

> h := unapply(MmaTranslator:-FromMma("Sqrt[\[Pi]] Gamma[3/4] Hypergeometric0F1Regularized[5/4, -(s

$$h := s \mapsto \frac{\sqrt{\pi} \cdot \Gamma\left(\frac{3}{4}\right) \cdot \text{hypergeom}\left(\left[\right], \left[\frac{5}{4}\right], -\frac{s^2}{4}\right)}{\Gamma\left(\frac{5}{4}\right)} \quad (1)$$

> h := unapply(simplify(h(s)), s);

$$h := s \mapsto \frac{\sqrt{\pi} \cdot \Gamma\left(\frac{3}{4}\right) \cdot \text{BesselJ}\left(\frac{1}{4}, s\right) \cdot 2^{\frac{1}{4}}}{s^{\frac{1}{4}}} \quad (2)$$

> j := (n, y) → BesselJ(n +  $\frac{1}{2}$ , y) · sqrt( $\frac{\text{Pi}}{2 \cdot y}$ )

$$j := (n, y) \mapsto \text{BesselJ}\left(n + \frac{1}{2}, y\right) \cdot \sqrt{\frac{\pi}{2 \cdot y}} \quad (3)$$

> pochhammer(1, - $\frac{1}{2}$ )

$$\sqrt{\pi} \quad (4)$$

> psi := unapply( $\sqrt{\frac{8 \cdot n + 2}{\text{Pi}}} \cdot (-1)^n \cdot j(2 \cdot n, y), n, y$ )

$$\psi := (n, y) \mapsto \frac{\sqrt{\frac{8 \cdot n + 2}{\pi}} \cdot (-1)^n \cdot \text{BesselJ}\left(2 \cdot n + \frac{1}{2}, y\right) \cdot \sqrt{2} \cdot \sqrt{\frac{\pi}{y}}}{2} \quad (5)$$

> fuck := (x) → sum(sqrt(lambda(n)) · psi(n, x), n = 0..infinity)

$$\text{fuck} := x \mapsto \sum_{n=0}^{\infty} \sqrt{\lambda(n)} \cdot \psi(n, x) \quad (6)$$

> evalf(fuck(2.3))

$$-0.02643929057 \quad (7)$$

> evalf(h(2.3))

$$0.5125173325 \quad (8)$$

> h(0)

Error, (in h) numeric exception: division by zero

> limit(h(t), t = 0)

$$\frac{2\sqrt{2}\Gamma\left(\frac{3}{4}\right)^2}{\sqrt{\pi}} \quad (9)$$

> plot(h(x), x = 0..40)

> evalf(sqrt(BesselJ(0, 2.3)))

$$0.2356688025 \quad (10)$$

$$\begin{aligned} &> \\ &> \text{evalf}\left(\frac{\text{fuck}(1.1, 2.3)}{\text{BesselJ}(0, 1.1 - 2.3)}\right) \\ &0.3707841547 \end{aligned} \quad (11)$$

$$\begin{aligned} &> \text{evalf}\left(\frac{\text{fuck}(1.1, 2.3)}{\text{BesselJ}(0, 1.1 - 2.3)}\right) \\ &0.3707841547 \end{aligned} \quad (12)$$

$$\begin{aligned} &> \text{evalf}\left(\frac{1}{\text{Pi}}\right) \\ &0.3183098861 \end{aligned} \quad (13)$$

$$\begin{aligned} &> \text{evalfe}() \\ &0.6711327443 \end{aligned} \quad (14)$$

$$\begin{aligned} &> \\ &> \text{lambda} := \text{unapply}(\text{simplify}(\text{int}(\text{psi}(n, x) \cdot \text{BesselJ}(0, x), x = 0..infinity)), n) \text{ assuming } n :: \\ &\text{nonnegint} \end{aligned}$$

$$\lambda := n \mapsto \frac{\sqrt{8 \cdot n + 2} \cdot \Gamma\left(n + \frac{1}{2}\right)^2}{2 \cdot \sqrt{\pi} \cdot \Gamma(n + 1)^2} \quad (15)$$

$$\begin{aligned} &> \text{sum}(\text{lambda}(n) \cdot (\text{psi}(n, x)), n = 0..infinity) \\ &\sum_{n=0}^{\infty} \frac{\sqrt{8n+2} \Gamma\left(n + \frac{1}{2}\right)^2 \sqrt{\frac{8n+2}{\pi}} (-1)^n \text{BesselJ}\left(2n + \frac{1}{2}, x\right) \sqrt{2} \sqrt{\frac{\pi}{x}}}{4\sqrt{\pi} \Gamma(n+1)^2} \end{aligned} \quad (16)$$

$$\begin{aligned} &> \text{evalf}(\text{eval}(\mathbf{(16)}, x = 2.3)) \\ &0.05553978444 \end{aligned} \quad (17)$$

$$\begin{aligned} &> \text{evalf}(\text{BesselJ}(0, 2.3)) \\ &0.05553978445 \end{aligned} \quad (18)$$

$$\begin{aligned} &> \text{evalf}(\text{eval}(\text{sum}(\text{sqrt}(\text{lambda}(n)) \cdot \text{psi}(n, x), n = 0..infinity), x = 5.3)) \\ &-0.01804174321 \end{aligned} \quad (19)$$

$$\begin{aligned} &> \text{evalf}(\text{BesselJ}(0, 5.3)) \\ &-0.07580311159 \end{aligned} \quad (20)$$

$$> \text{simplify0}(\text{int}(h(s)^2, s))$$

$$\frac{8\Gamma\left(\frac{3}{4}\right)^4 \text{shypergeom}\left(\left[\frac{1}{2}, \frac{3}{4}\right], \left[\frac{5}{4}, \frac{3}{2}, \frac{3}{2}\right], -s^2\right)}{\pi} \quad (21)$$

> *plot*((**21**), *s* = 0..40)  
> *limit*((**21**), *s* = infinity)

$$\pi^2 \quad (22)$$

>  
> *funcSeq* := [*seq*( $x^{(2^n)}$ , *n* = 0..8)]:  
 $w := \text{unapply}(\text{simplify}(\text{sqrt}(\frac{1}{\text{sqrt}(1-x^2)})), x):$   
*interval* := -1..1:  
*InnerProduct* := (*f*, *g*) → *int*(*f* \* *g* \* *w*(*x*), *x* = *interval*):  
*P* := []:  
for *i* to *nops*(*funcSeq*) do *f* := *funcSeq*[*i*] - (*add*((*InnerProduct*(*funcSeq*[*i*], *P*[*j*])) \*  
*P*[*j*], *j* = 1..*i* - 1)):  
*P* := [*op*(*P*), *simplify*(*f*/sqrt(*InnerProduct*(*f*, *f*)))]:  
end do:

$$> \text{int}(P[2] \cdot P[3] \cdot \text{sqrt}(\frac{1}{\text{sqrt}(1-x^2)}), x = -1..1) \quad 0 \quad (23)$$

> *plot*(*P*, *x* = -1..1)  
> *Q* := [*seq*(*simplify*(*int*(*P*[*n*] · exp(-*I* · *x* · *y*), *x* = -1..1)), *n* = 1..*nops*(*P*))]:  
> *int*(*Q*[1] · *h*(*x* - *y*), *y* = 0..infinity)

$$\int_0^\infty \frac{\sqrt{2} \pi^{\frac{3}{4}} \sin(y) \text{BesselJ}(\frac{1}{4}, x-y)}{y (x-y)^{\frac{1}{4}}} dy \quad (24)$$

> *Q*[1]

$$\frac{2^{\frac{1}{4}} \pi^{\frac{1}{4}} \sin(y)}{y \Gamma(\frac{3}{4})} \quad (25)$$

> *limit*(*h*(*t*), *t* = 0)

$$\frac{2\sqrt{2} \Gamma(\frac{3}{4})^2}{\sqrt{\pi}} \quad (26)$$

> *evalf*([sqrt((**24**)), (**26**)])

$$[2.205257706, 2.396280468] \quad (27)$$

> *plot*(*Q*, *y* = 1..30)  
> *S* := []:  
for *i* to *nops*(*Q*) do *f* := *Q*[*i*] - (*add*((*int*(*Q*[*i*] · *Q*[*j*], *y* = 0..infinity)) \* *Q*[*j*], *j* =

```

1..i-1)):
S := [op(S), simplify(f/sqrt(int(f·f, y = 0..infinity)))]:
end do:
> Digits := 40:
> Q[1], S[1]

```

$$\frac{2^{\frac{1}{4}} \pi^{\frac{1}{4}} \sin(y)}{y \Gamma\left(\frac{3}{4}\right)}, \frac{\sqrt{2} \sin(y)}{\sqrt{\pi} y} \quad (28)$$

```

> [seq(int(S[k]·h(y), y = 0..infinity), k = 1..4)]

```

$$\left[ 2\Gamma\left(\frac{3}{4}\right)^2, \frac{2\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2 2^{\frac{1}{4}}}{\sqrt{\sqrt{2}\pi^3 + 42\sqrt{2}\Gamma\left(\frac{3}{4}\right)^4 - 4\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2}}, \frac{112 2^{\frac{1}{4}} \pi^{\frac{3}{2}} \sqrt{15} \Gamma\left(\frac{3}{4}\right)^2}{5\sqrt{17227\sqrt{2}\pi^3 + 889728\sqrt{2}\Gamma\left(\frac{3}{4}\right)^4 - 89248\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2}}, \frac{112 2^{\frac{1}{4}} \pi^{\frac{3}{2}} \sqrt{15} \Gamma\left(\frac{3}{4}\right)^2}{5\sqrt{17227\sqrt{2}\pi^3 + 889728\sqrt{2}\Gamma\left(\frac{3}{4}\right)^4 - 89248\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2}}, \frac{112 2^{\frac{1}{4}} \pi^{\frac{3}{2}} \sqrt{15} \Gamma\left(\frac{3}{4}\right)^2}{5\sqrt{17227\sqrt{2}\pi^3 + 889728\sqrt{2}\Gamma\left(\frac{3}{4}\right)^4 - 89248\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2}}, \frac{112 2^{\frac{1}{4}} \pi^{\frac{3}{2}} \sqrt{15} \Gamma\left(\frac{3}{4}\right)^2}{5\sqrt{17227\sqrt{2}\pi^3 + 889728\sqrt{2}\Gamma\left(\frac{3}{4}\right)^4 - 89248\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2}} \right] \quad (29)$$

```

> evalf((29))

```

$$\begin{aligned} & [3.003292189361259431385684511618701903364, \\ & 1.655340177346592511697212309422638340199, \\ & 0.5113189621180808947286423648995738323325, \\ & 0.2568272866444580562039925201540020101747] \end{aligned} \quad (30)$$

```

> evalf((29))

```

$$0.4886435441678435587121541791815017611107 \quad (31)$$

```

>
> plot(Q, y = 1..40)
> plot(S, y = 1..40)
> [seq(simplify(int(S[n]·h(y), y = 0..infinity)), n = 1..4)]

```

$$\left[ 2\Gamma\left(\frac{3}{4}\right)^2, \frac{2\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2 2^{\frac{1}{4}}}{\sqrt{-4\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2 + \left(42\Gamma\left(\frac{3}{4}\right)^4 + \pi^3\right)\sqrt{2}}}, \frac{112 2^{\frac{1}{4}} \pi^{\frac{3}{2}} \sqrt{15} \Gamma\left(\frac{3}{4}\right)^2}{5\sqrt{17227\sqrt{2}\pi^3 - 89248\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2 + 889728\sqrt{2}\Gamma\left(\frac{3}{4}\right)^4}}, \frac{112 2^{\frac{1}{4}} \pi^{\frac{3}{2}} \sqrt{15} \Gamma\left(\frac{3}{4}\right)^2}{5\sqrt{17227\sqrt{2}\pi^3 - 89248\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2 + 889728\sqrt{2}\Gamma\left(\frac{3}{4}\right)^4}}, \frac{112 2^{\frac{1}{4}} \pi^{\frac{3}{2}} \sqrt{15} \Gamma\left(\frac{3}{4}\right)^2}{5\sqrt{17227\sqrt{2}\pi^3 - 89248\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2 + 889728\sqrt{2}\Gamma\left(\frac{3}{4}\right)^4}}, \frac{112 2^{\frac{1}{4}} \pi^{\frac{3}{2}} \sqrt{15} \Gamma\left(\frac{3}{4}\right)^2}{5\sqrt{17227\sqrt{2}\pi^3 - 89248\pi^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)^2 + 889728\sqrt{2}\Gamma\left(\frac{3}{4}\right)^4}} \right] \quad (32)$$

```

> cool := unapply(sum(S[n]·(32)[n], n = 1..4), y):
> S[1]

```

$$\frac{\sqrt{2} \sin(y)}{\sqrt{\pi} y} \quad (33)$$

```

> Digits := 40:
> Z1 := int(simplify(eval(S[1], y = x-y)·psi(0, x)), x = 0..infinity) assuming x >
0:
> Z2 := int(simplify(eval(S[2], y = x-y)·psi(0, x)), x = 0..infinity) assuming x >
0:

```

```

> Z3 := int(simplify(eval(S[3], y = x - y) · psi(0, x)), x = 0..infinity) assuming x >
0:
> plot([Z1 + Z2 + Z3, h(y)], y = -10..40)
> restart
> simplify(S[2])

```

$$\frac{2^{\frac{1}{4}} \left( \sin(y) \sqrt{2} \pi^{\frac{3}{2}} y^2 + 18 \Gamma\left(\frac{3}{4}\right)^2 \sin(y) y^2 + 60 \Gamma\left(\frac{3}{4}\right)^2 \cos(y) y - 60 \Gamma\left(\frac{3}{4}\right)^2 \sin(y) \right)}{\sqrt{-4 \pi^{\frac{3}{2}} \Gamma\left(\frac{3}{4}\right)^2 + \left(42 \Gamma\left(\frac{3}{4}\right)^4 + \pi^3\right) \sqrt{2} \sqrt{\pi} y^3}} \quad (34)$$

```

> plot([cool(y), h(y)], y = 1..40)
> evalf((32))

```

$$[3.003292188, 1.655340178, 0.5113189623, 0.2568272869] \quad (35)$$

```

> ? MmaTranslator
> simplify(int(S[5] · h(y), y = 0..infinity))

```

$$6 \sqrt{5005} \Gamma\left(\frac{3}{4}\right) \int_0^\infty \frac{85865472 \left( \frac{302171 y^2 \left( \left( y^6 - \frac{411888410}{2115197} y^4 + \frac{14330150952}{3323881} y^2 - \frac{220273794000}{23267167} \right) \sin(y) + \frac{6020686 y \cos(y) \left( y^4 - \frac{790778196}{13635083} y^2 + \frac{647864}{13635} \right)}{302171} \right)}{1115136} \right)}{\sqrt{1572408604855267985 \sqrt{2} \pi^3 + 9298462762113}} \quad (36)$$

```

> evalf(%);

```

$$0.5113189623 \quad (37)$$

```

> plot(S, y = 1..40)
> qlim := [seq(limit(Q[n], y = 0), n = 1..nops(Q))]:
> qlim

```

$$\left[ \frac{2^{\frac{1}{4}} \pi^{\frac{1}{4}}}{\Gamma\left(\frac{3}{4}\right)}, -\frac{\sqrt{3} 2^{\frac{3}{4}} \pi^{\frac{1}{4}}}{12 \Gamma\left(\frac{3}{4}\right)}, -\frac{\sqrt{595} 2^{\frac{3}{4}} \pi^{\frac{1}{4}}}{560 \Gamma\left(\frac{3}{4}\right)}, -\frac{5 2^{\frac{1}{4}} \sqrt{231} \pi^{\frac{1}{4}}}{2464 \Gamma\left(\frac{3}{4}\right)}, \right. \\ \left. -\frac{11 \sqrt{195} 2^{\frac{3}{4}} \pi^{\frac{1}{4}}}{11520 \Gamma\left(\frac{3}{4}\right)}, -\frac{2^{\frac{1}{4}} \sqrt{1893749} \pi^{\frac{1}{4}}}{107008 \Gamma\left(\frac{3}{4}\right)}, -\frac{7 2^{\frac{1}{4}} \sqrt{676039} \pi^{\frac{1}{4}}}{612352 \Gamma\left(\frac{3}{4}\right)}, \right. \\ \left. -\frac{19 \sqrt{391} 2^{\frac{3}{4}} \pi^{\frac{1}{4}}}{73728 \Gamma\left(\frac{3}{4}\right)}, -\frac{15 \sqrt{86822723} 2^{\frac{3}{4}} \pi^{\frac{1}{4}}}{34537472 \Gamma\left(\frac{3}{4}\right)} \right] \quad (38)$$

```

> LREtools[GuessRecurrence](qlim, a(n))

```

$$FAIL \quad (39)$$

> GR := [seq(piecewise(y = 0, qlim[n], Q[n]), n = 1..nops(Q))]:

>

>

> j := (n, y) → BesselJ(n +  $\frac{1}{2}$ , y) · sqrt( $\frac{\text{Pi}}{2 \cdot y}$ )

$$j := (n, y) \mapsto \text{BesselJ}\left(n + \frac{1}{2}, y\right) \cdot \sqrt{\frac{\pi}{2 \cdot y}} \quad (40)$$

> psi := unapply( $\sqrt{\frac{8 \cdot n + 2}{\text{Pi}}} \cdot (-1)^n \cdot j(2 \cdot n, y), n, y$ )

$$\psi := (n, y) \mapsto \frac{\sqrt{\frac{8 \cdot n + 2}{\pi}} \cdot (-1)^n \cdot \text{BesselJ}(2 \cdot n + \frac{1}{2}, y) \cdot \sqrt{2} \cdot \sqrt{\frac{\pi}{y}}}{2} \quad (41)$$

> simplify(int(eval(Q[1], y = x - y) · psi(0, x), x = 0..infinity)) assuming y > 0

$$\frac{2^{\frac{3}{4}} (-2 \cos(y) \text{Ei}_1(-2 \text{I} y) + (-2 \text{I} \cos(y) + 2 \sin(y)) \text{Si}(2y) + (\pi \text{I} - 2\gamma - 2 \ln(2)) 2 \ln(y) \cos(y) + 2\pi \sin(y))}{4\pi^{\frac{1}{4}} y \Gamma(\frac{3}{4})} \quad (42)$$

> simplify(int(eval(Q[1], y = x - y) · psi(2, x), x = 0..infinity)) assuming y > 0

$$\frac{3 \left( (-2y^4 + 90y^2 - 210) \cos(y) + (20y^3 - 210y) \sin(y) \right) \text{Ei}_1(-2 \text{I} y) + \left( (-210y + 20y^3 + 90 \text{I} y^2 - 2 \text{I} y^4 - 210 \text{I}) \right)}{(43)} \quad (43)$$

>

$$\frac{7}{3} \quad (44)$$

> simplify(int(eval(Q[1], y = x - y) · psi(3, x), x = 0..infinity)) assuming y > 0

$$(45)$$

$$21 \cdot 2^{\frac{3}{4}} \left( ((-990 + 450y^2 - 20y^4 + \frac{2}{21}y^6) \cos(y) - 2 \sin(y) y (y^4 - 60y^2 + 495)) \text{Ei}_1(-2 \text{I} y) + \left( (-990 \text{I} + \frac{2 \text{I} y^6}{21} - \right) \right)$$

> plot([(42) + (43) + (45)], y = 0..40)

> simplify(int(eval(R[1], y = x - y) · psi(n, x), y = 0..infinity)) assuming x > 0

$$\frac{2^{\frac{1}{4}} \pi^{\frac{1}{4}} \sqrt{4n + 1} (-1)^n \text{BesselJ}(2n + \frac{1}{2}, x) (\pi + 2 \text{Si}(x))}{2\sqrt{x} \Gamma(\frac{3}{4})} \quad (46)$$

> simplify(int(eval(R[2], y = x - y) · psi(n, x), y = 0..infinity)) assuming x > 0

$$(47)$$

$$\frac{\sqrt{4n + 1} 2^{\frac{3}{4}} \sqrt{3} (-1)^n \text{BesselJ}(2n + \frac{1}{2}, x) \pi^{\frac{1}{4}} (\pi x^2 + 2 \text{Si}(x) x^2 + 5 \cos(x) x - 5 \sin(x))}{4x^{\frac{5}{2}} \Gamma(\frac{3}{4})}$$

> simplify(int(eval(R[3], y = x - y) · psi(n, x), y = 0..infinity)) assuming x > 0

$$\frac{((-3x^3 + 234x) \cos(x) + (81x^2 - 234) \sin(x) + 2x^4 (\pi + 2 \operatorname{Si}(x))) (-1)^n 2^{\frac{3}{4}} \sqrt{595} \pi^{\frac{1}{4}} \sqrt{4n+1} \operatorname{BesselJ}(2n + \frac{1}{2}, x)}{112x^{\frac{9}{2}} \Gamma(\frac{3}{4})} \quad (48)$$

> simplify(int(eval(R[4], y = x - y) · psi(n, x), y = 0..infinity)) assuming x > 0

$$\frac{25 \left( \left( \frac{117}{20} x^5 - 884x^3 + 9282x \right) \cos(x) + \left( -\frac{377}{4} x^4 + 3978x^2 - 9282 \right) \sin(x) + x^6 (\pi + 2 \operatorname{Si}(x)) \right) \sqrt{231} \pi^{\frac{1}{4}} \operatorname{BesselJ}(2n + \frac{1}{2}, x)}{616x^{\frac{13}{2}} \Gamma(\frac{3}{4})} \quad (49)$$

> int(h(x - y) · psi(0, x), x = 0..infinity)

$$\int_0^\infty \frac{\Gamma(\frac{3}{4}) \operatorname{BesselJ}(\frac{1}{4}, x - y) 2^{\frac{3}{4}} \sqrt{\frac{1}{\pi}} \sin(x) \sqrt{\frac{\pi}{x}}}{(x - y)^{\frac{1}{4}} \sqrt{x}} dx \quad (50)$$

> R[1]

$$\begin{cases} \frac{2^{\frac{1}{4}} \pi^{\frac{1}{4}}}{\Gamma(\frac{3}{4})} & y = 0 \\ \frac{2^{\frac{1}{4}} \pi^{\frac{1}{4}} \sin(y)}{y \Gamma(\frac{3}{4})} & otherwise \end{cases} \quad (51)$$

> int(R[4] · h(y), y = 0..infinity)

$$0 \quad (52)$$

> R[1]

$$\begin{cases} \frac{2^{\frac{1}{4}} \pi^{\frac{1}{4}}}{\Gamma(\frac{3}{4})} & y = 0 \\ \frac{2^{\frac{1}{4}} \pi^{\frac{1}{4}} \sin(y)}{y \Gamma(\frac{3}{4})} & otherwise \end{cases} \quad (53)$$

>

> plot(eval([R[1], h(y)]), y = 10..40) assuming y > 0

> T0 := x → evalf(sum((49), n = 0..infinity))

$$T0 := x \mapsto \operatorname{evalf} \left( \sum_{n=0}^{\infty} \frac{2^{\frac{1}{4}} \cdot \pi^{\frac{1}{4}} \cdot \sqrt{4 \cdot n + 1} \cdot (-1)^n \cdot \operatorname{BesselJ}(2 \cdot n + \frac{1}{2}, x) \cdot (\pi + 2 \cdot \operatorname{Si}(x))}{2 \cdot \sqrt{x} \cdot \Gamma(\frac{3}{4})} \right) \quad (54)$$

> T0(50)

$$0.69496304639411432969348006968092384218795550668289 \quad (55)$$

> identify(%)

$$1.6203072135490037964031307528142182394016460992060 \quad (56)$$

> plot(T0(x), x = 1..40, numpoints = 10)

```
> evalf(qlim)
```

$$\begin{aligned} & [1.2919960074815039352250155313215753868047540488077, \\ & -0.26372758067023017667367968873263465960188389299788, \\ & -0.079587822977365377164737043736925066723833552034551, \\ & -0.039847076390798901044323244907309271068750757938882, \\ & -0.024363163580921390183284426196598896497406523783581, \\ & -0.016615221403589924483882721598533733575655269793582, \\ & -0.012143501934248353091005674889882946710960910765781, \\ & -0.0093107720887866508329712410511872322488968599373591, \\ & -0.0073942407012649535541762743085938008627232267738976] \end{aligned} \quad (57)$$

```
> evalf(T0(0))
```

Error, (in T0) numeric exception: division by zero

```
> simplify((43) + (45) + (46) + (47) + (48) + (49))
```

$$585 \, 2^{\frac{1}{4}} \left( \sqrt{4n+1} \left( \frac{20x^6 \left( \left( -\frac{11\sqrt{5}\sqrt{7}\sqrt{17}}{25} + \frac{154\sqrt{3}}{25} \right) \sqrt{2} + \sqrt{3}\sqrt{7}\sqrt{11} - \frac{308}{25} \right) \pi^{\frac{3}{2}}}{117} + \left( \frac{22x^2 \left( \sqrt{5}\sqrt{17} \left( -\frac{4x^4 \text{Si}(x)}{3} + \cos(x)x^3 - 27 \sin(x) \right)}{117} \right)}{117} \right) \right) \quad (58)$$

```
>
```

$$\frac{7}{3} \quad (59)$$

```
> plot((58), y = -20..50, axes, gridlines = true)
```

Warning, expecting only range variable y in expression -585/2464\*2^(1/4)/x^(13/2)\*((4\*n+1)^(1/2)\*(20/117

```
> plot(R, y = -10..40)
```

```
> plot(P, x = -1..1)
```

```
> Q := [seq(simplify(int(P[n] * exp(-I * x * y), x = -1..1)), n = 1..nops(P))]:
```

```
> int(Q[1] * Q[3], y = 0..infinity)
```

$$-\frac{\pi^{\frac{3}{2}}\sqrt{595}}{560\Gamma\left(\frac{3}{4}\right)^2} \quad (60)$$

```
> plot(Q[3], y = 0..30)
```

```
> h(y)
```

$$\frac{-\frac{1}{2} \left( \text{I}(-\text{I}y)^{\frac{1}{4}} \left( \text{BesselI}\left(\frac{1}{4}, \text{I}y\right) - \text{StruveL}\left(\frac{1}{4}, \text{I}y\right) \right) (\text{I}y)^{\frac{3}{4}} + y \left( \text{StruveL}\left(\frac{1}{4}, -\text{I}y\right) - \text{BesselI}\left(\frac{1}{4}, -\text{I}y\right) \right) \right) \Gamma\left(\frac{3}{4}\right) 2^{\frac{1}{4}} \sqrt{\pi}}{y^2} \quad (61)$$

```
> int(Q[1] * h(y), y = 0..infinity)
```



$$\int_0^\infty \frac{-\frac{1}{2}\sqrt{2}\pi^{\frac{3}{4}}\sin(y)\left(\mathrm{I}\left(-\mathrm{I}y\right)^{\frac{1}{4}}\left(\mathrm{BesselI}\left(\frac{1}{4},\mathrm{I}y\right)-\mathrm{StruveL}\left(\frac{1}{4},\mathrm{I}y\right)\right)\left(\mathrm{I}y\right)^{\frac{3}{4}}+y\left(\mathrm{StruveL}\left(\frac{1}{4},-\mathrm{I}y\right)-\mathrm{BesselI}\left(\frac{1}{4},-\mathrm{I}y\right)\right)}{y^3}dy$$

```
> evalf((62))
> plot(2^1/4*pi^1/4*sin(y)/Gamma(3/4)y*(-y^2+1)^1/4,y=0..20)
> plot(Q,y=0..50)
> plot(P,x=-1..1)
>
```