$$f:(i_{n-1}^1,\ldots,i_{n-1}^x,s_{n-1}^1,\ldots,s_{n-1}^y,o_{n-1}^1,\ldots,o_{n-1}^z,i_n^1,\ldots,i_n^x)\mapsto(s_n^1,\ldots,s_n^y,o_n^1,\ldots,o_n^z)$$