# Production planning and resource scheduling

Planning pallet execution for a set of boxes, we have the input data:

- Storage capacity (number of pallets)
- Storage cost per day for 1 pallet
- Pallet demand for an interval of time (number&type of pallets, client, date/position/interval)
- Pallet creation time
- Resources working costs (normal operation, overtime). 3 shifts types will be defined: the first time in the morning pallets are loaded into the trucks; 8-17 production and pallet creation in normal regime; evening overtime
- Decision variables
- · How many and what types of pallets are done in each day
- How many pallets and what types are done before time
- Objective function
- Cost minimization (robot assembly, storage and overtime)

### We start from the data of the problem:

|    | Α        | В  | С      | D  | E  | F               | G               | Н        |            |         | K For           | mula Baı | М               | N               | 0       | Р               | Q           | R     |                 | Т         | U               |
|----|----------|----|--------|----|----|-----------------|-----------------|----------|------------|---------|-----------------|----------|-----------------|-----------------|---------|-----------------|-------------|-------|-----------------|-----------|-----------------|
| 1  |          |    |        |    |    |                 |                 | Date pro | oblema(Pro | duction | planning        | and reso | irce sche       | duling)         |         |                 |             |       |                 |           |                 |
|    | Interval |    |        |    |    |                 |                 |          |            |         | aleti re        |          | _               |                 |         | fata            | latibil (in | valul | l               | ere clien |                 |
| 2  | (zile)   |    | Post 1 |    |    | Post 2          |                 |          | Post n     | inte    | erval cur       | ent      | Stoc pe         | ntru intervalul | urmator |                 | urmator)    |       | <u> </u>        | interval  |                 |
| 3  |          |    |        | 1. |    | paleti<br>tip 2 | paleti<br>tip 3 |          |            | •       | paleti<br>tip 2 |          | paleti<br>tip 1 | paleti tip 2    |         | paleti<br>tip 1 |             |       | paleti<br>tip 1 |           | paleti<br>tip 3 |
| 4  | 0        |    |        |    |    |                 |                 |          |            |         |                 |          |                 | porcer esp 2    |         |                 |             |       |                 |           |                 |
| 5  | 1        | 9  | 25     | 10 | 1  | 0               | 0               |          |            | 10      | 25              | 10       | 10              | 25              | 10      | 0               | 15          | 0     | 10              | 10        | 10              |
| 6  | 2        | 21 | 21     | 21 | 9  | 0               | 34              |          |            | 30      | 21              | 55       | 30              | 36              | 55      | 0               | 6           | 25    | 30              | 30        | 30              |
| 7  | 3        | 14 | 33     | 20 | 24 | 14              | 11              |          |            | 38      | 47              | 31       | 38              | 53              | 56      | 0               | 15          | 18    | 38              | 38        | 38              |
| 8  | 4        | 29 | 17     | 16 | 19 | 17              | 14              |          |            | 48      | 34              | 30       | 48              | 49              | 48      | 0               | 1           | 0     | 48              | 48        | 48              |
| 9  | 5        | 20 | 20     | 20 | 6  | 6               | 6               | Ť        |            | 26      | 26              | 26       | 26              | 27              | 26      | 6               | 7           | 6     | 20              | 20        | 20              |
| 10 | 6        | 14 | 14     | 14 | 6  | 6               | 6               | Ţ.       |            | 20      | 20              | 20       | 26              | 27              | 26      | 12              | 13          | 12    | 14              | 14        | 14              |
| 11 |          |    |        |    |    |                 |                 |          |            |         |                 |          |                 |                 |         |                 |             |       |                 |           |                 |

We need to find out the following characteristics: WORKING TIMES WORKSTATIONS, Total work P1, Total work P2, Difference between Production 1 and Production 2, NORMAL COSTS WORKSTATIONS, NORMAL TIMES WORKSTATIONS, STORAGE COSTS, OVERTIME TIMES WORKSTATIONS, OVERTIME COSTS and their constraints.

We have the following constraints:

|   | cost normal post 1 (um/dt)exemplu    | 20 um/min  | Constrangeri   |
|---|--------------------------------------|------------|--|
|   | cost normal post 2 (um/dt)           | 30 um/min  | stoc platibil / interval urmator >0  |
|   |                                      |            | variabile decizionale >0   |
|   | cost normal post n (um/dt)           | 100 um/min | timpi de lucru < 8 (+8) ore /zi  |
|   |                                      |            |  |
|   | cost overtime post 1 (um/dt)         | 40 um/min  |  |
|   | cost overtime post 2 (um/dt)         | 60 um/min  |  |
|   |                                      |            |  |
|   | cost overtime post n (um/dt)         | 200 um/min |  |
|   |                                      |            |  |
|   |                                      |            |  |
|   |                                      |            |  |
|   |                                      |            |  |
|   |                                      |            |  |
|   | timp realizare palet post 1          | 8 min      | aici ar trebui timpi diferiti pentru paleti diferiti pe fiecare tip de palet |
|   | timp realizare palet post 2          | 10 min     |  |
|   |                                      |            |  |
|   |                                      |            |  |
|   | timp realizare palet post n          | 20 min     |  |
|   |                                      |            |  |
|   | limita timp (normal) post 1n         | 480 min    | 8ore lucru normal  |
| - | limita timp (overtime) post 1n       | 480 min    | 8 ore lucru extra/overtime   |
|   |                                      |            |  |
|   |                                      |            |  |
|   |                                      | 20         |  |
| - | cost mentinere 1 palet 1 interval d€ | 20 um      |  |
| _ |                                      |            |  |

# **For WORKING TIMES WORKSTATIONS:**

Apply the following formulas for each cell: "timp realizare palet post 1" (8 min)\* pallet type 1/2/3 (from the workstation 1); "timp realizare palet post 2" (10 min)\* pallet type 1/2/3 (from the workstation 2). Then "\$B\$17:\$G\$22 >= 0" as solver constraint because time needs to be greater or equal to 0.

|          | TIMPI DE LUCRU POSTURI |        |        |        |        |        |  |        |
|----------|------------------------|--------|--------|--------|--------|--------|--|--------|
| Interval |                        |        |        |        |        |        |  |        |
| (zile)   |                        | Post 1 |        |        | Post 2 |        |  | Post n |
|          | paleti                 | paleti | paleti | paleti | paleti | paleti |  |        |
|          | tip 1                  | tip 2  | tip 3  | tip 1  | tip 2  | tip 3  |  |        |
| 0        | 0                      | 0      | 0      | 0      | 0      | 0      |  |        |
| 1        | 72                     | 200    | 80     | 10     | 0      | 0      |  |        |
| 2        | 168                    | 168    | 168    | 90     | 0      | 340    |  |        |
| 3        | 112                    | 264    | 160    | 240    | 140    | 110    |  |        |
| 4        | 232                    | 136    | 128    | 190    | 170    | 140    |  |        |
| 5        | 160                    | 160    | 160    | 60     | 60     | 60     |  | ·      |
| 6        | 112                    | 112    | 112    | 60     | 60     | 60     |  |        |
|          |                        |        |        |        |        |        |  |        |

# For Total work P1, Total work P2, Difference between Production 1 and Production 2:

| Total lucru P1 | Total lucru P2 | Diff P1 | Diff P2 |
|----------------|----------------|---------|---------|
|----------------|----------------|---------|---------|

| 1 | 352 | 10  | 342 | 342 |
|---|-----|-----|-----|-----|
|   |     |     |     |     |
| 2 | 504 | 430 | 74  | 74  |
| 3 | 536 | 490 | 46  | 46  |
| 4 | 496 | 500 | 4   | 4   |
| 5 | 480 | 180 | 300 | 300 |
| 6 | 336 | 180 | 156 | 156 |

For calculating "Total lucru P1/P2" we applied the previous results: "WORKING TIMES WORKSTATIONS" (Post 1 or 2)\*interval from the base table (B5 up to G10).

For Diff P1 and Diff P2: I applied the base math difference formula ABS("Total lucru P1"-"Total lucru P2") and vice-versa, I needed an absolute value for always having a positive number.

#### For: NORMAL TIMES WORKSTATIONS:

For each workstation, we need to calculate Post 1 = ("paleti tip 1" + "paleti tip 2" + "paleti tip 3") from the <u>WORKING TIMES WORKSTATIONS</u> table for the corresponding workstation.

|                    | TIMPI NORMALI POSTURI |        |  |           |  |  |  |
|--------------------|-----------------------|--------|--|-----------|--|--|--|
| Interval<br>(zile) | Post 1                | Post 2 |  | Post<br>n |  |  |  |
| 0                  |                       |        |  |           |  |  |  |
| 1                  | 352                   | 10     |  |           |  |  |  |
| 2                  | 504                   | 430    |  |           |  |  |  |
| 3                  | 536                   | 490    |  |           |  |  |  |
| 4                  | 496                   | 500    |  |           |  |  |  |
| 5                  | 480                   | 180    |  |           |  |  |  |
| 6                  | 336                   | 180    |  |           |  |  |  |

#### For: NORMAL COSTS WORKSTATIONS:

We calculate in a row of 6 days "Post 1" multiply by "cost normal post 1 (20 um/dt)", and "Post 2" is multiplied by "cost normal post 2 (30 um/dt)"

| COSTURI NORMALE POSTURI |        |        |  |      |  |  |  |  |
|-------------------------|--------|--------|--|------|--|--|--|--|
| Interval                |        |        |  | Post |  |  |  |  |
| (zile)                  | Post 1 | Post 2 |  | n    |  |  |  |  |
| 0                       |        |        |  |      |  |  |  |  |
| 1                       | 7040   | 300    |  |      |  |  |  |  |
| 2                       | 10080  | 12900  |  |      |  |  |  |  |
| 3                       | 10720  | 14700  |  |      |  |  |  |  |
| 4                       | 9920   | 15000  |  |      |  |  |  |  |

| 5 | 9600 | 5400 |  |
|---|------|------|--|
| 6 | 6720 | 5400 |  |

#### For OVERTIME TIMES WORKSTATIONS:

IF(SUM("paleti tip 1", "paleti tip 2", "paleti tip 3") - "limita timp (overtime) post 1..n(480 minutes)" greater or equal to 0, SUM("paleti tip 1", "paleti tip 2", "paleti tip 3") – "limita timp (normal) post 1..n(480 minutes)"

|                    | TIMPI OVERTIME POSTURI |        |  |           |  |  |  |
|--------------------|------------------------|--------|--|-----------|--|--|--|
| Interval<br>(zile) | Post 1                 | Post 2 |  | Post<br>n |  |  |  |
| 0                  |                        |        |  | •         |  |  |  |
| 1                  | 0                      | 0      |  |           |  |  |  |
| 2                  | 24                     | 0      |  |           |  |  |  |
| 3                  | 56                     | 10     |  |           |  |  |  |
| 4                  | 16                     | 20     |  | •         |  |  |  |
| 5                  | 0                      | 0      |  | •         |  |  |  |
| 6                  | 0                      | 0      |  | •         |  |  |  |

# For OVERTIME COSTS WORKSTATIONS:

Here we calculate from the previous table "Post 1"  $^{*}$  "cost overtime post 1 (40 um/dt)",

And same for the second workstation: "Post 2" \* "cost overtime post 2 (60 um/dt)".

|                    | COSTURI OVERTIME POSTURI |        |  |           |  |  |  |  |
|--------------------|--------------------------|--------|--|-----------|--|--|--|--|
| Interval<br>(zile) | Post 1                   | Post 2 |  | Post<br>n |  |  |  |  |
| 0                  |                          |        |  |           |  |  |  |  |
| 1                  | 0                        | 0      |  |           |  |  |  |  |
| 2                  | 960                      | 0      |  |           |  |  |  |  |
| 3                  | 2240                     | 600    |  |           |  |  |  |  |
| 4                  | 640                      | 1200   |  |           |  |  |  |  |
| 5                  | 0                        | 0      |  |           |  |  |  |  |
| 6                  | 0                        | 0      |  |           |  |  |  |  |

#### **For STORAGE COSTS:**

From the main table we calculate for each individual day: sum of "paleti tip 1/2/3" from the both workstations then we subtract with "Cerere client pe interval", then adding "Stoc platibil (in plus fata de intervalul urmator)", and the resulted number is multiplied with "cost mentinere 1 palet 1 interval de timp (20 um)"

| COSTURI<br>STOCARE |      |  |  |  |
|--------------------|------|--|--|--|
| Interval<br>(zile) |      |  |  |  |
| 0                  |      |  |  |  |
| 1                  | 600  |  |  |  |
| 2                  | 940  |  |  |  |
| 3                  | 700  |  |  |  |
| 4                  | -620 |  |  |  |
| 5                  | 740  |  |  |  |
| 6                  | 1100 |  |  |  |

And for the final <u>COST</u> we make a final sum between the "COSTURI NORMALE POSTURI", "COSTURI OVERTIME POSTURI", "COSTURI STOCARE".

B\$5:\$G\$10 = integer and >= 0,

\$J\$5:\$R\$10 greater or equal to 0, as last three constraints

| COST | 116880 |
|------|--------|