Machine Learning

Logistic Regression

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Logistic Regression is a classification model which is used to understand the relationship between the dependent variable and one or more independent variables by estimating probabilities using a logistic regression equation.

- The dependent variable should be binary like yes or no.
- It can help you predict the likelihood of an event happening or a choice being made.

Linear Regression outputs continuous value, and it has a straight line to map the input variables to the dependent variables. The output can be any of an infinite number of possibilities. On the other hand, Logistic Regression uses a logistic function to map the input variables to categorical dependent variables. In contrast to Linear Regression, Logistic Regression outputs a probability between 0 and 1.

Dataset: https://www.kaggle.com/rakeshrau/social-network-ads

This dataset shows which of the users purchased/not purchased a particular product.

The columns are:

- User ID
- Gender
- Age
- EstimatedSalary
- Purchased

Importing libraries

Attaching package: 'dplyr'

```
library(caTools)
library(caret)

## Loading required package: ggplot2

## Loading required package: lattice

library(dplyr)

##
```

```
## The following objects are masked from 'package:stats':
##
## filter, lag

## The following objects are masked from 'package:base':
##
intersect, setdiff, setequal, union
```

Loading dataset

5 19

We will only use Age, Salary and Purchased columns.

76000

0

Split data into Train and Test set

Purchased column is our dependent variable.

```
set.seed(123)
splitted = sample.split(dataset$Purchased, SplitRatio = 0.75)
trainSet = subset(dataset, splitted == TRUE)
testSet = subset(dataset, splitted == FALSE)
```

Feature Scaling

Feature scaling is a method used to normalize the range of independent variables or features of data.

We will scale all the features except our dependent variable, Purchased.

```
trainSet[, 1:2] = scale(trainSet[, 1:2])
testSet[, 1:2] = scale(testSet[,1:2])
```

Apply Logistic Regression

```
model = glm(formula = Purchased ~ ., family = binomial, data = trainSet)
```

Prediction

Probability prediction show us predicted probabilities that the user will buy the product.

```
probability.prediction = predict(model, type = 'response', newdata = testSet[-3])
probability.prediction
```

```
##
                                           5
                                                        9
                                                                                   18
                            4
                                                                     12
                              0.0037846461 0.0024527456 0.0073339436 0.2061576580
## 0.0162395375 0.0117148379
                                         22
                                                        29
                                                                     32
##
              19
                            20
                                                                                   34
   0.2669935073 0.3851475689 0.5448578778 0.0103005636 0.2994922143 0.0084168787
##
             35
                            38
                                         45
                                                        46
                                                                     48
                                                                                   52
   0.0494471952 0.0171641479
                              0.0485051303 0.0008343060 0.0102561619 0.0007055347
                                                                     82
##
             66
                            69
                                         74
                                                       75
   0.0058448457 0.0044534947 0.3933468488 0.0071065671 0.1068589185 0.2580084947
##
##
             85
                            86
                                         87
                                                       89
                                                                    103
   0.0303248927 0.3303649169 0.0051132916 0.0263861849 0.1310148056 0.7649772313
            107
                                                      117
##
                          108
                                        109
                                                                    124
   0.0034367786 0.0473827096 0.0327965105 0.1626049288 0.0675494054 0.2189658514
##
            127
                          131
                                        134
                                                      139
                                                                    148
                                                                                  154
   0.4142562486 0.0324337750 0.0043457839 0.0163538708 0.1030590600 0.0751093248
##
            156
                          159
                                        162
                                                      163
                                                                    170
                                                                                  175
   0.0048556976 0.0027487256 0.0306647902 0.0463555716 0.0122981409 0.1169016711
##
            176
                          193
                                        199
                                                      200
                                                                    208
   0.0011936610 0.0103005636 0.0252589417 0.0177353905 0.9870859806 0.9453359968
##
            224
                          226
                                        228
                                                      229
                                                                    230
                                                                                  234
##
   0.9969454446 0.1064430571 0.9979393884 0.3705093415 0.5807527959 0.9117762840
##
            236
                          237
                                        239
                                                      241
                                                                    255
   0.7817273411 \ 0.2310672929 \ 0.8037996043 \ 0.9682706714 \ 0.6686007827 \ 0.1451169281
##
            265
                          266
                                        273
                                                      274
                                                                    281
   0.9060311409 \ 0.8293112410 \ 0.9568520348 \ 0.6781064291 \ 0.9926955397 \ 0.4170486388
##
##
            292
                          299
                                        302
                                                      305
                                                                    307
   0.9220096987 0.7363498859 0.8247736816 0.2558136823 0.9932007105 0.1178058928
                          324
                                        326
                                                      332
                                                                    339
##
            316
   0.3442845494 0.3958138650 0.3059412440 0.9725035550 0.1431602303 0.9842795480
            343
                          347
                                        353
                                                      363
                                                                    364
                                                                                  367
##
   0.2073273008 0.9371909698 0.6843940060 0.5559479117 0.5698028861 0.9440512240
##
            368
                          369
                                        372
                                                      373
                                                                    380
                                                                                  383
   0.8427877409 0.2549836305 0.9928717092 0.3243409327 0.8519685008 0.9697473704
##
            389
                          392
                                        395
                                                      400
## 0.3793408625 0.2718336775 0.2040229226 0.5236436275
```

But we need binary variable like 0 and 1. If the probability is greater than 0.5 turn 1, otherwise return 0.

```
prediction = ifelse(probability.prediction > 0.5, 1, 0)
prediction
```

```
18
                                  19
                                            22
                                                                35
##
      0
           0
               0
                     0
                          0
                              0
                                    0
                                         0
                                             1
                                                  0
                                                       0
                                                            0
                                                                 0
                                                                      0
                                                                           0
                                                                                0
                                                                                     0
                                                                                          0
              82
                        85
                             86
                                       89
                                           103 104 107 108 109 117 124
                                                                             126
                                                                                  127
##
     74
         75
                   84
                                  87
                                                                                       131
##
               0
                     0
                          0
                               0
                                    0
                                         0
                                             0
                                                       0
                                                                 0
                                                                      0
                                                                           0
                                                                                0
                                                                                     0
                                                  1
   148
             156
                  159
                       162 163 170
                                      175
                                          176 193 199 200 208 213 224 226 228
                                             0
                                                  0
                                                       0
                     0
                              0
                                    0
                                         0
                                                            0
                                                                 1
                                                                      1
                                                                           1
```

```
## 236 237 239 241 255 264 265 266 273 274 281 286 292 299 302 305 307 310 316 324
                         0
                             1
                                     1
                                             1
                                                     1
                                                                          0
                                                                              0
        0
            1
                 1
                    1
                                 1
                                         1
                                                 0
                                                         1
                                                             1
                                                                 0
                                                                      1
## 326 332 339 341 343 347 353 363 364 367 368 369 372 373 380 383 389 392 395 400
                 1
                     0
                         1
                             1
                                 1
                                     1
                                         1
                                             1
                                                 0
                                                     1
                                                         0
                                                              1
                                                                      0
```

Confusion Matrix

```
# Generate confusion matrix
conf.matrix <- confusionMatrix(table(testSet[, 3], prediction))</pre>
conf.matrix
## Confusion Matrix and Statistics
##
##
      prediction
##
       0 1
     0 57 7
##
##
     1 10 26
##
##
                  Accuracy: 0.83
##
                    95% CI: (0.7418, 0.8977)
       No Information Rate: 0.67
##
       P-Value [Acc > NIR] : 0.0002624
##
##
##
                     Kappa: 0.6242
##
   Mcnemar's Test P-Value: 0.6276258
##
##
##
               Sensitivity: 0.8507
##
               Specificity: 0.7879
##
            Pos Pred Value: 0.8906
##
            Neg Pred Value: 0.7222
##
                Prevalence: 0.6700
##
            Detection Rate: 0.5700
##
      Detection Prevalence: 0.6400
##
         Balanced Accuracy: 0.8193
##
##
          'Positive' Class: 0
##
```

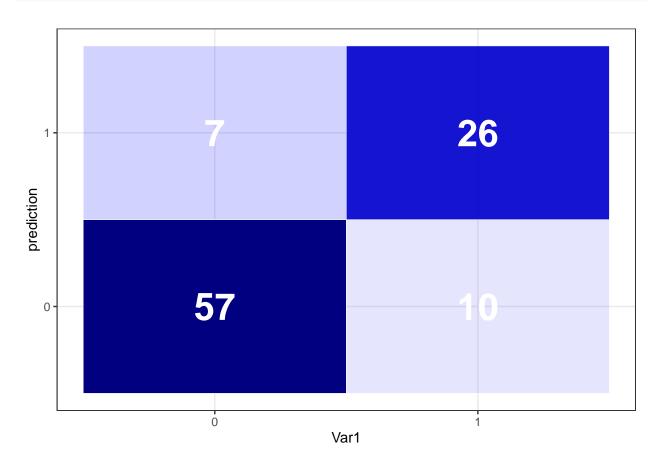
The accurary is 83%. We have 10 + 7 incorrect classifications.

```
# Heatmap visualization of confusion matrix
table <- data.frame(conf.matrix$table)

plotTable <- table %>%
    group_by(prediction) %>%
    mutate(prop = Freq/sum(Freq))

ggplot(data = plotTable, mapping = aes(x = Var1, y = prediction, alpha = prop)) +
    geom_tile(aes(fill = Freq), colour = "white") +
```

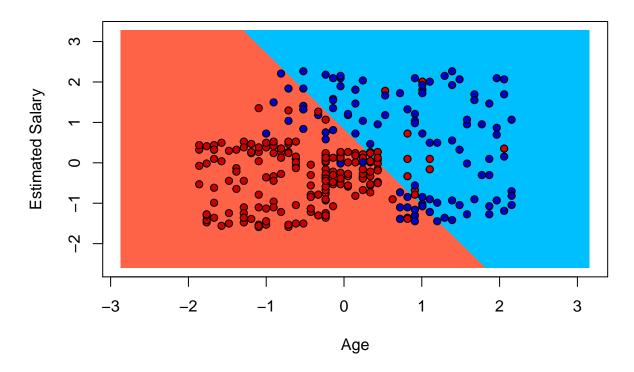
```
geom_text(aes(label = Freq), vjust = .5, fontface = "bold", alpha = 1, color="white", size=10) +
scale_fill_gradient(low = "blue", high = "navyblue") +
theme_bw() + theme(legend.position = "none")
```



Visualize Train Set Results

```
points(grid_set, pch = '.', col = ifelse(y_grid == 1, 'deepskyblue', 'tomato'))
points(set, pch = 21, bg = ifelse(set[, 3] == 1, 'blue3', 'red3'))
```

Logistic Regression (Train Set)



Young people who did not buy the product are on the red are with red points. On the other hand, older people who bought the product are on the blue part with blue points. The blue points which are on the red side are the ones who are young but bought the product. And those red points which are on the blue part, they are older people who did not buy the product.

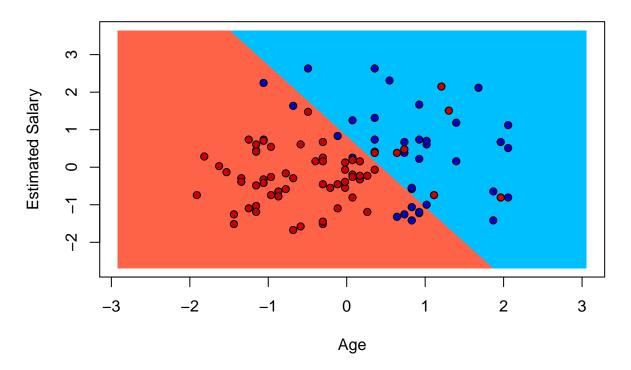
The straight line seen on the plot is called the Prediction Boundary.

Visualize Test Set Results

```
set = testSet
X1 = seq(min(set[, 1]) - 1, max(set[, 1]) + 1, by = 0.01)
X2 = seq(min(set[, 2]) - 1, max(set[, 2]) + 1, by = 0.01)
grid_set = expand.grid(X1, X2)

colnames(grid_set) = c('Age', 'EstimatedSalary')
prob_set = predict(model, type = 'response', newdata = grid_set)
y_grid = ifelse(prob_set > 0.5, 1, 0)
```

Logistic Regression (Test Set)



Majority of the blue and red points are on the right parts of the plot. We have 17 incorrect predictions.