

1.

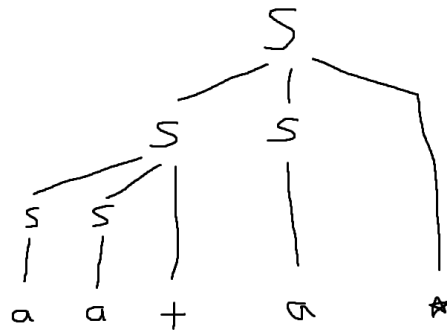
a.

$$S \xRightarrow{lm} SS^* \xRightarrow{lm} SS + S^* \xRightarrow{lm} aS + S^* \xRightarrow{lm} aa + S^* \xRightarrow{lm} aa + a^*$$

b.

$$S \xRightarrow{rm} SS^* \xRightarrow{rm} Sa^* \xRightarrow{rm} SS + a^* \xRightarrow{rm} Sa + a^* \xRightarrow{rm} aa + a^*$$

c.



2.

a.  $S \rightarrow A \mid B$

$A \rightarrow 1A \mid 1B \mid \epsilon$

$B \rightarrow 0A$

b.  $S \rightarrow 1S1 \mid 0S0 \mid \epsilon$

3.

a. This grammar is already left factored

b. The grammar is not suitable for top down parsing because it has left-recursion.

c.

repr	$\rightarrow$ rterm repr'
repr'	$\rightarrow$ + rterm repr' $\mid \epsilon$
rterm	$\rightarrow$ rfactor rterm'
rterm'	$\rightarrow$ rfactor rterm' $\mid \epsilon$
rfactor	$\rightarrow$ rprimary rfactor'
rfactor'	$\rightarrow$ * rfactor' $\mid \epsilon$
rprimary	$\rightarrow$ a $\mid$ b

d. The Grammar is now suitable for top down parsing because it is left factored and doesn't have left recursion.

4. Remove Left Recursion:

$S \rightarrow (S)S' \mid aS'$

$S' \rightarrow +SS' \mid SS' \mid *S' \mid \epsilon$

$\text{First}(S) = \{ (, a \}$

$\text{First}(S') = \{ +, *, \epsilon, \{, a \}$

Follow(S) = { \$, +, \*, (, a, ) }

Follow(S') = { \$, +, \*, (, a, ) }

Parsing Table:

	(	)	+	*	a	\$
S	$S \rightarrow (S)S'$				$S \rightarrow aS'$	
S'	$S' \rightarrow \epsilon$ $S' \rightarrow SS'$	$S' \rightarrow \epsilon$	$S' \rightarrow \epsilon$ $S' \rightarrow +SS'$	$S' \rightarrow \epsilon$ $S' \rightarrow *S'$	$S' \rightarrow \epsilon$ $S' \rightarrow SS'$	$S' \rightarrow \epsilon$