

```
> x0 := 0.5;
```

$x_0 := 0.5$  (1)

```
> N := 200;
```

$N := 200$  (2)

```
> x := x0; for k from 1 to N do x := x · (1 - x) : psi(k) := x : print(x); od: points := [ [n,psi(n) ] $n = 1 ..N] : with(plots) : pointplot(points, symbol=circle);
```

$x := 0.5$

0.25

0.1875

0.15234375

0.1291351318

0.1124592495

0.09981216670

0.08984969808

0.08177672983

0.07508929629

0.06945089387

0.06462746721

0.06045075769

0.05679646358

0.05357062530

0.05070081340

0.04813024092

0.04581372083

0.04371482382

0.04180383800

0.04005627713

0.03845177179

0.03697323304

0.03560621308

0.03433841067

0.03315928422

0.03205974609

0.03103191877

0.03006893879

0.02916479771

0.02831421228

0.02751251766

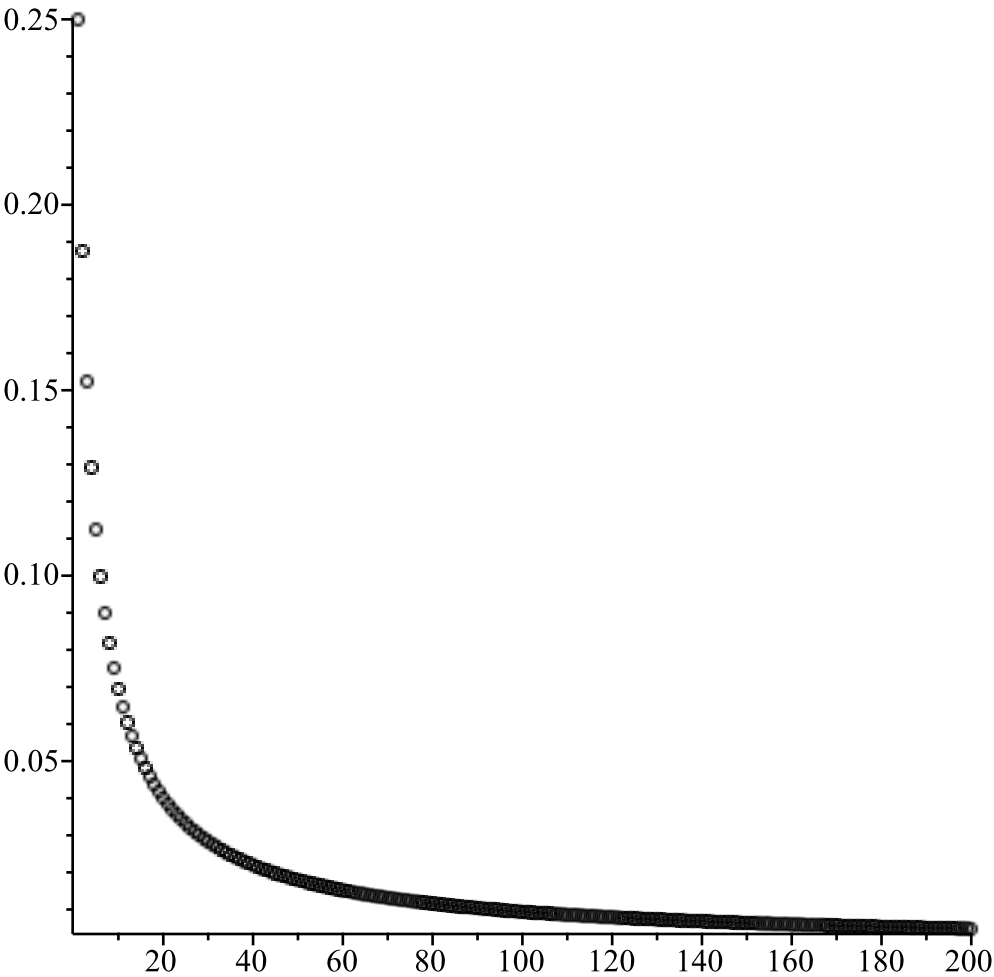
0.02675557903  
0.02603971802  
0.02536165111  
0.02471843776  
0.02410743659  
0.02352626809  
0.02297278280  
0.02244503405  
0.02194125450  
0.02145983585  
0.02099931130  
0.02055834022  
0.02013569487  
0.01973024866  
0.01934096595  
0.01896689299  
0.01860714996  
0.01826092393  
0.01792746259  
0.01760606867  
0.01729609502  
0.01699694012  
0.01670804415  
0.01642888541  
0.01615897713  
0.01589786459  
0.01564512249  
0.01540035263  
0.01516318177  
0.01493325969  
0.01471025744  
0.01449386577  
0.01428379362  
0.01407976686  
0.01388152702  
0.01368883023  
0.01350144616  
0.01331915711

0.01314175716  
0.01296905138  
0.01280085509  
0.01263699320  
0.01247729960  
0.01232161659  
0.01216979435  
0.01202169045  
0.01187716941  
0.01173610226  
0.01159836616  
0.01146384406  
0.01133242434  
0.01120400050  
0.01107847087  
0.01095573835  
0.01083571015  
0.01071829754  
0.01060341564  
0.01049098322  
0.01038092249  
0.01027315894  
0.01016762115  
0.01006424063  
0.009962951691  
0.009863691285  
0.009766398879  
0.009671016332  
0.009577487775  
0.009485759503  
0.009395779870  
0.009307499190  
0.009220869649  
0.009135845212  
0.009052381544  
0.008970435933  
0.008889967212  
0.008810935695

0.008733303107  
0.008657032524  
0.008582088312  
0.008508436072  
0.008436042587  
0.008364875772  
0.008294904625  
0.008226099182  
0.008158430474  
0.008091870486  
0.008026392118  
0.007961969148  
0.007898576196  
0.007836188690  
0.007774782837  
0.007714335589  
0.007654824615  
0.007596228275  
0.007538525591  
0.007481696223  
0.007425720445  
0.007370579121  
0.007316253685  
0.007262726117  
0.007209978926  
0.007157995130  
0.007106758236  
0.007056252224  
0.007006461529  
0.006957371026  
0.006908966015  
0.006861232204  
0.006814155697  
0.006767722979  
0.006721920905  
0.006676736684  
0.006632157871  
0.006588172353

0.006544768338  
0.006501934346  
0.006459659196  
0.006417931999  
0.006376742148  
0.006336079308  
0.006295933407  
0.006256294630  
0.006217153408  
0.006178500412  
0.006140326545  
0.006102622935  
0.006065380929  
0.006028592083  
0.005992248160  
0.005956341122  
0.005920863123  
0.005885806503  
0.005851163785  
0.005816927667  
0.005783091019  
0.005749646877  
0.005716588438  
0.005683909055  
0.005651602233  
0.005619661625  
0.005588081028  
0.005556854379  
0.005525975748  
0.005495439340  
0.005465239487  
0.005435370644  
0.005405827390  
0.005376604420  
0.005347696545  
0.005319098687  
0.005290805876  
0.005262813249

0.005235116046  
0.005207709606  
0.005180589367  
0.005153750861  
0.005127189713  
0.005100901639  
0.005074882442  
0.005049128010  
0.005023634316  
0.004998397414  
0.004973413437  
0.004948678596  
0.004924189176  
0.004899941537  
0.004875932110  
0.004852157396  
0.004828613965



```
> x0 := 0;
```

```
x0 := 0
```

(3)

```
> x := x0; for k from 1 to N do x := x · (1 - x) : psi(k) := x : print(x); od: points := [ [n,  
psi(n) ] $n = 1 ..N] : with(plots) : pointplot(points, symbol=circle);
```

```
x := 0
```

```
0
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0
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0
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0
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0
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0
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0
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0
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0
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0
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0
```

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0
```

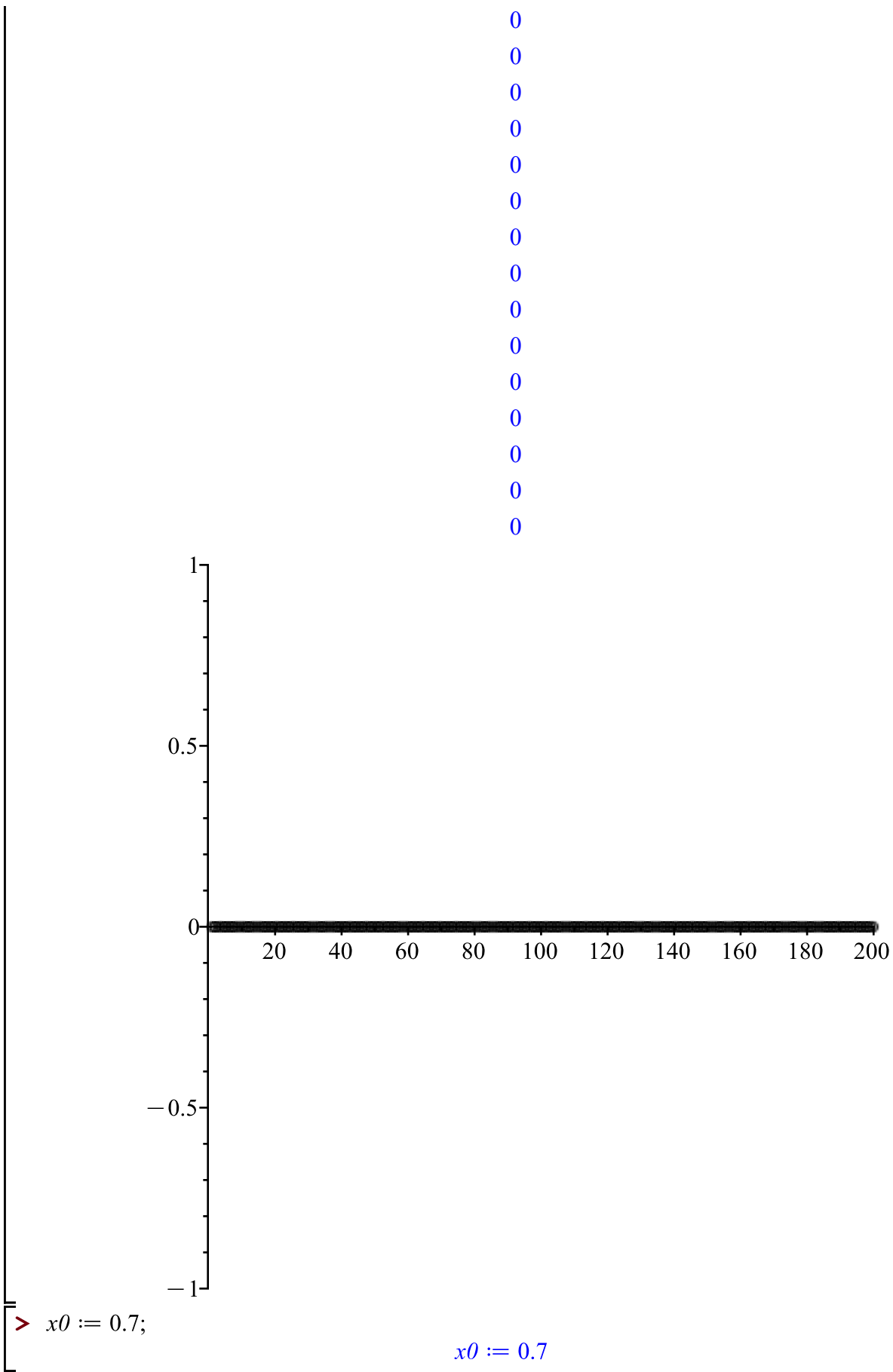
[illegible]



[illegible]

[illegible]

[illegible]



```
> x := x0; for k from 1 to N do x := x · (1 - x) : psi(k) := x : print(x); od: points := [[n,  
psi(n)] $n = 1 ..N] : with(plots) : pointplot(points, symbol=circle);
```

$x := 0.7$

0.21

0.1659

0.13837719

0.1192289433

0.1050134024

0.09398558772

0.08515229702

0.07790138333

0.07183275781

0.06667281272

0.06222754877

0.05835528094

0.05494994213

0.05193044599

0.04923367477

0.04680972004

0.04461857015

0.04262775335

0.04081062799

0.03914512063

0.03761278016

0.03619805893

0.03488775946

0.03367060370

0.03253689415

0.03147824467

0.03048736478

0.02955788537

0.02868421678

0.02786143249

0.02708517307

0.02635156647

0.02565716141

0.02499887148

0.02437392790

0.02377983954  
0.02321435877  
0.02267545232  
0.02216127618  
0.02167015402  
0.02120055845  
0.02075109477  
0.02032048684  
0.01990756466  
0.01951125353  
0.01913056452  
0.01876458602  
0.01841247633  
0.01807345705  
0.01774680720  
0.01743185803  
0.01712798836  
0.01683462037  
0.01655121593  
0.01627727318  
0.01601232356  
0.01575592905  
0.01550767975  
0.01526719162  
0.01503410448  
0.01480808018  
0.01458880094  
0.01437596783  
0.01416929938  
0.01396853033  
0.01377341049  
0.01358370365  
0.01339918665  
0.01321964845  
0.01304488935  
0.01287472021  
0.01270896179  
0.01254744408

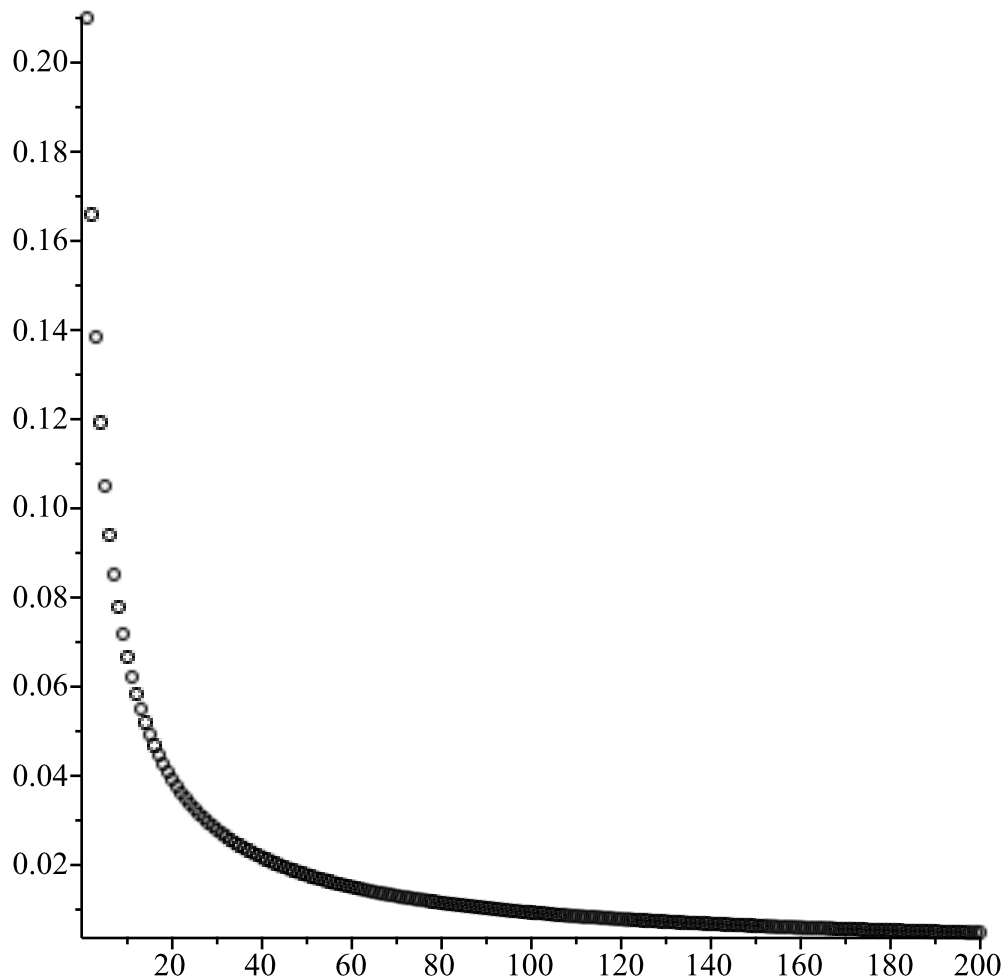
0.01239000573  
0.01223649349  
0.01208676172  
0.01194067191  
0.01179809226  
0.01165889728  
0.01152296739  
0.01139018861  
0.01126045221  
0.01113365443  
0.01100969617  
0.01088848276  
0.01076992370  
0.01065393244  
0.01054042616  
0.01042932558  
0.01032055475  
0.01021404090  
0.01010971427  
0.01000750795  
0.009907357734  
0.009809201997  
0.009712981553  
0.009618639542  
0.009526121316  
0.009435374329  
0.009346348041  
0.009258993820  
0.009173264854  
0.009089116065  
0.009006504034  
0.008925386919  
0.008845724388  
0.008767477548  
0.008690608886  
0.008615082203  
0.008540862562  
0.008467916228

0.008396210623  
0.008325714270  
0.008256396752  
0.008188228664  
0.008121181575  
0.008055227985  
0.007990341287  
0.007926495733  
0.007863666399  
0.007801829150  
0.007740960612  
0.007681038141  
0.007622039794  
0.007563944303  
0.007506731050  
0.007450380039  
0.007394871877  
0.007340187747  
0.007286309391  
0.007233219086  
0.007180899628  
0.007129334309  
0.007078506901  
0.007028401641  
0.006979003212  
0.006930296726  
0.006882267713  
0.006834902104  
0.006788186217  
0.006742106745  
0.006696650742  
0.006651805611  
0.006607559093  
0.006563899256  
0.006520814482  
0.006478293460  
0.006436325174  
0.006394898892



0.006354004160  
0.006313630791  
0.006273768857  
0.006234408681  
0.006195540829  
0.006157156103  
0.006119245532  
0.006081800366  
0.006044812070  
0.006008272317  
0.005972172981  
0.005936506131  
0.005901264026  
0.005866439109  
0.005832024001  
0.005798011497  
0.005764394560  
0.005731166315  
0.005698320048  
0.005665849197  
0.005633747350  
0.005602008241  
0.005570625745  
0.005539593874  
0.005508906774  
0.005478558720  
0.005448544114  
0.005418857481  
0.005389493464  
0.005360446824  
0.005331712434  
0.005303285277  
0.005275160442  
0.005247333125  
0.005219798620  
0.005192552322  
0.005165589722  
0.005138906405

0.005112498046  
 0.005086360410  
 0.005060489348  
 0.005034880796  
 0.005009530771  
 0.004984435372  
 0.004959590776  
 0.004934993235  
 0.004910639077  
 0.004886524701  
 0.004862646577  
 0.004839001245  
 0.004815585312



```
> x0 := 0.5;
```

*x0 := 0.5*

(5)

```
> x := x0; for k from 1 to N do x := 2 · x · (1 - x) : psi(k) := x : print(x); od: points := [[n,
  psi(n) ] $n = 1 ..N] : with(plots) : pointplot(points, symbol=circle);
```

$x := 0.5$

0.50

0.5000

0.50000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

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0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

0.5000000000

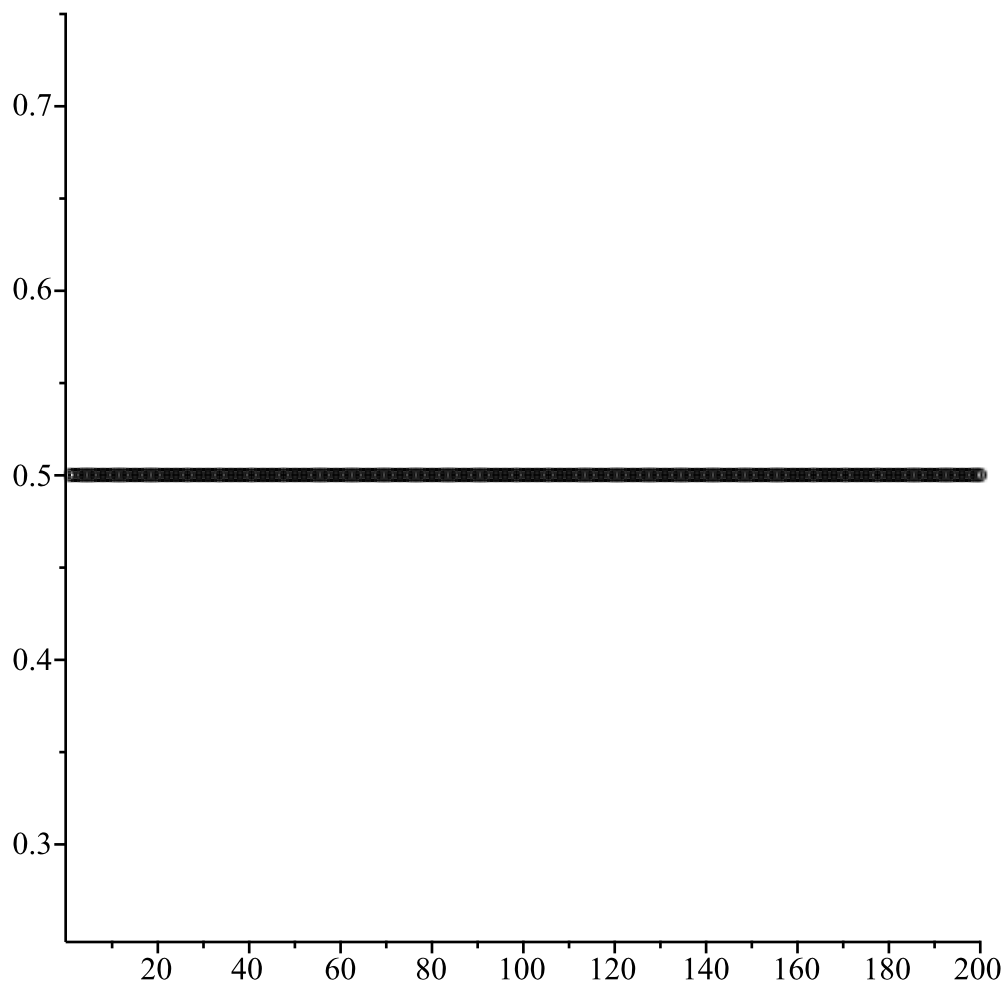
[illegible]

[illegible]

[illegible]

[illegible]

```
0.5000000000
0.5000000000
0.5000000000
0.5000000000
0.5000000000
0.5000000000
0.5000000000
0.5000000000
0.5000000000
0.5000000000
0.5000000000
```



```
> x := x0; for k from 1 to N do x := 3.5 · x · (1 - x) : psi(k) := x : print(x); od: points := [[n,
psi(n)] $n = 1 ..N] : with(plots) : pointplot(points, symbol=circle);
```

```
x := 0.5
0.875
0.3828125
0.8269348143
```



0.5008976952  
0.8749971794  
0.3828199039  
0.8269408878  
0.5008837956  
0.8749972662  
0.3828196760  
0.8269407010  
0.5008842230  
0.8749972634  
0.3828196834  
0.8269407069  
0.5008842097  
0.8749972637  
0.3828196827  
0.8269407062  
0.5008842111  
0.8749972637  
0.3828196827  
0.8269407062  
0.5008842111  
0.8749972637  
0.3828196827  
0.8269407062  
0.5008842111  
0.8749972637  
0.3828196827  
0.8269407062  
0.5008842111  
0.8749972637  
0.3828196827  
0.8269407062  
0.5008842111  
0.8749972637

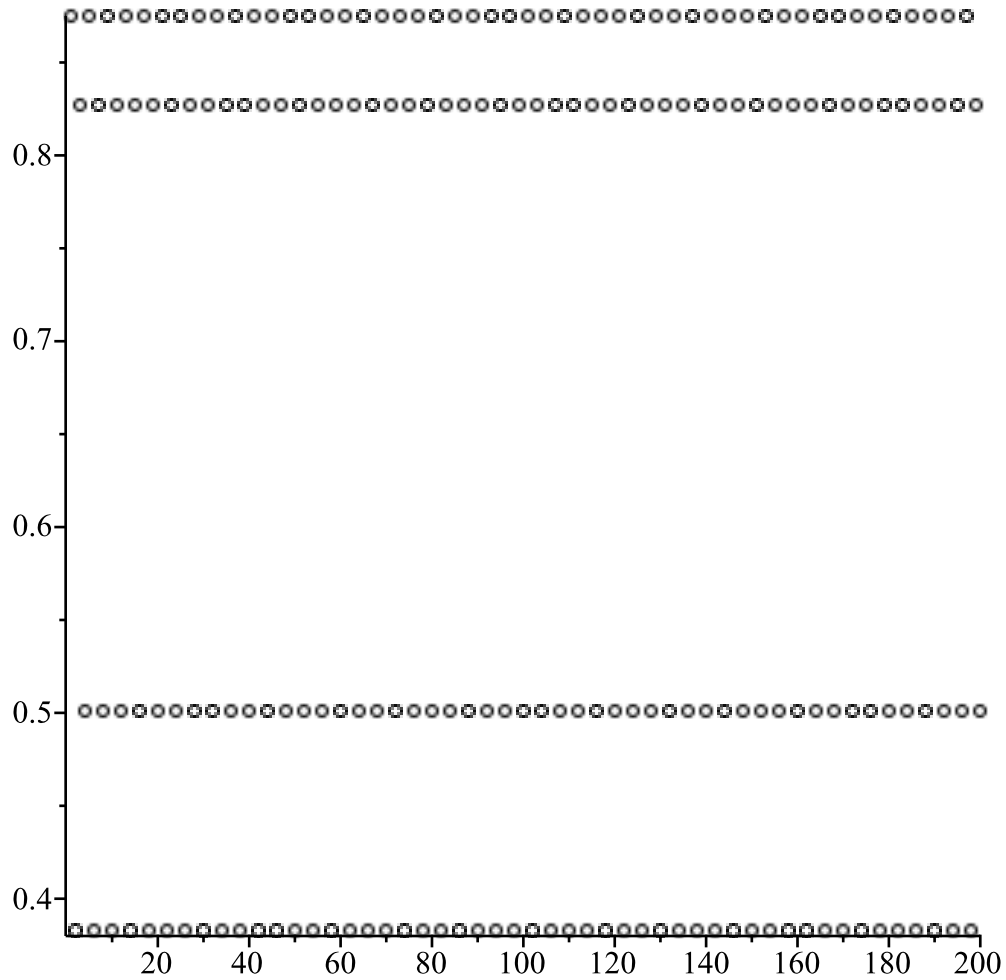
[illegible]

[illegible]

[illegible]

[illegible]

0.3828196827  
0.8269407062  
0.5008842111  
0.8749972637  
0.3828196827  
0.8269407062  
0.5008842111



```
> x := x0; for k from 1 to N do x := 3.6 · x · (1 - x) : psi(k) := x : print(x); od: points := [[n,
psi(n)] $n = 1 ..N] : with(plots) : pointplot(points, symbol=circle);
```

$x := 0.5$

0.900

0.3240000

0.7884864000

0.6003921492

0.8637170990

0.4237555388

0.8790724156

0.3826947733  
0.8504621417  
0.4578346339  
0.8935994948  
0.3422859757  
0.8104546314  
0.5530245185  
0.8898782414  
0.3527818448  
0.8219765333  
0.5267920032  
0.8974158790  
0.3314182288  
0.7976886710  
0.5809732387  
0.8763960046  
0.3899737717  
0.8564192248  
0.4426752103  
0.8881699266  
0.3575667891  
0.8269660094  
0.5151356233  
0.8991752864  
0.3263727266  
0.7914728516  
0.5941568765  
0.8680841374  
0.4122506441  
0.8722801818  
0.4010668783  
0.8647640546  
0.4210098642  
0.8775380102  
0.3868741832  
0.8539291786  
0.4490428914  
0.8906521432

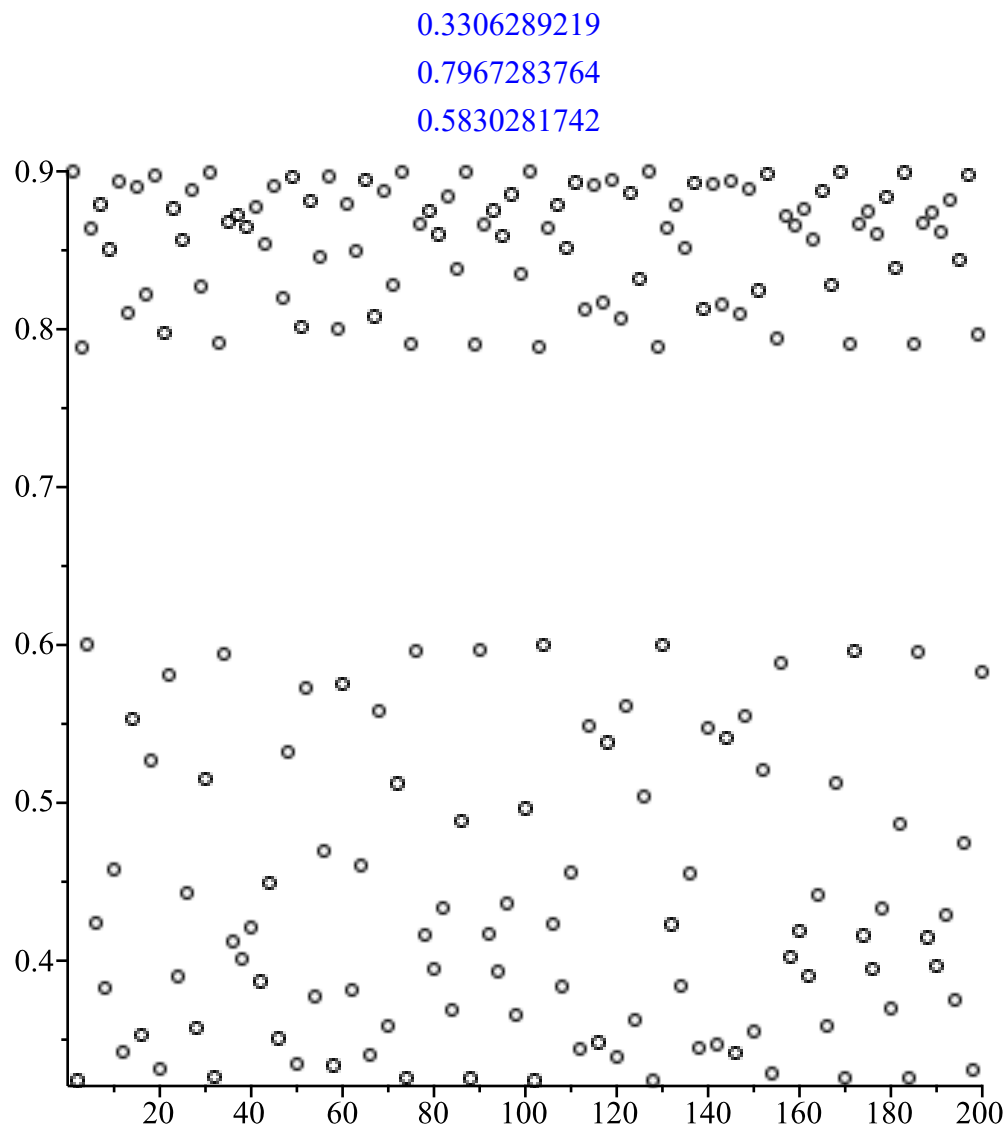
0.3506072508  
0.8196545034  
0.5321555946  
0.8962776637  
0.3346704477  
0.8015981008  
0.5725389082  
0.8810571845  
0.3772635196  
0.8457687230  
0.4695983647  
0.8966726662  
0.3335428652  
0.8002512803  
0.5754570073  
0.8795024640  
0.3815203673  
0.8494652758  
0.4603464756  
0.8943393528  
0.3401873094  
0.8080556540  
0.5583661704  
0.8877362047  
0.3587782880  
0.8282031412  
0.5122177132  
0.8994626190  
0.3255466177  
0.7904376626  
0.5963254708  
0.8665970533  
0.4161837618  
0.8747094175  
0.3945342686  
0.8599571262  
0.4335511223  
0.8841043681



0.3688698038  
0.8380975378  
0.4884841976  
0.8995225907  
0.3253741183  
0.7902208850  
0.5967786164  
0.8662820378  
0.4170148877  
0.8752084960  
0.3931869042  
0.8589274654  
0.4362158686  
0.8853537046  
0.3654090806  
0.8347870238  
0.4965035353  
0.8999559889  
0.3241267450  
0.7886469535  
0.6000585703  
0.8639578170  
0.4231249466  
0.8787248143  
0.3836430540  
0.8512598200  
0.4558195400  
0.8929731132  
0.3440596763  
0.8124574154  
0.5485333090  
0.8915202644  
0.3481627772  
0.8170036481  
0.5382312736  
0.8947381309  
0.3390545088  
0.8067475760

0.5612613286  
0.8864893786  
0.3622534567  
0.8316932033  
0.5039266280  
0.8999444938  
0.3241598468  
0.7886888658  
0.5999714597  
0.8640205459  
0.4229605519  
0.8786337242  
0.3838914104  
0.8514676634  
0.4552937338  
0.8928048593  
0.3445356330  
0.8129909902  
0.5473319044  
0.8919348869  
0.3469933599  
0.8157202852  
0.5411545254  
0.8939026980  
0.3414263922  
0.8094758792  
0.5552088487  
0.8890271388  
0.3551683870  
0.8244856940  
0.5209525238  
0.8984195701  
0.3285426462  
0.7941685529  
0.5884735050  
0.8718207800  
0.4022975074  
0.8656352024

0.4187192357  
0.8762163746  
0.3904604622  
0.8568039229  
0.4416874582  
0.8877587310  
0.3587153995  
0.8281391821  
0.5123688379  
0.8994492425  
0.3255850896  
0.7904859804  
0.5962244227  
0.8666670978  
0.4159988618  
0.8745977117  
0.3948355958  
0.8601856132  
0.4329587664  
0.8838197028  
0.3696567685  
0.8388383112  
0.4866789560  
0.8993611793  
0.3258383345  
0.7908037715  
0.5955593994  
0.8671262443  
0.4147859545  
0.8738588390  
0.3968264466  
0.8616787844  
0.4290784448  
0.8818924788  
0.3749692846  
0.8437223527  
0.4746777995  
0.8976916303



```
> x := x0; for k from 1 to N do x := 3.8 · x · (1 - x) : psi(k) := x : print(x); od: points := [[n,
psi(n)] $n = 1 ..N] : with(plots) : pointplot(points, symbol=circle);
```

$x := 0.5$   
 $0.950$   
 $0.1805000$   
 $0.5620950500$   
 $0.9353479782$   
 $0.2297941239$   
 $0.6725573811$   
 $0.8368510108$   
 $0.5188193067$   
 $0.9486541681$   
 $0.1850958623$   
 $0.5731744596$

0.9296528943  
0.2485138836  
0.7096679865  
0.7829494745  
0.6457704606  
0.8692536966  
0.4318764885  
0.9323649114  
0.2396302169  
0.6923887888  
0.8093489048  
0.5863523694  
0.9216644195  
0.2743566459  
0.7565232918  
0.6999440430  
0.7980850429  
0.6123521674  
0.9020325639  
0.3358053067  
0.8475523903  
0.4909878768  
0.9496913701  
0.1815551523  
0.5646529402  
0.9341159897  
0.2338645685  
0.6808533420  
0.8257098611  
0.5468697283  
0.9416522687  
0.2087844395  
0.6277352897  
0.8879980440  
0.3779385678  
0.8933838258  
0.3619468293  
0.8775770240

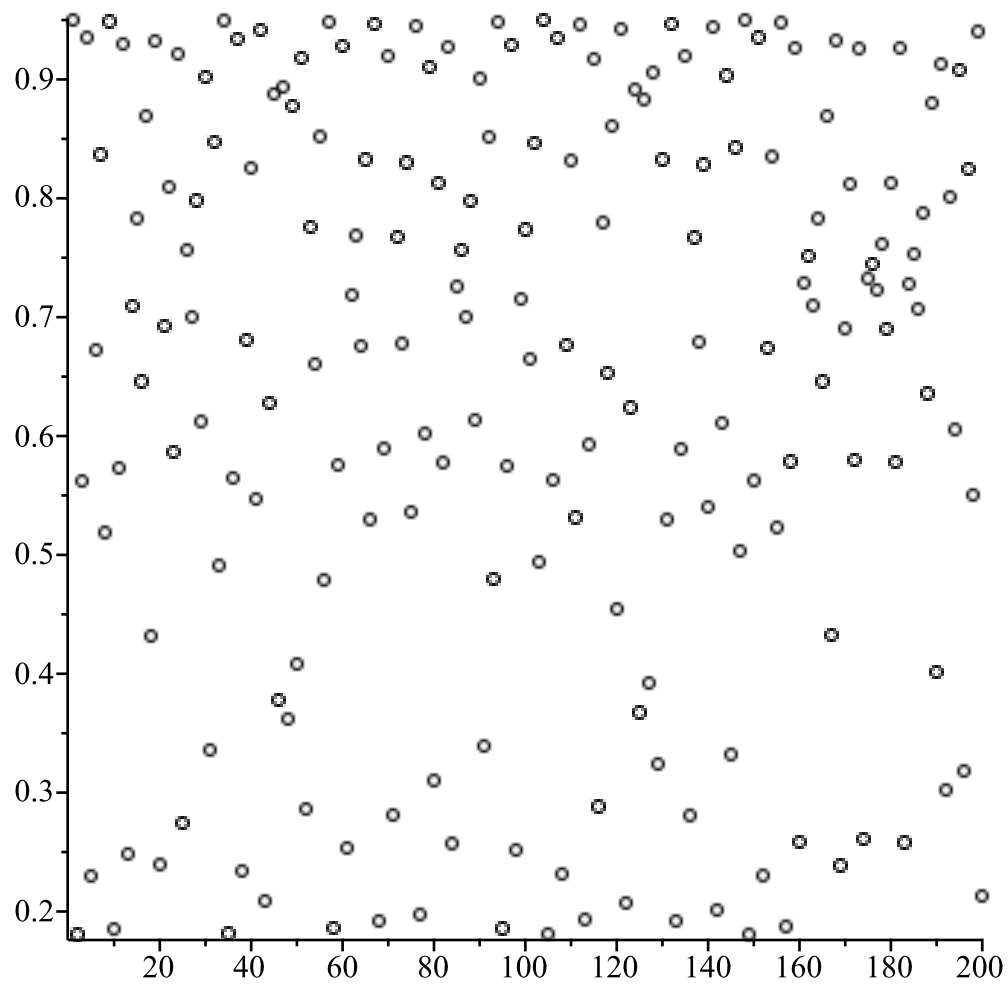
0.4082552454  
0.9180150200  
0.2860010836  
0.7759769624  
0.6605795216  
0.8520140254  
0.4791272784  
0.9483444521  
0.1861515586  
0.5756967920  
0.9282259837  
0.2531655261  
0.7184764215  
0.7686186022  
0.6758073771  
0.8325487116  
0.5297631467  
0.9466337894  
0.1919693810  
0.5894451236  
0.9195983656  
0.2809614040  
0.7676839553  
0.6777121404  
0.8299899018  
0.5362053259  
0.9450188627  
0.1974412050  
0.6021410673  
0.9103553691  
0.3101121900  
0.8129819545  
0.5777607256  
0.9270224245  
0.2570770261  
0.7257560294  
0.7563300178  
0.7003207036

0.7975121397  
0.6136488015  
0.9009190096  
0.3392030014  
0.8517484358  
0.4798375440  
0.9484552065  
0.1857741255  
0.5747959792  
0.9287411337  
0.2514879530  
0.7153186975  
0.7738238623  
0.6650778711  
0.8464473267  
0.4939021492  
0.9498587016  
0.1809831646  
0.5632673831  
0.9347895052  
0.2316407274  
0.6763365430  
0.8318406097  
0.5315508772  
0.9462172600  
0.1933825961  
0.5927459169  
0.9173131406  
0.2882290222  
0.7795816014  
0.6529696872  
0.8610810442  
0.4545578221  
0.9421530323  
0.2071026449  
0.6240023297  
0.8915690044  
0.3673601162

0.8831453126  
0.3921587437  
0.9058070009  
0.3242185765  
0.8325833866  
0.5296755058  
0.9466535847  
0.1919021860  
0.5892878006  
0.9197052171  
0.2806206168  
0.7671162076  
0.6788659401  
0.8284265069  
0.5401169125  
0.9438844065  
0.2012732079  
0.6108967541  
0.9032672576  
0.3320269720  
0.8427832352  
0.5034986841  
0.9499534850  
0.1806590731  
0.5624812151  
0.9351651716  
0.2303988390  
0.6737978132  
0.8352184164  
0.5229887305  
0.9479917695  
0.1873528229  
0.5785566223  
0.9265496570  
0.2586104824  
0.7285781830  
0.7514576543  
0.7097223828



0.7828627844  
0.6459568518  
0.8690470701  
0.4324561884  
0.9326637673  
0.2386478450  
0.6904411942  
0.8121821761  
0.5796606978  
0.9258858582  
0.2607606960  
0.7325053105  
0.7445768663  
0.7226921947  
0.7615511083  
0.6900458673  
0.8127537595  
0.5783033264  
0.9267006386  
0.2581209471  
0.7276791904  
0.7530163079  
0.7067344420  
0.7875913079  
0.6357067105  
0.8800180171  
0.4012279655  
0.9129275238  
0.3020652683  
0.8011229996  
0.6054347686  
0.9077573365  
0.3181890272  
0.8243901268  
0.5501299733  
0.9404505460  
0.2128126028



```

> x := x0; for k from 1 to N do x := 3.1 · x · (1 - x) : psi(k) := x : print(x); od: points := [[n,
psi(n)] $n = 1 ..N] : with(plots) : pointplot(points, symbol=circle);
x := 0.5
0.775
0.5405625
0.7698995192
0.5491781734
0.7675026726
0.5531711926
0.7662357553
0.5552674201
0.7655310881
0.5564290480
0.7651288638
0.5570907254
0.7648960122
0.5574733184

```

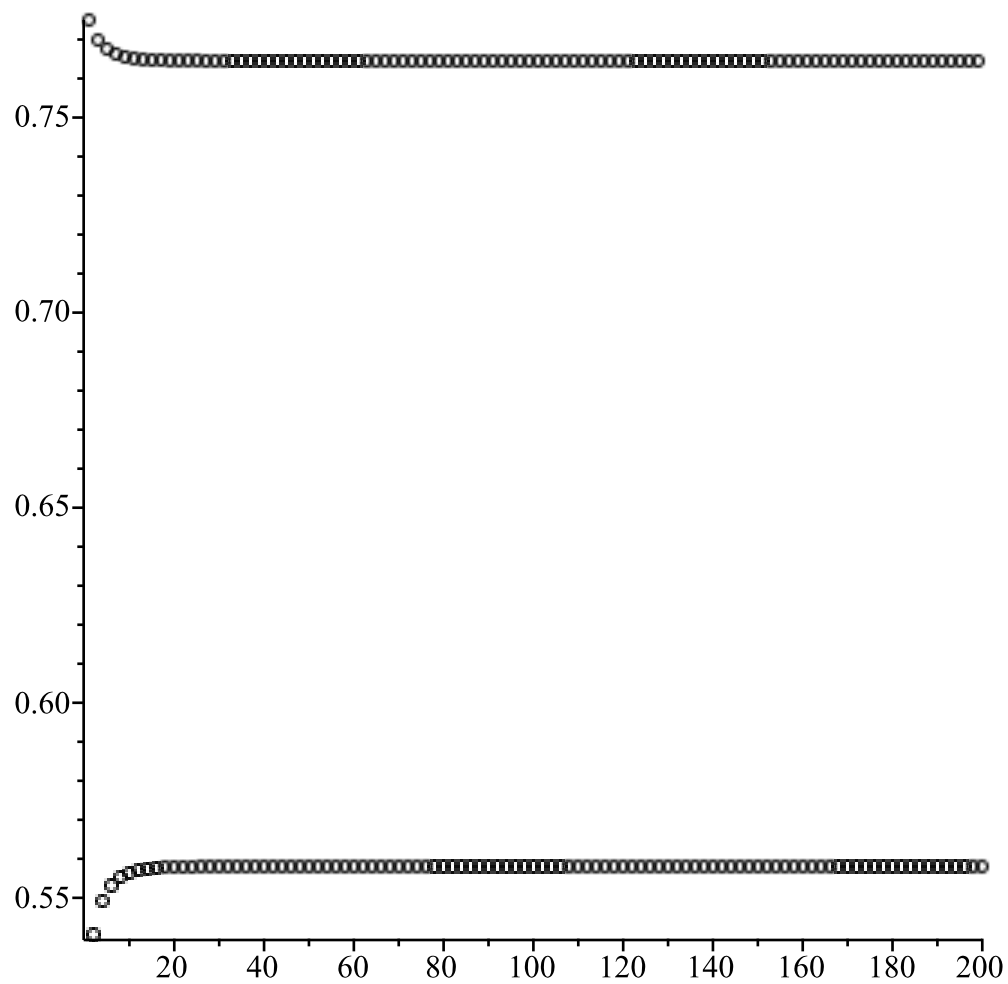
0.7647601349  
0.5576964201  
0.7646804816  
0.5578271524  
0.7646336632  
0.5579039753  
0.7646061018  
0.5579491938  
0.7645898618  
0.5579758355  
0.7645802878  
0.5579915410  
0.7645746417  
0.5580008029  
0.7645713114  
0.5580062657  
0.7645693466  
0.5580094885  
0.7645681875  
0.5580113900  
0.7645675037  
0.5580125116  
0.7645671004  
0.5580131731  
0.7645668623  
0.5580135637  
0.7645667218  
0.5580137941  
0.7645666391  
0.5580139298  
0.7645665901  
0.5580140101  
0.7645665613  
0.5580140573  
0.7645665445  
0.5580140848  
0.7645665346  
0.5580141013

[illegible]

[illegible]

[illegible]

[illegible]



```
> x := x0; for k from 1 to N do x := 3.55 · x · (1 - x) : psi(k) := x : print(x); od: points := [[n,
psi(n)] $n = 1 ..N] : with(plots) : pointplot(points, symbol=circle);
```

$x := 0.5$

0.8875

0.3544453125

0.8122891068

0.5412880740

0.8814482969

0.3709650486

0.8283924336

0.5046623541

0.8874228319

0.3546576001

0.8125083331

0.5408018230

0.8815899998

0.3705812060



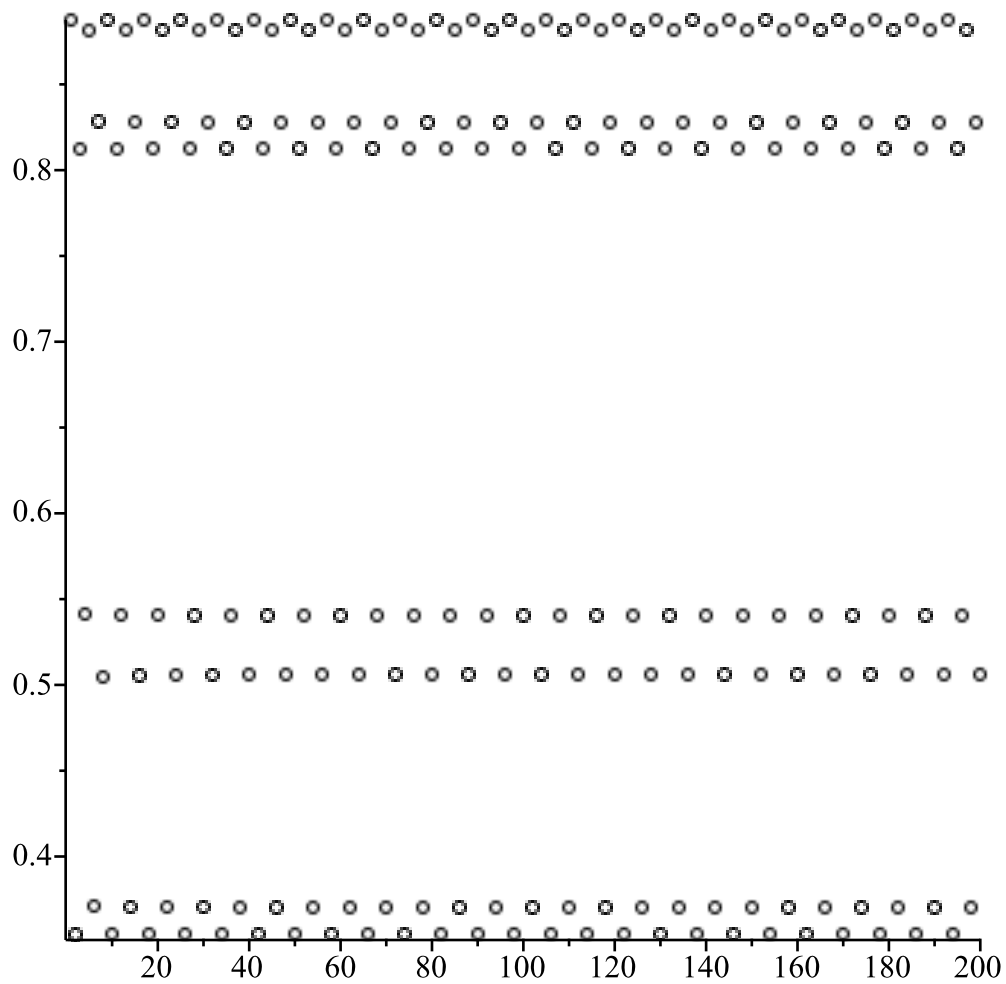
0.8280402541  
0.5054830505  
0.8873932735  
0.3547389034  
0.8125922090  
0.5406156937  
0.8816437972  
0.3704354430  
0.8279062409  
0.5057951151  
0.8873807789  
0.3547732691  
0.8126276479  
0.5405370360  
0.8816664579  
0.3703740379  
0.8278497401  
0.5059266450  
0.8873753059  
0.3547883219  
0.8126431682  
0.5405025854  
0.8816763691  
0.3703471800  
0.8278250194  
0.5059841863  
0.8873728727  
0.3547950141  
0.8126500680  
0.5404872692  
0.8816807726  
0.3703352467  
0.8278140339  
0.5060097552  
0.8873717839  
0.3547980087  
0.8126531550  
0.5404804167

0.8816827424  
0.3703299089  
0.8278091196  
0.5060211929  
0.8873712955  
0.3547993519  
0.8126545399  
0.5404773424  
0.8816836260  
0.3703275141  
0.8278069147  
0.5060263248  
0.8873710761  
0.3547999554  
0.8126551618  
0.5404759618  
0.8816840226  
0.3703264395  
0.8278059253  
0.5060286273  
0.8873709777  
0.3548002260  
0.8126554409  
0.5404753423  
0.8816842008  
0.3703259567  
0.8278054809  
0.5060296618  
0.8873709334  
0.3548003479  
0.8126555666  
0.5404750633  
0.8816842810  
0.3703257391  
0.8278052807  
0.5060301275  
0.8873709135  
0.3548004026

0.8126556230  
0.5404749380  
0.8816843169  
0.3703256418  
0.8278051908  
0.5060303370  
0.8873709042  
0.3548004282  
0.8126556493  
0.5404748798  
0.8816843336  
0.3703255967  
0.8278051493  
0.5060304336  
0.8873709003  
0.3548004389  
0.8126556606  
0.5404748545  
0.8816843410  
0.3703255765  
0.8278051308  
0.5060304765  
0.8873708986  
0.3548004436  
0.8126556652  
0.5404748442  
0.8816843438  
0.3703255690  
0.8278051237  
0.5060304932  
0.8873708979  
0.3548004455  
0.8126556674  
0.5404748393  
0.8816843453  
0.3703255651  
0.8278051202  
0.5060305014

0.8873708975  
0.3548004466  
0.8126556684  
0.5404748372  
0.8816843460  
0.3703255630  
0.8278051184  
0.5060305056  
0.8873708972  
0.3548004474  
0.8126556691  
0.5404748357  
0.8816843463  
0.3703255623  
0.8278051177  
0.5060305070  
0.8873708972  
0.3548004474  
0.8126556691  
0.5404748357  
0.8816843463  
0.3703255623  
0.8278051177  
0.5060305070  
0.8873708972  
0.3548004474  
0.8126556691  
0.5404748357  
0.8816843463  
0.3703255623  
0.8278051177  
0.5060305070  
0.8873708972  
0.3548004474  
0.8126556691  
0.5404748357  
0.8816843463  
0.3703255623

0.8278051177  
0.5060305070  
0.8873708972  
0.3548004474  
0.8126556691  
0.5404748357  
0.8816843463  
0.3703255623  
0.8278051177  
0.5060305070  
0.8873708972  
0.3548004474  
0.8126556691  
0.5404748357  
0.8816843463  
0.3703255623  
0.8278051177  
0.5060305070  
0.8873708972  
0.3548004474  
0.8126556691  
0.5404748357  
0.8816843463  
0.3703255623  
0.8278051177  
0.5060305070  
0.8873708972  
0.3548004474  
0.8126556691  
0.5404748357  
0.8816843463  
0.3703255623  
0.8278051177  
0.5060305070



```
> x0 := 0.67; y0 := 0.6701;
```

```
x0 := 0.67
```

```
y0 := 0.6701
```

(6)

```
> N := 40
```

```
N := 40
```

(7)

```
> x := x0; y := y0; for k from 1 to N do x := 4 · x · (1 - x) : y := 4 · y · (1 - y) : print(x, y);  
od;
```

```
x := 0.67
```

```
y := 0.6701
```

```
0.8844, 0.88426396
```

```
0.40894656, 0.4093648360
```

```
0.9668370844, 0.9671410680
```

```
0.1282525465, 0.1271168904
```

```
0.4472153232, 0.4438327464
```

```
0.9888551116, 0.9873809584
```

```
0.04408271944, 0.04983920556
```

```
0.1685577332, 0.1894210366
```

```

0.5605840952, 0.6141628300
0.9853182696, 0.9478673928
0.05786470876, 0.1976591939
0.2180655370, 0.6343601480
0.6820518344, 0.9277894024
0.8674285184, 0.2679849088
0.4599851356, 0.7846759900
0.9935952424, 0.6758383228
0.02545494672, 0.8763235368
0.09922796964, 0.4335223828
0.3575271188, 0.9823229056
0.9188059124, 0.06945845892
0.2984064310, 0.2585359256
0.8374401316, 0.7667804032
0.5445366304, 0.7153128660
0.9920659544, 0.8145614788
0.03148438608, 0.6042043044
0.1219724780, 0.9565658516
0.4283807704, 0.1661904926
0.9794827440, 0.5542848512
0.08038519284, 0.9882126196
0.2956936545, 0.04659375224
0.8330356688, 0.1776910980
0.5563489732, 0.5844678868
0.9872991728, 0.9714607044
0.05015806476, 0.1108992168
0.1905689332, 0.3944023220
0.6170096596, 0.9553965216
0.9452349584, 0.1704560324
0.2070633273, 0.5656030936
0.6567524232, 0.9827849364
0.9017147112, 0.06767482076

```

(8)

```
> x0 := 0.67; y0 := 0.67;
```

```
x0 := 0.67
```

```
y0 := 0.67
```

(9)

```
> N := 40
```

```
N := 40
```

(10)

```
> x := x0; y := y0; for k from 1 to N do x := 4 · x · (1 - x) : y := 4 · y - 4 · y2 : print(x, y); od:
```

$x := 0.67$   
 $y := 0.67$   
0.8844, 0.8844  
0.40894656, 0.40894656  
0.9668370844, 0.9668370843  
0.1282525465, 0.1282525471  
0.4472153232, 0.4472153251  
0.9888551116, 0.9888551126  
0.04408271944, 0.04408271593  
0.1685577332, 0.1685577203  
0.5605840952, 0.5605840609  
0.9853182696, 0.9853182860  
0.05786470876, 0.05786464510  
0.2180655370, 0.2180653118  
0.6820518344, 0.6820513264  
0.8674285184, 0.8674292580  
0.4599851356, 0.4599829615  
0.9935952424, 0.9935945465  
0.02545494672, 0.02545769466  
0.09922796964, 0.09923840176  
0.3575271188, 0.3575605655  
0.9188059124, 0.9188440300  
0.2984064310, 0.2982787141  
0.8374401316, 0.8372340914  
0.5445366304, 0.5450926701  
0.9920659544, 0.9918666046  
0.03148438608, 0.03226897351  
0.1219724780, 0.1249107474  
0.4283807704, 0.4372322103  
0.9794827440, 0.9842408184  
0.08038519284, 0.06204331879  
0.2956936545, 0.2327757815  
0.8330356688, 0.7143648682  
0.5563489732, 0.8161908130  
0.9872991728, 0.6000934791  
0.05015806476, 0.9599251820  
0.1905689332, 0.1538753078  
0.6170096596, 0.5207907898



```

0.9452349584, 0.9982709723
0.2070633273, 0.006904152853
0.6567524232, 0.02742594211
0.9017147112, 0.1066950392

```

(11)

```

> de := diff(y(x), x) = 2 * x * y(x);
de := d/dx y(x) = 2 x y(x)

```

(12)

```

> sol := dsolve({de, y(0) = 1}, y(x));
sol := y(x) = e^x^2

```

(13)

```

> h := 0.1; N := 1/h;
h := 0.1
N := 10.

```

(14)

```

> x := 0; y := 1; for k from 0 to (N - 1) do y := y + h * 2 * x * y : x := x + h : print(x, y) : od:
x := 0
y := 1
0.1, 1.
0.2, 1.02
0.3, 1.0608
0.4, 1.124448
0.5, 1.21440384
0.6, 1.335844224
0.7, 1.496145531
0.8, 1.705605905
0.9, 1.978502850
1.0, 2.334633363

```

(15)

```

> x := 0; y := 1; for k from 0 to (N - 1) do y := y + h * x * y + h * (x + h) * (y + h * 2 * x
  * y) : x := x + h : print(x, y) : od:
x := 0
y := 1
0.1, 1.01
0.2, 1.040704
0.3, 1.093988045
0.4, 1.173192779
0.5, 1.283472900
0.6, 1.432355756

```

0.7, 1.630593792

0.8, 1.893445511

0.9, 2.242596863

1.0, 2.709057011

(16)

> abs(1.21440384 - 1.283472900)

0.069069060

(17)

>  $de1 := \text{diff}(y(x), x) = y(x)^2 + x^2$ ;  $soll := \text{dsolve}(\{de1, y(0) = 1\}, y(x))$ ;  $h := 0.1$ ;  $N := \frac{2}{h}$ ;

$$de1 := \frac{d}{dx} y(x) = y(x)^2 + x^2$$

$soll := y(x)$

$$= \begin{cases} \left( \frac{\text{BesselJ}\left(-\frac{3}{4}, \frac{x^2}{2}\right) \left(\Gamma\left(\frac{3}{4}\right)^2 + \pi\right)}{\Gamma\left(\frac{3}{4}\right)^2} - \text{BesselY}\left(-\frac{3}{4}, \frac{x^2}{2}\right) \right) x & x < 0 \\ - \frac{\left(\Gamma\left(\frac{3}{4}\right)^2 + \pi\right) \text{BesselJ}\left(\frac{1}{4}, \frac{x^2}{2}\right)}{\Gamma\left(\frac{3}{4}\right)^2} + \text{BesselY}\left(\frac{1}{4}, \frac{x^2}{2}\right) & x = 0 \\ \left( \frac{\text{BesselJ}\left(-\frac{3}{4}, \frac{x^2}{2}\right) \left(\Gamma\left(\frac{3}{4}\right)^2 - \pi\right)}{\Gamma\left(\frac{3}{4}\right)^2} - \text{BesselY}\left(-\frac{3}{4}, \frac{x^2}{2}\right) \right) x & 0 < x \\ - \frac{\left(\Gamma\left(\frac{3}{4}\right)^2 - \pi\right) \text{BesselJ}\left(\frac{1}{4}, \frac{x^2}{2}\right)}{\Gamma\left(\frac{3}{4}\right)^2} + \text{BesselY}\left(\frac{1}{4}, \frac{x^2}{2}\right) & \end{cases}$$

$h := 0.1$

$N := 20.$

(18)

>  $x := 0$ ;  $y := 0$ ; **for**  $k$  **from** 0 **to**  $(N - 1)$  **do**  $y := y + h \cdot (y^2 + x^2)$ ;  $x := x + h$ ; *print*( $x, y$ );  
**od**:

$x := 0$

$y := 0$

0.1, 0.

0.2, 0.001

0.3, 0.0050001

0.4, 0.01400260010

```

0.5, 0.03002220738
0.6, 0.05511234067
0.7, 0.09141607768
0.8, 0.1412517676
0.9, 0.2072469738
1.0, 0.2925421046
1.1, 0.4011001929
1.2, 0.5381883294
1.3, 0.7111529972
1.4, 0.9307268557
1.5, 1.213352104
1.6, 1.585574437
1.7, 2.092979066
1.8, 2.820035203
1.9, 3.939295058
2.0, 5.852099613

```

(19)

```

> x := 0; y := 0; for k from 0 to (N - 1) do y := y +  $\frac{h}{2} \cdot (x^2 + y^2) + h \cdot (x + h) \cdot \left(y + \frac{h}{2} \cdot (x^2 + y^2)\right)$  : x := x + h : print(x, y) : od:

```

```

x := 0

```

```

y := 0

```

```

0.1, 0.

```

```

0.2, 0.0005100000000
0.3, 0.002585313395
0.4, 0.007369073490
0.5, 0.01614037808
0.6, 0.03037260789
0.7, 0.05180804394
0.8, 0.08255762742
0.9, 0.1252392729
1.0, 0.1831758684
1.1, 0.2606874276
1.2, 0.3635355633
1.3, 0.4996221195
1.4, 0.6801276852
1.5, 0.9214448239
1.6, 1.248621508

```



1.7, 1.701851922

1.8, 2.349576966

1.9, 3.317247049

2.0, 4.857544138

**(20)**