 + v_0 t + s_0$$

$$f'(x) = \frac{d}{dx} f(x) = 2ax + b \quad v(t) = \frac{ds(t)}{dt} = -gt + v_0$$

$$\frac{d}{dx} \left(\frac{d}{dx} f(x) \right) = 2a$$

$$a(t) = \frac{dv(t)}{dt} = \frac{ds(t)}{dt^2} = -g$$

$$f''(x) = \frac{d^2}{dx^2} f(x) = 2a$$

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REPERTÓRIO DE DERIVADAS

2) $f(x) = ax^2 + bx + c \quad s(t) = -\frac{g}{2}t^2 + v_0 t + s_0$

$$f'(x) = \frac{d}{dx} f(x) = 2ax + b \quad v(t) = \frac{ds(t)}{dt} = -gt + v_0$$

$$\frac{d}{dx} \left(\frac{d}{dx} f(x) \right) = 2a$$

$$a(t) = \frac{dv(t)}{dt} = \frac{ds(t)}{dt^2} = -g$$

$$f''(x) = \frac{d^2}{dx^2} f(x) = 2a$$

