



# Constant-Time Big Numbers (for Go)

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# Contents

<b>1</b>	<b>Introduction</b>	<b>3</b>
<b>2</b>	<b>Background</b>	<b>3</b>
2.1	Big Numbers in Cryptography . . . . .	3
2.1.1	Implementing Big Numbers . . . . .	4
2.1.2	Big Numbers in go/crypto . . . . .	4
2.2	Timing Attacks . . . . .	5
2.2.1	Actual Attacks . . . . .	5
2.2.2	Our Threat-Model . . . . .	6
2.3	Vulnerabilities in big.Int . . . . .	6
2.3.1	Padding . . . . .	7
2.3.2	Leaky Algorithms . . . . .	7
2.3.3	Mitigations . . . . .	7
<b>3</b>	<b>Implementation</b>	<b>8</b>
3.1	The safenum library . . . . .	8
3.1.1	Handling Size . . . . .	9
3.1.2	Moduli . . . . .	10
3.2	Constant-Time Operations . . . . .	11
3.2.1	Building Primitives . . . . .	12
3.3	Algorithm Choices . . . . .	13
3.4	Implementation Techniques . . . . .	13
3.4.1	Saturated or Unsaturated Limbs . . . . .	13
3.4.2	Redundant Reductions . . . . .	14
<b>4</b>	<b>Results</b>	<b>15</b>
4.1	Comparison with big.Int . . . . .	15
4.2	Comparison with go/crypto . . . . .	15
<b>5</b>	<b>Further Work</b>	<b>15</b>
5.1	Upstreaming to go/crypto . . . . .	15
5.2	Optimizing Assembly Routines . . . . .	15
<b>6</b>	<b>Conclusion</b>	<b>15</b>
	<b>Acknowledgements</b>	<b>15</b>

# 1 Introduction

With the Internet cemented as a principal keystone in communication, and ever increasing activity taking place digitally, the importance of secure communication and Cryptography has never been greater. Thankfully, after 50 years of Public Key Cryptography [13], we have good theoretical systems to provide these guarantees.

Most of these systems rely on modular arithmetic with large numbers, such as RSA or Elliptic Curve Cryptography [25, 20]. Working with such numbers is not natively supported by hardware, requiring a "Big Number" software library to provide this functionality.

Unfortunately, even though Public Key Cryptosystems have been heavily scrutinized *in theory*, in practice many vulnerabilities arise in software implementations of these systems.

One particularly pernicious class of vulnerability are **timing attacks** [15], where an implementation leaks information about secret values through its execution time or cache usage, among many side-channels.

Libraries for Big Numbers that are not designed with Cryptography in mind are pervasively vulnerable to this class of attack.

In particular, Go [3] provides a general purpose Big Number type, `big.Int`, which suffers from these vulnerabilities, as we detail later in this report. Unfortunately, this library gets used for Cryptography [11], including inside of Go's own standard library, in `go/crypto`.

We've addressed this issue by creating a library [18] designed to work with Big Numbers in the context of Public Key Cryptography. Our library provides the necessary operations for implementing these systems, all while avoiding the leakage of secret information. To demonstrate its utility, we've modified Go's `go/crypto` package, replacing the use of `big.Int` in the DSA and RSA systems.

## 2 Background

In this section, we explain how Big Numbers are used in Public Key Cryptography, what timing attacks are, and how they affect our threat model, as well as what kind of side-channels are present in Go's `big.Int` type.

### 2.1 Big Numbers in Cryptography

As mentioned previously, most Public Key Cryptosystems rely on modular arithmetic.

In RSA [25], for example, a public key  $(e, N)$  consists of modulus  $N \in \mathbb{N}$ , usually 2048 bits long, and an exponent taken modulo  $\varphi(N)$ . To encrypt a message  $m \in \mathbb{Z}/N\mathbb{Z}$ , we calculate

$$c := m^e \mod N$$

The typical word size on computers is now 64 bits. Because of this, to do arithmetic modulo  $N$ , we need a Big Number library to work with these large numbers, as well as to provide optimized implementations of operations like modular exponentiation, which aren't natively supported.

DSA [26] also relies on modular arithmetic, this time using a large prime  $p$  of around 2048 bits, and working in the multiplicative group  $(\mathbb{Z}/p\mathbb{Z})^*$ .

Elliptic Curve Cryptography [20] relies on complex formulas for adding points on an elliptic curve, built over a finite field  $K$ . This field is usually either a prime field  $\mathbb{Z}/p\mathbb{Z}$ , in which case arithmetic modulo  $p$  is used, or a binary extension field  $\text{GF}(2^n)$ , in which case binary arithmetic in combination with polynomial addition and multiplication are used.

For prime fields, a Big Number library is once again necessary, because the size of the prime is greater than 200 bits.

In summary, large modular arithmetic is a cornerstone of Public Key cryptosystems, requiring Big Numbers in some form.

### 2.1.1 Implementing Big Numbers

Describe different strategies in place for providing numbers for Cryptography.

### 2.1.2 Big Numbers in go/crypto

Go [3] provides implementations of numerous cryptographic algorithms as part of its standard library, including the aforementioned Public Key systems, in the `go/crypto` package.

Unfortunately [11], the general purpose `big.Int` type gets used in this package for Cryptography, despite its potential vulnerability to timing attacks.

For DSA [26], Go uses `big.Int` for all operations, including key generation, signing, and verification.

For RSA [25], Go uses `big.Int` for all operations, and fixes this type as part of the API for this package. Key generation, encryption, decryption, signing, and verification all use `big.Int`.

For ECC [20], Go defines a general interface for Elliptic Curves, requiring operations like point addition, scalar multiplication, etc. All of these are defined in terms of `big.Int`. Some of the curves have specialized implementations of their prime field, only converting from `big.Int` to satisfy the interface curves. The remaining curves directly make use `big.Int` for their field arithmetic.

## 2.2 Timing Attacks

A side-channel [14] leaks secret information about a program not directly, but indirectly, through the observable properties of its execution. For example, timing side-channels use the execution time of a program to infer properties of the secret data it processes. A timing attack is the use of a timing side-channel to break the security of some program or cryptographic protocol.

If a program takes a different number of steps based on the value of some secret, then this constitutes an obvious timing side-channel. For example, if a naive program for comparing inputs with a secret password stops as soon as a mismatch is found, then the algorithm itself has a timing side-channel. This side-channel can be exploited, to allow the secret password to be guessed byte by byte.

Not all timing side-channels are this simple, however. Algorithms that take the same number of steps regardless of the value of secret data can still have timing side-channels because of how the underlying hardware executing the program works. For example, a processor may execute an operation faster for some inputs, or the presence of a cache could be used to infer what addresses are being accessed. These microarchitectural timing side-channels are also of concern. See [12] for a survey of these vulnerabilities.

### 2.2.1 Actual Attacks

The presence of a side-channel does not directly lead to vulnerabilities. As early as 1995, Paul Kocher demonstrated the potential for timing attacks against cryptographic algorithms [15, 16]. These specific attacks rely on algorithms that perform a varying number of operations based on secret data.

One common objection to timing attacks more generally is that they while a timing side-channel is catastrophic in theory, in practice this channel is too noisy to exploit. Unfortunately, through gathering many samples, it's possible to exploit these attacks even across a network [8, 7].

The use of caches as a potential side-channel was identified early on as well [22]. The idea is that accessing data that is not present in the cache takes longer than accessing data inside of the cache. If what data is being accessed depends on a secret value, the observed execution time will thus also depend on this secret value. If an attacker is located on the same machine they can place data into the cache as well, and probe the cache themselves, to learn fine-grained information about the program's access patterns. While seemingly far-fetched, this is easy to achieve now that so many applications are run on cloud computing.

A wide variety of attacks involving caches have been mounted against

various cryptosystems [4, 27, 9] , making accessing data based on secret values fraught with peril.

### 2.2.2 Our Threat-Model

Although the variety of potential timing side-channels is quite daunting, we can distill them into a simple, albeit pessimistic set of rules:

1. Any loop leaks the number of iterations taken.
2. Any memory access leaks the address accessed.
  - (a) As a consequence, accessing an array leaks the index accessed.
3. Any conditional statement leaks which branch was taken.

Rule 1 is justified by theoretical concerns, since a longer loop requires more operations. In practice, it's difficult to observe the iterations of each loop in a program from an overall timing signal, making this a pessimistic rule.

Rule 2 is justified by various cache based side-channels and attacks [4, 27, 9]. Since caches only load information an entire line at a time, it might seem that our rule is too pessimistic, and that only which cache line was accessed should be kept secret [6]. Unfortunately, the potential for attacks on much finer grained level has been demonstrated [5, 21, 27]. Because of these concerns, we take a pessimistic position, and assume that accessing an array leaks the exact index accessed.

Rule 3 is justified in two ways. First, if different branches of a conditional statement execute a different number of operations, this leaks information about which branch was taken in a fundamental way. Second, even if both branches execute identical operations, the CPU's branch predictor can be exploited, leaking information about which branch was taken [2, 1, 10].

In addition to these rules, we assume that addition, multiplication, logical operations, and shifts, as implemented in hardware, are constant-time in their inputs. This is the case on most processors, one notable exception being microprocessors [23]. For the platforms which Go, and thus our library, targets, this assumption is reasonable.

## 2.3 Vulnerabilities in `big.Int`

Go provides a general purpose type for Big Numbers: `big.Int`. This implementation is concerned with being broadly applicable, and well-optimized. It does not focus on security, or on hardening itself against timing side-channels.

Unfortunately, its broad applicability makes it useful for cryptography, and it gets used throughout Go’s standard cryptography library, as we’ve seen previously.

In this section, we look at some of the important implementation aspects of `big.Int`, and how they might be potentially vulnerable according to our threat model.

### 2.3.1 Padding

The `big.Int` type always normalizes numbers internally, removing any leading zero limbs. Even if you initialize a number using bytes zero-padded to a certain length, the resulting value will immediately chop off these zeros. These extra zeros don’t change the value of a number. By discarding them, operations on this number will have fewer limbs to process, and will be faster.

Unfortunately, this means that `big.Int` leaks information about the padding of numbers pervasively. Since every operation on a number takes more time the more limbs the number uses, the removal of padding leaks the true sizes of numbers at every operation. Leaking this padding has been exploited in OpenSSL [19], and might potentially be a vulnerability in Go’s cryptography library, because of `big.Int`.

### 2.3.2 Leaky Algorithms

Because `big.Int` is not written with Cryptography in mind, its methods violate the rules set in 2.2.2. Many methods take a different number of iterations based on their values, branch conditionally on values, and access memory depending on values. Because `big.Int` is designed for general purpose use, this problem should only get worse as the library is further developed and optimized.

Ultimately, the problem is not the existence of `big.Int`, but it’s use in Go’s cryptography library, and in the broader ecosystem.

### 2.3.3 Mitigations

Although `big.Int` gets used in Go’s cryptography library, the authors are aware of its shortcomings, and have implemented several mitigations to try and make its timing side-channels harder to exploit.

One of the most important ones is a mitigation for RSA: blinding [16]. The decrypt a ciphertext  $c = m^e \bmod N$ , we normally calculate:

$$c^d \bmod N$$

with  $d$  our private key, and  $(e, N)$  our public key. When exponentiation is not implemented in a constant-time way, like with `big.Int`, this process

can leak information about  $m$ . If an adversary can choose  $c$ , then this can leak information about  $d$  as well.

To mitigate this, instead of decrypting  $c$  directly, we first generate a random integer  $r \in [0, N - 1]$ , and make sure it has an inverse  $r^{-1} \bmod N$ . Then we decrypt  $r^e \cdot c$ . This gives us the value  $r \cdot m$ , and we can recover  $m$  by multiplying by  $r^{-1}$ .

While this does effectively mitigate the simplest attacks against exponentiation, a very leaky operation, the other operations involving these values are still left unprotected, and may have exploitable leakages in more subtle ways. We also have the unaddressed issue of padding, which has lead to attacks in OpenSSL [19].

### 3 Implementation

We've implemented a library, called `safenum` [18], intended to provide a replacement for `big.Int`, suitable for use in Cryptography. In order to demonstrate its utility, we've replaced some of `go/crypto`'s usage of `big.Int` with our own library, in a separate repository [17].

In this section, we go over the design and implementation of our library.

#### 3.1 The `safenum` library

`Safenum` defines a `Nat` type, which is intended to replace `big.Int`. This type represents arbitrary numbers in  $\mathbb{N}$ . Unlike `big.Int`, we do not handle negative numbers. Handling a sign bit in constant-time is exceedingly tricky. Thankfully, we haven't found this limitation to be restrictive when replacing `big.Int` in Go's cryptography library.

We represent numbers in base  $W := 2^{64}$ . Concretely, we store a number as a slice of type `[]uint`, in little endian order. We call these the "limbs" of a number. For example, the slice:

```
[]uint{13, 47, 52}
```

represents the number:

$$52 \cdot 2^{128} + 47 \cdot 2^{64} + 13$$

These limbs might be padded, to conceal the true value of a number, as we'll see later.

We provide operations for addition and multiplication of `Nats`, all other operations are for modular arithmetic. For modular arithmetic, we provide numerous operations, including modular addition, subtraction, multiplication, exponentiation, inversion, reduction, and taking square roots modulo prime numbers. We also provide the usual operations for serializing to and from bytes.



We try and structure the API in a similar way to `big.Int`, where an operation is performed on a buffer `Nat`, which can receive the result. For example, this is the signature for modular addition:

```
func (z *Nat) ModAdd(x *Nat, y *Nat, m *Modulus) *Nat
```

This calculates  $z \leftarrow x + y \bmod m$ , returning `z`. The advantage of structuring the API this way, instead of simply returning a new value, is that we can reuse the memory of `z` for the result.

We go one step further, in fact, and use the memory of the buffer `Nat` for all scratch space needed inside of an operation. Structuring our operations this way allows us to limit unnecessary waste of allocation.

### 3.1.1 Handling Size

Unlike `big.Int`, a `Nat` doesn't truncate its limbs to remove any zero padding. Because of this, we distinguish between the *true size* of a number, which is how many significant bits or limbs it actually has, and the *announced size* of a number, which is how many limbs are actually used to store that number. The announced size is allowed to be leaked, while the true size should be kept secret. The true size is always at most the announced size.

Because of this, we need to ensure that there's always a clear announced size to use for the results that we produced. For modular operations, we have an obvious choice: the size of the modulus. When doing a modular operation, the result will always receive the same announced size as the modulus does.

For example, when doing modular addition:

```
func (z *Nat) ModAdd(x *Nat, y *Nat, m *Modulus) *Nat
```

our result `z` will have the same announced size as `m`. After modular addition, we have that  $z \in [0, m - 1]$  by definition. Because of this, leaking the fact that the true size of `z` is at most that of `m` leaks no information about what value `z` actually has, beyond what's knowable just by inspecting the call graph in the source code of a program.

When serializing a `Nat`, we respect its announced size, and produce zeros for padding as necessary. This is done without any special handling, because we already store padded limbs anyways.

Similarly, when deserializing a `Nat` from bytes, we respect any padding, unlike `big.Int`. For example, if 32 big endian bytes are deserialized, we will end up with a `Nat` with an announced size of 256 bits, regardless of the value of those bytes.

This leaves us with non-modular addition and multiplication of numbers. One approach is to use the maximum possible resulting size for our result's announced length. For example, if we multiply numbers  $x_1$  and

$x_2$ , of announced size  $b_1$  and  $b_2$ , then our result will need a size of at most  $b_1 + b_2$ . In situations where we know that our result will be smaller, this size explosion can be undesirable.

Because of this, we opt towards letting users specify exactly how many resulting bits they need in the output. For example, multiplication has the following signature:

```
func (z *Nat) Mul(x *Nat, y *Nat, cap uint) *Nat
```

Here cap is the number of bits that the result should have. We use this to determine the result's announced length. Any output beyond that capacity will simply be discarded.

In summary, the announced size of a Nat is always clear based on how it's produced, and results from deserializing a value, from using the same size as a modulus, or from manually deciding on an output size.

### 3.1.2 Moduli

In our library, we've decided to make a separate type for representing the moduli used in modular arithmetic: Modulus. There are several reasons for doing this.

First, various operations in modular arithmetic require different properties of the modulus which can be pre-computed. For example, montgomery multiplication requires us to know  $m^{-1} \bmod W$ , with  $W$  our base, and  $m$  our modulus. By using a separate type for moduli, we can precompute these values.

Second, the true size of a modulus is considered to be leakable. As a consequence, moduli are stored *without* padding. This is desirable because modular reduction needs access to the most significant bits of a modulus, and fetching this information without leaking padding is exceedingly difficult. Furthermore, by storing moduli without padding, the announced size of numbers produced through modular operations is as tight as possible, which speeds up operation.

This assumption is safe in cryptography. Moduli are often public, like with the public modulus  $N$  in RSA. In this case, leaking the true size is fine, since even the exact value is known. There are some cases where a secret modulus is necessary. For example, when generating an RSA key, we use the factorization  $N = pq$  of the modulus, and calculate our private key modulo  $\varphi(N) := (p - 1)(q - 1)$ :

$$d := e^{-1} \bmod \varphi(N)$$

Leaking the value of  $\varphi(N)$  would be catastrophic. On the other hand, it's clear that the true size of  $\varphi(N)$  is approximately that of  $N$ , which is known. In this case, leaking the true size of  $\varphi(N)$  is fine.

Using a separate modulus type is necessary to have this weaker constraint on its announced size.

### 3.2 Constant-Time Operations

The rules we established in our threat model 2.2.2 are quite stringent. For many operations, we want to have conditional behavior depending on the values and results we see. Without access to branching, this would seem impossible. Thankfully, there are workarounds to enable us to have conditional behavior, all while not leaking information about which conditions are selected. The core idea here is that whenever we're faced with a choice, we perform both branches, and then combine the results together without revealing which result we end up using.

For example, an standard algorithm for modular subtraction would look like this (in pseudo-Go):

```
func (z *Nat) ModSub(x *Nat, y *Nat, m *Modulus) *Nat {
    borrow := z.Sub(x, y)
    if borrow == 1 {
        z.Add(z, m)
    }
}
```

The problem here is that by conditionally adding in  $m$ , we reveal whether or not  $y > x$ , and a borrow occurred. Our solution requires a new primitive:

```
func (z *Nat) ctCondCopy(v choice, y *Nat) *Nat
```

This function assigns  $y$  to  $z$  if  $v = 1$ , and does nothing otherwise. Furthermore, this primitive shouldn't leak any information about whether or not the condition was true.

With this in place, we can implement modular subtraction without leakage:

```
func (z *Nat) ModSub(x *Nat, y *Nat, m *Modulus) *Nat {
    borrow := z.Sub(x, y)
    scratch := new(Nat).Add(z, m)
    z.ctCondCopy(choice(borrow), scratch)
}
```

We always perform the addition, and copy over the result if necessary, without leaking the value of borrow.

This kind of rearrangement is the foundation that allows us to replace branching in algorithms with constant-time operations.

### 3.2.1 Building Primitives

The question remains: how do you build up the primitives like `ctCondCopy`, which let you choose results without leaking which result was chosen?

The methods for constant-time choice are analagous to the standard programming methods for conditional branching. Instead of using `bool` to represent the result of a condition, we use

```
type choice Word
```

The value of a choice is either 1 or 0, but we use the same type as full limbs, to try and avoid having the compiler turning our manipulations back into branches.

From this choice value, we can build a primitive that selects between two limbs without leaking which choice was selected:

```
func ctIfElse(v choice, x, y Word) Word {  
    mask := -Word(v)  
    return y ^ (mask & (y ^ x))  
}
```

This routine returns  $x$  if  $v = 1$ , and  $y$  otherwise. Unlike a conditional statement, this is implemented through bitwise operations, and doesn't leak information about what was selected.

If  $v = 0$ , then `mask` contains only zeros, and we're left with  $y$ . When  $v == 1$ , then `mask` only contains ones. The  $y$ 's cancel eachother out, leaving us with  $x$ .

We can use this primitive to build up a larger selection primitive, allowing us to assign one slice to another, conditionally:

```
func ctCondCopy(v choice, x, y []Word) {  
    for i := 0; i < len(x); i++ {  
        x[i] = ctIfElse(v, y[i], x[i])  
    }  
}
```

These primitives allow us to use `choice` to introduce conditional behavior without leaking our choices, but we also need primitives to create choice values in the first place. These are built up in a similar way from small primitives to large primitives.

We can decide whether or not two limbs are equal using some bitwise trickery:

```
func ctEq(x, y Word) choice {  
    q := uint64(x ^ y)  
    return 1 ^ choice((q|-q)>>63)  
}
```

To understand why this trick works, first realize that in two's complement, either the most significant bit of a number is set, or the most significant bit of a number's negation is set, unless that number is zero. Thus, the expression

```
choice((q|-q)>>63)
```

simply checks, using only bitwise operations, that `q` is not zero. Since `q` is zero precisely when `x` and `y` are equal, we can simply negate the non-zero check.

We can use this primitive to compare entire slices of limbs in constant time:

```
func cmpEq(x []Word, y []Word) choice {
    res := choice(1)
    for i := 0; i < len(x) && i < len(y); i++ {
        res &= ctEq(x[i], y[i])
    }
    return res
}
```

We can't exit early, since that would leak information about the value of `x` and `y`. Instead, we combine all the results together, using the fact that two slices are equal when every one of their matching limbs are equal.

### 3.3 Algorithm Choices

Describe the algorithm choices we've used for different things.

### 3.4 Implementation Techniques

In this section, we describe a few remaining implementation choices and techniques of interest.

#### 3.4.1 Saturated or Unsaturated Limbs

As mentioned previously, we store numbers in base  $W := 2^{64}$ . This means that we use the full width of a register to store each limb. Because of this, we say that our limbs are *saturated*. It's also possible to store limbs *unsaturated*, by using fewer than 64 bits. BearSSL [24] takes this approach, using only 31 bits of the available 32 bits in the integers it uses. For 64 bit registers, using 63 bit unsaturated limbs would be the option of choice.

There are two compelling reasons for using unsaturated limbs.

The first is that this leaves an extra bit of space to hold a carry or borrow after an addition or subtraction, respectively. This allows us to chain together carries to implement operations over multiple limbs, without

having to use assembly instructions. In Go, this isn't really an issue, because `bits.Add` and `bits.Sub` are provided to implement this intrinsic in a cross-platform way.

The second comes that if we use  $w$  bits for each limb, then montgomery multiplication needs to work with a value of size  $2w + 1$  bits. With a fully saturated limb of 64 bits, we need 129 bits. This uses an extra register compared to unsaturated limbs of 63 bits. Because montgomery multiplication is called very often during exponentiation, this can yield considerable savings.

The disadvantage of using unsaturated limbs comes when converting numbers to and from bytes. With fully saturated limbs, our 64 bit limbs are nicely composed of 8 bytes. With 63 bit limbs, this isn't the case, making conversion to and from bytes more complicated, and expensive. Using unsaturated limbs would also require storing additional information about the exact announced size of a number, instead of being able to use the number of limbs directly.

Ultimately, we opted to use saturated limbs, in order to reuse the assembly routines already implemented for low level operations in `big.Int`. These were designed with saturated limbs in mind, and thankfully, are constant-time.

### 3.4.2 Redundant Reductions

Our library is defined to prevent misuse. Because of this, modular operations work even if their inputs are not already reduced. For example, addition modulo  $m$  should return the right result, even if the inputs are greater than  $m$ . Unfortunately, the cost of reducing inputs modulo  $m$  when they were already in range is not desirable, since this operation is relatively expensive. Ideally, we'd like to avoid reducing inputs when we already know that they're correctly reduced.

To implement this, each number stores a pointer to a modulus, indicating that it is already reduced by this modulus. When we reduce a number modulo  $m$ , we check this pointer, and skip this reduction if it matches  $m$ . If we modify the value of a number, we update the modulus it points to accordingly, based on what method was called. For example:

```
z.ModAdd(x, y, m)
```

will set  $z$ 's modulus to  $m$ .

We only set this modulus pointer based on what methods are called, never on the actual value of a result. Because of this, the dynamic checks of this pointer only depend on the callgraph of our program. Since this graph is statically determined, these redundant reduction checks don't impact the constant-time properties of our library.

## 4 Results

We’ve compared the performance of our library with `big.Int` operation by operation, as well as in the context of the `go/crypto` package. Overall, our library is about 2.6x slower than using `big.Int`. In this section, we present these results in detail.

### 4.1 Comparison with `big.Int`

Describe the final performance results we’ve managed to achieve.

Operation	op / s ( <code>big.Int</code> )	op / s (Nat)	ratio
Addition	7,811,989	10,622,287	0.74
Multiplication	1,282,808	434,802	2.95
Modular Addition	9,088,922	3,121,003	2.91

### 4.2 Comparison with `go/crypto`

Describe the benchmarks on actual code.

## 5 Further Work

### 5.1 Upstreaming to `go/crypto`

Describe our work in providing a patch for RSA, and what results we’ve managed to achieve.

### 5.2 Optimizing Assembly Routines

## 6 Conclusion

Summarize the things we put in the introduction.

## Acknowledgements

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