

ANSWER No. 01

(a)

$$\frac{dAC}{dQ} = \frac{-25,000}{Q^2} + 3 = 0$$

$$Q = 91.3$$

$$AC = \frac{25,000}{91.3} + 150 + 3(91.3)$$

$$AC = 697.7$$

(b)

- Monthly output for this firm would be 91.3 units

ANSWER no#02
(a)

$$140,000 - 10,000p = 80,000 + 5,000p$$

$$140,000 - 80,000 = 10,000p + 5,000p$$

$$60,000 = 15,000p$$

$$\frac{60,000}{15,000} = p$$

$$\boxed{4=p} \text{ or } p=4$$

Statement:

- Equilibrium price of a box would be $\boxed{4}$, and yes, this is the long-run equilibrium.

(b)

At minimum level,

$$\frac{d(AVC)}{dQ} = 0, \quad \frac{d^2(AVC)}{dQ^2} > 0$$

$$\frac{d(AVC)}{dQ} = -12 + 2Q = 0, \quad \frac{d^2(AVC)}{dQ^2} = 2 > 0$$

$$-12 + 2Q = 0 \quad \text{i.e. } \boxed{Q = 6}$$

• Hence, at $Q = 6$ AVC is at minimum.

Similarly, At minimum,

$$\frac{d(MC)}{dQ} = 0, \quad \frac{d^2(MC)}{dQ^2} > 0$$

$$= -24 + 6Q = 0, \quad = 6 > 0$$

$$-24 + 6Q = 0 \quad \text{i.e. } \boxed{Q = 4}$$

Hence, it is noted at $Q = 4$, MC is minimum.

Statement:

- It is calculated that both AVC and MC carries a minimum rate at $Q=6$ and $Q=4$, at other level of output.
- AVC and MC both are higher, which means the "Curve will be in the shape of U".

(C)

when $Q=6$

$$AVC = 60 - 12Q + Q^2$$

$$AVC = 60 - 12(6) + 6(6)$$

$$AVC = 60 - 72 + 36$$

$$AVC = 24$$

now, calculating MC

$$MC = 60 - 24Q + 3Q^2$$

$$MC = 60 - 24(6) + 3(6)(6)$$

$$MC = 60 - 144 + 108$$

$$MC = 24$$

(b)

At minimum level,

$$\frac{d(AVC)}{dQ} = 0, \quad \frac{d^2(AVC)}{dQ^2} > 0$$

$$\frac{d(AVC)}{dQ} = -12 + 2Q = 0, \quad \frac{d^2(AVC)}{dQ^2} = 2 > 0$$

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• Hence, at $Q = 6$ AVC is at minimum.

Similarly, At minimum,

$$\frac{d(MC)}{dQ} = 0, \quad \frac{d^2(MC)}{dQ^2} > 0$$

$$= -24 + 6Q = 0, \quad = 6 > 0$$

$$-24 + 6Q = 0 \quad \text{i.e. } \boxed{Q = 4}$$

Hence, it is noted at $Q = 4$, MC is minimum.

ANSWER NO# 03

(a)

$$TC = 100 + 60Q - 12Q^2 + Q^3$$

As we know that,

$$TC = \text{Total Fixed cost} + \text{Total Variable cost}$$

Hence, Total Fixed cost = 100

- Total Variable cost = $60Q - 12Q^2 + Q^3$
- $AVC = \frac{TVC}{Q} = 60 - 12Q + Q^2$
- $MC = \frac{d(TC)}{dQ} = 60 - 24Q + 3Q^2$

(b)

$$Q_d = 140,000 - 10,000(4) = 100,000$$

$$Q_s = 80,000 + 5,000(4) = 100,000$$

- It is noted that each firm produces 1,000 units, hence.

$$\frac{100,000}{1,000} = \boxed{100} \text{ firms}$$

Statement: Number of 100 firms are in this industry when it is ~~comes~~ in the long-run equilibrium.

ANSWER NO#04

$$\text{Total Revenue (TR)} = \text{Price} \times \text{Quantity}$$

$$TR = 4Q$$

$$\text{Profit} = \text{Total Revenue (TR)} - \text{Total Costs (TC)}$$

$$\text{Profit} = 4Q - (0.04Q^3 - 0.9Q^2 + 10Q + 5)$$

$$\text{Profit} = -0.04Q^3 + 0.9Q^2 - 6Q - 5$$

$$\frac{dP}{dQ} = 0$$

$$-0.12Q^2 + 1.8Q - 6$$

$$-Q^2 + 15Q - 50 = 0$$

$$Q(-Q + 10) - 5(10 - Q) = 0$$

$$(Q - 5)(Q - 10) = 0$$

$$(Q = 5) \text{ and } (Q = 10)$$

For $Q = 5$

$$\begin{aligned} \text{Profit} &= -0.04(5)^3 + 0.9(5)^2 - 6(5) - 5 \\ &= \boxed{-17.5} \end{aligned}$$

For $Q = 10$

$$\begin{aligned} \text{Profit} &= -0.04(10)^3 + 0.9(10)^2 - 6(10) - 5 \\ &= \boxed{-15} \end{aligned}$$

Statement:

- As according to this calculation, we found out that the firm would be operating at loss. Hence, the firm should not produce this level of output
- Evidence shows that by selling at \$4 per unit ~~from~~ generates negative profit.

ANSWER no# 05

$$TC = 1500 + 15Q - 6Q^2 + Q^3$$

- Fixed cost is the constant of total cost, constant of TC is ~~1500~~ 1,500
Hence,

$$\text{Fixed Cost (FC)} = 1,500$$

$$AFC = \frac{FC}{Q}$$

- It is understood that total fixed cost (TFC) is constant irrespective of the quantity produced.

(a)

Total fixed cost at 1,000 units and 500 units are 1,500

Total Fixed Cost at,

$$Q = 1000 \text{ is } FC = 1,500$$

$$Q = 500 \text{ is } FC = 1,500$$

(b)

$$AFC = \frac{FC}{Q}$$

• at $Q = 1,000$

$$AFC = \frac{1500}{1000}$$

$$AFC = 1.5$$

• at $Q = 500$

$$AFC = \frac{1500}{500}$$

$$AFC = 3$$

(i) AFC at $Q = 1000$ is 1.5

(ii) AFC at $Q = 500$ is 3

(C)

TVC is the variable part of total cost.

$$TVC = TC - FC = 15Q - 6Q^2 + Q^3$$

$$AVC = \frac{TVC}{Q} = 15 - 6Q + Q^2$$

$$AC = \frac{TC}{Q} = \frac{1500}{Q} + 15 - 6Q + Q^2$$

$$MC = \frac{dTC}{dQ} = 15 - 12Q + 3Q^2$$

at $Q = 50$

$$TVC = 15(50) - 6(50)^2 + (50)^3$$

$$TVC = 750 - 15,000 + 125,000$$

$$TVC = 110,750$$

now, we find AVC,

$$AVC = \frac{TVC}{Q}$$

$$AVC = \frac{110,750}{50} = \boxed{2,215}$$

now, we find AC

$$AC = \frac{1500}{50} + 15 - 6(50) + 50^2$$

$$\boxed{AC = 2,245}$$

now, we find MC

$$MC = 15 - 12(50) + 3 - (50)^2$$

$$\boxed{MC = 6,915}$$

At 50 units of output:

- $TVC = 110,750$
- $AVC = 2,215$
- $AC = 2,245$
- $MC = 6,915$