

# Interactive Simulations for CfE Physics

Craig Roy

Supervisor: Gordon Robb

University of Strathclyde

## Introduction

### Aim

The aim of this project was to create interactive simulations to aid the teaching of the new Higher and Advanced Higher Physics Curriculum for Excellence courses.

### Motivation

Since the Curriculum for Excellence programme was implemented, there has been a demand for resources to aid in teaching the new elements of the Higher and Advanced Higher Physics curriculum.

### Choice of topics

The topics chosen for this project were:

- Special Relativity
- Particle Accelerators
- The Doppler Effect

These topics were all introduced with the Curriculum for excellence program. The topics were chosen for this project from a SUPA<sup>[1]</sup> video competition with the same goal of creating more resources for the new physics courses.

### Practical considerations

The tool used to create the simulations was a program called EjsS or “Easy Java(Script) Simulations”. EjsS<sup>[2]</sup> is a tool created as a part of the Open Source Physics project. It is designed to make creating computer simulations easy for people such as science teachers and students who are otherwise unfamiliar with programming in Java or JavaScript.

This program was chosen so that simulations could be developed with relative ease, and so that there is a no barrier to entry for someone who wants to modify the simulations. Developing the simulations as Java programs also meets the needs of physics teachers who cannot access the internet while teaching to view Flash simulations or Java Applets.

## The Simulations

**Topic:** Our Dynamic Universe

**Subtopic:** Special relativity

The first simulation shows a pair of digital clocks. One relatively stationary in a lab, and the other travelling at a relativistic speed specified by the user. The observer is in the reference frame of the lab clock and can observe the slowing down of the moving clock.

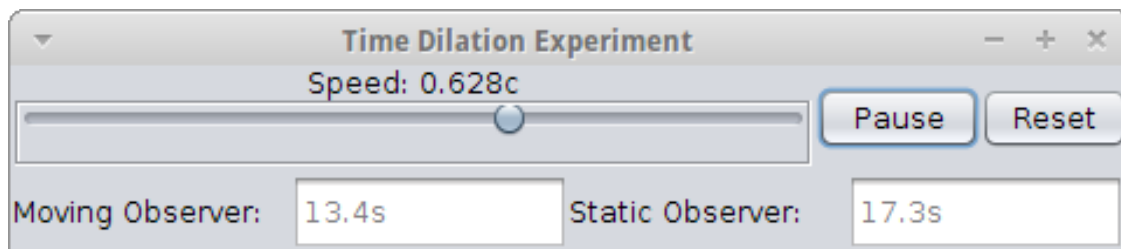


Figure 1: Screenshot of the digital clock simulation

## Analogue Clocks

**Topic:** Our Dynamic Universe

**Subtopic:** Special relativity

The second simulation shows a pair of analogue clocks, one of which is travelling at relativistic speeds. In this simulation, the observer is in the reference frame of the clock travelling at a relativistic speed specified by the user. The user can observe that the stationary clock speeds up as the velocity is increased.

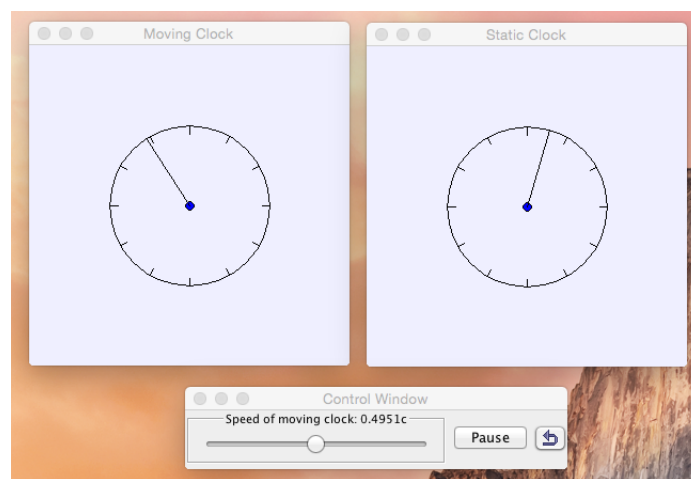


Figure 2: Screenshot of the analogue clock simulation

## Photon Clocks

**Topic:** Our Dynamic Universe

**Subtopic:** Special relativity

This simulation shows a pair of model photon clocks, with a ‘photon’ bouncing between two mirrors. The user is in the reference frame of the lab clock. As the user sets the speed of the moving clock, it begins to move across the window. At relativistic speeds, the motion of the photon appears to slow and the moving photon clock contracts in size due to time dilation. This simulation was inspired by a similar flash simulation developed by the King’s Center for Visualisation in Science<sup>[3]</sup>.

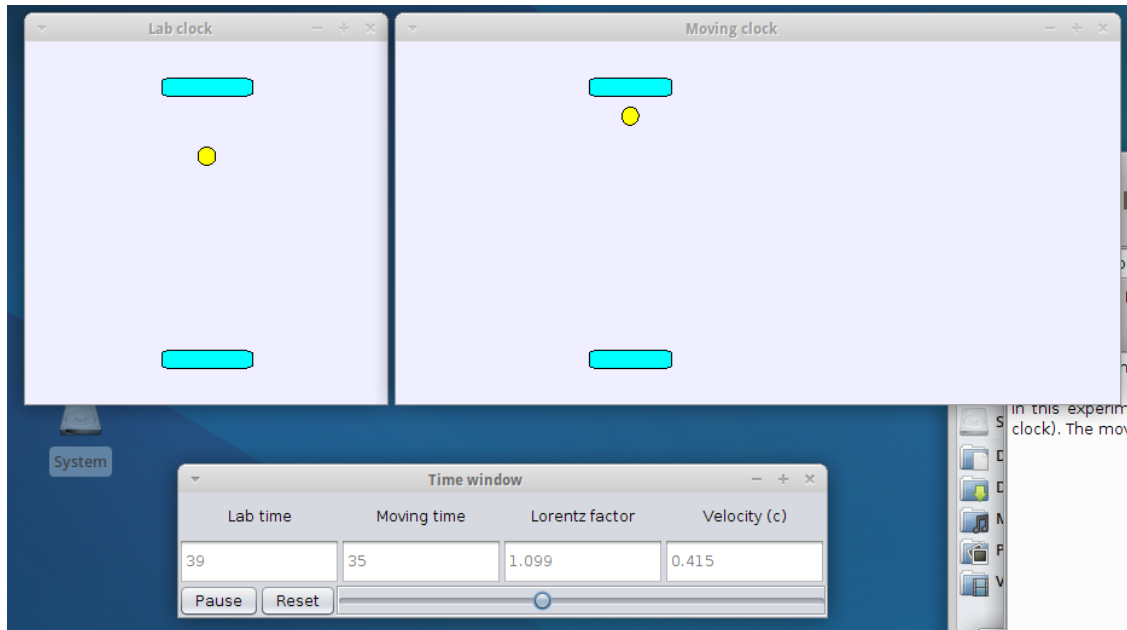


Figure 3: Screenshot of the photon clock simulation

## Cyclotron

**Topic: Electromagnetism**

**Subtopic: Particle Accelerators**

This simulation models a cyclotron particle accelerator which is relevant to the electromagnetism section of the Advanced Higher course. The user may set variables such as the strength of the electric field, the charge of the particle, and the frequency of oscillation of the electric field and the accelerator will apply the Lorentz force accordingly. This simulation was inspired by a similar Java Applet created by the National Taiwan Normal University<sup>[4]</sup>.

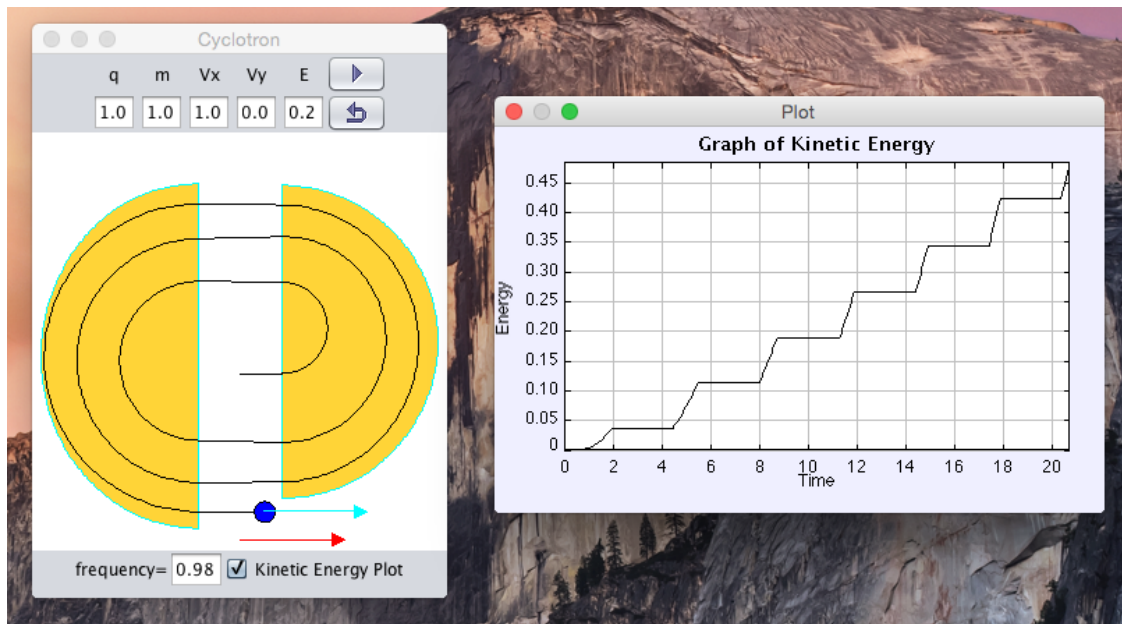


Figure 4: Screenshot of the cyclotron simulation

## Doppler Effect

**Topic: Our Dynamic Universe**

**Subtopic: The Expanding Universe**

This simulation demonstrates the concept of the doppler shift as well as the concept of using spectroscopy on exoplanets. The simulation consists of a model exoplanet which is orbiting a star. The planet is being monitored using spectroscopy. The absorption lines are shown on a spectrum of visible light at the bottom of the window. The user chooses the angular velocity of the planet and star, and a Doppler shift is applied to the spectral lines when the planet is moving towards the observer or further away. This experiment was inspired by a similar Flash simulation created by the University of Nebraska-Lincoln<sup>[5]</sup>.

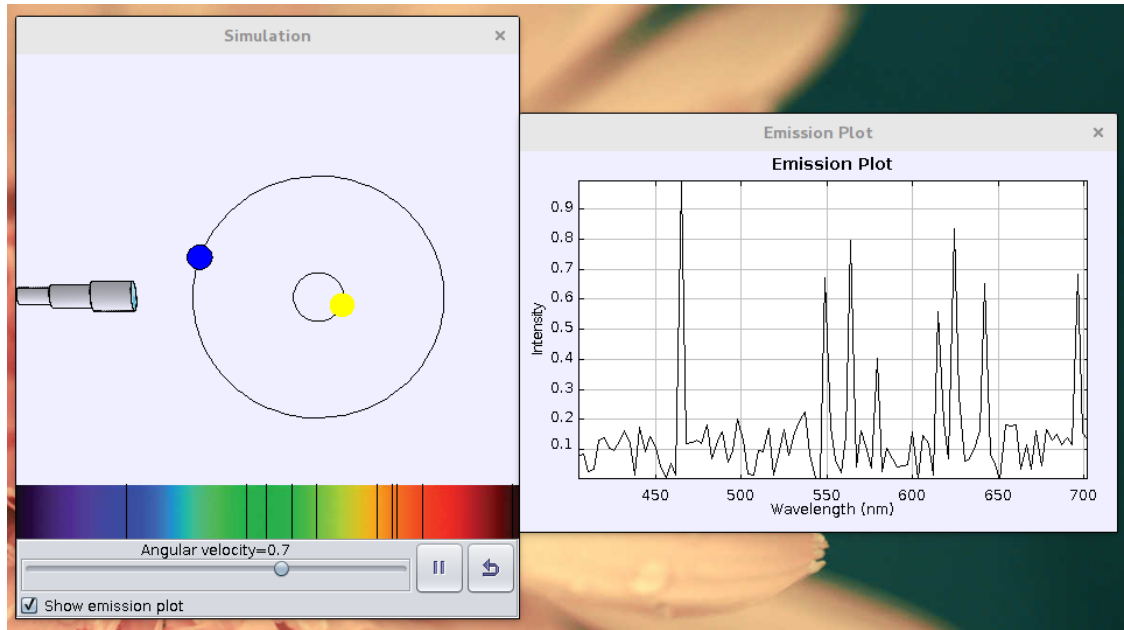


Figure 5: Screenshot of the Doppler Effect simulation

## Conclusion

These simulations were produced during the limited time frame of the project which was six weeks. Given more time, more of the syllabus could be covered by such simulations.

All of the simulations produced in this project are open source and available online<sup>[6]</sup>. They can be easily used or modified by anyone with the inclination.

## Acknowledgements

We acknowledge and are grateful for partial support from the Scottish Universities Physics Alliance.

## References

- [1] SUPA Video Competition, [http://www.supa.ac.uk/events/supa\\_videos\\_2014](http://www.supa.ac.uk/events/supa_videos_2014)
- [2] Easy Java(Script) Simulations, Francisco Esquembre, Open Source Physics, <http://fem.um.es/Ejs>
- [3] Photon Clock, Special Relativity, King's Center for Visualization in Science, [http://www.kcvs.ca/site/projects/specialRelativity.html#Photon\\_Clock](http://www.kcvs.ca/site/projects/specialRelativity.html#Photon_Clock)
- [4] Cyclotron Applet, Fu-Kwun Hwang, Dept. of physics, National Taiwan Normal University, Modified: 11/14/2007, <http://www.schulphysik.de/ntnujava/cyclotron/cyclotron.html>
- [5] Extrasolar Planet Radial Velocity Demonstrator, University of Nebraska-Lincoln, <http://astro.unl.edu/classaction/animations/light/radialvelocitydemo.html>
- [6] Github, ComPADRE TBA

# A Special Relativity Report

## Description

This simple time-dilation experiment consists of two ‘clocks’ showing how the time experienced by a clock moving at a relativistic speed specified by the user in the ‘vField’.

## How it works

### Variables

- $v$  is the speed of the moving clock which is specified by the user.
- $t$  is the time shown on the slower, moving clock. It is used to calculate  $t2$ .
- $t2$  is the time shown on the static clock, it is calculated for each evolution, by multiplying  $t$  by the lorentz factor,  $\gamma$ .

### Evolution

The independant variable which is incremented at each evolution is  $t$ . The animation runs at 20fps, incrementing  $t$  by 0.05 each time, meaning that  $t$  increases by 1 second per second. The variable  $t2$  increments at  $\frac{0.05\gamma}{frame}$ , so  $\gamma$  seconds per second.

### UI

In the ‘control panel’ on top, the UI consists of a field in which the user can enter the speed of the moving clock, along with pause and reset buttons. In the bottom ‘time panel’, the time passed for both the moving and the static clocks is shown. These time fields display the values to one decimal point as a number of seconds.

## Experiment 2: Analogue Clocks

### Description

This experiment is very similar to the previous one, but the information is displayed with model analogue clocks rather than digital displays. Hopefully, this is a clearer demonstration of the concept at hand, and more fun to watch. In this experiment the moving clock runs at 1 second per second, and the static clock runs faster, whereas in the previous experiment, the static clock ran at 1 second per second and the moving clock ran slower.

## How it works

### Variables

- $v$  is the speed of the moving clock which is entered by the user.
- $t_{ic}$  is designed to be the independent variable in the ODE page. It is equivalent to the angle in degrees from the 12th hour on the slower moving clock.

- $a1$  is the angle from the 12th hour of the slower moving clock in radians. It is calculated by  $\frac{tic \times \pi}{180}$ .
- $x1, y1$  are the x and y coordinates of the slower clock's hands. They are calculated from  $a1$  using trigonometry in the fixed relations page.
- $lorentz$  is the lorentz factor,  $\gamma$ , dependant on the speed entered by the user.
- $a2$  is the angle from the 12th hour of the faster clock in radians. It is found by  $\gamma \times a1$ .
- $x2, y2$  are the angles needed for the hands of the faster clock. Calculated using  $a2$  rather than  $a1$ .

## Evolution

The variables  $a1$  and  $a2$  evolve according to the independant variable  $tic$ . In  $a1$ , simply converts  $tic$  to radians and  $a2$  multiplies  $a1$  by  $\gamma$ . The simulation runs at 6fps, where  $tic$  is incremented by 1 every frame. This means that the angle of the hand on the slower clock increases by  $6^\circ$  every second.  $6^\circ$  is the angle between 1 second increments on an analogue clock. From the increments in  $a1$  and  $a2$ , the corresponding  $x$  and  $y$  values are calculated using the fixed relations  $x = -0.5 \cos(a)$  and  $y = 0.5 \sin(a)$ .

## UI

The experiments UI consists of three windows:

- *Spaceship Clock* shows time moving at 1 second per second in the moving rest frame.
- *Earth Clock* shows time in the static observer frame accelerated by a lorentz factor.
- *Control Panel* contains a field for the user to input the speed of the moving (spaceship) frame, a play/pause button and a reset button.

## Experiment 3: Photon Clock

### Description

This experiment involves the concept of a photon clock. A photon clock is a device which measures the passage of time when a photon hits a sensor.

In this experiment there is a stationary clock (the lab clock) and a moving photon clock (the moving clock)

### How to use it

The slider can be used to adjust the speed of the clock in the moving frame. Observe how at speeds very close to the speed of light, the width of the moving photon clock changes. The times measured by the two clocks are shown in a third window, and so is the Lorentz factor of the second clock and the speed.



## How it works

### Variables

- Simulation variables
  - $x$ ,  $vx$  are the position and velocity of the moving photon clock system along the x-axis within the frame. The  $x$  position of the clock is incremented by  $vxdt$ .
  - $y$ ,  $vy$  are the position and velocity of the photon in the y-axis for the lab clock.  $y$  is incremented by  $vydt$  for each evolution of the system.
  - $y2$ ,  $vy2$  are the position and velocity of the photon in the y-axis for the moving photon clock system.  $y2$  is incremented by  $vy2dt2$  each evolution of the system.
  - $lorentz$  is the value of the Lorentz factor for the moving clock based on the speed of the clock as specified by the user
  - $t$  is the time observed by the lab clock.
  - $dt$  is the interval in which the lab clock is incremented.
  - $t2$  is the time observed by the moving clock.
  - $dt2$  is the interval with which the variables in the moving clock system are incremented. It is defined as  $\frac{dt}{\gamma}$ .
- Length scaling variables
  - $mirror$  is the width of the mirrors in the moving clock window. It is a fixed relation  $\frac{2.5}{\gamma}$  so it varies with the speed of the system in order to demonstrate length contraction.
  - $photon$  is the width of the photon in the moving clock window. It is of the fixed relation  $\frac{0.5}{\gamma}$  so that it also shrinks at high speeds in order to demonstrate length contraction.
  - $upper$  is point at which the photon should hit the upper mirror and start moving in the opposite direction.
  - $lower$  is the point at which the photon should hit the lower mirror and start moving in the opposite direction.

### Evolution

Like the previous simulations, this simulation runs at 20fps. The evolution of this system is specified with code, rather than ODEs. There are two time variables  $t$  and  $t2$ . As the system evolves,  $t$  is incremented in real time and  $t2$  is incremented by  $t2 = \frac{realtime}{\gamma}$ .

The x-coordinate for the moving clock system simply increases by  $vxdt$  on each evolution, the y-coordinate for the moving system similarly increases by  $vydt$ .

### UI

The UI consists of three frames:

- Lab clock frame  
The lab clock frame consists of two mirrors with a photon bouncing between them.

- Moving clock frame

The moving clock frame consists of a photon clock just like in the lab clock frame, but the frame is twice as wide, and as such, the scaling factors in the x axis for the objects are half the value as in the lab clock frame.

This whole system begins to move when the simulation is started and the speed is greater than  $0c$ .

- Time frame

The timing frame consists of a series of fields showing values of variables and a velocity slider.

- *Velocity slider* is the widget used to increase the velocity of the moving clock system. It has a maximum value of  $1c$  and a minimum value of  $0c$ . Its value is shown by the velocity field.
- *Lab time field* shows the time observed on the photon clock which is at rest in the lab.
- *Moving time field* shows the time observed on a photon clock which is moving away from the lab at a relativistic speed specified by the slider.
- *Lorentz factor field* shows the Lorentz factor used in making the time dilation and length contraction calculations based on the speed of the moving clock.
- *Velocity field* shows the velocity of the moving clock as a fraction of  $c$ .

## B Cyclotron Report

### Description

This experiment simulates a kind of particle accelerator called a cyclotron. A cyclotron operates by applying an alternating electric field between two D-shaped metal structures referred to as “Dees”. This causes a static particle between the Dees to enter one of the Dees where it is then shielded from the electric field, but exposed to a magnetic field within the Dee. This magnetic field causes the particle’s trajectory to rotate so that it then leaves the Dee and reenters the electric field, increasing its velocity and thus putting it in a wider and wider spiral until the particle exits the cyclotron entirely.

This experiment allows the user to observe the effects of adjusting the frequency at which the electric field oscillates in the cyclotron. It also allows the user to change the initial velocity of the particle, the charge and the mass.

### How to use it

Along the top of the simulation window, the editable fields for the values of charge, x and y components of the velocity are shown, along with the play/pause and reset buttons. The cyclotron frequency is the field displayed at the bottom of the window. A plot of the kinetic energy can be shown by clicking the “Kinetic Energy Plot” checkbox at the bottom of the screen.

### How it works

#### Variables

- Var table
  - $b$  is the magnetic field vector.
  - $x, y$  are the x and y positions of the particle.
  - $vx, vy$  are the velocity of the particle in the x and y directions respectively.
  - $q$  is the charge of the particle in the simulation. It is initially set to 1, so that the particle acts as a proton.
  - $m$  is the mass of the particle in the simulation.
  - $t$  is the time variable of the system.
- Plotting
  - $ke$  is the kinetic energy of the system, given by  $ke = \frac{1}{2}mv^2$ .
  - $fx$  is the force acting on the particle in the x direction due to the magnetic field.
  - $fy$  is the force acting on the particle in the y direction due to the magnetic field.
  - $showPlot$  is the variable behind the “Kinetic Energy Plot” checkbox.
- E field
  - $e$  is the electric field vector.
  - $freq$  is the frequency at which the electric field direction oscillates.

- *amp* is the magnitude of the electromagnetic field.
- Semicircle
  - *semiCircX* is the array of points used to plot one of the Dees along the x-axis.
  - *semiCircY* is the array of points used to plot one of the Dees along the y-axis.
  - *r* is the radius of the semicircle.

## Initialisation

The initialisation section of the simulation is used to populate the arrays of points which are used to plot the semicircle using the custom method *getX*.

## Evolution

The evolution page sets up a couple of ODEs such that the rate and which *x* and *y* increase are equal to *vx* and *vy* respectively.

The rate at which *vx* increases is proportional to the Lorentz force in the x-direction. If the particle is in one of the Dees then the Lorentz force is only affected by the magnetic field strength. If the particle is between the Dees, the Lorentz force is only affected by the electric field strength. The Lorentz force is calculated using the custom functions *calcForce* and *eForce*. These values are then divided by mass of the particle to find the acceleration from the force.

The rate at which *vy* increases is not affected by the electric field strength, so it is calculated using *calcForce* when the particle is in one of the Dees.

The electric field vector *e* is given by the cosine function,

$$A \cdot \cos ft$$

where *A* is the variable *amp* and *f* is the variable *freq*.

## Custom

- *calcForce* takes arguments of the current x and y position and a velocity and returns the Lorentz force acting on the particle due to the magnetic field. It uses the function *isInDee* to determine whether the particle is in one of the Dees. If the particle is not in one of the Dees, the *calcForce* returns zero.
- *eForce* returns the Lorentz force acting on the particle due to the electric field. If the particle is not in the electric field, *eForce* returns zero.
- *getX* is used to plot the Dees. Given a y-coordinate and the radius of the circle, it returns the corresponding x-coordinate.
- *isInDee* is used to determine whether the particle is in a Dee or not, by checking the x-coordinate and the y-coordinate.

## Fixed Relations

The only fixed relation is to set the kinetic energy, *ke* equal to  $\frac{1}{2}mv^2$ .

## UI

- Top panel  
The panel along the top consists of various fields and labels, as well as the play/pause button and the reset button.
- Drawing panel  
This panel consists of the drawn part of the simulation. The proton/electron particle in the system is represented by a 2dObject called ‘particle’.
  - *rightDee* is a shape which is formed using the points in *semiCircX* and *semiCircY*. It is shifted to the right by 0.2.
  - *leftDee* is created using the same arrays as for *rightDee*, but it is rotated 180°.
  - *eArrow* is the arrow which displays the magnetic field vector. It is displayed at the bottom and its size is equal to the variable *e*.
  - *bArrow* is the arrow which shows the Lorentz force due to the magnetic field on the particle. It originates from the position of the particle and its size is determined by the variables *fx* and *fy*.
  - *vArrow* is the arrow which shows the velocity of the particle. The arrow originates at the particle and its size is determined by the variables *vx* and *vy*.
- Bottom panel  
The bottom panel contains the label and field for the frequency that the electric field oscillates, given by the variable *freq*.
- Plotting dialog  
This is the window with the kinetic energy plot on it, with *ke* on the y-axis and *t* on the x-axis.

## C Doppler Effect Report

### Description

This experiment consists of a spectrometer observing an exoplanet. The relatively stationary observer will see that the absorption spectra for the exoplanet differ when it is moving towards and away from them.

### How to use it

The angular velocity of the planet is set using the slider at the bottom of the window. The absorption spectra for the exoplanet are shown above the slider. When the slider is moved so the angular velocity isn't 0, the absorption spectra will begin to shift.

There is also a plot of the emission spectra for the exoplanet which can be opened by checking the "Show emission plot" checkbox at the bottom of the window.

### How it works

#### Variables

- $a$  is the angle of rotation of the exoplanet from the northern position.
- $r$ ,  $r2$  are the radius of the path travelled by the exoplanet and the radius of the path travelled by the star it orbits respectively.
- $x$ ,  $y$  are the x and y coordinates of the exoplanet. These coordinates are determined from the angle of the planet,  $a$ , and the radius of the path travelled by the exoplanet,  $r$ .
- $vx$ ,  $vy$  are the velocity of the exoplanet in the x and y axes respectively. They are also calculated from the angle of the planet, as well as the angular velocity of the system,  $\omega$ .
- $t$  is the time variable for the evolution of the system.
- $off$  is the offset added to the position of the star-planet system to move it to the right of the spectrometer image.
- $segment$  is the two-dimensional array of coordinates for the absorption lines.
- $posRef$  is the array of positions of the absorption lines before the Doppler shift is applied.
- $offset$  is the amount which the position of the absorption lines should be offset by the Doppler shift caused by the motion of the planet.
- $x2$ ,  $y2$  are the x and y positions of the star.
- $\omega$  is the angular velocity of both the exoplanet and the star.

## Plotting Variables

- *xPoints*, *yPoints* are the arrays of coordinates for the points to plot on the emission spectrum plot.
- *waveOffset* is the amount which the wavelengths of the emission lines should be shifted due to the Doppler effect.
- *showPlot* is the variable behind the “Show Emission Plot” checkbox.
- *lamRef* is the array of x-coordinates for the points on the graph not considering the Doppler shift.

## Initialisation

In the initialisation, an array of four random wavelengths between 400nm and 700nm are randomly generated and used to populate the arrays, *xPoints* and *lamRef*. They are given a corresponding value in *yPoints* between 0 and 0.2. Then, ten points from the array are randomly chosen as the absorption spectra and these points are given corresponding y-coordinates with values between 0.2 and 1. These wavelengths are then scaled down to values between -1 and 1 for use plotting the absorption lines on the spectrum of visible light. These are used to populate the two-dimensional array, *segment*, where the second dimension is the y-coordinate, -1 in order to place the lines at the bottom of the screen.

## Evolution

### Evol Page

The first evolution page introduces the relationship between the angle of rotation, *a*, and the angular velocity, *omega*.

### Spectra

For each step of the evolution of the system, this page sets the positions and the points of the spectral lines equal to their reference values plus the appropriate Doppler shift.

## Fixed relations

The fixed relations page contains relationships generating x and y coordinates and velocities from the angle of the planet and star. It also generates the offset for the positions and wavelengths of the absorption spectra based on the magnitude of the velocity in the x-axis.

## Custom

- *positionToWavelength* takes a position on the spectrum between -1 and 1 and converts it to the equivalent wavelength in nanometers (between 400nm and 700nm) for plotting on the graph.
- *wavelengthToPosition* does the opposite of the *positionToWavelength* method.

- *randomPosition* generates a random value between -1 and 1 to be used as a position for an absorption line.

## UI

### Frames

The UI of this experiment consists of two windows: the simulation window and the plotting window. The plotting window is hidden by default and is opened with the “Show emission plot” checkbox at the bottom of the simulation window.

The simulation window contains the model exoplanet orbiting a star, showing their paths. It also shows the absorption lines for the exoplanet plotted on the spectrum of visible light. It has a slider at the bottom to change the angular velocity of the planet, as well as the play/pause button, the reset button and the checkbox to show the emission spectrum plot.

### Images

This simulation makes use of two images. A drawing of a telescope, to act as a mock spectrometer, and a picture of the spectrum of visible light, to be the background for the spectral lines. Both of these images are freely licensed.