Proof of Equality

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Proof. We will prove that:

$$\frac{1}{2} \sqrt{\frac{8\,n+2}{\pi}} \, \sqrt{2} \, \sqrt{\frac{4\,n+1}{\pi}} = \frac{4\,n+1}{\pi}$$

1. Start with the left side of the equation:

$$\frac{1}{2} \left(\frac{8n+2}{\pi} \right)^{\frac{1}{2}} 2^{\frac{1}{2}} \left(\frac{4n+1}{\pi} \right)^{\frac{1}{2}}$$

2. Simplify $2^{\frac{1}{2}}$:

$$\frac{1}{2}\!\!\left(\frac{8\,n+2}{\pi}\right)^{\!\frac{1}{2}}\!\!\sqrt{2}\!\left(\frac{4\,n+1}{\pi}\right)^{\!\frac{1}{2}}$$

3. Combine terms under square roots:

$$\frac{1}{2}\sqrt{\frac{8\,n+2}{\pi}}\,\sqrt{2}\,\sqrt{\frac{4\,n+1}{\pi}}$$

4. Combine $\sqrt{2}$ with one of the other square roots:

$$\frac{1}{2}\sqrt{\frac{8\,n+2}{\pi}}\,\sqrt{\frac{2\,(4\,n+1)}{\pi}}$$

5. Multiply terms under the square roots:

$$\frac{1}{2}\sqrt{\frac{8\,n+2}{\pi}}\,\sqrt{\frac{8\,n+2}{\pi}}$$

6. Multiply equal square roots:

7. Multiply
$$\frac{1}{2}$$
 by $(8n+2)$: $\frac{1}{2} \frac{8n+2}{\pi}$

This is exactly the right side of the equation we were trying to prove.

Therefore, we have shown that:

$$\frac{1}{2} \sqrt{\frac{8\,n+2}{\pi}} \, \sqrt{2} \, \sqrt{\frac{4\,n+1}{\pi}} = \frac{4\,n+1}{\pi}$$

The proof is complete.