

$$\begin{aligned}
& \text{de} := \text{diff}(x(t), t) + x(t) = \frac{2}{\text{sqrt}(\text{Pi})} \cdot \exp(-t^2 - t); \\
& \text{de} := \frac{d}{dt} x(t) + x(t) = \frac{2 e^{-t^2 - t}}{\sqrt{\pi}} \quad (1) \\
& e := \exp(\text{int}(1, t)); \\
& e := e^t \quad (2) \\
& \text{dsolve}(\text{de}); \\
& x(t) = (\text{erf}(t) + _CI) e^{-t} \quad (3) \\
& \text{integral} := \text{int}\left(\left(\frac{2}{\text{sqrt}(\text{Pi})}\right) \cdot \exp(-t^2 - t), t\right); \\
& \text{integral} := e^{\frac{1}{4}} \text{erf}\left(t + \frac{1}{2}\right) \quad (4) \\
& \text{ex2} := \text{diff}(x(t), t, t) + 3 \cdot \text{diff}(x(t), t) + x(t) = 1; \\
& \text{ex2} := \frac{d^2}{dt^2} x(t) + 3 \frac{d}{dt} x(t) + x(t) = 1 \quad (5) \\
& \text{sol} := \text{dsolve}(\text{ex2}, x(t)); \\
& \text{sol} := x(t) = e^{\frac{(\sqrt{5}-3)t}{2}} _C2 + e^{-\frac{(3+\sqrt{5})t}{2}} _CI + 1 \quad (6) \\
& s_sol := \text{simplify}(\text{sol}); \\
& s_sol := x(t) = e^{\frac{(\sqrt{5}-3)t}{2}} _C2 + e^{-\frac{(3+\sqrt{5})t}{2}} _CI + 1 \quad (7) \\
& \text{lim} := \text{limit}(\text{sol}, t = \text{infinity}); \\
& \text{lim} := \lim_{t \rightarrow \infty} x(t) = 1 \quad (8) \\
& \text{ex3} := \text{diff}(x(t), t\$2) + 4 x(t) = 1 \\
& \text{ex3} := \frac{d^2}{dt^2} x(t) + 4 x(t) = 1 \quad (9) \\
& \text{cond} := x(0) = \frac{5}{4}, D(x)(0) = 0; \\
& \text{cond} := x(0) = \frac{5}{4}, D(x)(0) = 0 \quad (10) \\
& \text{solution} := \text{dsolve}(\{\text{ex3}, \text{cond}\}, x(t)); \\
& \text{solution} := x(t) = \frac{1}{4} + \cos(2t) \quad (11)
\end{aligned}$$