

## Instructions of as use the runvectors2dim.py program.

In the Windows operating system:

After the download the [repositorio](#) access the `runvectors2dim.py` program given two clicks and follow the news instructions in display.

In the Linux operating system:

After the download the [repositorio](#) access the `runvectors2dim.py` program. Exist two options to run the `runvectors2dim.py` program.

1.) In any Terminal linux type the following command:

`python3 runvectors2dim.py` after key ENTER

2.) Open the `runvectors2dim.py` file using the IDLE3 and use the Run ==> Run Module options. After follow the news instructions.

**[Warning]:** When the `runvectors2dim.py` program request type the `[components]` or `[coordinates]`, always key ENTER after to continue, Ok!

Now will use the `runvectors2dim.py` program in the examples below.

**Example1** – Given the vectors:  $a = \langle 3, 1 \rangle$  and  $b = \langle -2, 4 \rangle$ , find the Scalar Product  $a \cdot b$  of this vectors.

**Solution:** Use the option: [1] and enter the `[components]`:  $a_1 = 3$ ,  $a_2 = 1$ ,  $b_1 = -2$ , and  $b_2 = 4$  when requested by `runvectors2dim.py` program.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
--[Version: 1.2 -- Stable]--
```

```
**[INSTRUCTIONS OF USE]**
```

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h), and [Area(A)] of the TrianglePQR givens the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors] A and B multiplyed by scalars[coeffic1 and coeffic2] key [12]

```
[$] Select an previous [option] that will used--Ok!
```

```
(^>^) Provide the [new] value? 1
```

```
**[The typed number]: 1 is a [valid integer number!] ]**
```

**\*\*[TO FIND THE [SCALAR PRODUCT] OF [TWO VECTORS: A and B] IN THE BI-DIMENSIONAL(XY) PLANE]\*\***

- Attribute the [Components] of the [1° vectorA]!

- Enter the 1° [Component(x)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 3

\*\*[ [The typed number]: 3.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 1

\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

- Provide the [Components] of the [2° vectorB]!

- Enter the 1° [Component(x)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? -2

\*\*[ [The typed number]: -2.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 4

\*\*[ [The typed number]: 4.0 is a [valid integer or float number!] ]\*\*

-- The [vectorA]: vectorA [3.0, 1.0]

-- The [vectorB]: vectorB [-2.0, 4.0]

**\*[ANSWER]\***

-- The [Vector] of the [terms of the Scalar Product]: vectorAB [-6.0, 4.0]

-- The [Scalar Product(vectorAB)] of the vectors is: -2.00

. . . Key [ENTER] to exit -- Ok! . . .

### **[Warning]:**

When any user run the **runvectors2dim.py program** to solve exercises that provide vertexes A, B, and C to triangles do the following:

(xA,yA) = (xP, yP) ==> xP = xA and yP = yA replace the coordinates: xA and yA into the coordinates: xP and yP of the point: P when the runvectors2dim.py program request to enter the coordinates: xP and yP. Of the same manner to the vertexes B and C so:

(xB,yB) = (xQ, yQ) ==> xQ = xB and yQ = yB replace the coordinates: xB and yB into the coordinates: xQ and yQ of the point: Q when the runvectors2dim.py program request to enter the coordinates: xQ and yQ.

(xC,yC) = (xR, yR) ==> xR = xC and yR = yC replace the coordinates: xC and yC into the coordinates: xR and yR of the point: R when the runvectors2dim.py program request to enter the coordinates: xR and yR.

Of the same manner do to the vertexes: A, B, C, and D of the parallelogram as too to the parallelepiped. Replace your coordinates when the runvectors2dim.py program request enter the coordinates of the points: P, Q, R, and S.

Will be confused standardize the letters: A, B, and C to the vectors and too to the vertexes points: A, B, and C of the triangle into the code of functions developed.

**Example** – Find the dimensions of the triangle ABC with vertexes points: A(-1,0), B(2,1), and C(1,-2)

**Solution:** Do:  $A(-1,0) = P(x_P, y_P) \Rightarrow x_P = -1$ , and  $y_P = 0$   
 $B(2,1) = Q(x_Q, y_Q) \Rightarrow x_Q = 2$ , and  $y_Q = 1$   
 $C(1,-2) = R(x_R, y_R) \Rightarrow x_R = 1$ , and  $y_R = -2$

Begin using the option[2] and provide the coordinates:  $x_P = -1$ ,  $y_P = 0$ ,  $x_Q = 2$ ,  $y_Q = 1$ ,  $x_R = 1$ , and  $y_R = -2$ , when the **runvectors2dim.py program** request.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**  
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**  
--[Version: 1.2 -- Stable]--
```

```
**[INSTRUCTIONS OF USE]**
```

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR givens the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M( $x_M, y_M$ )] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subraction] between [Two Vectors] A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

```
[$] Select an previous [option] that will used--Ok!
```

```
(^>^>) Provide the [new] value? 2
```

```
**[The typed number]: 2 is a [valid integer number!] ]**
```

```
**[TO CALCULATE THE [PERIMETER(P), HEIGHTS(H1,H2,H3),AND AREA(A) OF THE]**  
**[[TRIANGLE-PQR] GIVENS THE POINTS: P, Q, AND R IN THE BI-DIMENSIONAL(XY)  
PLANE]**
```

```
-- Enter the [coordinates]: (xP, yP) of the (point P)?
```

```
* Introduce the 1° [Coordinate(x)].
```

```
(^<^<) Enter the [new] value? -1
```

```
**[ [The typed number]: -1.0 is a [valid integer or float number!] ]**
```

\* Enter with the 2° [Coordinate(y)].  
(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 0  
\*\*[ [The typed number]: 0.0 is a [valid integer or float number!] ]\*\*

-- Introduce the [coordinates]: (xQ, yQ) of the (point Q)?

\* Introduce the 1° [Coordinate(x)].  
(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 2  
\*\*[ [The typed number]: 2.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].  
(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 1  
\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

-- Provide the [coordinates]: (xR, yR) of the (point R)?

\* Introduce the 1° [Coordinate(x)].  
(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 1  
\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].  
(<sup>a</sup><<sup>a</sup>) Enter the [new] value? -2  
\*\*[ [The typed number]: -2.0 is a [valid integer or float number!] ]\*\*

- The (Point P): P (-1.0, 0.0)  
- The (Point Q): Q (2.0, 1.0)  
- The (Point R): R (1.0, -2.0)

\*[ANSWER]\*

-- The [vectorA] = vectorQR [-1.0, -3.0]  
-- The [vectorB] = vectorRP [-2.0, 2.0]  
-- The [vectorC] = vectorPQ [3.0, 1.0]

-- The [sideA of the triangle(PQR)] is: 3.16  
-- The [sideB of the triangle(PQR)] is: 2.83  
-- The [sideC of the triangle(PQR)] is: 3.16

-- The [terms] of the [Scalar Product(PQ°QR)] is: [-3.0, -3.0]  
-- The [terms] of the [Scalar Product(QR°RP)] is: [2.0, -6.0]  
-- The [terms] of the [Scalar Product(RP°PQ)] is: [-6.0, 2.0]

-- The [Scalar Product(PQ°QR)] is: -6.00  
-- The [Scalar Product(QR°RP)] is: -4.00  
-- The [Scalar Product(RP°PQ)] is: -4.00

-- The [Perimeter] of the [triangle(PQR)] is 9.15  
-- The [Height(h1) relative as sideQR] is 2.53  
-- The [Height(h2) relative as sideRP] is 2.83  
-- The [Height(h3) relative as sidePQ] is 2.53  
-- The [Area(A)] of the [triangle(PQR)] is 4.00

. . . Key [ENTER] to exit -- Ok! . . .

To calculate all the three Inner angles of the triangle type the option [7] when requested by runvectors2dim.py program.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
--[Version: 1.2 -- Stable]--
```

```
**[INSTRUCTIONS OF USE]**
```

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR gives the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subraction] between [Two Vectors] A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

```
[$] Select an previous [option] that will used--Ok!
```

```
(^>^ ) Provide the [new] value? 7
```

```
**[The typed number]: 7 is a [valid integer number!] ]**
```

```
**[ TO FIND THE THREES [INNER ANGLES] OF THE [TRIANGLE(PQR)] ]**
```

```
-- Enter the [coordinates]: (xP, yP) of the (point P)?
```

```
* Introduce the 1° [Coordinate(x)].
```

```
(^<^ ) Enter the [new] value? -1
```

```
**[ [The typed number]: -1.0 is a [valid integer or float number!] ]**
```

```
* Enter with the 2° [Coordinate(y)].
```

```
(^<^ ) Enter the [new] value? 0
```

```
**[ [The typed number]: 0.0 is a [valid integer or float number!] ]**
```

```
-- Introduce the [coordinates]: (xQ, yQ) of the (point Q)?
```

```
* Introduce the 1° [Coordinate(x)].
```

```
(^<^ ) Enter the [new] value? 2
```

```
**[ [The typed number]: 2.0 is a [valid integer or float number!] ]**
```

```
* Enter with the 2° [Coordinate(y)].
```

```
(^<^ ) Enter the [new] value? 1
```

```
**[ [The typed number]: 1.0 is a [valid integer or float number!] ]**
```

-- Provide the [coordinates]: (xR, yR) of the (point R)?

\* Introduce the 1° [Coordinate(x)].

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 1

\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? -2

\*\*[ [The typed number]: -2.0 is a [valid integer or float number!] ]\*\*

- The (Point P): P (-1.0, 0.0)

- The (Point Q): Q (2.0, 1.0)

- The (Point R): R (1.0, -2.0)

\*[ANSWER]\*

- The [vectorB]=vectorPR [2.0, -2.0]

- The [vectorC]=vectorPQ [3.0, 1.0]

- The Scalar Product: [b \* c] is: 4.00

- The value of the [ANGLE ALPHA] was calculate is: 63.43

- The [vectorA]=vectorQR [-1.0, -3.0]

- The [vectorC]=vectorQP [-3.0, -1.0]

- The Scalar Product: [a \* c] is: 6.00

- The value of the [ANGLE BETA] was calculate is: 53.13

- The [vectorA]=vectorRQ [1.0, 3.0]

- The [vectorB]=vectorRP [-2.0, 2.0]

- The Scalar Product: [a \* b] is: 4.00

- The value of the [ANGLE GAMA] was calculate is: 63.43

-- The triangle is [Isosceles]!

- THE [ADD] OF THE [INNER ANGLES] OF THE [TRIANGLE-PQR] is: 180.00

--[END CALCULUS-OK!!--

. . . Key [ENTER] to exit -- Ok! . . .

**Example2** – Find the measures of the sides: sideA, sideB, and sideC, perimeter(P), height(h1,h2,h3), area(A), Scalar Products: c\*a, b\*c, a\*b, and the inner angles of the Triangle whose vertexes are P(-6,0), Q(10,-5), and R(-2, 4).

**Solution:** To find the sides: sideA, sideB, and sideC as too the perimeter(P), area(A) key in the option: [2] and after ENTER. Wait the runvectors2dim.py program request enter the coodinates of the points: P, Q, and R according viewed below.

\*\*[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]\*\*

\*\*[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]\*\*

--[Version: 1.2 -- Stable]--

**\*\*[INSTRUCTIONS OF USE]\*\***

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR gives the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subraction] between [Two Vectors] A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

[§] Select an previous [option] that will used--Ok!

(°>°) Provide the [new] value? 2

\*\*[The typed number]: 2 is a [valid integer number!] ]\*\*

**\*\*[TO CALCULATE THE [PERIMETER(P), HEIGHTS(H1,H2,H3),AND AREA(A) OF THE]  
\*\*[[TRIANGLE-PQR] GIVENS THE POINTS: P, Q, AND R IN THE BI-DIMENSIONAL(XY)  
PLANE]\*\***

-- Enter the [coordinates]: (xP, yP) of the (point P)?

\* Introduce the 1° [Coordinate(x)].

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? -6

\*\*[ [The typed number]: -6.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 0

\*\*[ [The typed number]: 0.0 is a [valid integer or float number!] ]\*\*

-- Introduce the [coordinates]: (xQ, yQ) of the (point Q)?

\* Introduce the 1° [Coordinate(x)].

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 10

\*\*[ [The typed number]: 10.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? -5

\*\*[ [The typed number]: -5.0 is a [valid integer or float number!] ]\*\*

-- Provide the [coordinates]: (xR, yR) of the (point R)?

\* Introduce the 1° [Coordinate(x)].

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? -2

\*\*[ [The typed number]: -2.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].  
 (°<°) Enter the [new] value? 4  
 \*\*[ [The typed number]: 4.0 is a [valid integer or float number!] ]\*\*

- The (Point P): P (-6.0, 0.0)
- The (Point Q): Q (10.0, -5.0)
- The (Point R): R (-2.0, 4.0)

\*[ANSWER]\*

- The [vectorA] = vectorQR [-12.0, 9.0]
- The [vectorB] = vectorRP [-4.0, -4.0]
- The [vectorC] = vectorPQ [16.0, -5.0]

- The [sideA of the triangle(PQR)] is: 15.00
- The [sideB of the triangle(PQR)] is: 5.66
- The [sideC of the triangle(PQR)] is: 16.76

- The [terms] of the [Scalar Product(PQ°QR)] is: [-192.0, -45.0]
- The [terms] of the [Scalar Product(QR°RP)] is: [48.0, -36.0]
- The [terms] of the [Scalar Product(RP°PQ)] is: [-64.0, 20.0]

- The [Scalar Product(PQ°QR)] is: -237.00
- The [Scalar Product(QR°RP)] is: 12.00
- The [Scalar Product(RP°PQ)] is: -44.00

- The [Perimeter] of the [triangle(PQR)] is 37.42
- The [Height(h1) relative as sideQR] is 5.60
- The [Height(h2) relative as sideRP] is 14.85
- The [Height(h3) relative as sidePQ] is 5.01
- The [Area(A)] of the [triangle(PQR)] is 42.00

. . . Key [ENTER] to exit -- Ok! . . .

To calculate all the threes Inner angles of the triangle type the option [7] when requested by runvectors2dim.py program.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
--[Version: 1.2 -- Stable]--
```

\*\*[INSTRUCTIONS OF USE]\*\*

- To find the [Scalar Product: a \* b] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h), and [Area(A)] of the TrianglePQR given the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]



- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors]
- A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

[§] Select an previous [option] that will used--Ok!

(°>°) Provide the [new] value? 7

\*\*[The typed number]: 7 is a [valid integer number!] ]\*\*

\*\*[ TO FIND THE THREES [INNER ANGLES] OF THE [TRIANGLE(PQR)] ]\*\*

-- Enter the [coordinates]: (xP, yP) of the (point P)?

\* Introduce the 1° [Coordinate(x)].

(^<^ ) Enter the [new] value? -6

\*\*[ [The typed number]: -6.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(^<^ ) Enter the [new] value? 0

\*\*[ [The typed number]: 0.0 is a [valid integer or float number!] ]\*\*

-- Introduce the [coordinates]: (xQ, yQ) of the (point Q)?

\* Introduce the 1° [Coordinate(x)].

(^<^ ) Enter the [new] value? 10

\*\*[ [The typed number]: 10.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(^<^ ) Enter the [new] value? -5

\*\*[ [The typed number]: -5.0 is a [valid integer or float number!] ]\*\*

-- Provide the [coordinates]: (xR, yR) of the (point R)?

\* Introduce the 1° [Coordinate(x)].

(^<^ ) Enter the [new] value? -2

\*\*[ [The typed number]: -2.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(^<^ ) Enter the [new] value? 4

\*\*[ [The typed number]: 4.0 is a [valid integer or float number!] ]\*\*

- The (Point P): P (-6.0, 0.0)

- The (Point Q): Q (10.0, -5.0)

- The (Point R): R (-2.0, 4.0)

\*[ANSWER]\*

- The [vectorB]=vectorPR [4.0, 4.0]

- The [vectorC]=vectorPQ [16.0, -5.0]

- The Scalar Product: [b \* c] is: 44.00

- The value of the [ANGLE ALPHA] was calculate is: 62.35

- The [vectorA]=vectorQR [-12.0, 9.0]
- The [vectorC]=vectorQP [-16.0, 5.0]

- The Scalar Product: [a \* c] is: 237.00
- The value of the [ANGLE BETA] was calculate is: 19.52

- The [vectorA]=vectorRQ [12.0, -9.0]
- The [vectorB]=vectorRP [-4.0, -4.0]

- The Scalar Product: [a \* b] is: -12.00
- The value of the [ANGLE GAMA] was calculate is: 98.13

-- The triangle is [Scalene]!

- THE [ADD] OF THE [INNER ANGLES] OF THE [TRIANGLE-PQR] is: 180.00

--[END CALCULUS-OK!]

. . . Key [ENTER] to exit -- Ok! . . .

**Example3** – Find the cosine of the angle between the vectors  $a = i - 3j$  and  $b = -4i + j$ .

**Solution:** Use the option: [5] and enter the [components]:  $a_1 = 1$ ,  $a_2 = -3$ ,  $b_1 = -4$ , and  $b_2 = 1$  when requested by runvectors2dim.py program.

```

**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
--[Version: 1.2 -- Stable]--

```

**\*\*[INSTRUCTIONS OF USE]\*\***

- To find the [Scalar Product: a \* b] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h), and [Area(A)] of the TrianglePQR givens the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors] A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

[\$] Select an previous [option] that will used--Ok!

(°>°) Provide the [new] value? 5

\*\*[The typed number]: 5 is a [valid integer number!] ]\*\*

```
**[TO CALCULATE THE [VALUE] OF THE [COSSINE THETA] BETWEEN  
[TWO VECTORS] GIVEN: A AND B]**
```

- Attribute the [Components] of the [1° vectorA]!

- Enter the 1° [Component(x)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 1

\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? -3

\*\*[ [The typed number]: -3.0 is a [valid integer or float number!] ]\*\*

- Provide the [Components] of the [2° vectorB]!

- Enter the 1° [Component(x)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? -4

\*\*[ [The typed number]: -4.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 1

\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

-- The [vectorA]: vectorA [1.0, -3.0]

-- The [vectorB]: vectorB [-4.0, 1.0]

\*[ANSWER]\*

- The [VectorA\*B]: [-4.0, -3.0]

- The [length] of a [vectorA]: 3.16

- The [length] of a [vectorB]: 4.12

- The [Scalar Product] of the [VectorA\*B] is: -7.00

- The value of the [COSINE THETA IN RADIANS] calculated is: -0.54

. . . Key [ENTER] to exit -- Ok! . . .

**Example4** – Find the [distance] between the points: P(3,-5), and Q(2,8).

**Solution:** Use the option: [6] and after provide the coordinates of the points when requested by runvectors2dim.py program.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
```

```
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
```

```
--[Version: 1.2 -- Stable]--
```

```
**[INSTRUCTIONS OF USE]**
```

- To find the [Scalar Product: a \* b] between [two vectors] key [1]

- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR givens the [points: P, Q, and R] key[2]

- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given

the [points: P, Q, R, and S] key[3]

- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors] A and B multiplyed by scalars[coeffic1 and coeffic2] key [12]

[§] Select an previous [option] that will used--Ok!

(°>°) Provide the [new] value? 6

\*\*[The typed number]: 6 is a [valid integer number!] ]\*\*

\*\*[TO GET THE [DISTANCE(D)] BETWEEN ANY [TWO POINTS] GIVEN P AND Q]\*\*

-- Enter the [coordinates]: (xP, yP) of the (point P)?

\* Introduce the 1° [Coordinate(x)].

(^<^ ) Enter the [new] value? 3

\*\*[ [The typed number]: 3.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(^<^ ) Enter the [new] value? -5

\*\*[ [The typed number]: -5.0 is a [valid integer or float number!] ]\*\*

-- Introduce the [coordinates]: (xQ, yQ) of the (point Q)?

\* Introduce the 1° [Coordinate(x)].

(^<^ ) Enter the [new] value? 2

\*\*[ [The typed number]: 2.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(^<^ ) Enter the [new] value? 8

\*\*[ [The typed number]: 8.0 is a [valid integer or float number!] ]\*\*

- The (Point P): P (3.0, -5.0)

- The (Point Q): Q (2.0, 8.0)

\*[ANSWER]\*

-- The [vectorPQ]: vectorPQ [-1.0, 13.0]

-- The [Quadratic Components] of the [vectorPQ]: VectorQUAD [1.0, 169.0]

-- The [Distance(D)] geted between Two (Points) P and Q is: 13.04

. . . Key [ENTER] to exit -- Ok! . . .

**Example5** – Find the Area(A) and Height(h) of the parallelogram whose vertexes are the points: P(-1,2), Q(2,0), R(7,1), and S(4,3).

**Solution:** Use the option: [3] and after provide the [coordinates] of the points when requested by runvectors2dim.py program.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
--[Version: 1.2 -- Stable]--
```

```
**[INSTRUCTIONS OF USE]**
```

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR givens the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M( $x_M, y_M$ )] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R| Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors] A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

```
[$] Select an previous [option] that will used--Ok!
```

```
(^>^ ) Provide the [new] value? 3
```

```
**[The typed number]: 3 is a [valid integer number!] ]**
```

```
**[TO GET THE [AREA(S) AND HEIGHT(H) OF THE [PARALLELOGRAM(PQRS)] GIVEN ]**
**[THE POINTS: P, Q, R AND S IN THE BI-DIMENSIONAL(XY) PLANE]**
```

```
-- Enter the [coordinates]: (xP, yP) of the (point P)?
```

```
* Introduce the 1° [Coordinate(x)].
```

```
(^<^ ) Enter the [new] value? -1
```

```
**[ [The typed number]: -1.0 is a [valid integer or float number!] ]**
```

```
* Enter with the 2° [Coordinate(y)].
```

```
(^<^ ) Enter the [new] value? 2
```

```
**[ [The typed number]: 2.0 is a [valid integer or float number!] ]**
```

```
-- Introduce the [coordinates]: (xQ, yQ) of the (point Q)?
```

```
* Introduce the 1° [Coordinate(x)].
```

```
(^<^ ) Enter the [new] value? 2
```

```
**[ [The typed number]: 2.0 is a [valid integer or float number!] ]**
```

```
* Enter with the 2° [Coordinate(y)].
(a<a) Enter the [new] value? 0
**[ [The typed number]: 0.0 is a [valid integer or float number!] ]**
```

```
-- Provide the [coordinates]: (xR, yR) of the (point R)?
```

```
* Introduce the 1° [Coordinate(x)].
(a<a) Enter the [new] value? 7
**[ [The typed number]: 7.0 is a [valid integer or float number!] ]**
```

```
* Enter with the 2° [Coordinate(y)].
(a<a) Enter the [new] value? 1
**[ [The typed number]: 1.0 is a [valid integer or float number!] ]**
```

```
-- Provide the [coordinates]: (xS, yS) of the (point S)?
```

```
* Introduce the 1° [Coordinate(x)].
(a<a) Enter the [new] value? 4
**[ [The typed number]: 4.0 is a [valid integer or float number!] ]**
```

```
* Enter with the 2° [Coordinate(y)].
(a<a) Enter the [new] value? 3
**[ [The typed number]: 3.0 is a [valid integer or float number!] ]**
```

```
- The (Point P): P (-1.0, 2.0)
- The (Point Q): Q (2.0, 0.0)
- The (Point R): R (7.0, 1.0)
- The (Point S): S (4.0, 3.0)
```

```
*[ANSWER]*
```

```
-- The [vectorPQ]:vectorPQ [3.0, -2.0]
-- The [vectorPS]:vectorPS [5.0, 1.0]
```

```
-- The [sideA] relative as [vectorPQ]: 3.61
-- The [sideB] relative as [vectorPS]: 5.10
-- The [Perimeter(P)] is: 17.41
```

```
-- The [terms] of the Scalar Product(vectorPS°PQ) is: [15.0, -2.0]
-- The [Scalar Product(PQ°PS)] is: 13.0
-- The [Height(h)] relative as [sideA]=|vectorPQ| is: 3.61
-- The [Area(S)] of the [Parallelogram(PQRS)]: 13.00
```

```
. . . Key [ENTER] to exit -- Ok! . . .
```

**Example6** – Find the addition and subtraction of the vectors  $a = -11i + 4j$  and  $b = 3i - j$ .

**Solution:** Use the option: [9] and enter the [components]:  $a_1 = -11$ ,  $a_2 = 4$ ,  $b_1 = 3$ , and  $b_2 = -1$  when requested by runvectors2dim.py program.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
--[Version: 1.2 -- Stable]--
```

**\*\*[INSTRUCTIONS OF USE]\*\***

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR given the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors] A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

[§] Select an previous [option] that will used--Ok!

(°>°) Provide the [new] value? 9

\*\*[The typed number]: 9 is a [valid integer number!] ]\*\*

**\*\*[TO FIND THE [ADDITION AND SUBTRACTION] OF [TWO VECTORS: A and B] IN THE BI-DIMENSIONAL(XY) PLANE]\*\***

- Attribute the [Components] of the [1° vectorA]!

- Enter the 1° [Component(x)]!

(^<^a) Enter the [new] value? -11

\*\*[ [The typed number]: -11.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(^<^a) Enter the [new] value? 4

\*\*[ [The typed number]: 4.0 is a [valid integer or float number!] ]\*\*

- Provide the [Components] of the [2° vectorB]!

- Enter the 1° [Component(x)]!

(^<^a) Enter the [new] value? 3

\*\*[ [The typed number]: 3.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(^<^a) Enter the [new] value? -1

\*\*[ [The typed number]: -1.0 is a [valid integer or float number!] ]\*\*

-- The [vectorA]: vectorA [-11.0, 4.0]

-- The [vectorB]: vectorB [3.0, -1.0]

\*[ANSWER]\*

- The [Addition]: vector[a+b]: [-8.0, 3.0]
- The [Subtraction]: vector[a-b]: [-14.0, 5.0]

. . . Key [ENTER] to exit -- Ok! . . .

**Example7** – Find the angle between the vectors  $a = -3i + 5$  and  $b = 7i - 2j$ .

**Solution:** Use the option: [4] and enter the [components]:  $a_1 = -3$ ,  $a_2 = 5$ ,  $b_1 = 7$ , and  $b_2 = -2$  when requested by runvectors2dim.py program.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
--[Version: 1.2 -- Stable]--
```

\*\*[INSTRUCTIONS OF USE]\*\*

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR gives the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors] A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

[\$] Select an previous [option] that will used--Ok!

(°>°) Provide the [new] value? 4

\*\*[The typed number]: 4 is a [valid integer number!] ]\*\*

\*\*[WILL FIND THE [VALUE] OF THE [THETA ANGLE] BETWEEN [TWO VECTORS] GIVEN: A AND B]\*\*

- Attribute the [Components] of the [1° vectorA]!

- Enter the 1° [Component(x)]!

(^<^a) Enter the [new] value? -3

\*\*[ [The typed number]: -3.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(^<^a) Enter the [new] value? 5

\*\*[ [The typed number]: 5.0 is a [valid integer or float number!] ]\*\*



- Provide the [Components] of the [2° vectorB]!

- Enter the 1° [Component(x)]!

(<sup>a<a</sup>) Enter the [new] value? 7

\*\*[ [The typed number]: 7.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(<sup>a<a</sup>) Enter the [new] value? -2

\*\*[ [The typed number]: -2.0 is a [valid integer or float number!] ]\*\*

-- The [vectorA]: vectorA [-3.0, 5.0]

-- The [vectorB]: vectorB [7.0, -2.0]

\*[ANSWER]\*

- The [terms] of the [VectorA\*B] is: [-21.0, -10.0]

- The [length] of a [vectorA]: 5.83

- The [length] of a [vectorB]: 7.28

- The [Scalar Product] is: -31.00

- The value of the [THETA ANGLE IN DEGREES] was calculate is: 136.91

. . . Key [ENTER] to exit -- Ok! . . .

**Example8** – The three displacement vectors A, B, and C are specified by their magnitudes  $A = 10$ ,  $B = 7$ , and  $C = 8$ , respectively, and by their respective direction angles with the horizontal direction  $\theta = 35^\circ$ ,  $\beta = -110^\circ$ , and  $\phi = 30^\circ$ . The physical units of the magnitudes are centimeters. Find the Resultant(|R) Vector.

**Solution:** Use the option: [10] and enter the data problem when requested by runvectors2dim.py program.

\*\*[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]\*\*

\*\*[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]\*\*

--[Version: 1.2 -- Stable]--

\*\*[INSTRUCTIONS OF USE]\*\*

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]

- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR given the [points: P, Q, and R] key[2]

- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]

- To find the [angle] between [two vectors] in plane key[4]

- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]

- To get the [Distance] between [two points] given P and Q key [6]

- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]

- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]

- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]

- To calculate the [Resultant(|R) Vector] key [10]

- To find the[VectorA] and [length] of givens Points: P, AND Q key [11]

- To find the [Addition] and [Subtraction] between [Two Vectors]  
A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

[§] Select an previous [option] that will used--Ok!

(°>°) Provide the [new] value? 10

\*\*[The typed number]: 10 is a [valid integer number!] ]\*\*

\*\*[TO GET THE VALUE OF THE RESULTANT(|R) VECTOR]\*\*

+ How much [Vectors] will necessary to get the [Resultant(R) Vector]?

(°>°) Provide the [new] value? 3

\*\*[The typed number]: 3 is a [valid integer number!] ]\*\*

\*\*[Warning]\*\*

- All the [Vectorials Components] will can be:  
[positive] or [negative] or Zero!

+ What are the arguments: [angle] and [radius] of the( 1 )[vector]?

- Enter with the [new value] of the [angle] in degree?

(^<^a) Enter the [new] value? 35

\*\*[ [The typed number]: 35.0 is a [valid integer or float number!] ]\*\*

- Provide the [new value] of the [radius] of vector?

(^<^a) Enter the [new] value? 10

\*\*[ [The typed number]: 10.0 is a [valid integer or float number!] ]\*\*

\_ \_ . . .[Running]. . . \_ \_

\* [answer] \*

- The component of the 1 vector:  $V_x(1) = 8.19$

- The component of the 1 vector:  $V_y(1) = 5.74$

+ What are the arguments: [angle] and [radius] of the( 2 )[vector]?

- Enter with the [new value] of the [angle] in degree?

(^<^a) Enter the [new] value? -110

\*\*[ [The typed number]: -110.0 is a [valid integer or float number!] ]\*\*

- Provide the [new value] of the [radius] of vector?

(^<^a) Enter the [new] value? 7

\*\*[ [The typed number]: 7.0 is a [valid integer or float number!] ]\*\*

\_ \_ . . .[Running]. . . \_ \_

\* [answer] \*

- The component of the 2 vector:  $V_x(2) = -2.39$

- The component of the 2 vector:  $V_y(2) = -6.58$

+ What are the arguments: [angle] and [radius] of the( 3 )[vector]?

- Enter with the [new value] of the [angle] in degree?

(^<^a) Enter the [new] value? 30

```
**[ [The typed number]: 30.0 is a [valid integer or float number!] ]**
```

- Provide the [new value] of the [radius] of vector?

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 8

```
**[ [The typed number]: 8.0 is a [valid integer or float number!] ]**
```

```
_ _ . . . [Running]. . . _ _
```

```
* [answer] *
```

- The component of the 3 vector:  $V_x(3) = 6.93$

- The component of the 3 vector:  $V_y(3) = 4.00$

+ The sum of all the components of x\_axis:  $R_x = 12.73$

+ The sum of all the components of y\_axis:  $R_y = 3.16$

+ The resultant vector:  $[Resultant(R)_Vector] = 13.11$

+ The theta angle  $[theta\_degrees] = 13.94$

```
**[End Processing of the [ RESULTANTVECTOR.PY FUNCTION ]--Ok! ]**
```

. . . Key [ENTER] to exit -- Ok! . . .

**Example9** – Given the vectors:  $a = 2i + 3j$  and  $b = 5i - j$  find the [vectors and modules]:  $a + b$ ,  $a - b$ ,  $|a + b|$ ,  $|a - b|$ , and  $2a - 3b$ .

**Solution** – Begin the runtoolsvectors.py program and key the option[12] and wait the display present instructions to select the options: [1] or [2]. Follow type the option[1] and provide the [components];  $a_1 = 2$ ,  $a_2 = 3$ ,  $b_1 = 5$ , and  $b_2 = -1$ . Following the program will wait the user enter the [coefficients]. Do (1°)  $[coefficient] = 1$  and (2°)  $[coefficient] = 1$  and key ENTER to process.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
```

```
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
```

```
--[Version: 1.2 -- Stable]--
```

```
**[INSTRUCTIONS OF USE]**
```

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]

- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR given the [points: P, Q, and R] key[2]

- To get the [Area(S) and Height(h)] of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]

- To find the [angle] between [two vectors] in plane key[4]

- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]

- To get the [Distance] between [two points] given P and Q key [6]

- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]

- To calculate the [midPoint M( $x_M, y_M$ )] between the points: P and Q key [8]

- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]

- To calculate the [Resultant(|R) Vector] key [10]

- To find the [VectorA] and [length] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors] A and B multiplied by scalars [coeffic1 and coeffic2] key [12]

[§] Select an previous [option] that will used--Ok!

(<sup>0</sup>><sup>0</sup>) Provide the [new] value? 12

\*\*[The typed number]: 12 is a [valid integer number!] ]\*\*

\*\*[ GIVENS [TWO VECTORS: A AND B] MULTIPLIED BY THE [SCALARS]: [COEFFIC1] AND [COEFFIC2] OR ]\*\*

\*\*[ GIVENS [THE POINTS: P, Q, AND R] FIND [TWO VECTORS]: VECTOR(A)=VECTOR(PQ) AND VECTOR(B)=VECTOR(PR) ]\*\*

\*\*[ AND MULTIPLY BY THE [SCALARS]: [COEFFIC1] AND [COEFFIC2] AND TOO GET THE [ADDITION] AND [SUBTRACTION] ]\*\*

- To enter the [Components] of the [vectors] type [1].
- To introduce the [Coordinates] of the [points] type [2].

(<sup>0</sup>><sup>0</sup>) Provide the [new] value? 1

\*\*[The typed number]: 1 is a [valid integer number!] ]\*\*

- Provide the [Components] of the [vectors]: vectorA and vectorB.

- Attribute the [Components] of the [1° vectorA]!

- Enter the 1° [Component(x)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 2

\*\*[ [The typed number]: 2.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 3

\*\*[ [The typed number]: 3.0 is a [valid integer or float number!] ]\*\*

- Provide the [Components] of the [2° vectorB]!

- Enter the 1° [Component(x)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 5

\*\*[ [The typed number]: 5.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? -1

\*\*[ [The typed number]: -1.0 is a [valid integer or float number!] ]\*\*

-- The [vectorA]: vectorA [2.0, 3.0]

-- The [vectorB]: vectorB [5.0, -1.0]

- Enter with new [value] to the (1°)[coefficient]?

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 1

\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

- Give the new [value] to the (2°)[coefficient]?

(<sup>a</sup><<sup>a</sup>) Enter the [new] value? 1

\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

**\*[ANSWER]\***

```
+ The [product]: [vectorA]*[scalar(coeffic1)]=vectorAcoeffic1 [2.0, 3.0]
+ The [product]: [vectorB]*[scalar(coeffic2)]=vectorBcoeffic2 [5.0, -1.0]

-- The [Addition]=[vectorA(coeffic1)+vectorB(coeffic2)] [7.0, 2.0]
-- The [Subtraction]=[vectorA(coeffic1)-vectorB(coeffic2)] [-3.0, 4.0]

-- The [length] of the [vectorAddition] is: 7.28
-- The [length] of the [vectorSubtraction] is: 5.00
```

... Key [ENTER] to exit -- Ok! ...

After the processing previous the [ vectors and modules ]:  $a + b$ ,  $a - b$ ,  $|a + b|$ ,  $|a - b|$  was find.

Now to get the vector:  $2a - 3b$  and module:  $|2a - 3b|$ , run the runtoolsvectors.py program again and key the option[12] and wait the display present instructions to select the options: [1] or [2]. Follow type the option[1] and provide again the [components];  $a_1 = 2$ ,  $a_2 = 3$ ,  $b_1 = 5$ , and  $b_2 = -1$ . Following the program will wait the user enter the [coefficients]. Do (1°)[coefficient] = 2 and (2°)[coefficient] = -3 and key ENTER to process.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**
--[Version: 1.2 -- Stable]--
```

**\*\*[INSTRUCTIONS OF USE]\*\***

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h), and [Area(A)] of the TrianglePQR givens the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subraction] between [Two Vectors] A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

[§] Select an previous [option] that will used--Ok!

(°>°) Provide the [new] value? 12

\*\*[The typed number]: 12 is a [valid integer number!] ]\*\*

```
**[ GIVENS [TWO VECTORS: A AND B] MULTIPLYED BY THE [SCALARS]:
[COEFFIC1] AND [COEFFIC2] OR ]**
```

```
**[ GIVENS [THE POINTS: P, Q, AND R] FIND [TWO VECTORS]:
```

VECTOR(A)=VECTOR(PQ) AND VECTOR(B)=VECTOR(PR) ]\*\*

\*\*[ AND MULTIPLY BY THE [SCALARS]: [COEFFIC1] AND [COEFFIC2] AND  
TOO GET THE [ADDITION] AND [SUBTRACTION] ]\*\*

- To enter the [Components] of the [vectors] type [1].

- To introduce the [Coordinates] of the [points] type [2].

(°>°) Provide the [new] value? 1

\*\*[The typed number]: 1 is a [valid integer number!] ]\*\*

- Provide the [Components] of the [vectors]: vectorA and vectorB.

- Attribute the [Components] of the [1° vectorA]!

- Enter the 1° [Component(x)]!

(^<^ ) Enter the [new] value? 2

\*\*[ [The typed number]: 2.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(^<^ ) Enter the [new] value? 3

\*\*[ [The typed number]: 3.0 is a [valid integer or float number!] ]\*\*

- Provide the [Components] of the [2° vectorB]!

- Enter the 1° [Component(x)]!

(^<^ ) Enter the [new] value? 5

\*\*[ [The typed number]: 5.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(^<^ ) Enter the [new] value? -1

\*\*[ [The typed number]: -1.0 is a [valid integer or float number!] ]\*\*

-- The [vectorA]: vectorA [2.0, 3.0]

-- The [vectorB]: vectorB [5.0, -1.0]

- Enter with new [value] to the (1°)[coefficient]?

(^<^ ) Enter the [new] value? 2

\*\*[ [The typed number]: 2.0 is a [valid integer or float number!] ]\*\*

- Give the new [value] to the (2°)[coefficient]?

(^<^ ) Enter the [new] value? -3

\*\*[ [The typed number]: -3.0 is a [valid integer or float number!] ]\*\*

\*[ANSWER]\*

+ The [product]: [vectorA]\*[scalar(coeffic1)]=vectorAcoeffic1 [4.0, 6.0]

+ The [product]: [vectorB]\*[scalar(coeffic2)]=vectorBcoeffic2 [-15.0, 3.0]

-- The [Addition]=[vectorA(coeffic1)+vectorB(coeffic2)] [-11.0, 9.0]

-- The [Subtraction]=[vectorA(coeffic1)-vectorB(coeffic2)] [19.0, 3.0]

-- The [length] of the |vectorAddition| is: 14.21

-- The [length] of the |vectorSubtraction| is: 19.24

. . . Key [ENTER] to exit -- Ok! . . .

**Example10** – Given the points: P(2, 0), Q(0, 3), and R(3, 4) find the [vectors and modules]:  $a + b$ ,  $a - b$ ,  $|a + b|$ , and  $|a - b|$ .

**Solution** – Begin the runtoolsvectors.py program and key the option[12] and wait the display present instructions to select the options: [1] or [2]. Follow type the option[2] and provide the [coordinates]:  $x_P = 2$ ,  $y_P = 0$ ,  $x_Q = 0$ ,  $y_Q = 3$ ,  $x_R = 3$  and  $y_R = 4$ . Following the program will wait the user enter the [coefficients]. Do (1°)[coefficient] = 1 and (2°)[coefficient] = 1 and key ENTER to process.

```
**[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]**  
**[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]**  
--[Version: 1.2 -- Stable]--
```

```
**[INSTRUCTIONS OF USE]**
```

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h), and [Area(A)] of the TrianglePQR givens the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]
- To calculate the [midPoint M( $x_M, y_M$ )] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R| Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors] A and B multiplied by scalars[coefficient1 and coefficient2] key [12]

```
[$] Select an previous [option] that will used--Ok!
```

```
(°>°) Provide the [new] value? 12
```

```
**[The typed number]: 12 is a [valid integer number!] ]**
```

```
**[ GIVENS [TWO VECTORS: A AND B] MULTIPLIED BY THE [SCALARS]:  
[COEFFIC1] AND [COEFFIC2] OR ]**
```

```
**[ GIVENS [THE POINTS: P, Q, AND R] FIND [TWO VECTORS]:  
VECTOR(A)=VECTOR(PQ) AND VECTOR(B)=VECTOR(PR) ]**
```

```
**[ AND MULTIPLY BY THE [SCALARS]: [COEFFIC1] AND [COEFFIC2] AND  
TOO GET THE [ADDITION] AND [SUBTRACTION] ]**
```

- To enter the [Components] of the [vectors] type [1].
- To introduce the [Coordinates] of the [points] type [2].

```
(°>°) Provide the [new] value? 2
```

```
**[The typed number]: 2 is a [valid integer number!] ]**
```

- Give the [Coordinates] of the [givens points: P and Q].

-- Enter the [coordinates]: (xP, yP) of the (point P)?

\* Introduce the 1° [Coordinate(x)].

(^a<a) Enter the [new] value? 2

\*\*[ [The typed number]: 2.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(^a<a) Enter the [new] value? 0

\*\*[ [The typed number]: 0.0 is a [valid integer or float number!] ]\*\*

-- Introduce the [coordinates]: (xQ, yQ) of the (point Q)?

\* Introduce the 1° [Coordinate(x)].

(^a<a) Enter the [new] value? 0

\*\*[ [The typed number]: 0.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(^a<a) Enter the [new] value? 3

\*\*[ [The typed number]: 3.0 is a [valid integer or float number!] ]\*\*

- The (Point P): P (2.0, 0.0)

- The (Point Q): Q (0.0, 3.0)

\*[ANSWER]\*

-- The [vectorA]: vectorA=vectorPQ [-2.0, 3.0]

-- The [length] of the vectorA=|vectorA|: 3.61

- Enter the [Coordinates] of the [givens points: P and R].

-- Enter the [coordinates]: (xP, yP) of the (point P)?

\* Introduce the 1° [Coordinate(x)].

(^a<a) Enter the [new] value? 2

\*\*[ [The typed number]: 2.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(^a<a) Enter the [new] value? 0

\*\*[ [The typed number]: 0.0 is a [valid integer or float number!] ]\*\*

-- Provide the [coordinates]: (xR, yR) of the (point R)?

\* Introduce the 1° [Coordinate(x)].

(^a<a) Enter the [new] value? 3

\*\*[ [The typed number]: 3.0 is a [valid integer or float number!] ]\*\*

\* Enter with the 2° [Coordinate(y)].

(^a<a) Enter the [new] value? 4

\*\*[ [The typed number]: 4.0 is a [valid integer or float number!] ]\*\*

- The (Point P): P (2.0, 0.0)

- The (Point R): R (3.0, 4.0)



\*[ANSWER]\*

-- The [vectorB]: vectorB=vectorPR [1.0, 4.0]  
-- The [length] of the vectorB=|vectorB|: 4.12

-- The [vectorA]: vectorA [-2.0, 3.0]  
-- The [vectorB]: vectorB [1.0, 4.0]

- Enter with new [value] to the (1°)[coefficient]?

(<sup>a<a</sup>) Enter the [new] value? 1

\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

- Give the new [value] to the (2°)[coefficient]?

(<sup>a<a</sup>) Enter the [new] value? 1

\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

\*[ANSWER]\*

+ The [product]: [vectorA]\*[scalar(coefficient)]=vectorAcoefficient1 [-2.0, 3.0]  
+ The [product]: [vectorB]\*[scalar(coefficient)]=vectorBcoefficient2 [1.0, 4.0]

-- The [Addition]=[vectorA(coefficient1)+vectorB(coefficient2)] [-1.0, 7.0]  
-- The [Subtraction]=[vectorA(coefficient1)-vectorB(coefficient2)] [-3.0, -1.0]

-- The [length] of the |vectorAddition| is: 7.07  
-- The [length] of the |vectorSubtraction| is: 3.16

. . . Key [ENTER] to exit -- Ok! . . .

**[Warning]:** In the new version: 1.2 of the runvectors2dim.py program was improve the security of datas enter to the user type only *positive integer number* in the menu options. View below using the runvectors2dim.py program when any user type: -2 or p or @ or J or 0(zero) or key ENTER.

\*\*[ WELCOME IN USING THE [RUNVECTORS2DIM.PY] PROGRAM ]\*\*  
\*\*[ TO [SOLVE] VARIOUS PROBLEMS OF [VECTORS] in the [PLANE] ]\*\*  
--[Version: 1.2 -- Stable]--

\*\*[INSTRUCTIONS OF USE]\*\*

- To find the [Scalar Product:  $a \cdot b$ ] between [two vectors] key [1]
- To calculate the [Perimeter(P)], [Height(h)], and [Area(A)] of the TrianglePQR gives the [points: P, Q, and R] key[2]
- To get the [Area(S) and Height(h) of the [Parallelogram(PQRS)] given the [points: P, Q, R, and S] key[3]
- To find the [angle] between [two vectors] in plane key[4]
- To calculate the [value] of the [CossineTheta] between [two vectors] a and b key [5]
- To get the [Distance] between [two points] given P and Q key [6]
- To find the three [Inner Angles] of the [Triangle] of three points given: P, Q, R key [7]

- To calculate the [midPoint M(xM,yM)] between the points: P and Q key [8]
- To get the [Addition and Subtraction] of [Two Vectors: a and b] key [9]
- To calculate the [Resultant(|R) Vector] key [10]
- To find the[VectorA] and [lenght] of givens Points: P, AND Q key [11]
- To find the [Addition] and [Subtraction] between [Two Vectors]
- A and B multiplied by scalars[coeffic1 and coeffic2] key [12]

[§] Select an previous [option] that will used--Ok!

(°>°) Provide the [new] value? -2

\*[ NO TYPE AN [NEGATIVE INTEGER NUMBER] or equal [ZERO]--Ok! ]\*

(°>°) Provide the [new] value? p

./§\  
 @>@ [Warning!]: invalid literal for int() with base 10: 'p'  
 \~/ [ TYPE AN [NEW POSITIVE INTEGER NUMBER ]  
 [ IN NEXT INSTRUCTION -- OK! ]

(°>°) Provide the [new] value? @

./§\  
 @>@ [Warning!]: invalid literal for int() with base 10: '@'  
 \~/ [ TYPE AN [NEW POSITIVE INTEGER NUMBER ]  
 [ IN NEXT INSTRUCTION -- OK! ]

(°>°) Provide the [new] value? J

./§\  
 @>@ [Warning!]: invalid literal for int() with base 10: 'J'  
 \~/ [ TYPE AN [NEW POSITIVE INTEGER NUMBER ]  
 [ IN NEXT INSTRUCTION -- OK! ]

(°>°) Provide the [new] value? 0

\*[ NO TYPE AN [NEGATIVE INTEGER NUMBER] or equal [ZERO]--Ok! ]\*

(°>°) Provide the [new] value? Typed ENTER

./§\  
 @>@ [Warning!]: invalid literal for int() with base 10: "  
 \~/ [ TYPE AN [NEW POSITIVE INTEGER NUMBER ]  
 [ IN NEXT INSTRUCTION -- OK! ]

(°>°) Provide the [new] value? 23

\*\*[The typed number]: 23 is a [valid integer number!] ]\*\*

\*\*[NEITHER OF THE PREVIOUS OPTIONS WAS SELECTED]\*\*  
 [ RUN THE RUNVECTORS2DIM.PY PROGRAM AGAIN -- OK! ]

. . . Key [ENTER] to exit -- Ok! . . .

**[Warning]:** The runvectors2dim.py program will follow only when the user typer any *positive integer number* between 1 to 12 – Ok! If type any positive integer number bigger than 12 the user will have that run the runvectors2dim.py program again. View the last previous test.

(°>°) Provide the [new] value? 1

\*\*[The typed number]: 1 is a [valid integer number!] ]\*\*

\*\*[TO FIND THE [SCALAR PRODUCT] OF [TWO VECTORS: A and B] IN THE  
 BI-DIMENSIONAL(XY) PLANE]\*\*

- Attribute the [Components] of the [1° vectorA]!

- Enter the 1° [Component(x)]!

(a<a) Enter the [new] value? 3

\*\*[ [The typed number]: 3.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(a<a) Enter the [new] value? 1

\*\*[ [The typed number]: 1.0 is a [valid integer or float number!] ]\*\*

- Provide the [Components] of the [2° vectorB]!

- Enter the 1° [Component(x)]!

(a<a) Enter the [new] value? -2

\*\*[ [The typed number]: -2.0 is a [valid integer or float number!] ]\*\*

- Introduce the 2° [Component(y)]!

(a<a) Enter the [new] value? 4

\*\*[ [The typed number]: 4.0 is a [valid integer or float number!] ]\*\*

-- The [vectorA]: vectorA [3.0, 1.0]

-- The [vectorB]: vectorB [-2.0, 4.0]

\*[ANSWER]\*

-- The [Vector] of the [terms of the Scalar Product]: vectorAB [-6.0, 4.0]

-- The [Scalar Product(vectorAB)] of the vectors is: -2.00

. . . Key [ENTER] to exit -- Ok! . . .

**Note:** The Components of Vectors and Coordinates of Points will can be: Negative or Zero or Positive; but the options of menu of the runvectors2dim.py program only can be typed *positive integer number*.

Developer: **Cristovom A. Girodo**