

# MPC for Group Reconstruction Circuits

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June 7, 2022

## Abstract

In this paper, we present a thing.

## 1 Introduction

Write the introduction

## 2 Background

Throughout this paper, we let  $\mathbb{G}$  denote a group of prime order  $q$ , with generators  $G$  and  $H$ . Let  $\mathbb{F}_q$  denote the scalar field associated with this group, and let  $\mathbb{Z}/(q)$  denote the additive group of elements in this field.

We make heavy use of group homomorphisms throughout this paper. We let

$$\varphi(P_1, \dots, P_m) : \mathbb{A} \rightarrow \mathbb{B}$$

denote a homomorphism from  $\mathbb{A}$  to  $\mathbb{B}$ , parameterized by some public values  $P_1, \dots, P_m$ . Commonly  $\mathbb{A}$  will be a product of several groups  $\mathbb{G}_1, \dots, \mathbb{G}_n$ , in which case we'd write:

$$\varphi(P_1, \dots, P_m)(x_1, \dots, x_n)$$

to denote the application of  $\varphi$  to an element  $(x_1, \dots, x_n)$  of the product group. We also often leave the public values  $P_i$  implicit.

### 2.1 Pedersen Commitments

### 2.2 Sigma Protocols

### 2.3 Maurer's $\varphi$ -Proof

In [Mau09], Maurer generalized Schnorr's sigma protocol for knowledge of the discrete logarithm [Sch90] to a much larger class of relations. In particular, Maurer provided a sigma protocol for proving knowledge of the pre-image of a group homomorphism  $\varphi$ . We denote this protocol as a “ $\varphi$ -proof”, and recapitulate the scheme here.

- 2.4 UC Security and the Hybrid Model**
- 2.5 Ideal Functionalities for Sigma Protocols**
- 2.6 Broadcast Functionalities**
- 3 Group Reconstruction Circuits**
  - 3.1 Formal Definition**
  - 3.2 Normalized Form**
- 4 MPC Protocol for GRCs**
- 5 Security Analysis**
- 6 Applications**
- 7 Limitations and Further Work**
- 8 Conclusion**

## **References**

- [Mau09] Ueli Maurer. Unifying Zero-Knowledge Proofs of Knowledge. In *AFRICACRYPT 2009*, volume 5580 of *LNCS*, pages 272–286. Springer, Berlin, Heidelberg, 2009.
- [Sch90] C. P. Schnorr. Efficient Identification and Signatures for Smart Cards. In *CRYPTO 1989*, volume 435 of *LNCS*, pages 239–252, New York, NY, 1990. Springer.