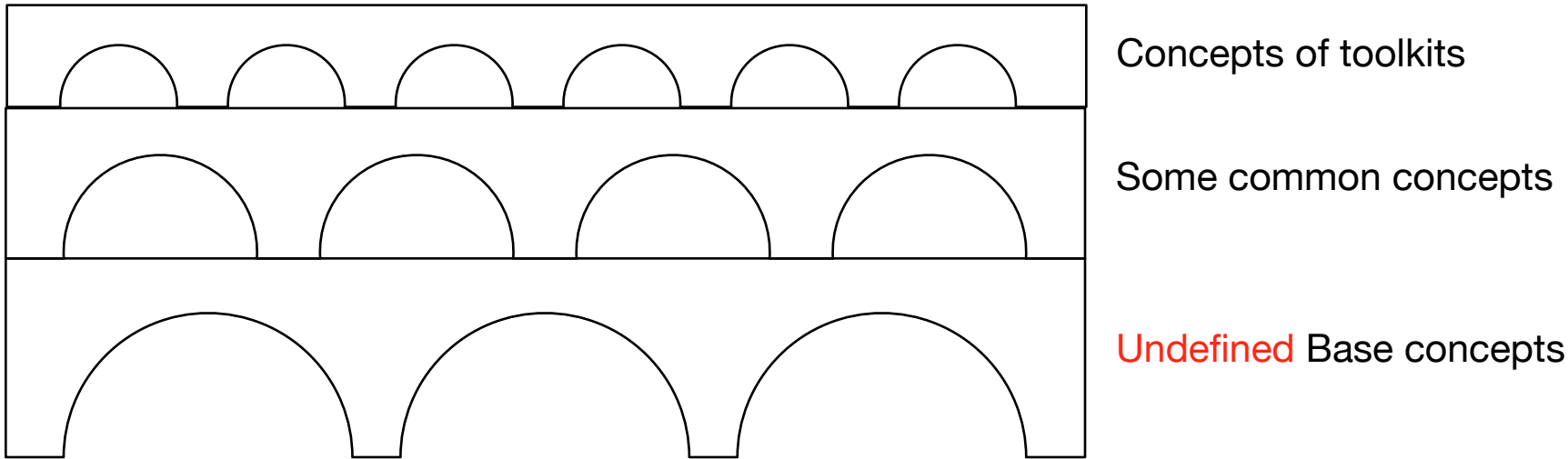
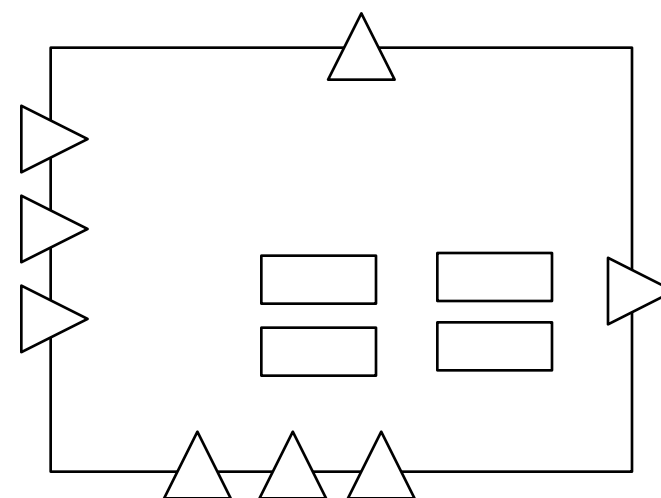
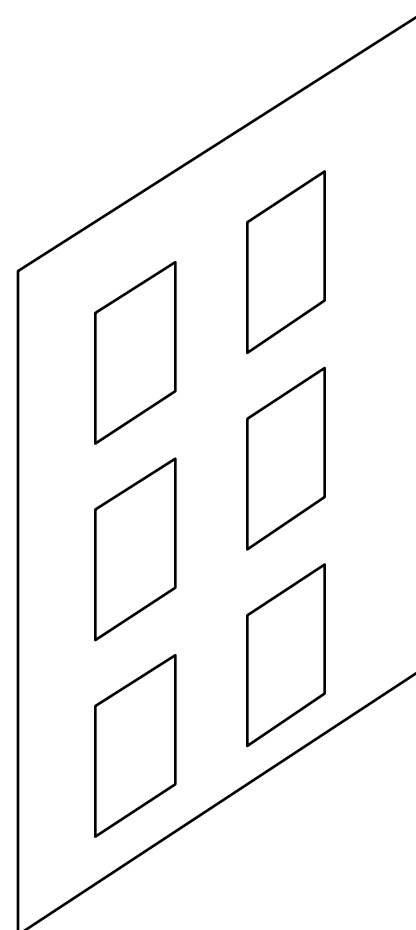
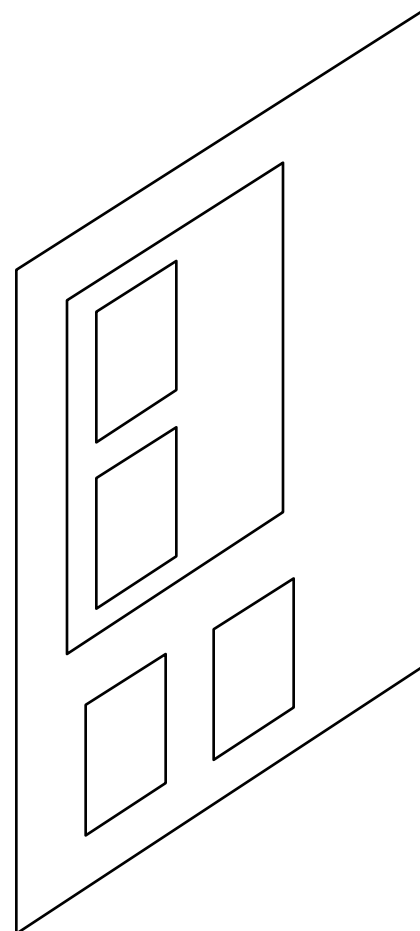
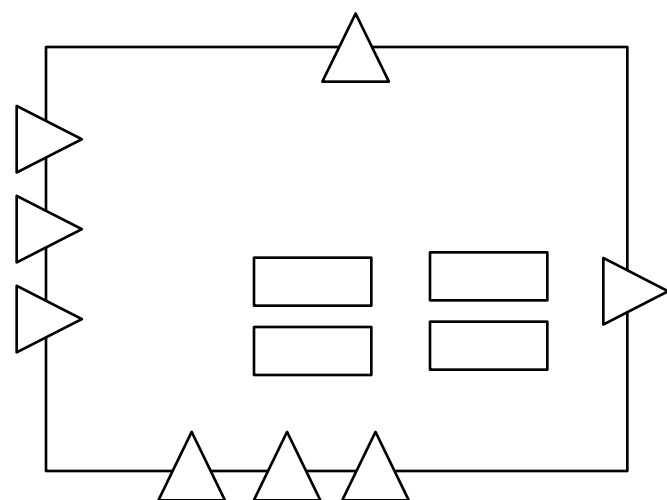


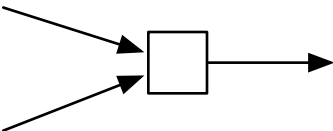
# The Roman aqueduct model



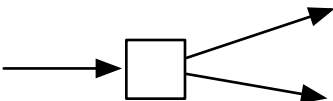


Grandes dualités

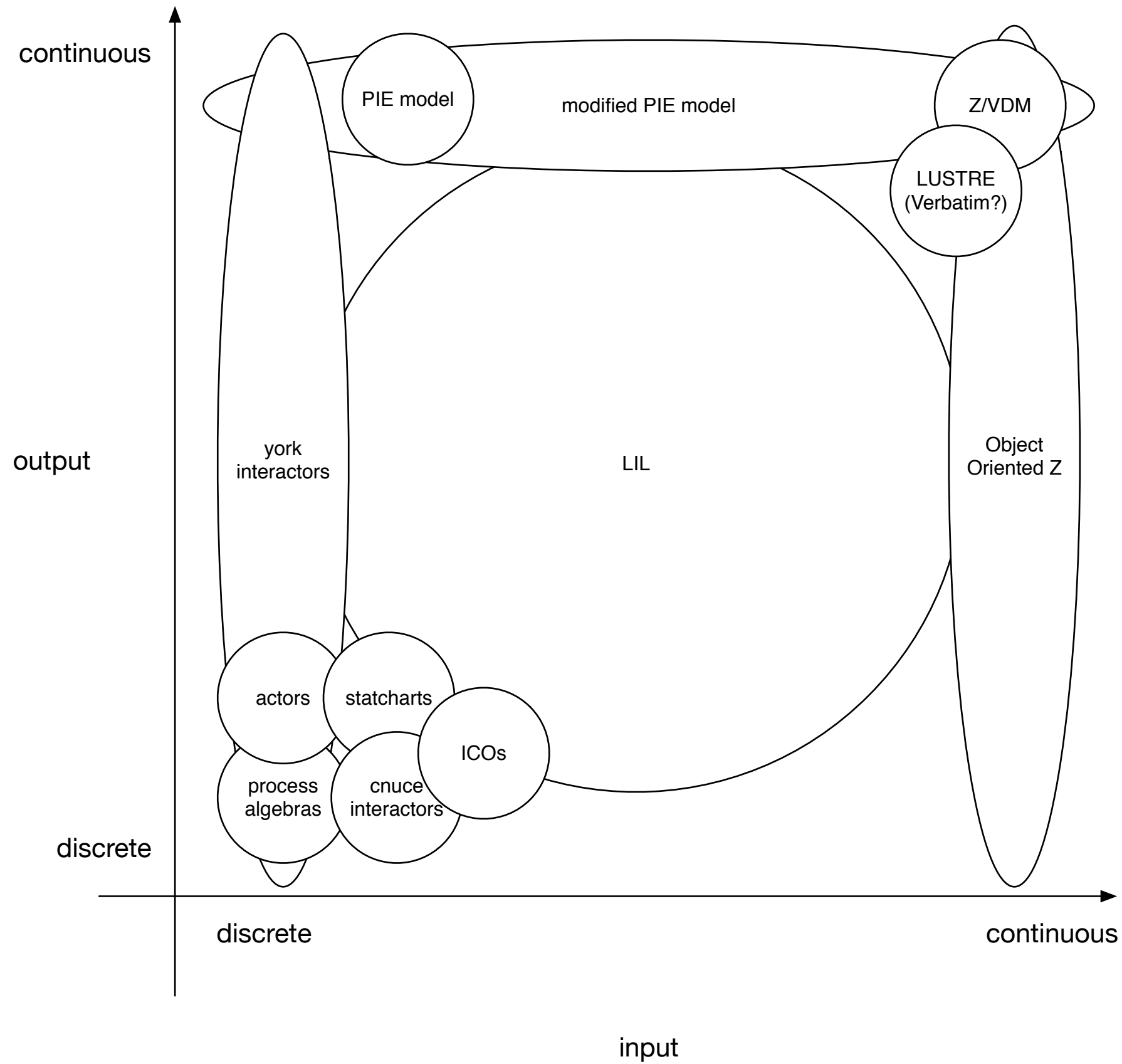
Continu / Discret  
[abowd22integrating]



Structuration / Destructuration



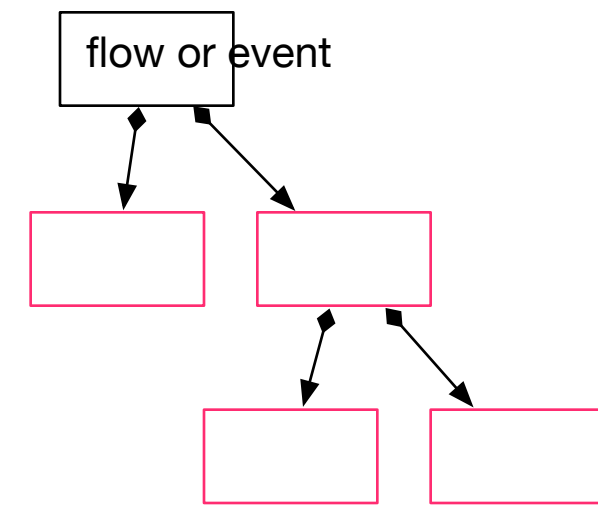
Synthetized / State  
React synthesized variables vs state



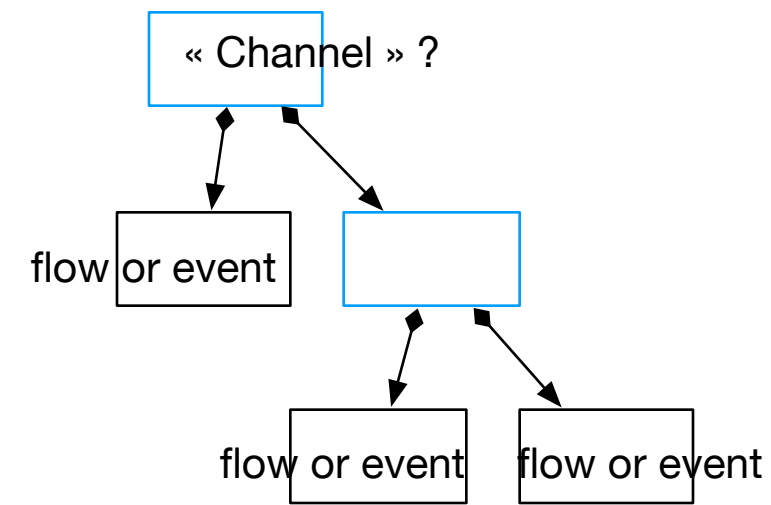
# Concept of composition of flows and events

Top - Down

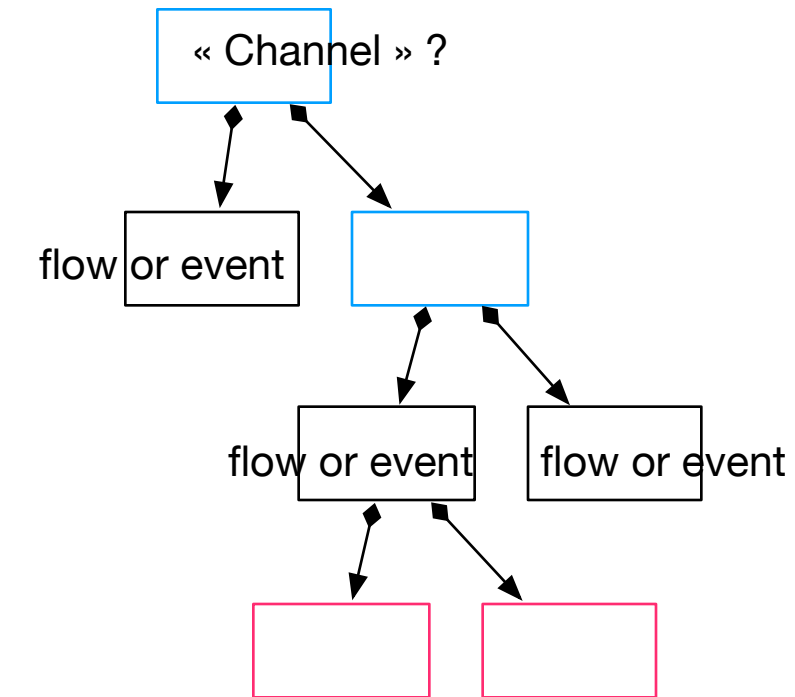
(OLD) LIL



Bottom - Leafs



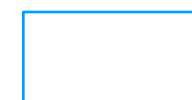
Mixed ?



data: not specified if flow or event, just data



flow or event



channel : combination of flows and events

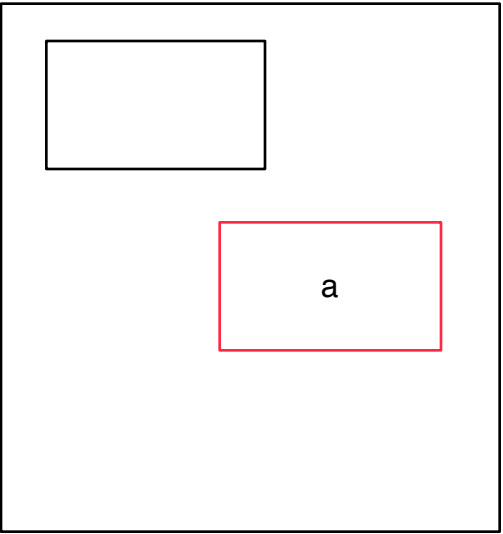
```
parent : channel{
  active: boolean flow in,
  visible : boolean flow in,
  selection : void event out,
  mouse : channel{
    position : position flow in,
    click : button event in
  }
}
```

# Concept of multi-composition

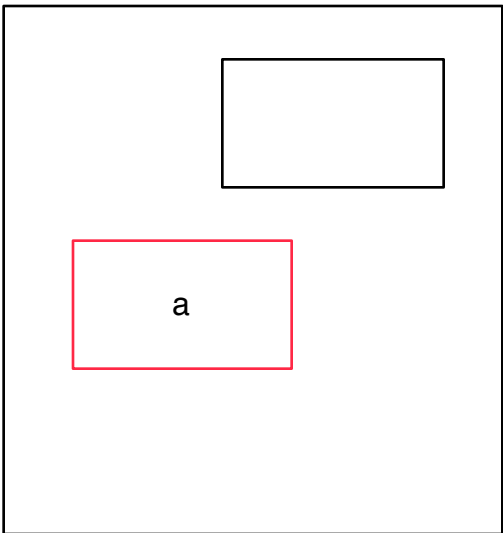
an interaction is part of MULTIPLE interactors  
it is SHARED between them

one has access to it and so does the other

an interactor has multiple parents



user hierarchy

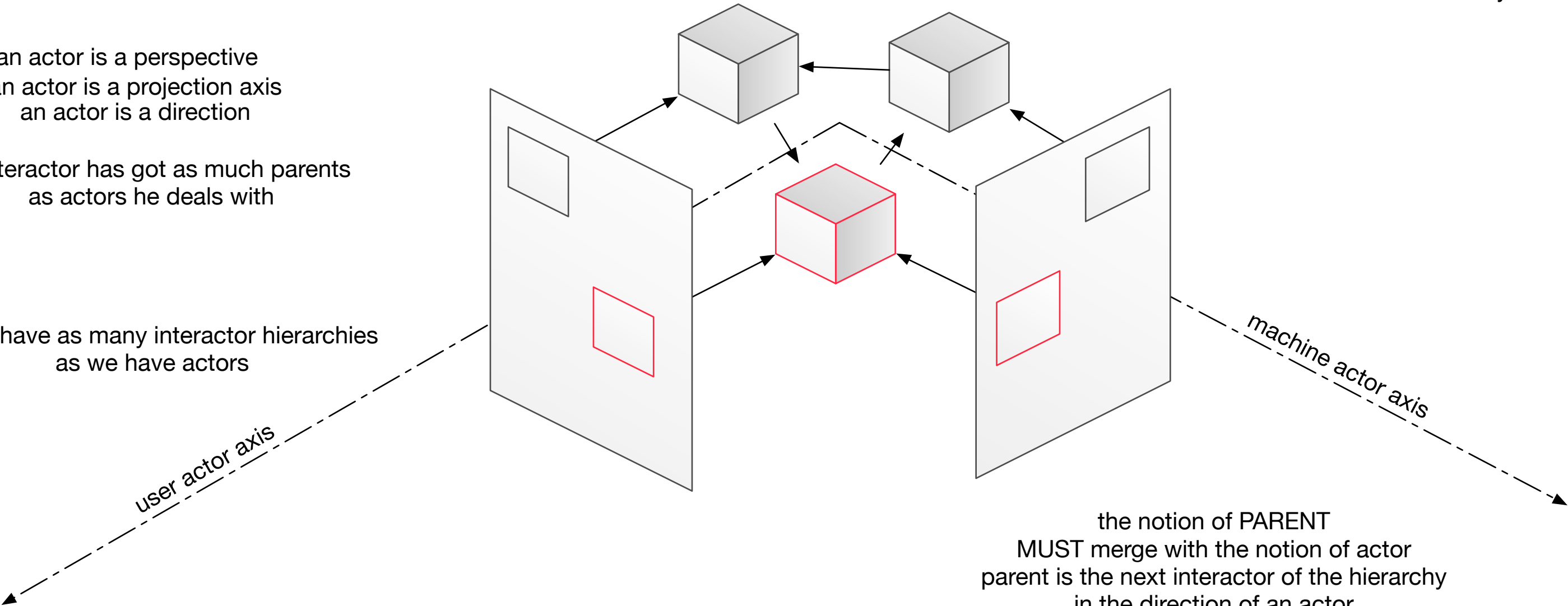


machine hierarchy

an actor is a perspective  
an actor is a projection axis  
an actor is a direction

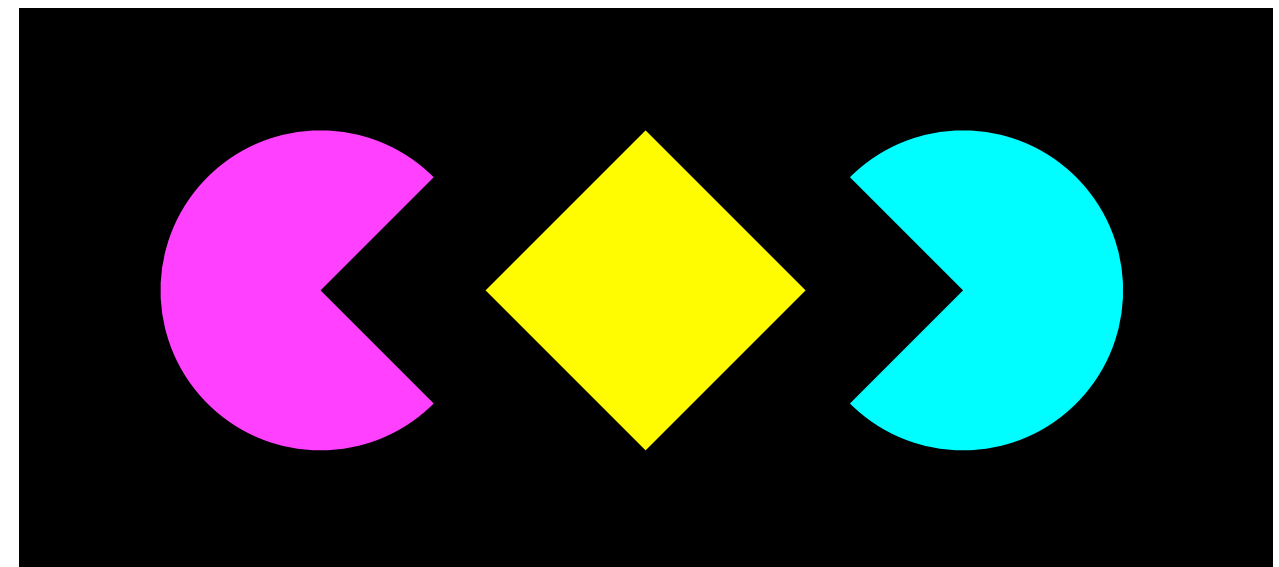
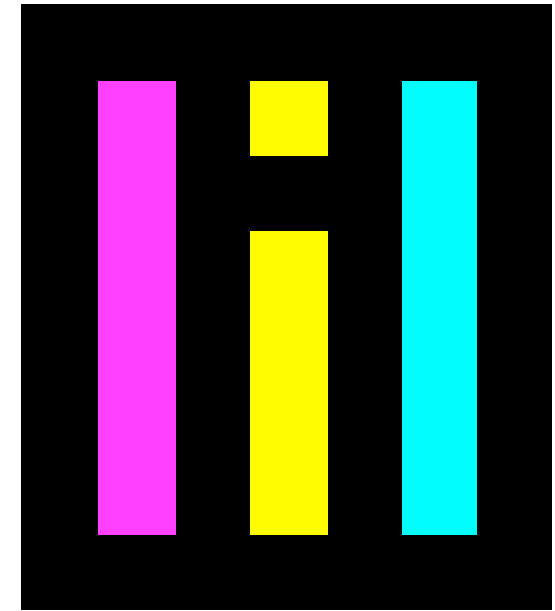
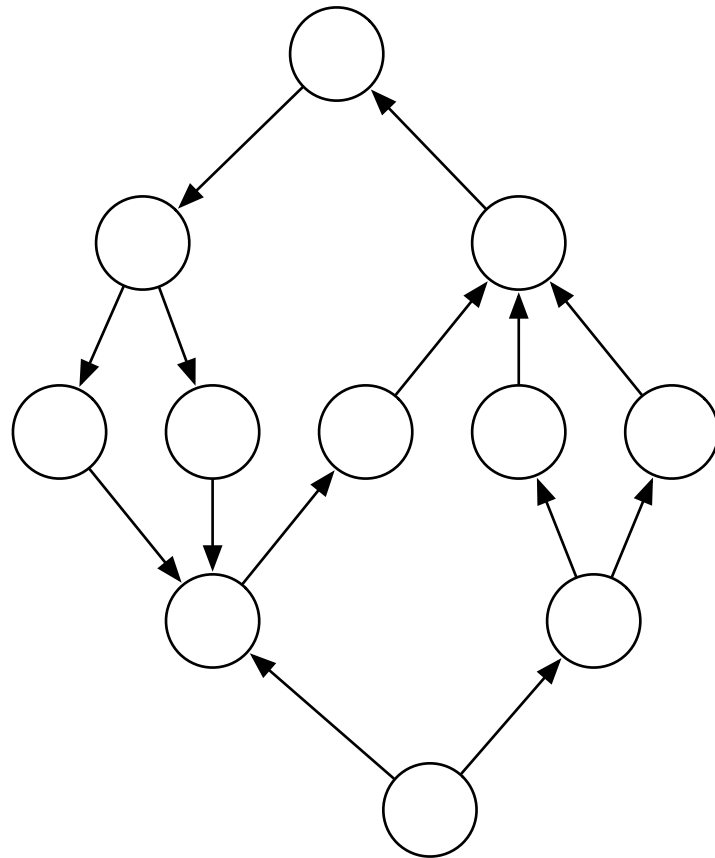
an interactor has got as much parents  
as actors he deals with

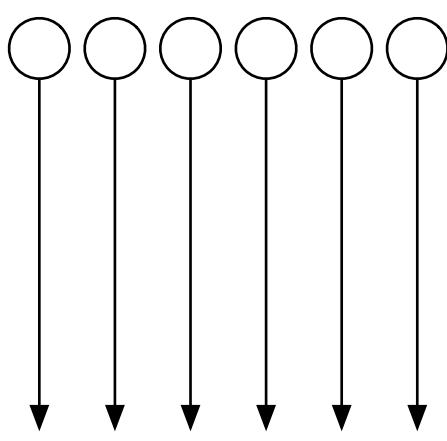
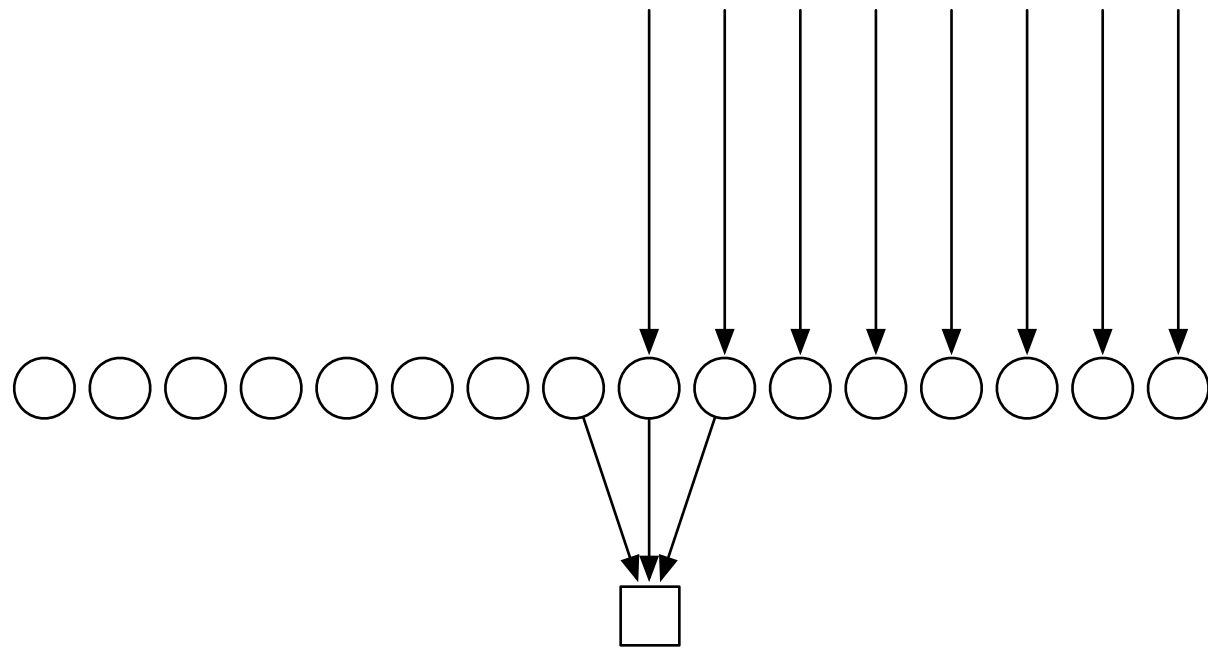
So we have as many interactor hierarchies  
as we have actors



the notion of PARENT  
MUST merge with the notion of actor  
parent is the next interactor of the hierarchy  
in the direction of an actor

button interactor







# Multi composition example

Example multimodal

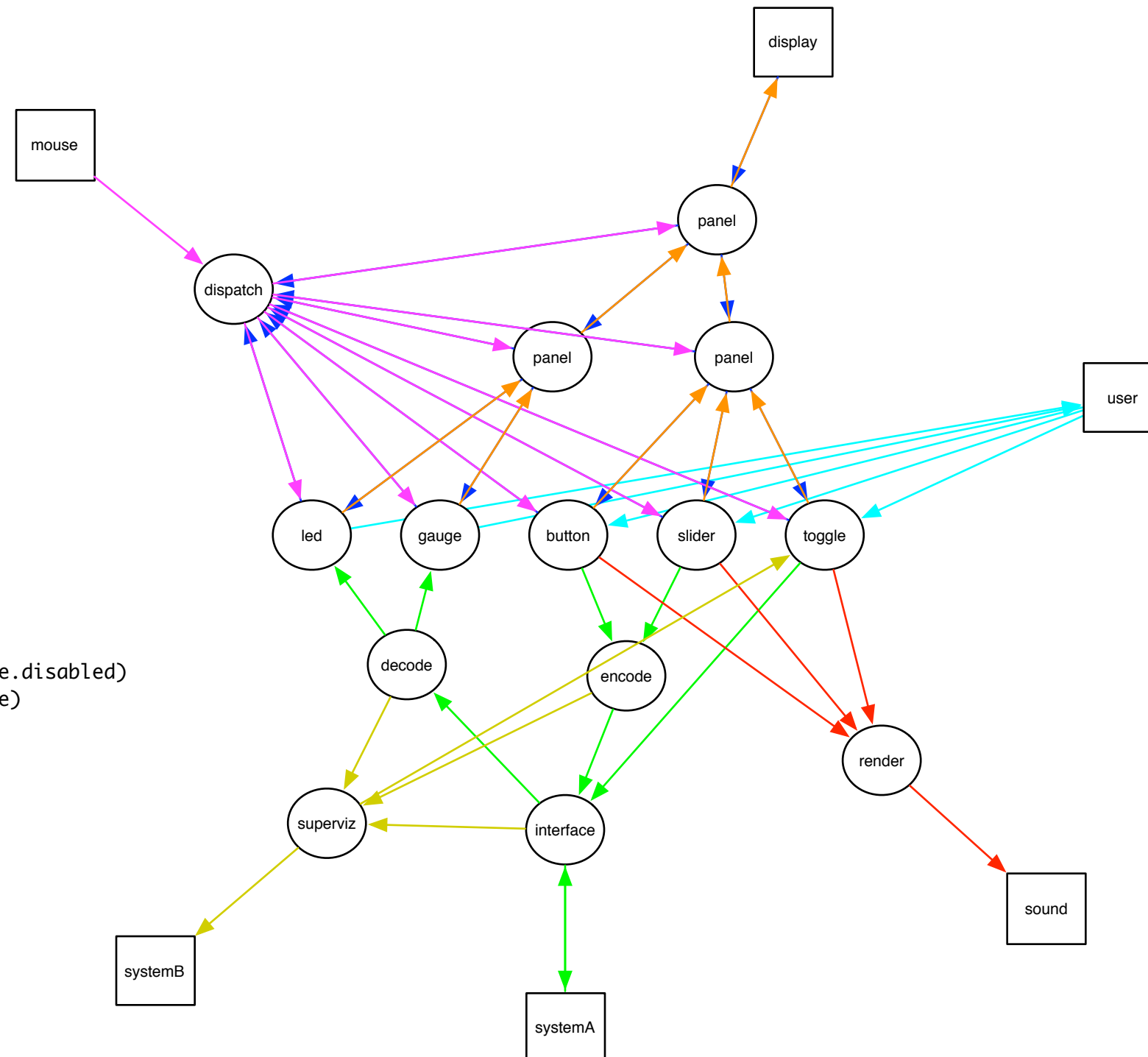
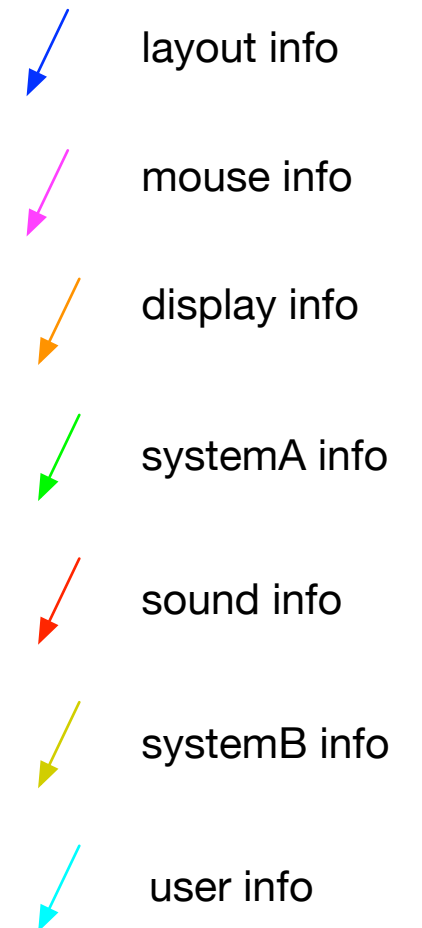
modalités en haut de chaque hierarchie

Led interactor:

status : Boolean flow from system to user  
mousePos : MousePosition flow from mouse  
position : Layout flow from screen to mouse  
display : Svg flow to screen  
theme : Theme flow from screen  
focused : Boolean flow internal

focused = (mousePos inside position)

```
display =  
  <circle  
    fill=(if status then theme.highlight else theme.disabled)  
    stroke = (if focused then theme.focus else none)  
    x=position.x  
    y=position.y  
  />
```



Check that :

(signal to user)  $\Leftrightarrow$  ((signal to sound) U (signal to screen))

signal from user  $\Leftrightarrow$  signal from mouse

# Multi composition example

Example multimodal

modalités en haut de chaque hierarchie

- layout info
- mouse info
- display info
- systemA info
- sound info
- systemB info
- user info

Led interactor:

status : Boolean flow from system to user  
mousePos : MousePosition flow from mouse  
position : Layout flow from screen to mouse  
display : Svg flow to screen  
theme : Theme flow from screen  
focused : Boolean flow internal

focused = (mousePos inside position)

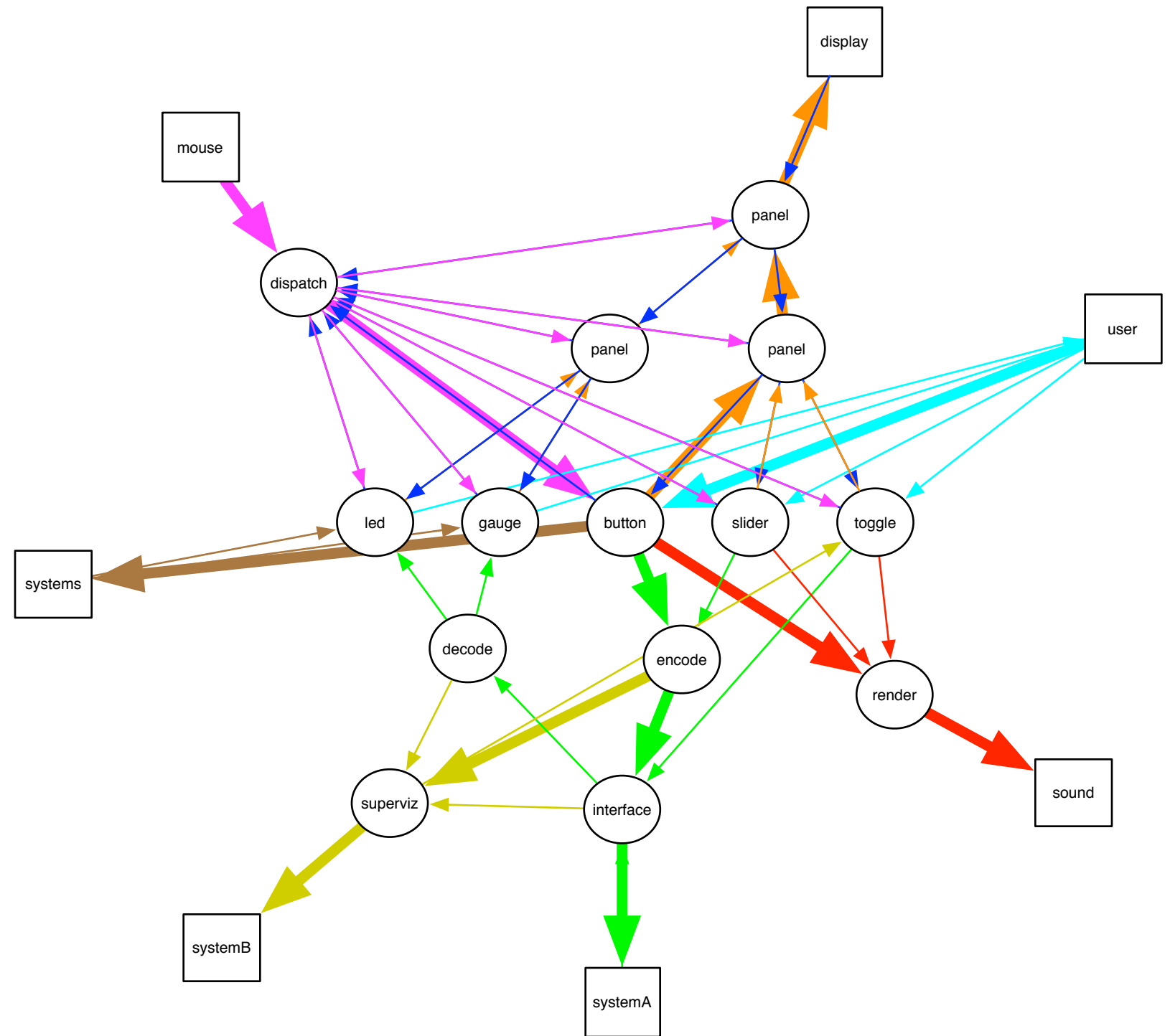
```
display =  
<circle  
  fill=(if status then theme.highlight else theme.disabled)  
  stroke = (if focused then theme.focus else none)  
  x=position.x  
  y=position.y  
>
```

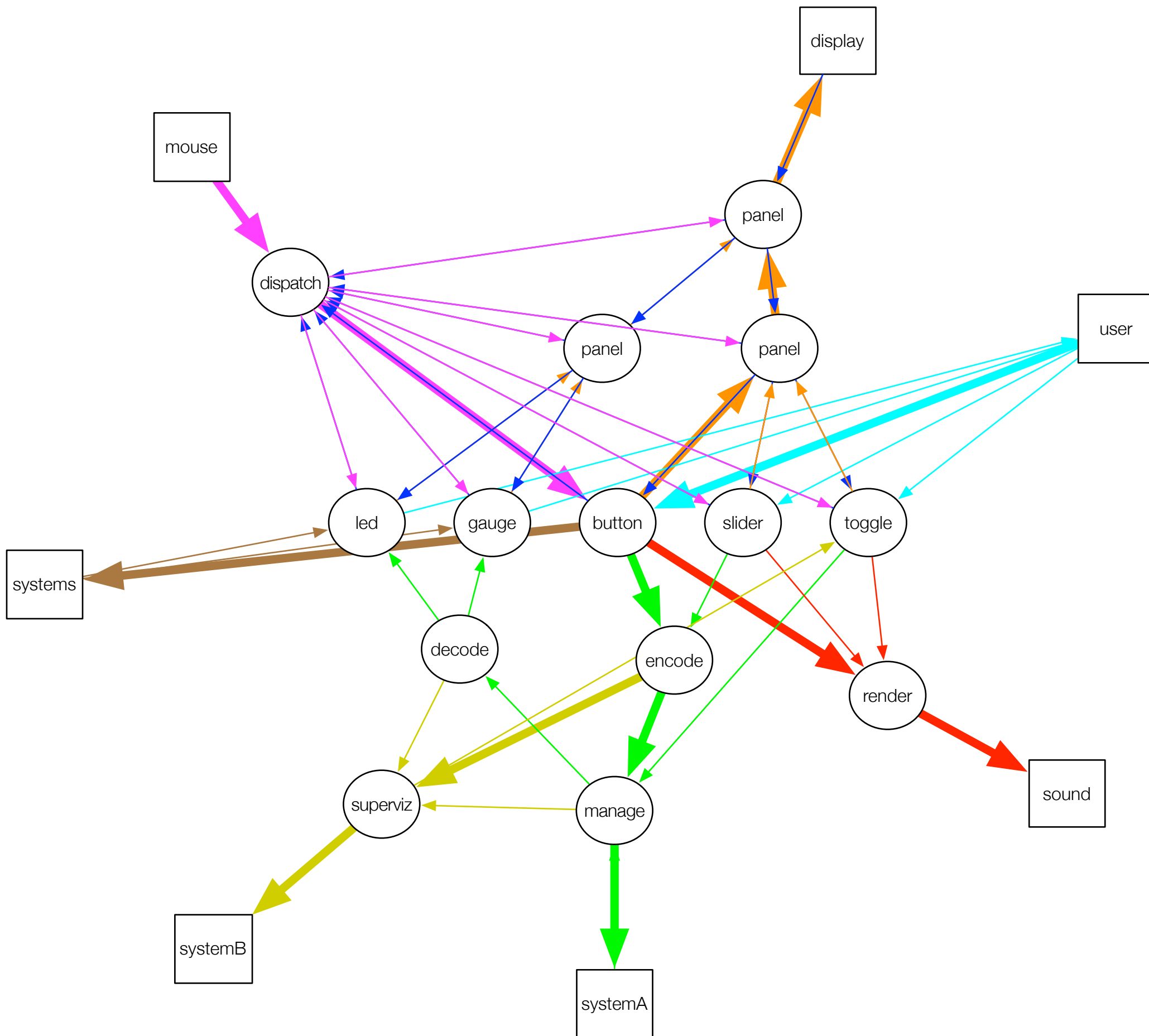
Check that :

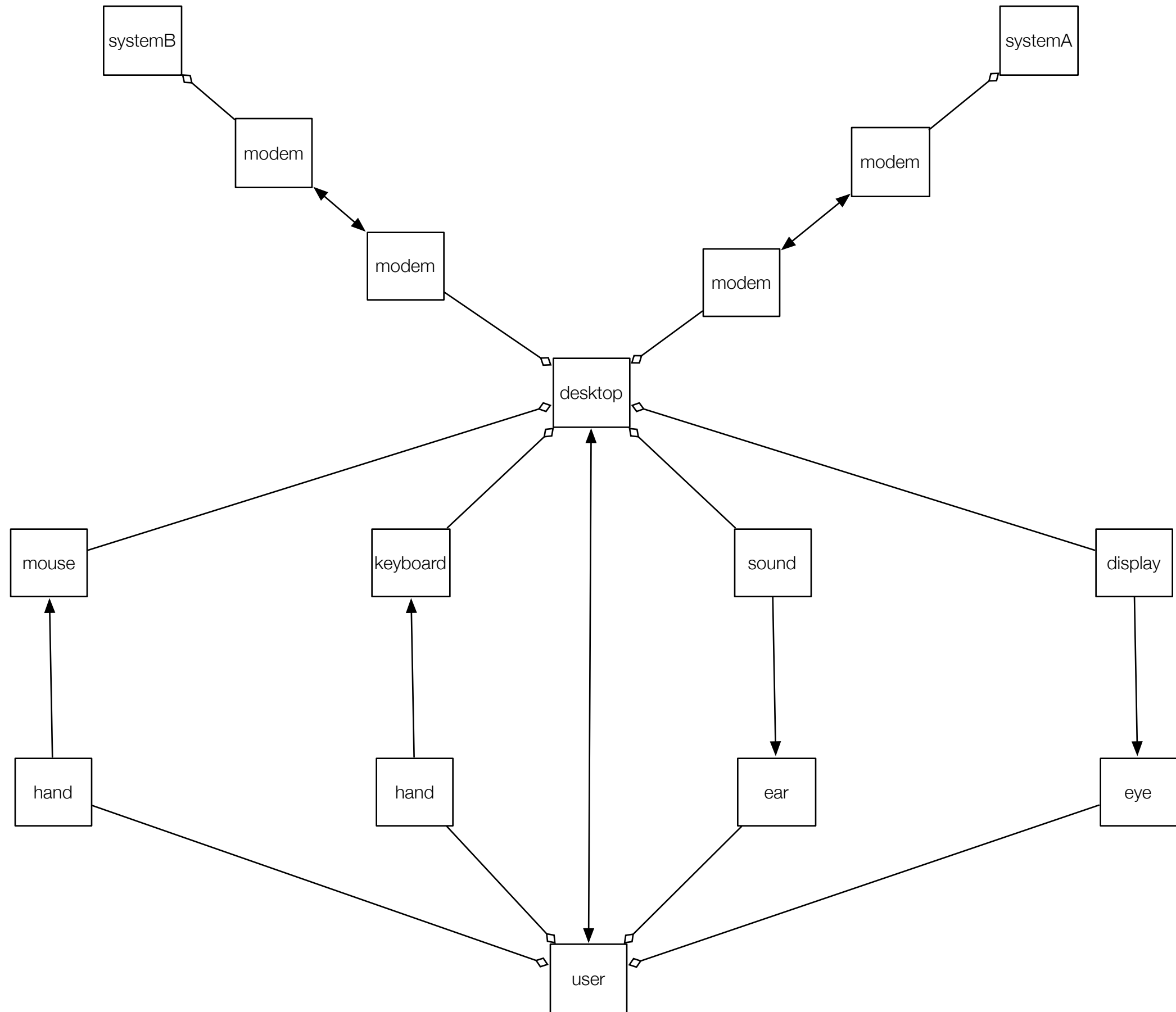
(signal to user) <=> ((signal to sound) U (signal to screen))

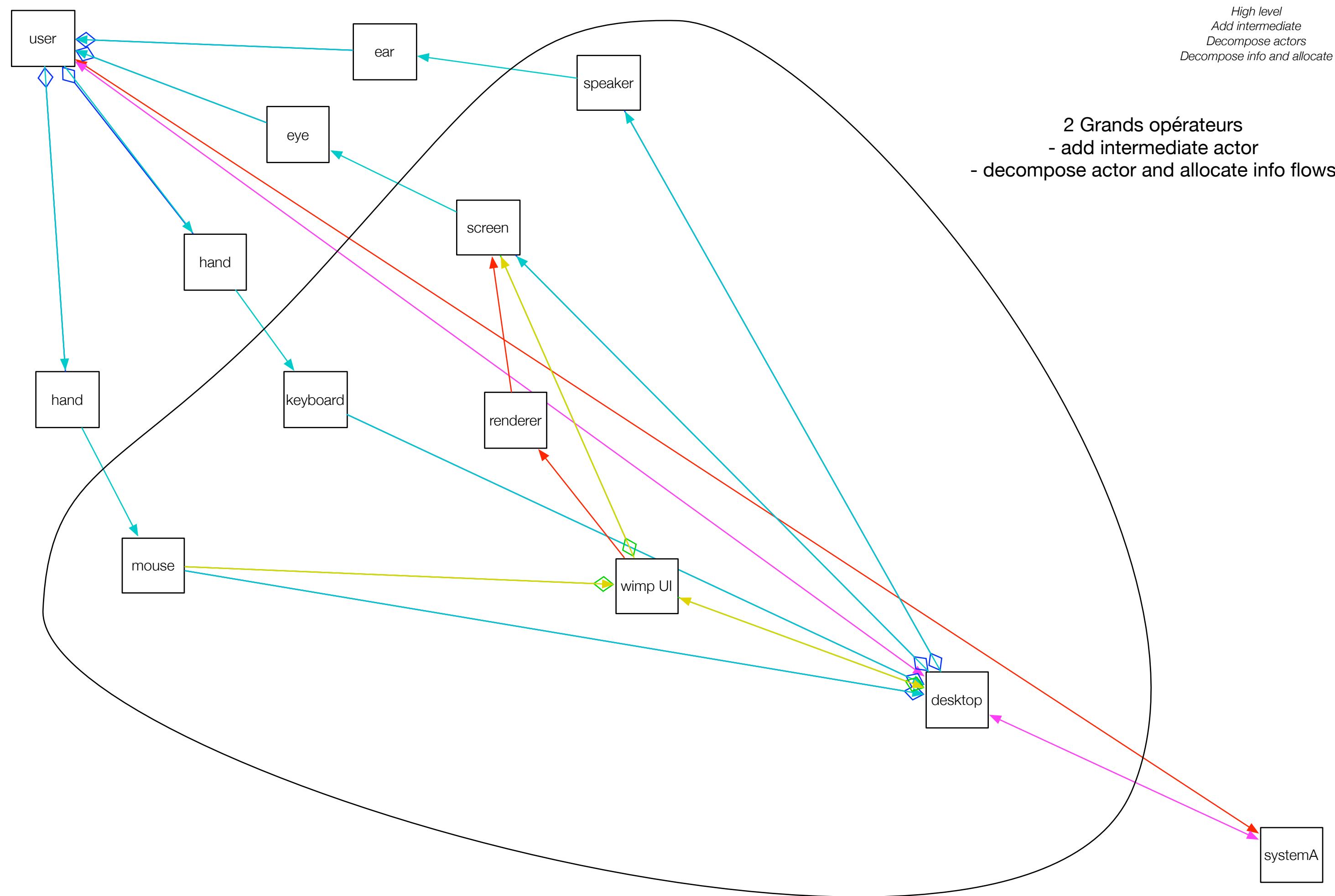
signal from user <=> signal from mouse

(signal to systems) <=> signal to systemA U signal to systemB

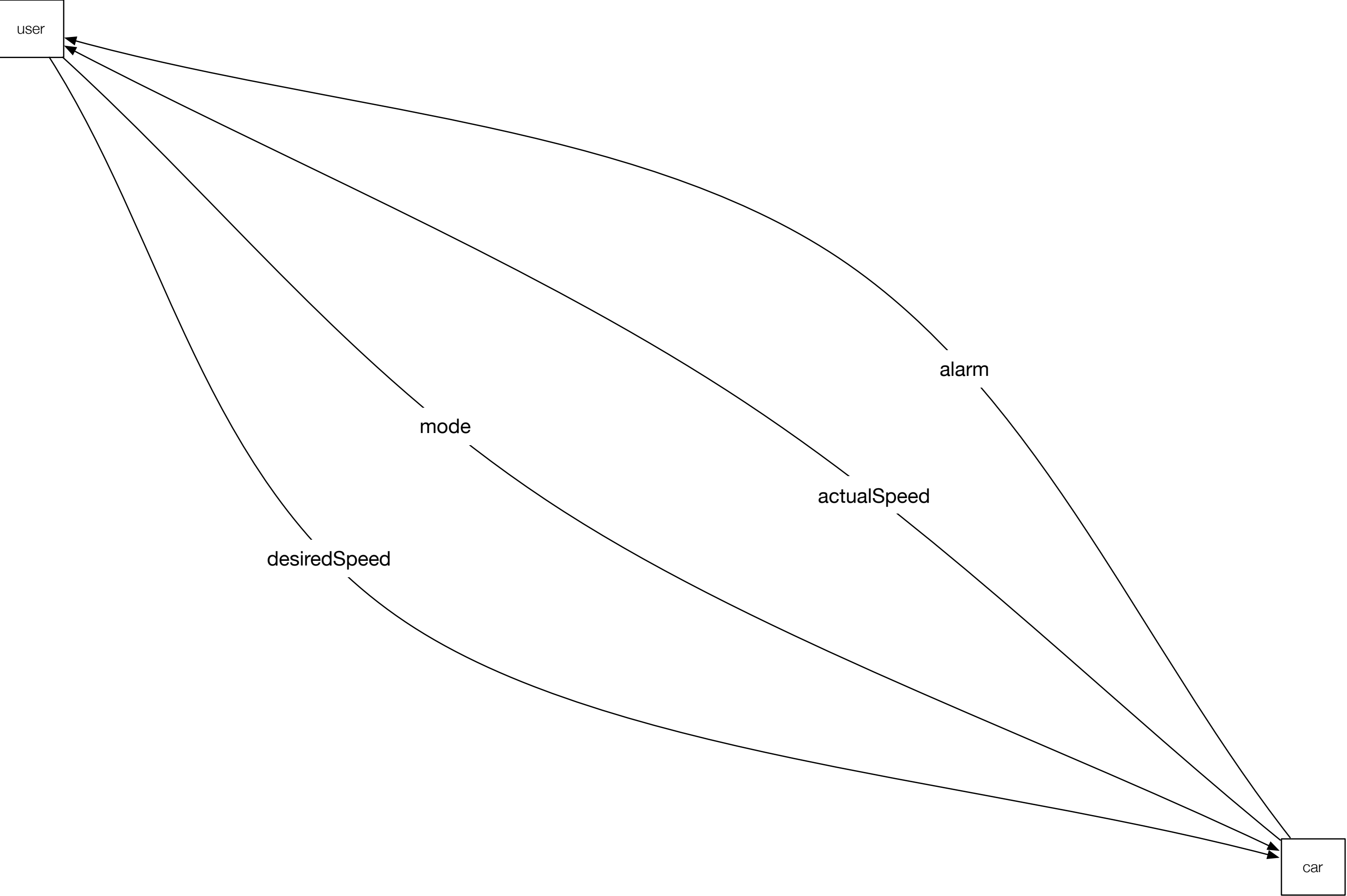


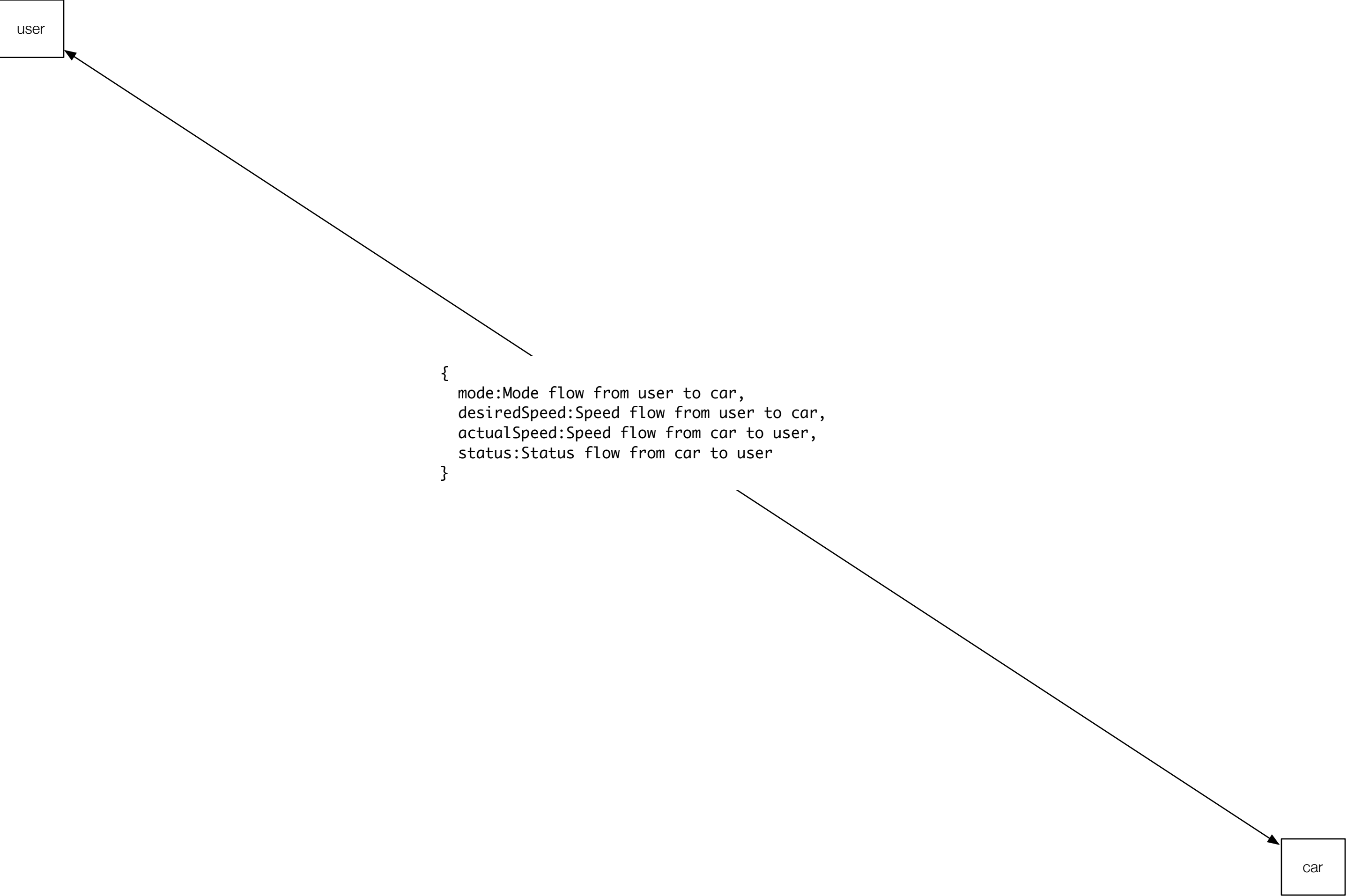


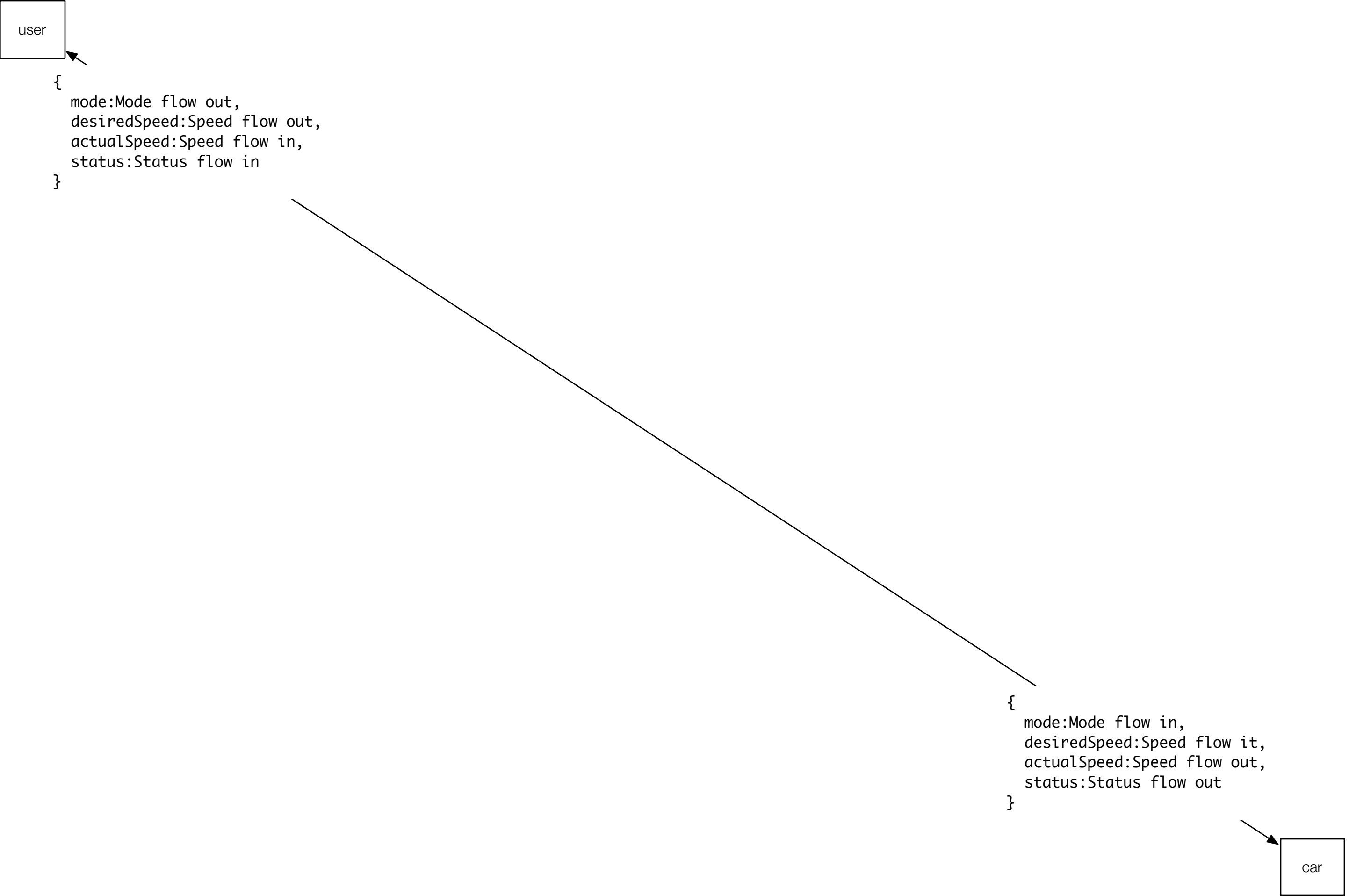




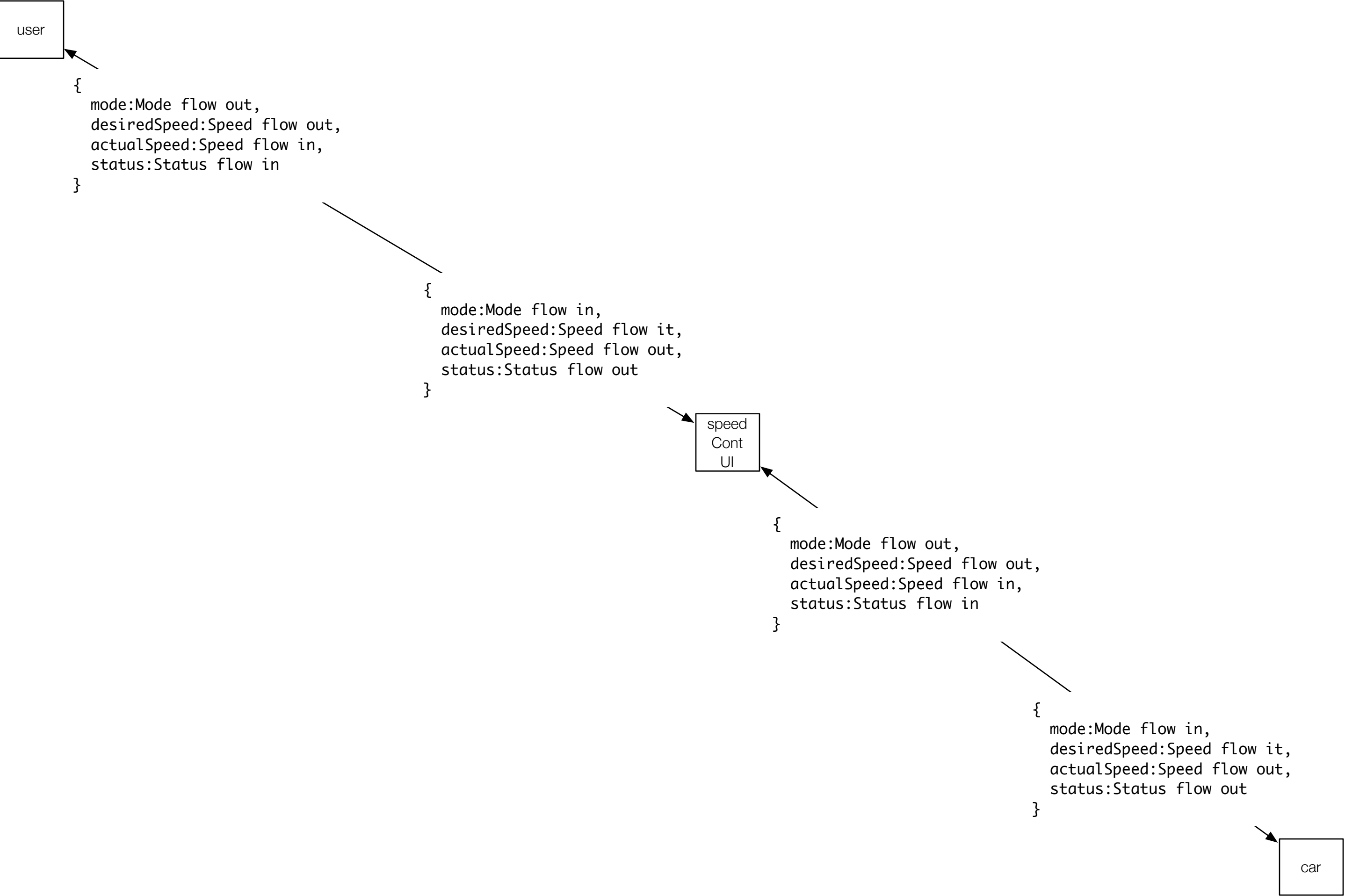
desktop INTERMEDIATE BETWEEN (user, systemA)  
desktop MADE OFF (screen, keyboard, speaker, mouse)

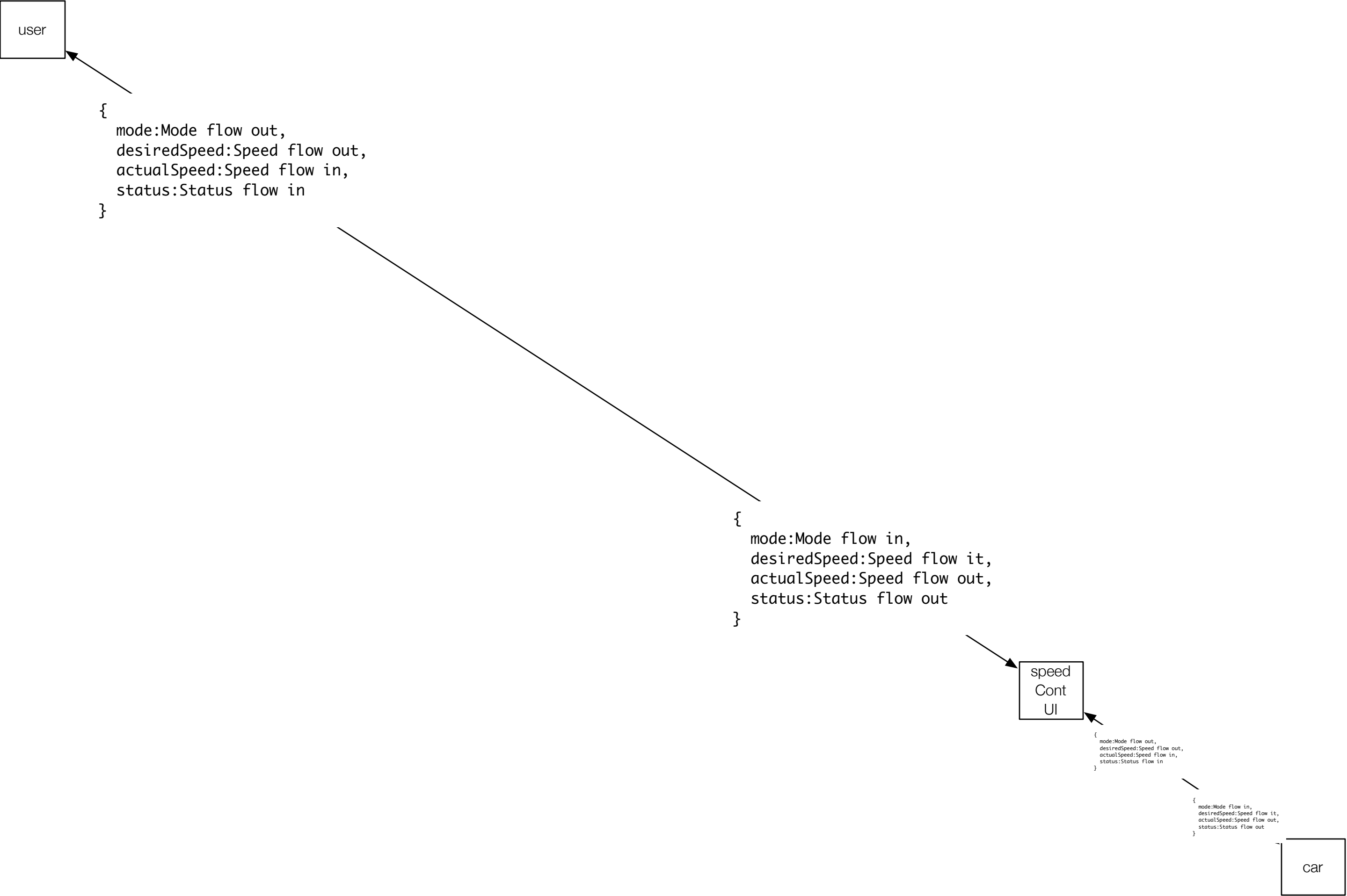


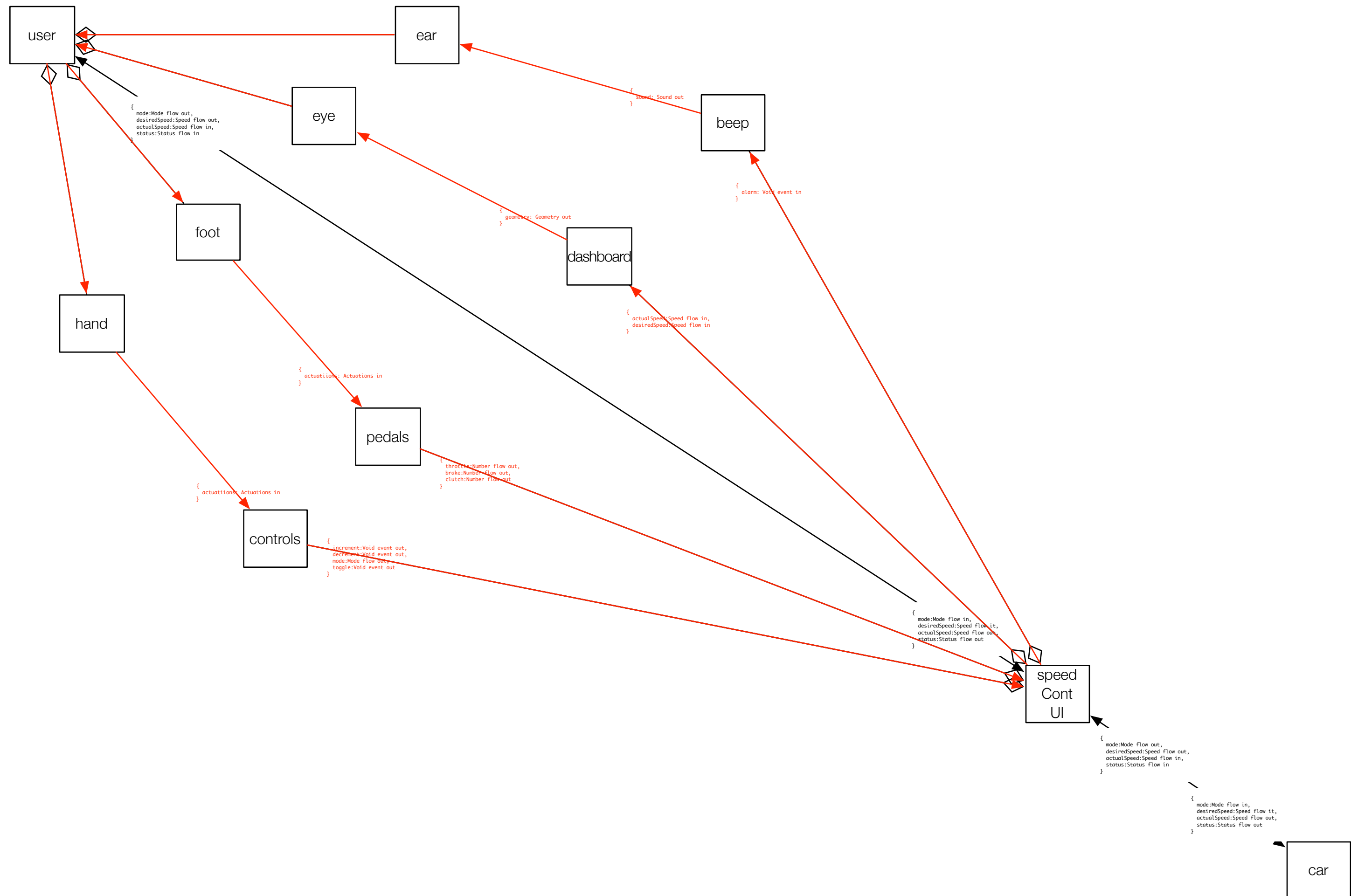


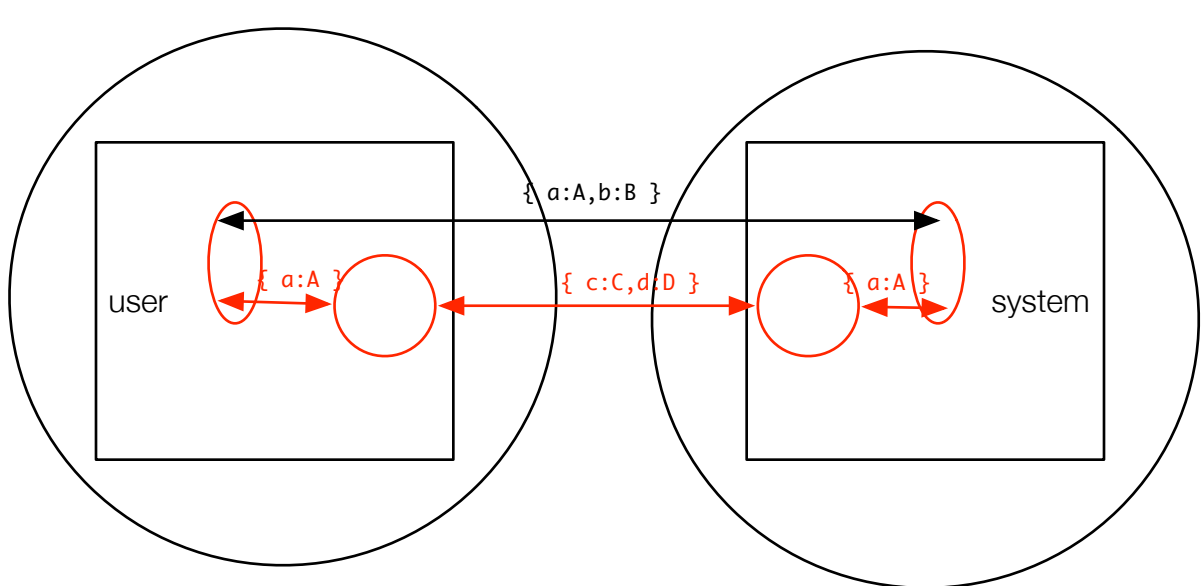
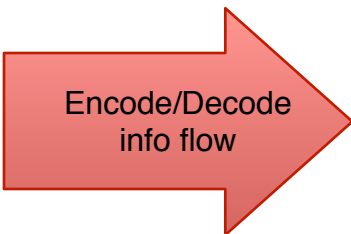
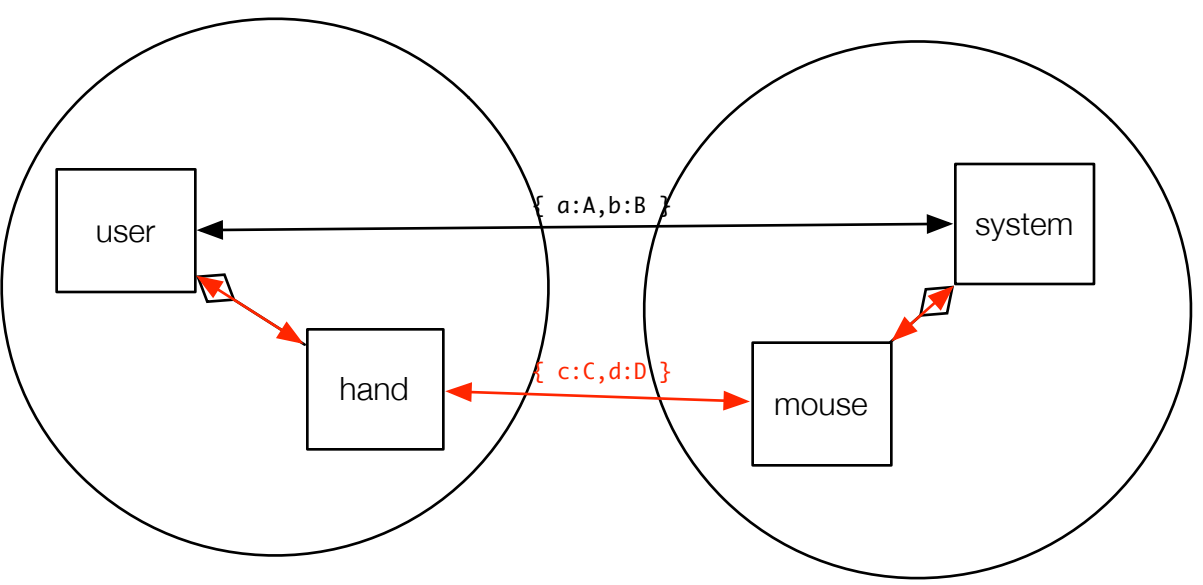
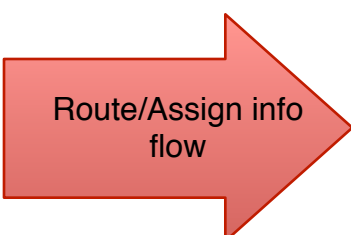
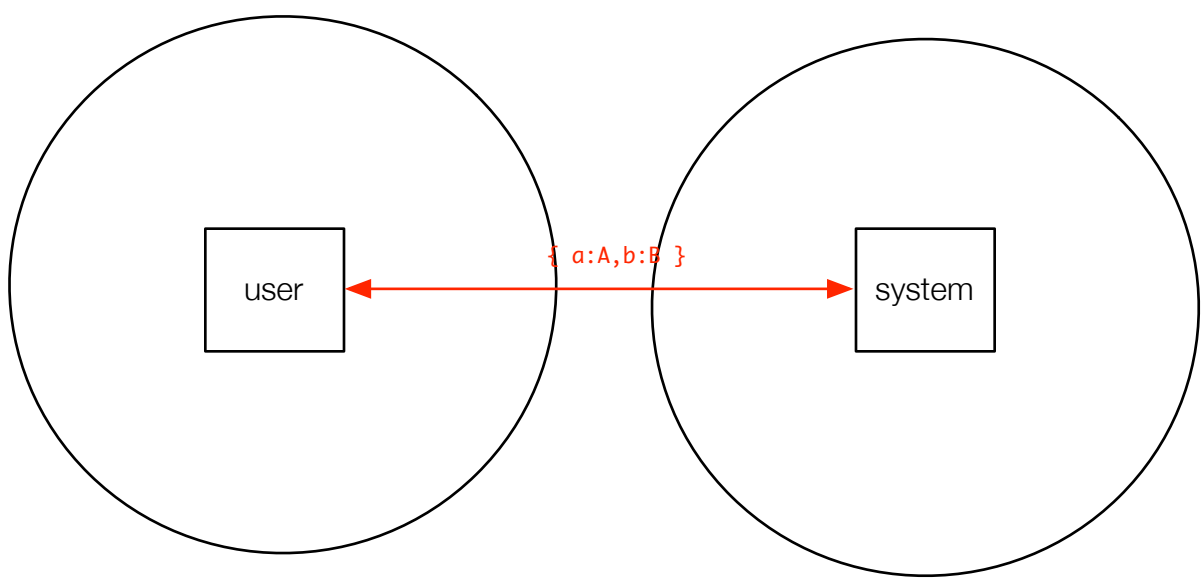
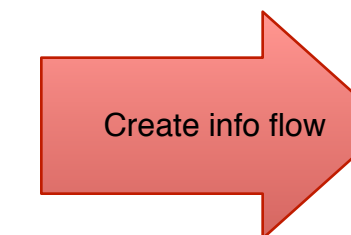
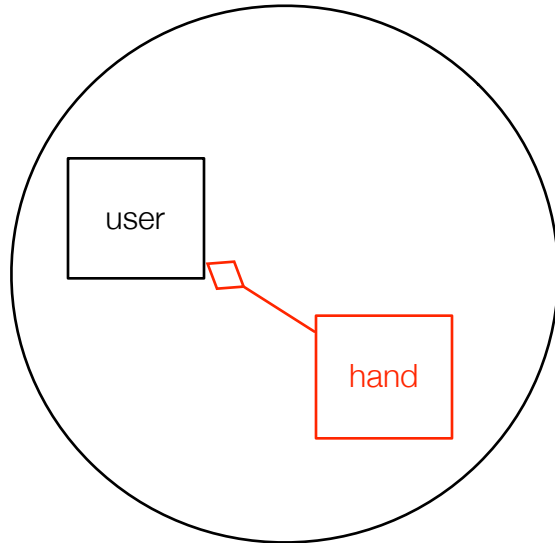
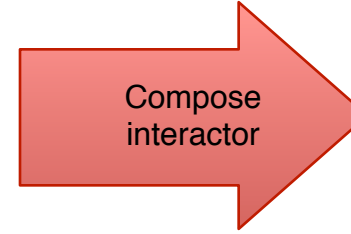
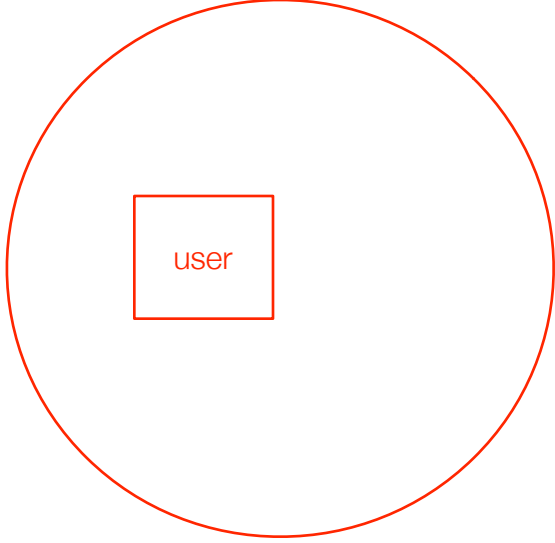
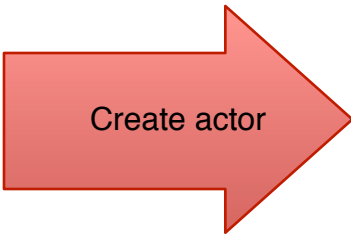












An actor IS a (super?)interactor

A behavior IS an (sub)interactor !

NO INTERACTORS, ACTORS, BEHAVIOR : ONLY INTERACTION

WE DESCRIBE THE SET OF POSSIBLE INTERACTIONS FOR AN ENTITY

And their relationship

exemple:

inc/dec to set speed behavior

=

an interactor :

inputs from driver : inc dec

inputs from parent : limits

output to parent : value

# Data Computation Interaction

*we have Languages to describe data (e.g. : C, JSON, XML)*

*we have Languages to describe computation (e.g. : C, JS)*

*we don't have Languages to describe interaction ?????*

Set of possible interactions and their relationship

Human interaction:

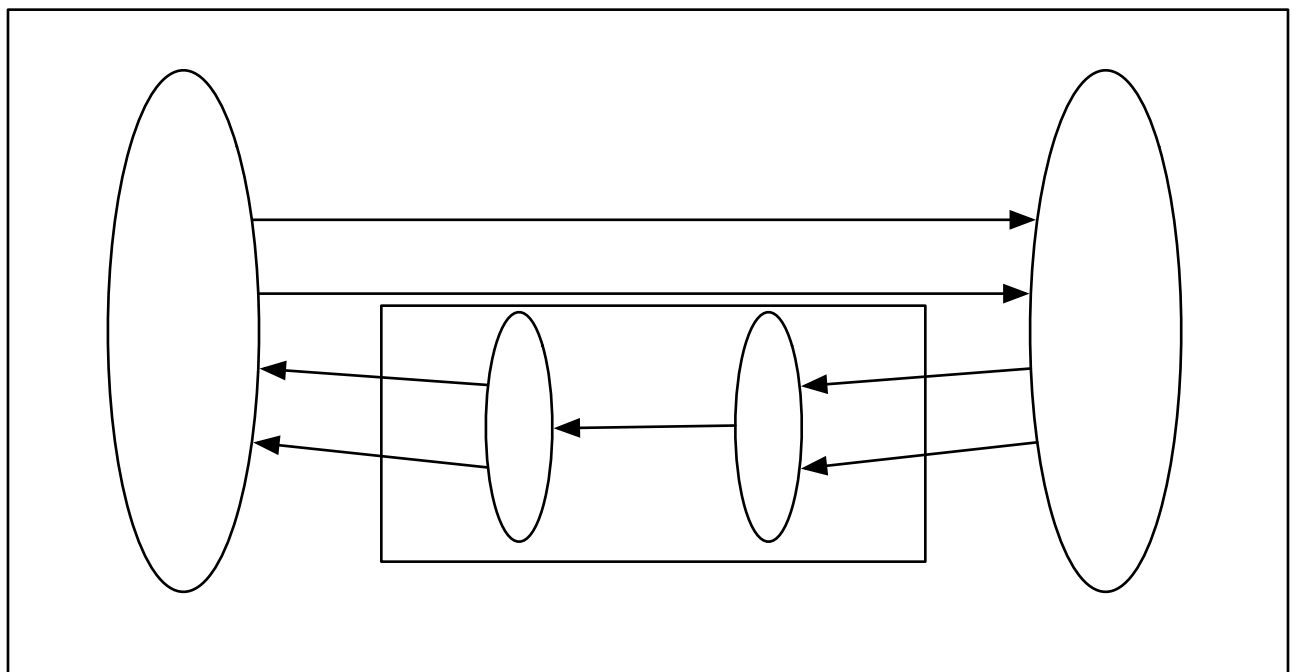
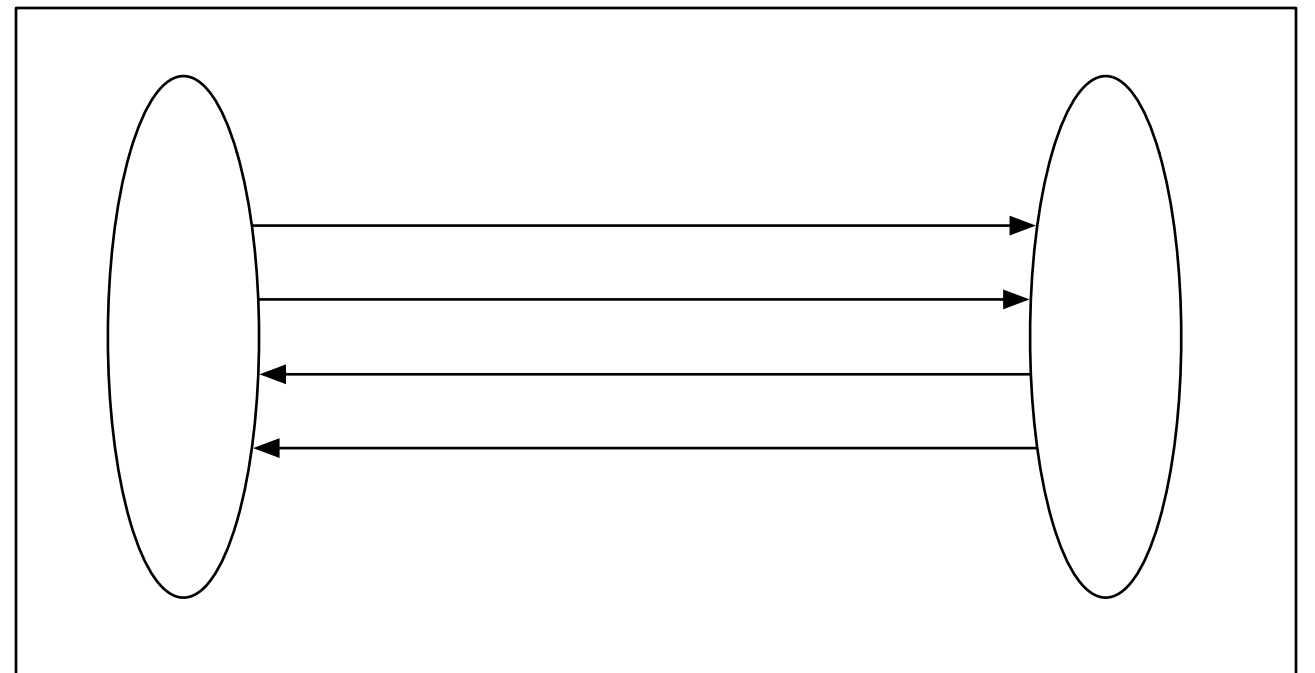
- hands : Hands interaction
- foots : Foots interaction
- eyes : Eyes interaction
- ears : Ears interaction

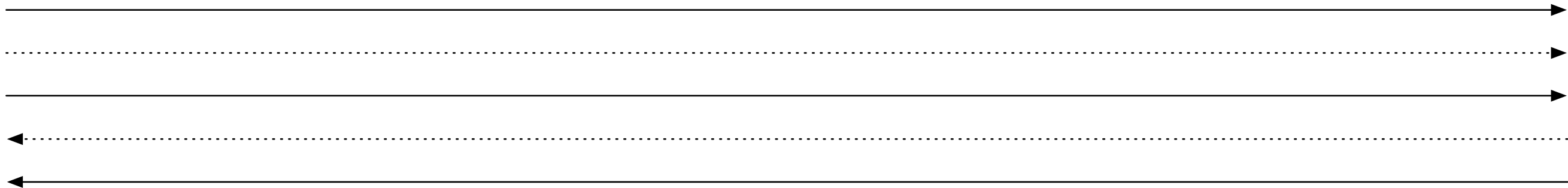
SpeedController interaction:

- controls : Controls interaction
- pedals : Pedals interaction
- dashboard : Dashboard interaction

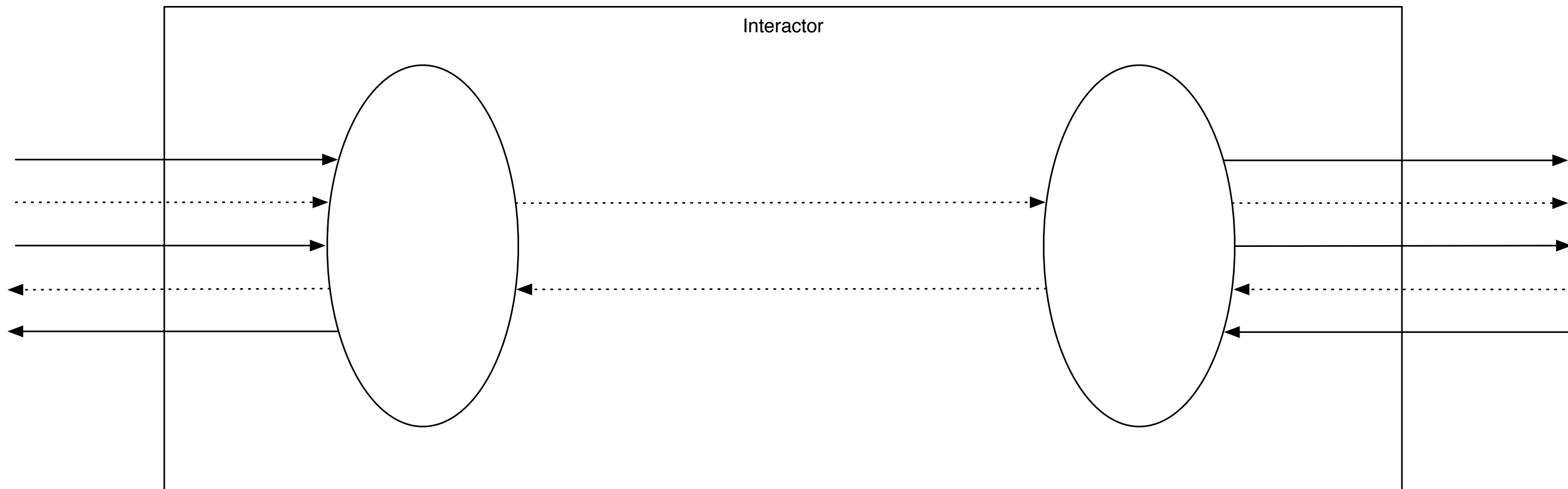
Controls interaction:

- increment : Void event in
- decrement : Void event in
- mode : Mode flow in





**=**



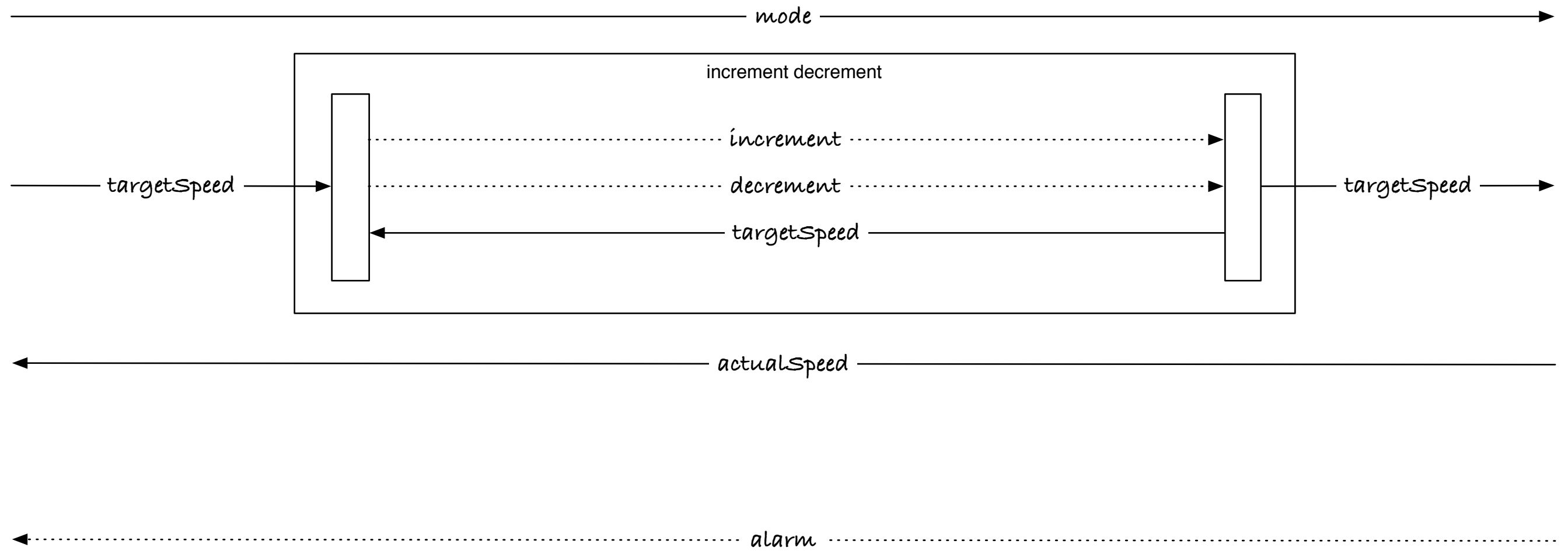
mode

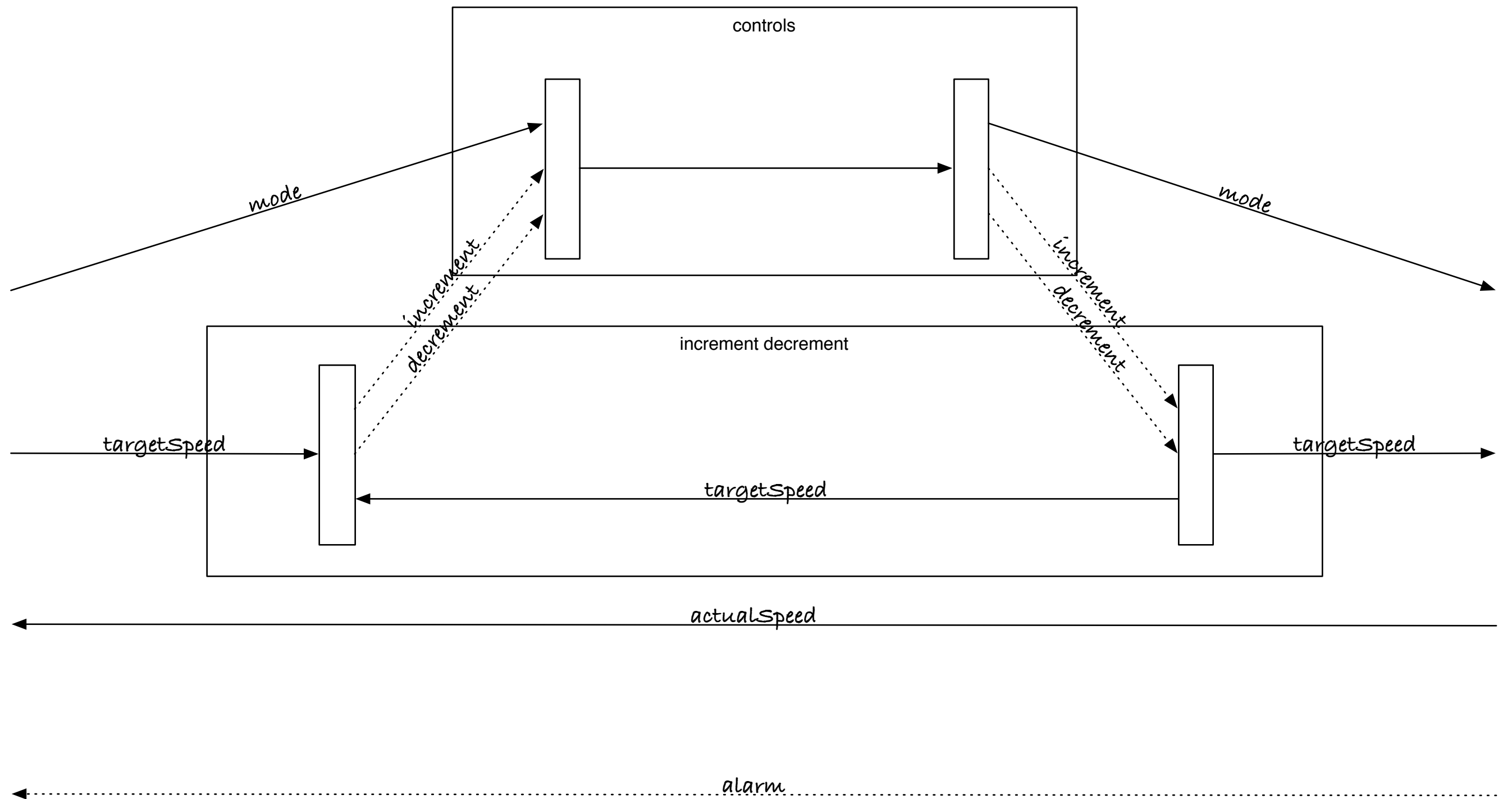
targetSpeed

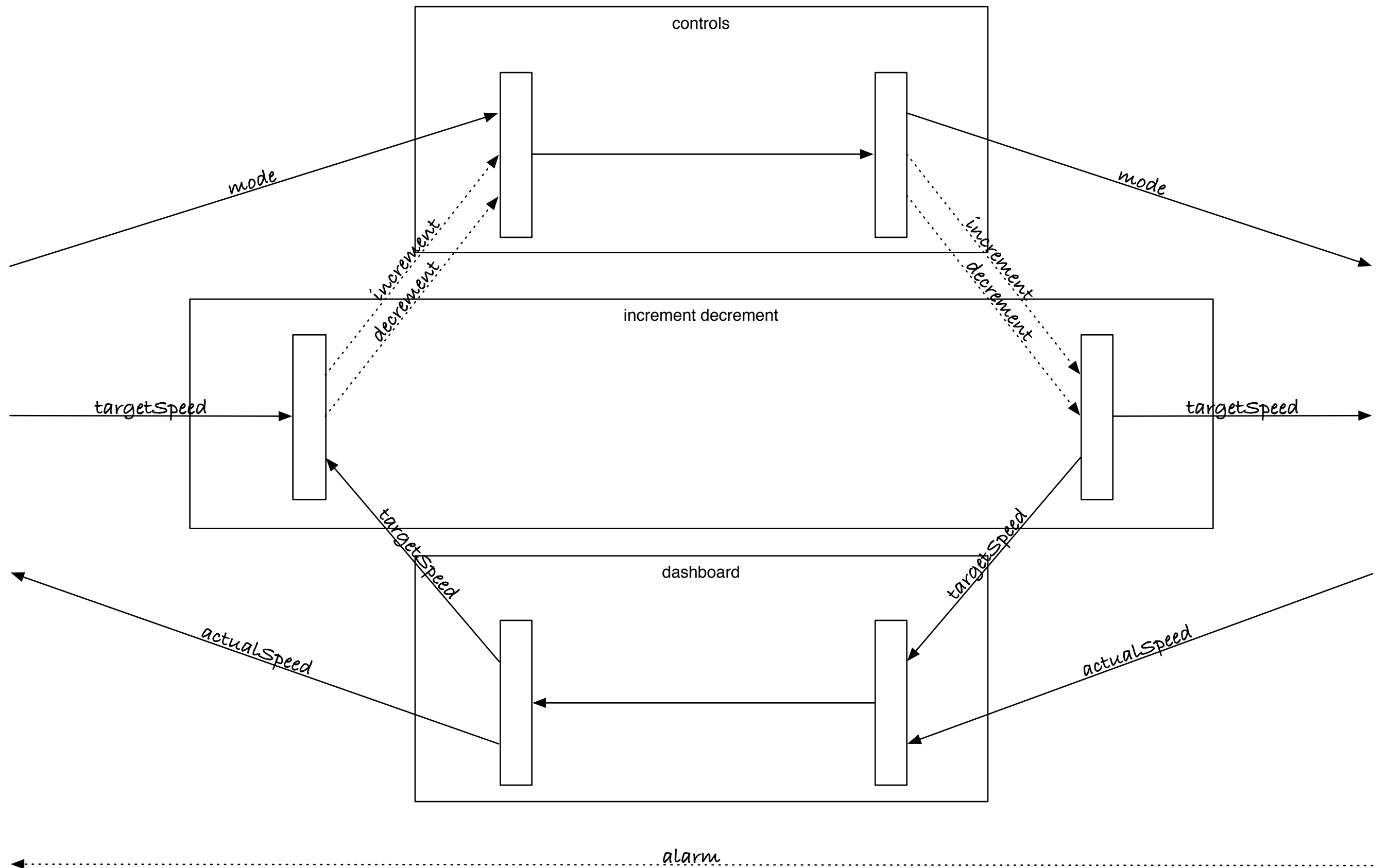
actualSpeed

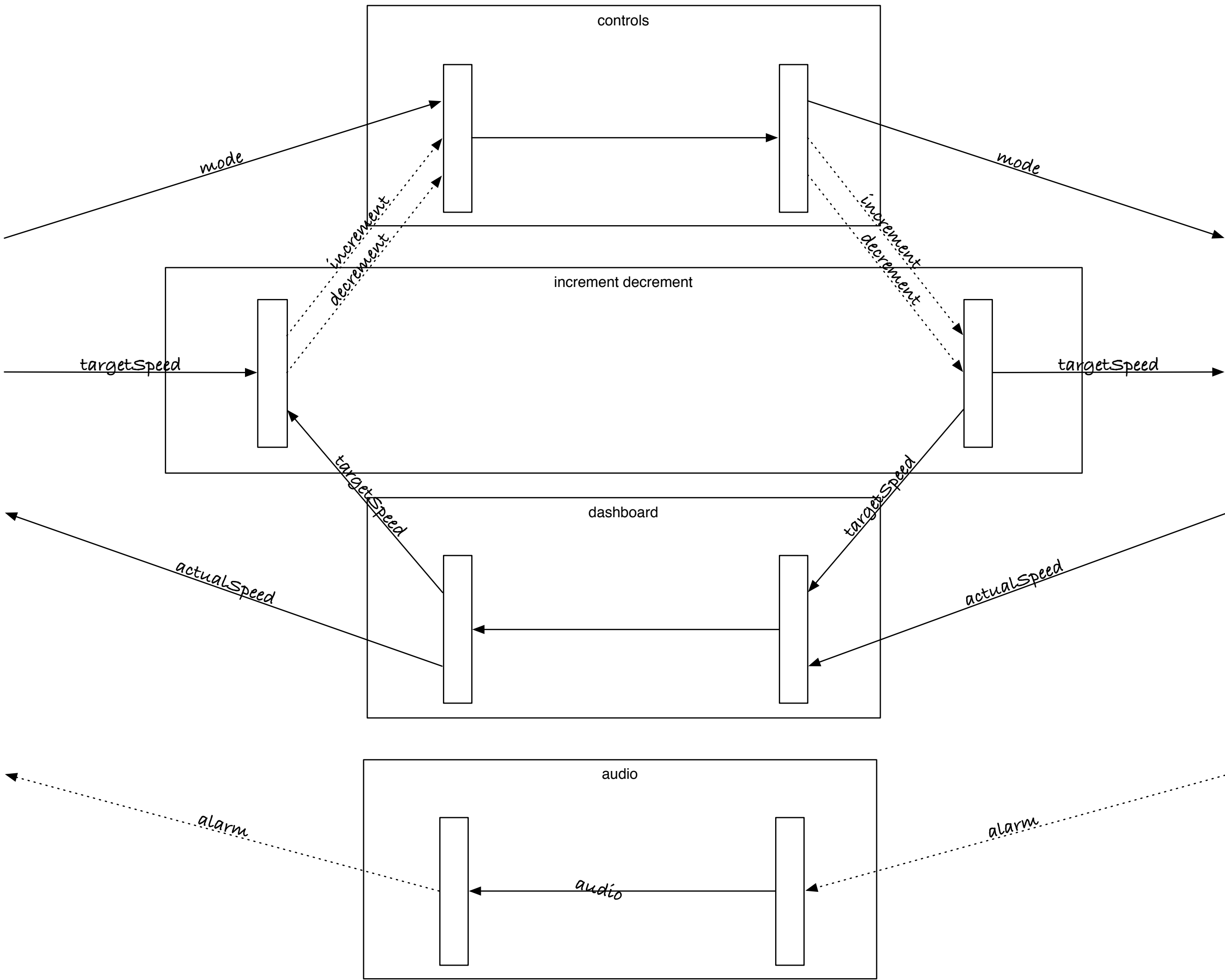
alarm

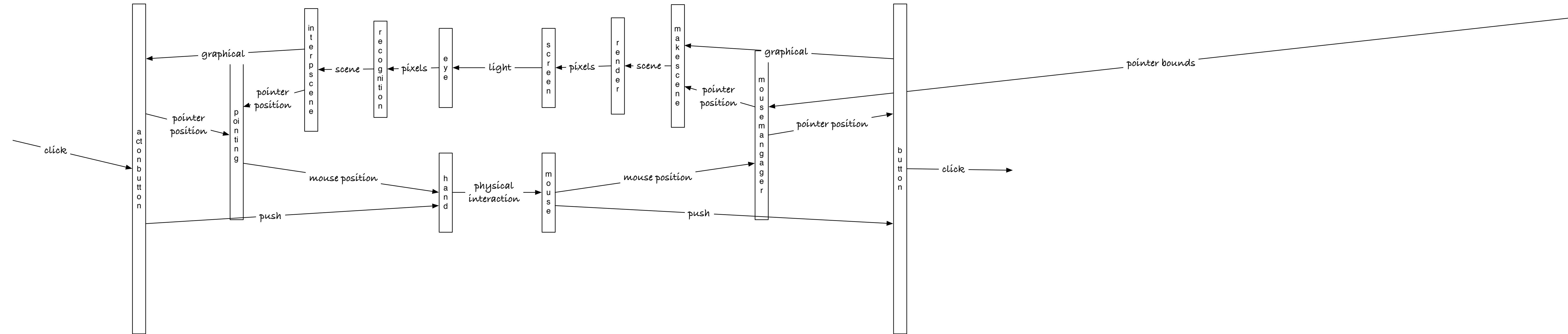


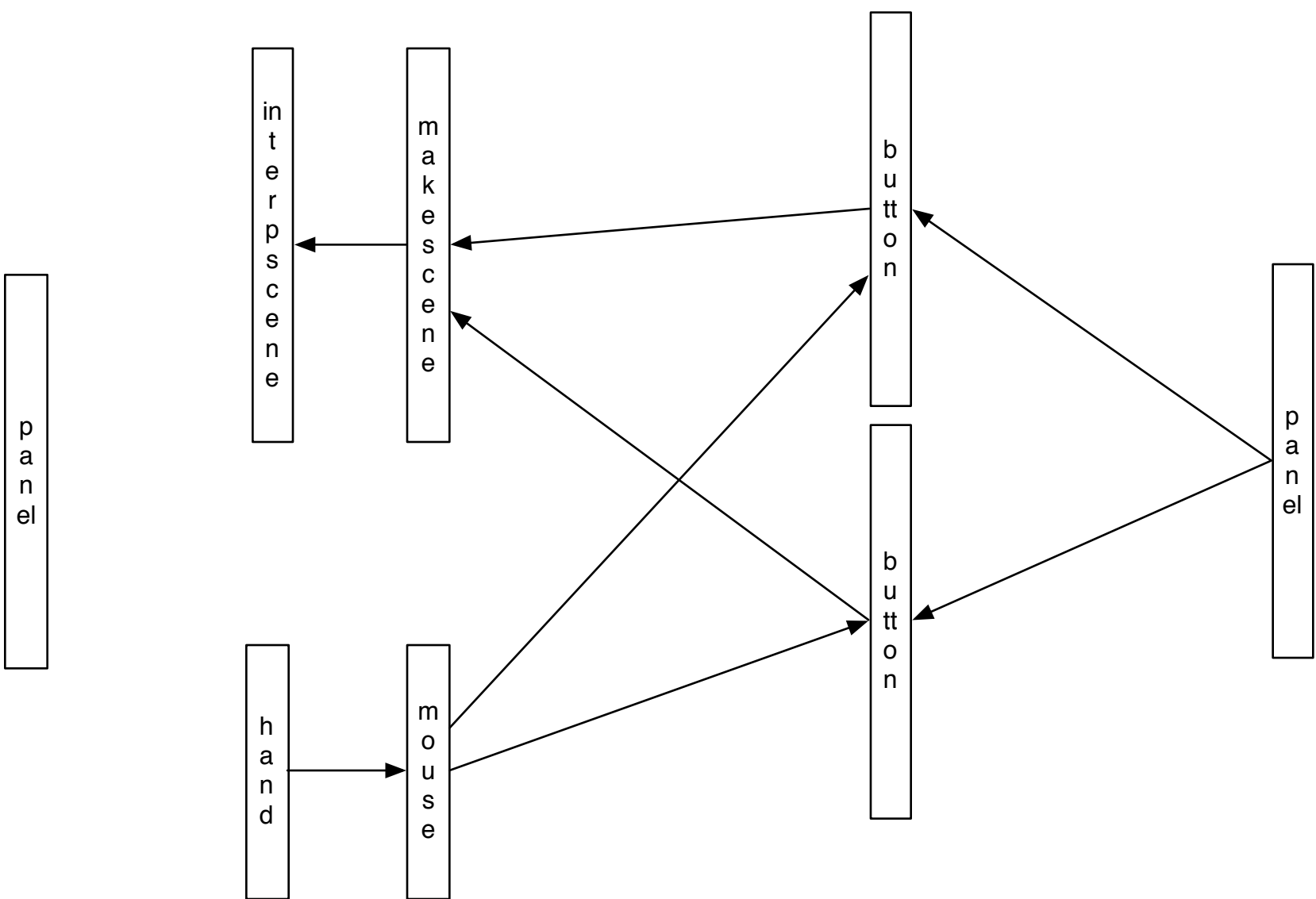


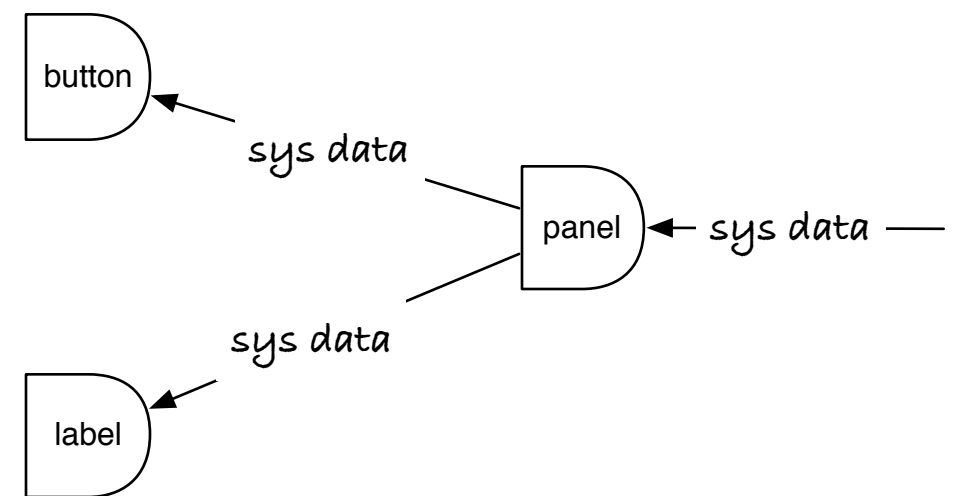
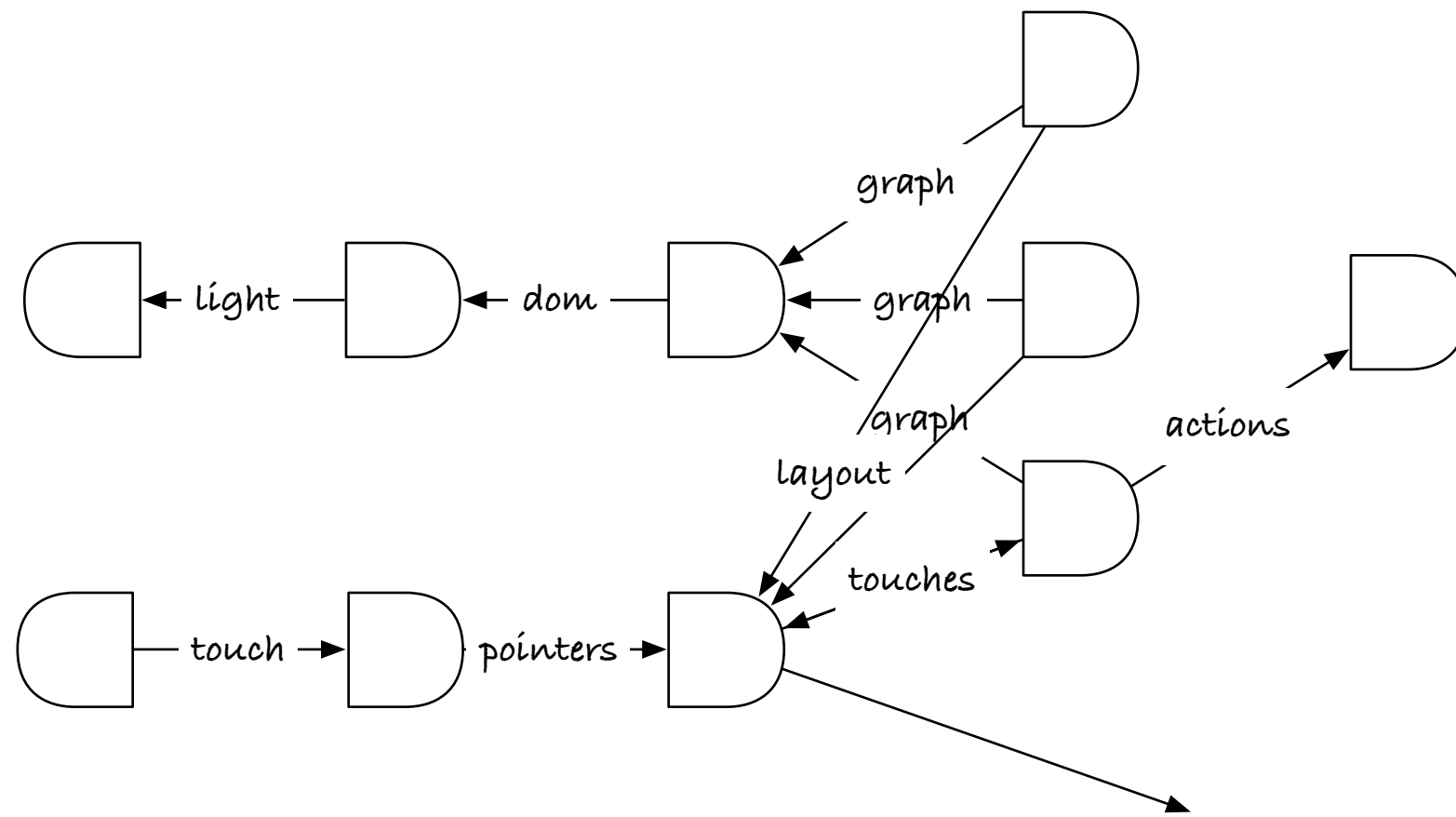


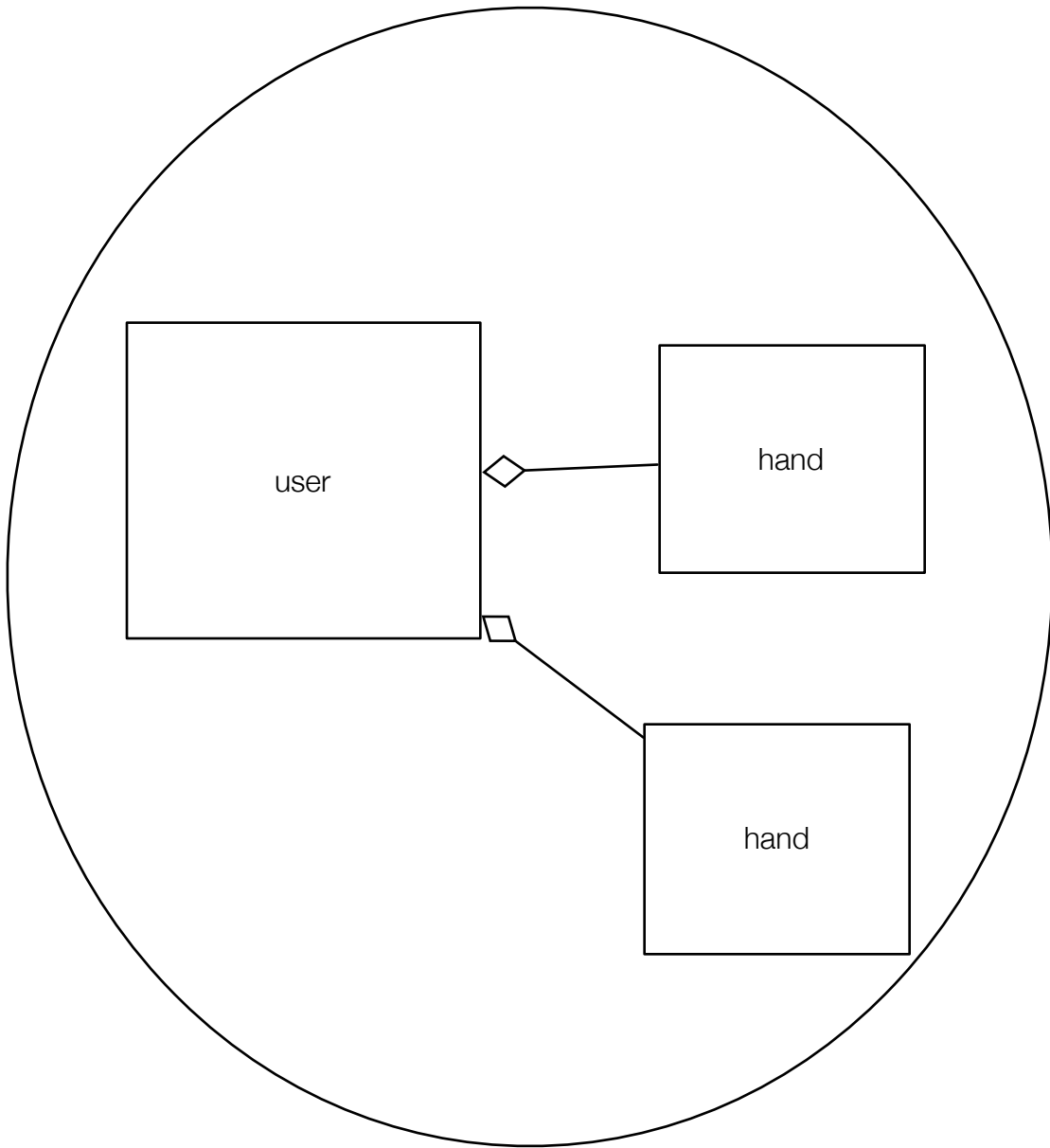
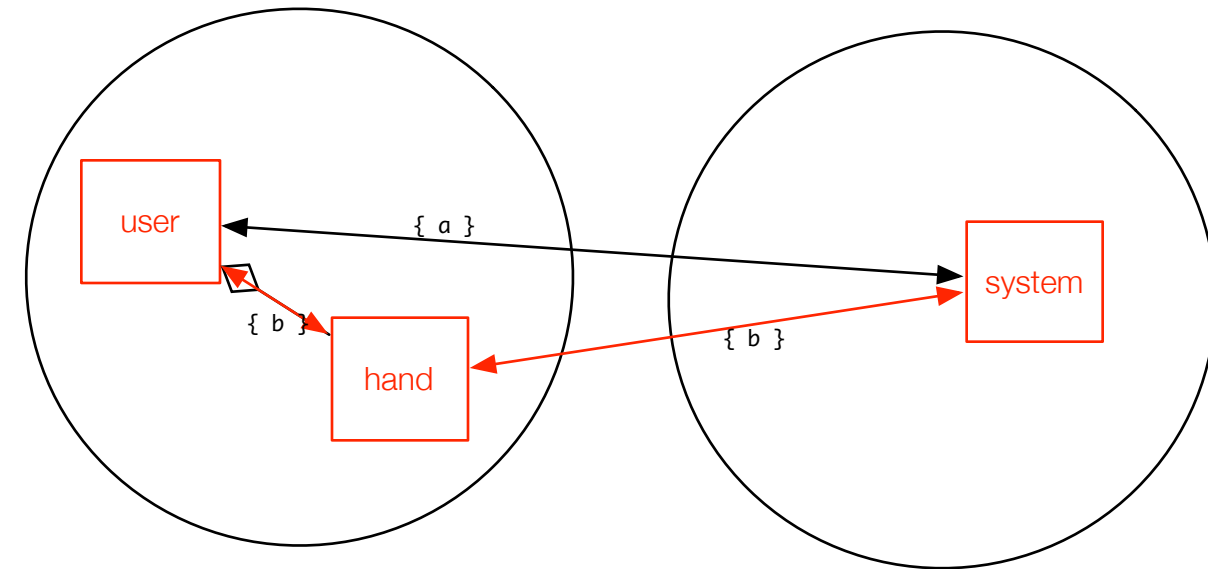
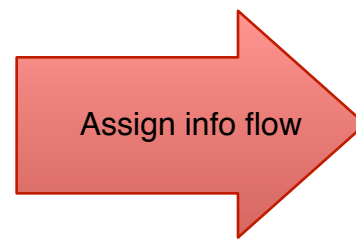
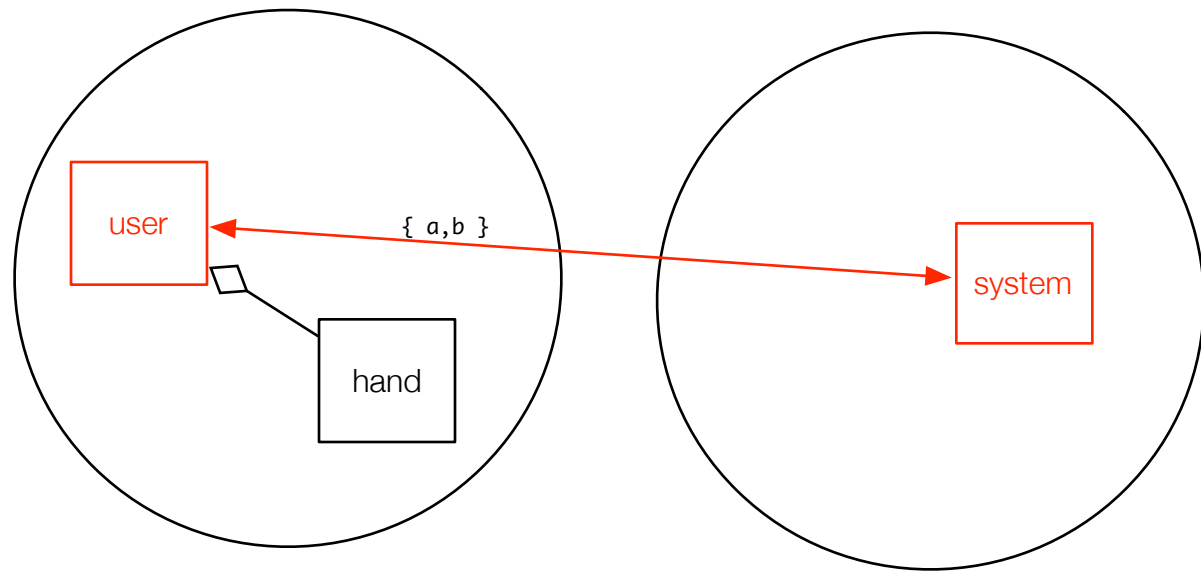








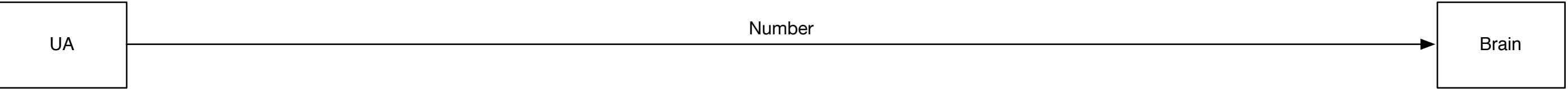




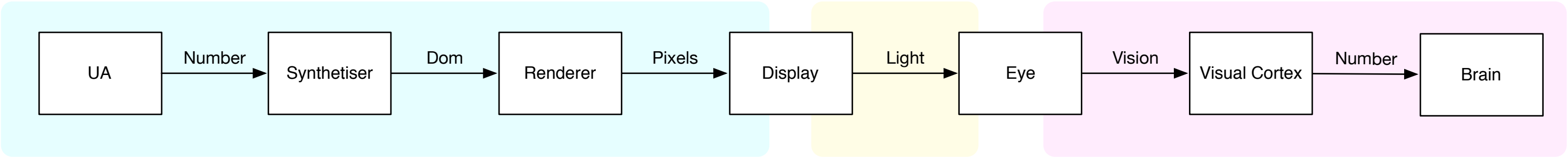


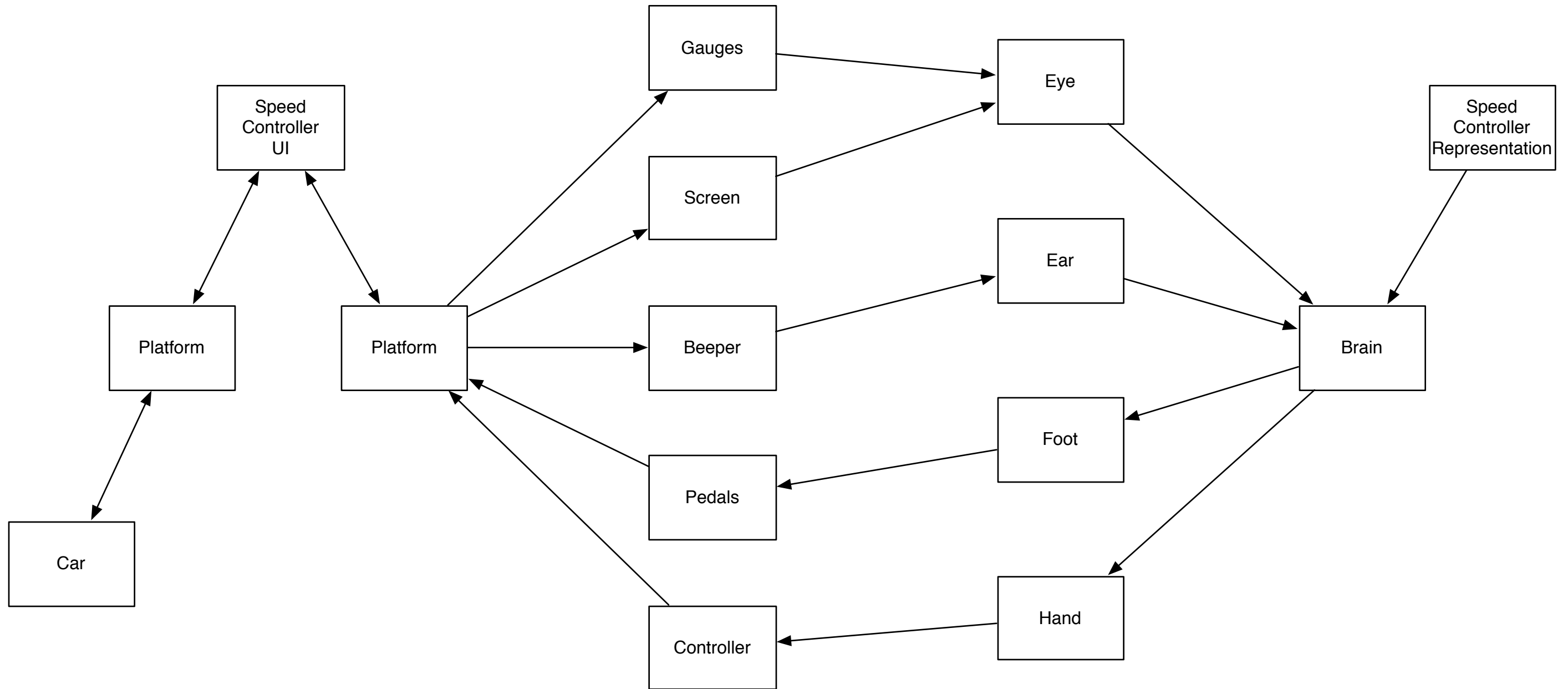
Kind of OSI layer model

Model checking context



Actual context

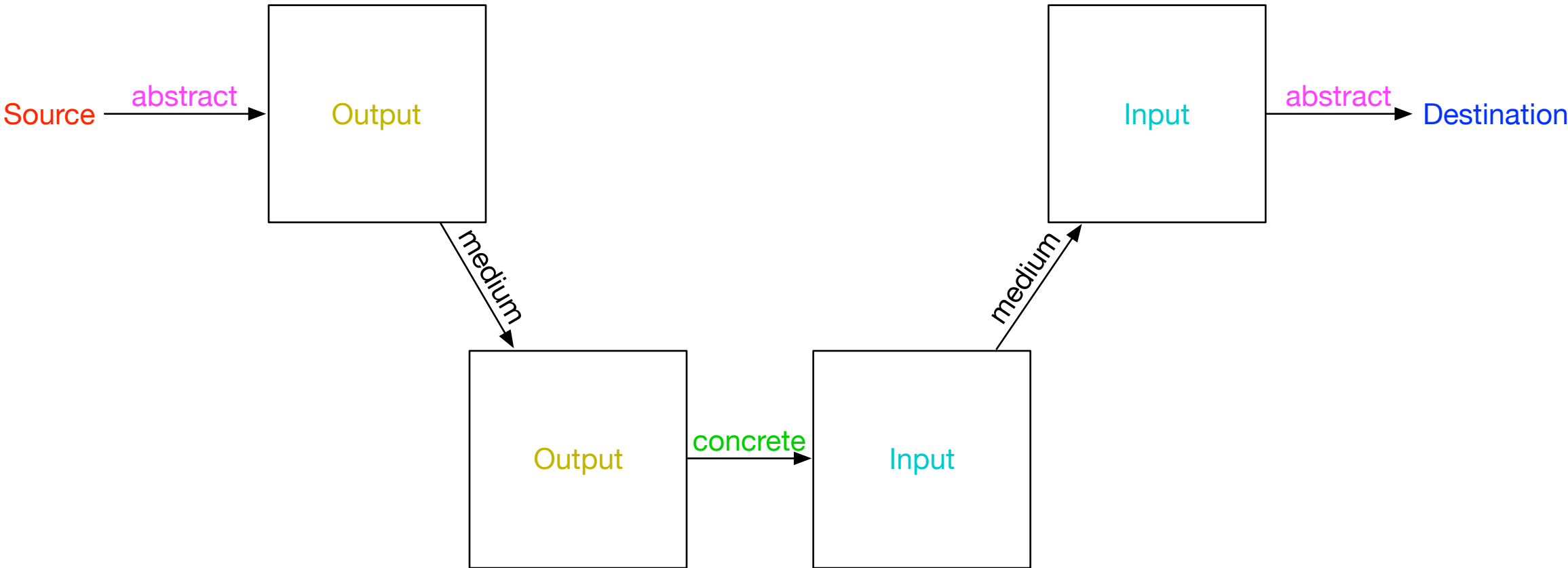
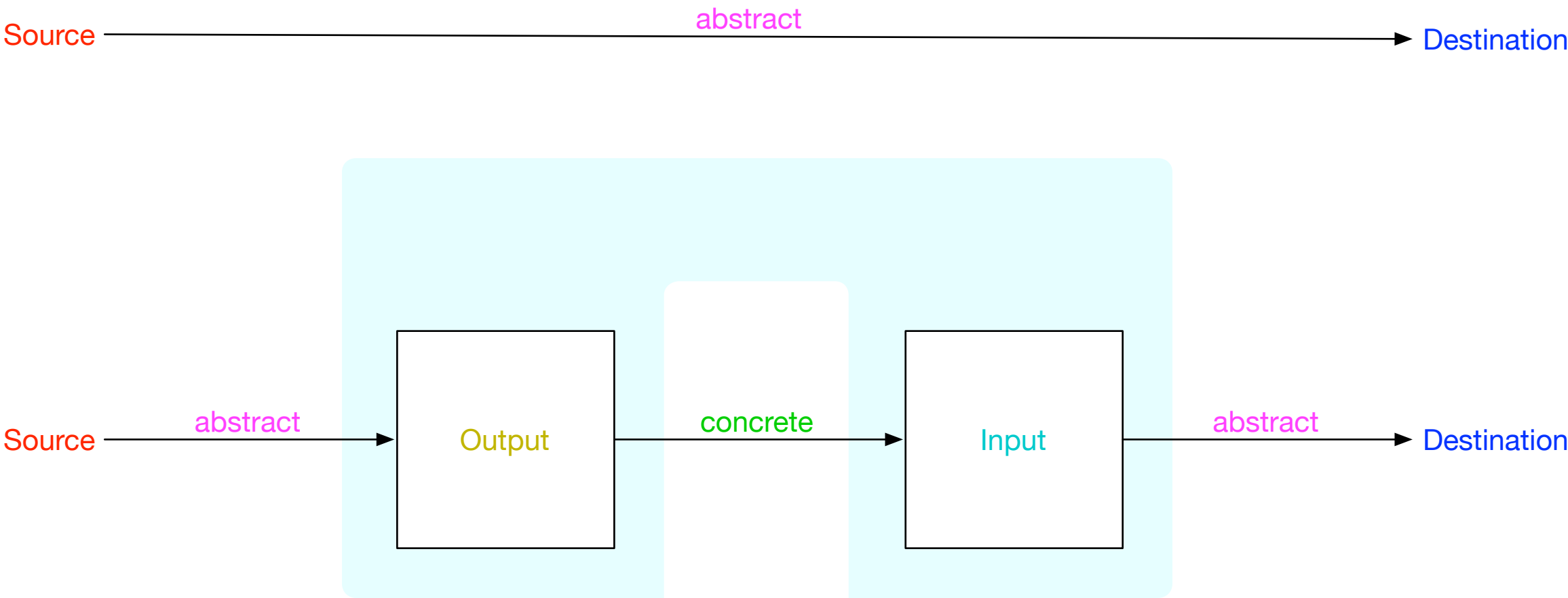




What is an interactive system ?

A generalization of the OSI model

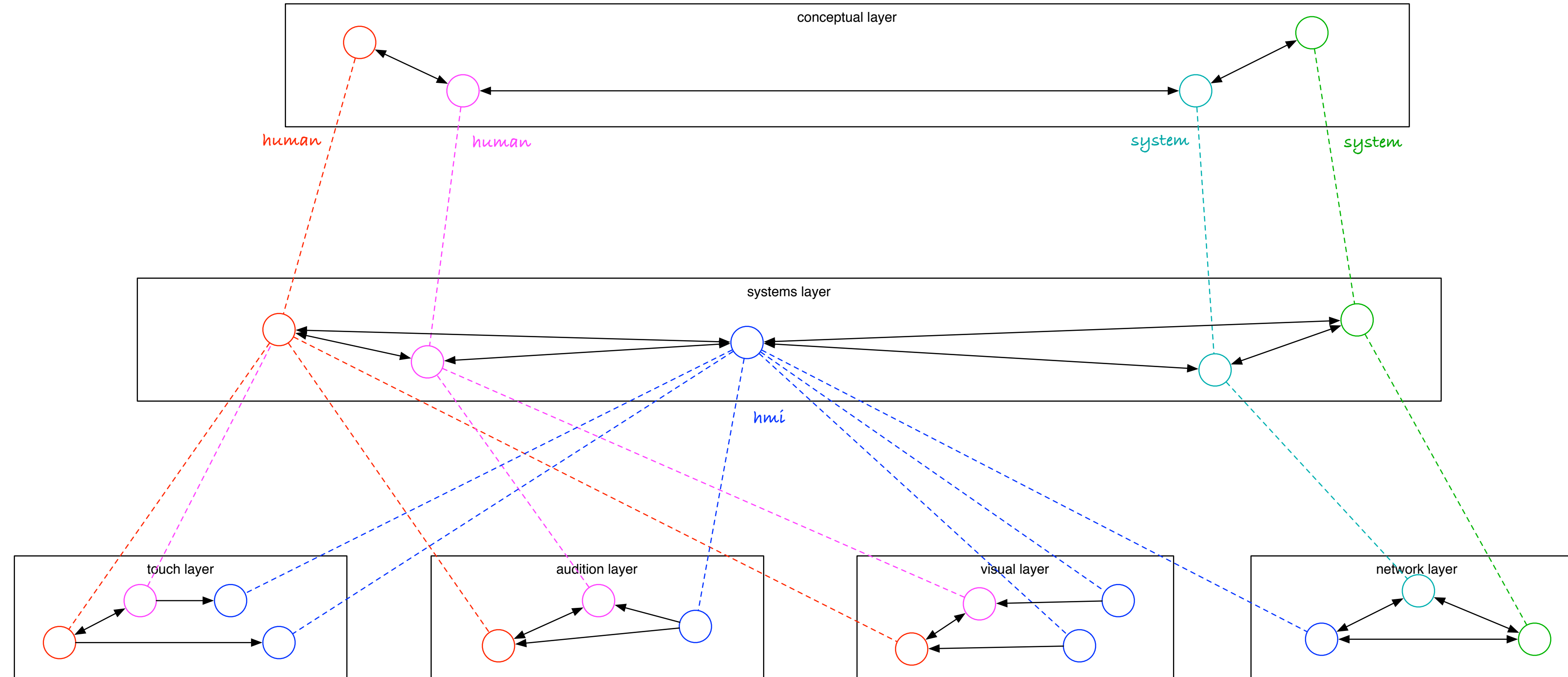
A system that takes an **abstract** flow of information between a **source** and a **destination**, and transforms it into a **concrete** flow of information between an **output** and an **input**, mapping the output to the source, and the input to the destination. An important thing is that abstract and concrete are relative notions.

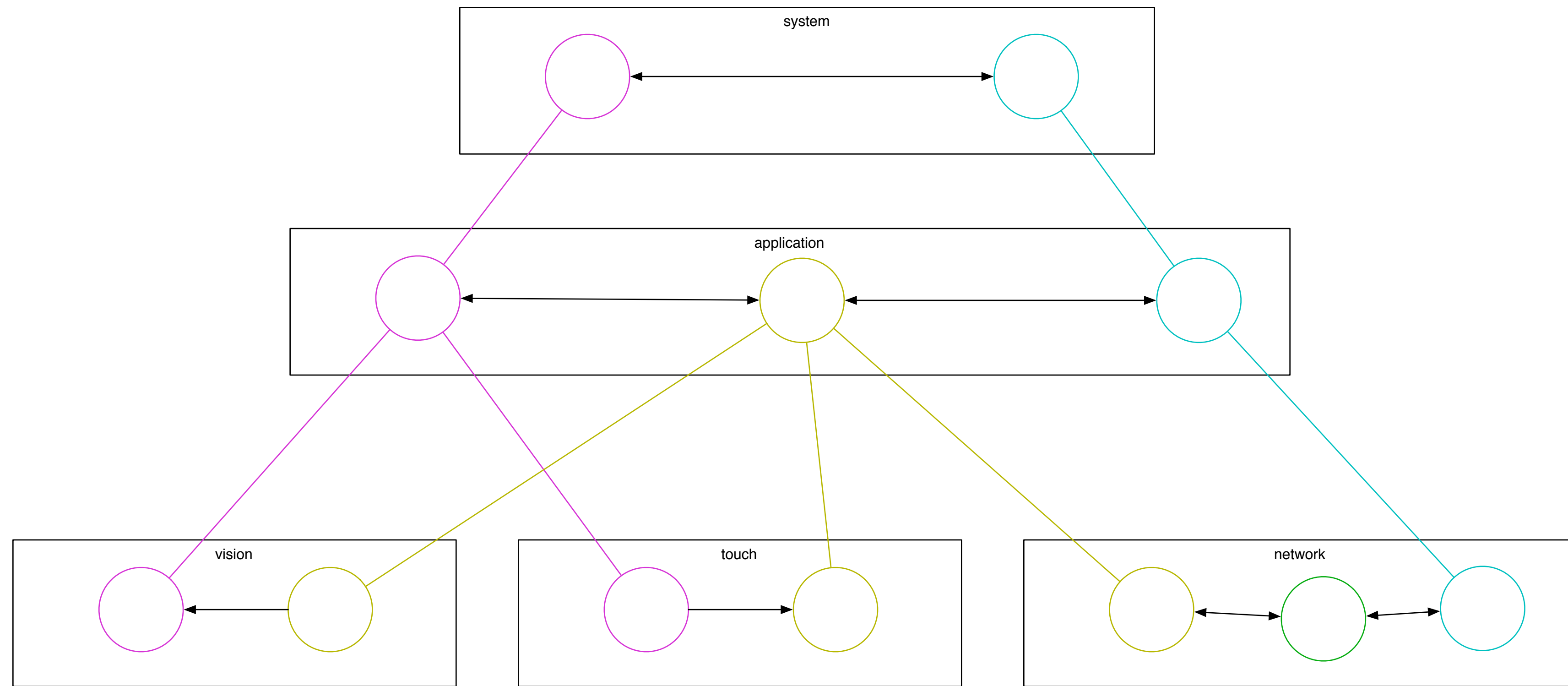


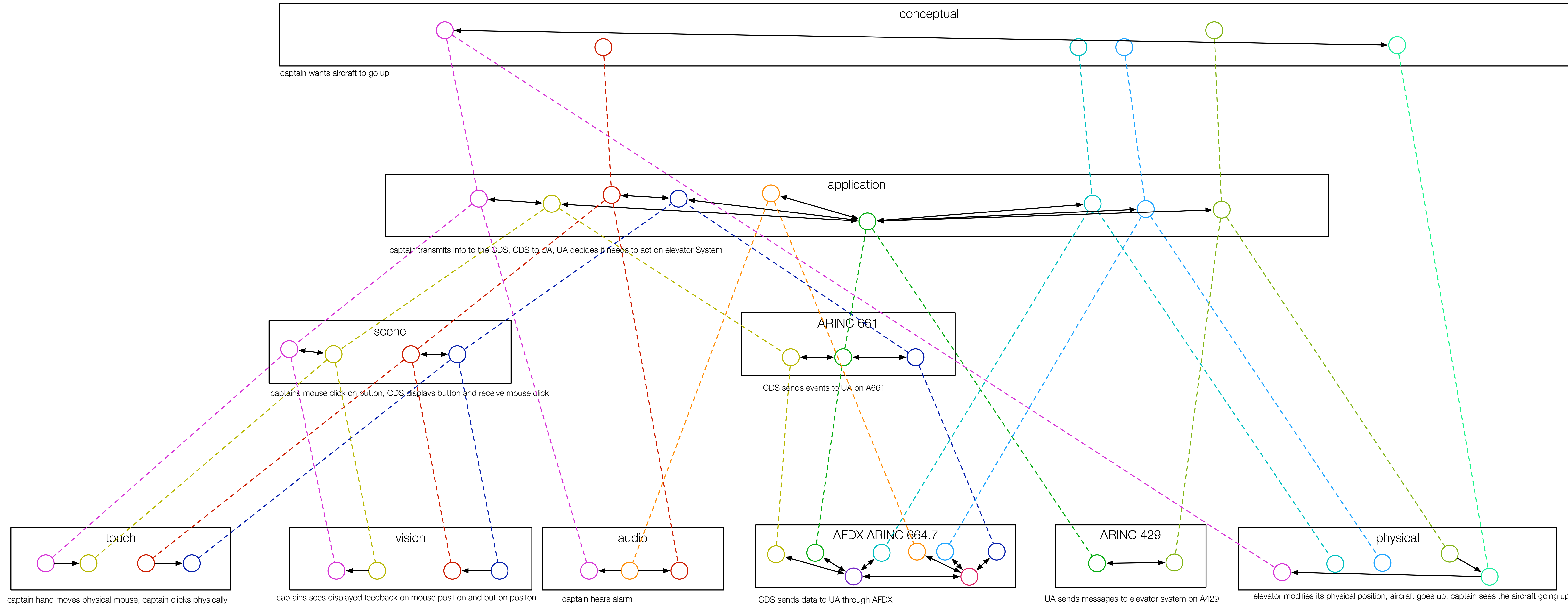
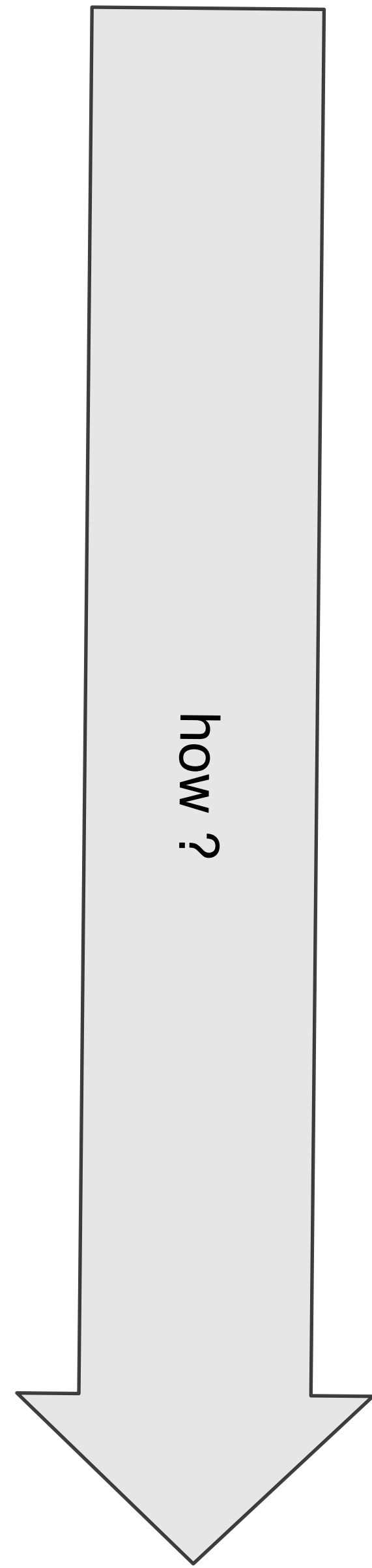
### **Different ways of concretization**

- concretize signals origins and destination
- instantiate concrete sub components

Pamela Zave geomorphic layer model of networks







state variables and dynamic evolution and behavior are INSIDE Circles

flight warning FWS

first officer      right display CDS R1

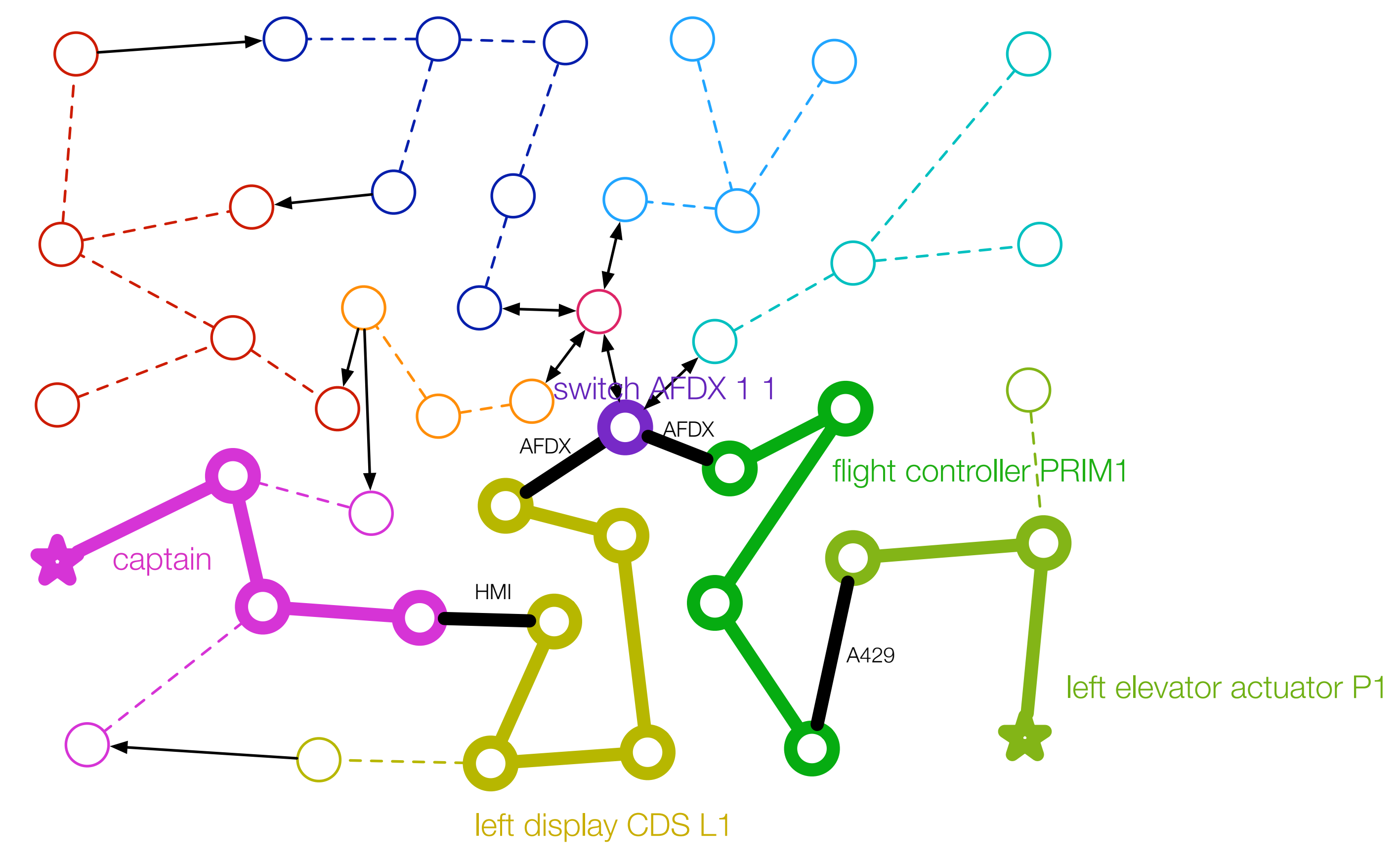
captain            left display CDS L1

engine EEC2            switch AFDX 1 1

engine EEC1            switch AFDX 1 2

left elevator actuator P1      flight controller PRIM1

aircraft





```

emission:
    active(identifier)
    value(identifier)
    {identifier:emission,...,identifier:emission}

```

```
reception:
    active(identifier)
    value(identifier)
    operator(reception,...,reception)
    {identifier:reception,...,identifier:reception}
```

```
behavior:
    affect(reception,emission)
    on(reception,behavior)
    always(behavior)
    and(behavior,...,behavior)
    or(behavior,...,behavior)
```

```

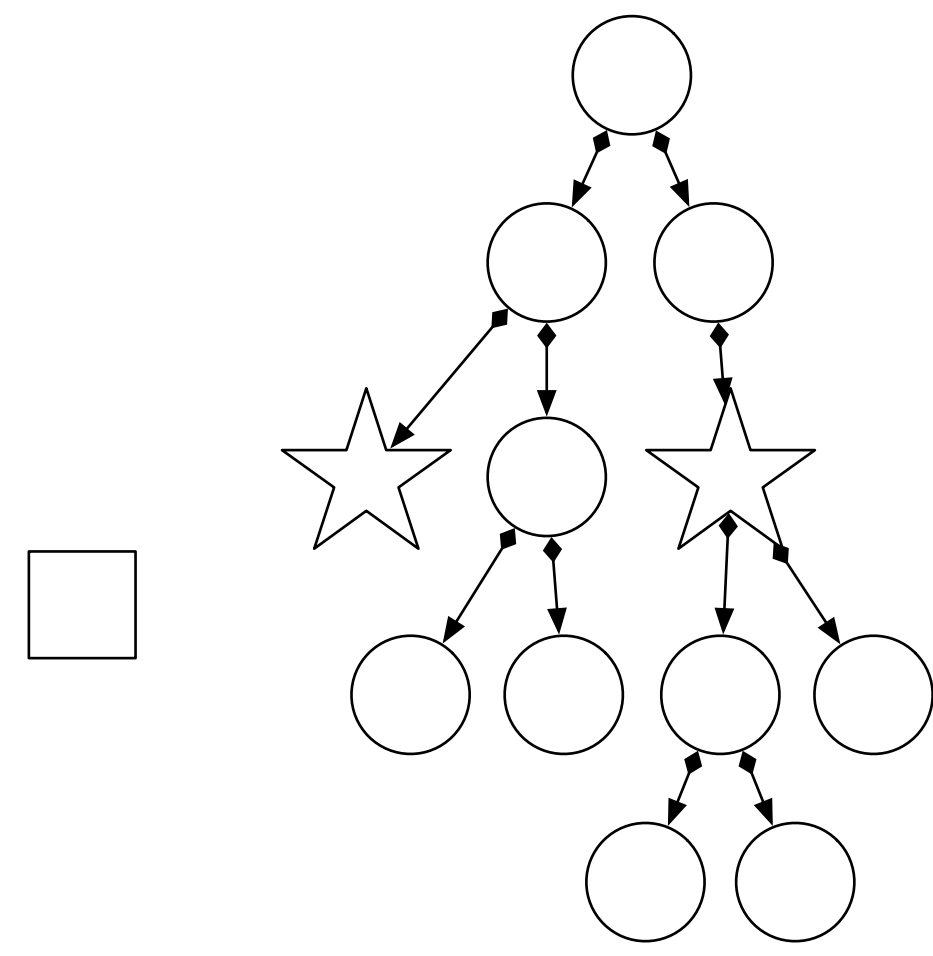
stepManager := behavior(in := reception, max := reception, init := reception, step := reception, var := emission, increment := reception, decrement := reception) := on(
  on(
    declareTemp,
    on(inTick,
      affect<in(t, var)
    ),
    on(increment,
      affect<add(pre(var), +1), temp)
    ),
    on(decrement,
      affect<add(pre(var), -1), temp)
    ),
    ensureIsInRange(0, 100, temp, var)
  )
)

```

```

stepManager::Behavior(min::reception,max::reception,init::reception,step::reception,var::emission,increment::reception,decrement::reception) :=
and(
  declare(temp),
  on(init(),
    affect(init,var)
  ),
  on(increment,
    affect(add(pre(var),+1), temp)
  ),
  on(decrement,
    affect(add(pre(var),-1), temp)
  ),
  ensureIsInRange(0,100,temp,var)
)

```

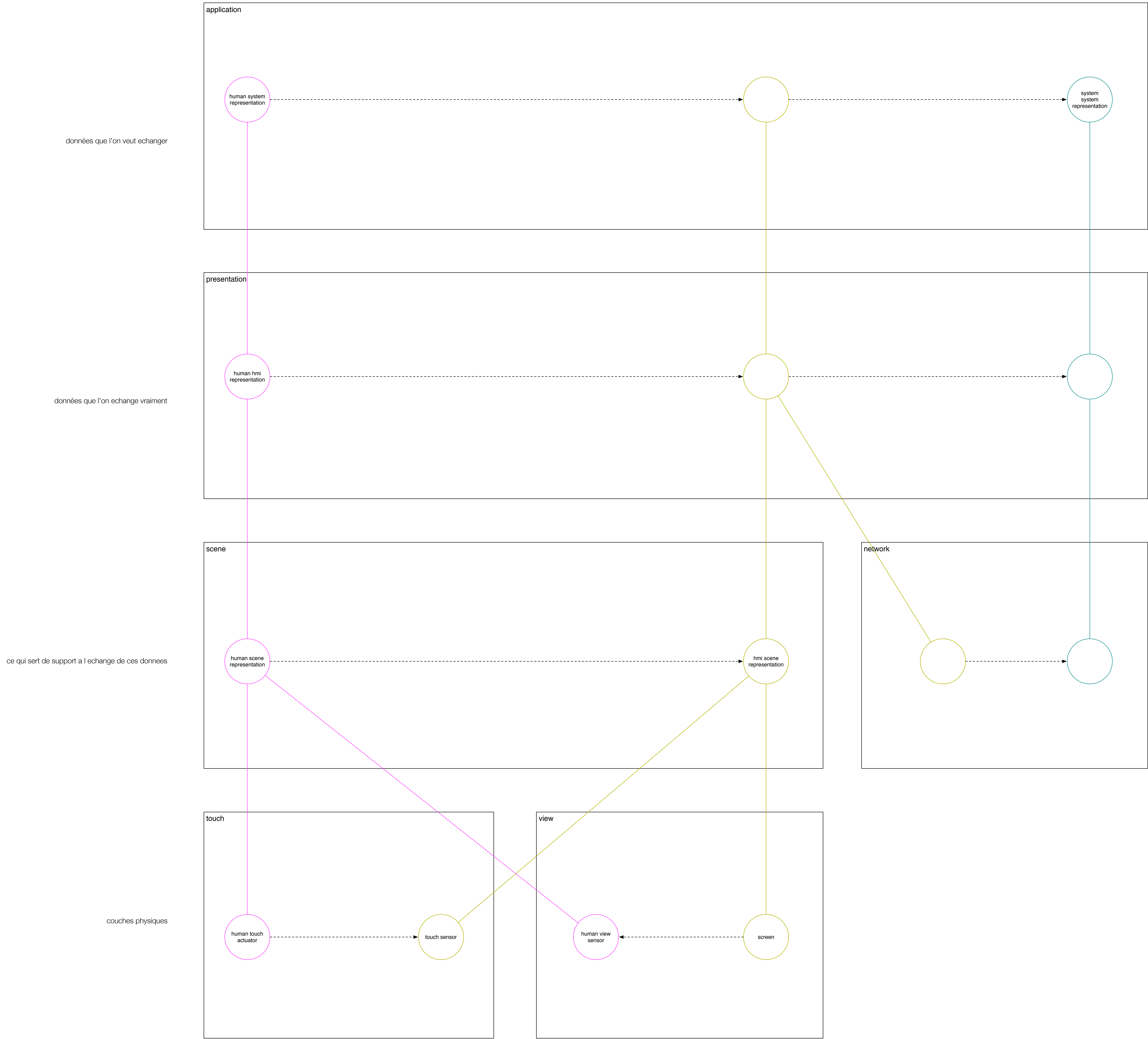


```
ensureIsInRange::behavior(min::reception,max::reception,temp::reception,var::emission) :=
    affect (max (min, min (max, temp)), var)
```

```
trigger::behavior(a::identifier,b::reception) :=
    and(affect(true,active(a)),affect(b,value(a)))
```

[illegible]

```
speedcontroller:continuous:{
  driver:continuous:{
    actualspeed:continuous:number:in,
    desiredspeed:continuous:number:out,
    increment:discrete:void:in,
    decrement:discrete:void:in,
    toggle:discrete:void:in,
  }
}
```



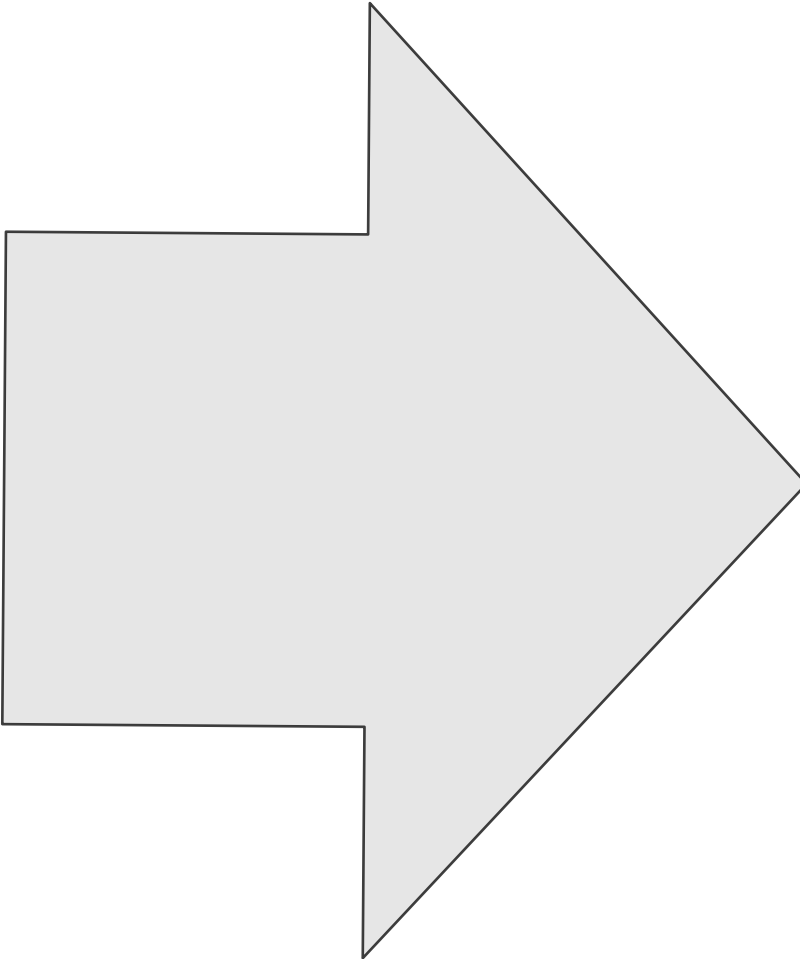
=

behavior:

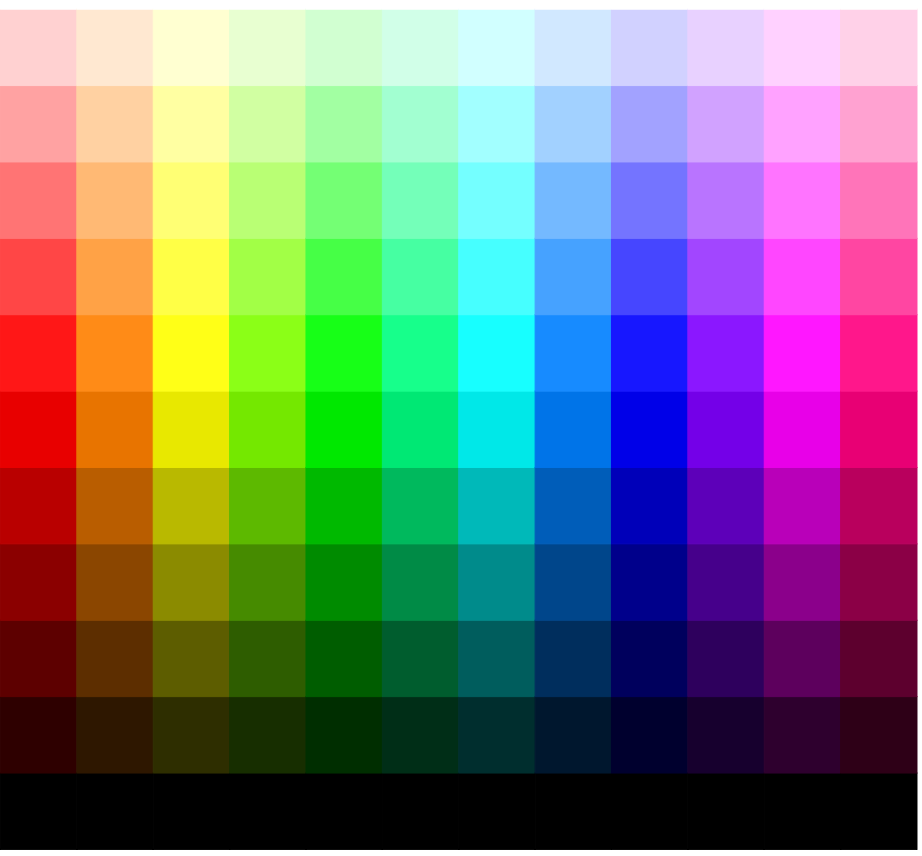
- affect(reception,emission)
- on(reception,behavior)
- always(behavior)
- and(behavior,...,behavior)
- or(behavior,...,behavior)

```
on(a,
  on(b,
    c = d
  )
)

on(e,
  on(f,
    c = g
  )
)
```

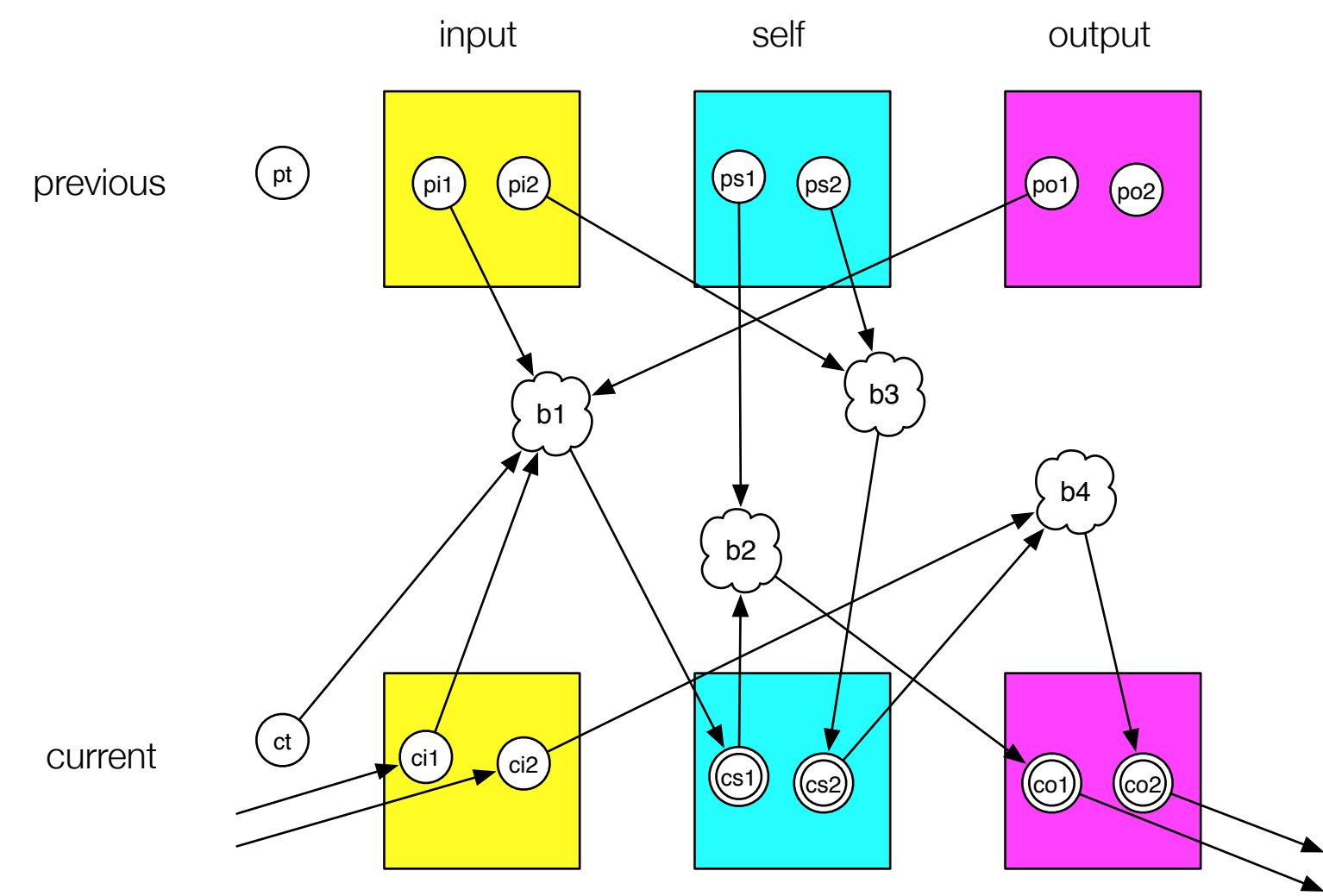


```
c =
  if((a&&b)&&not(e&&f)),
    d,
    if(e&&f,
      g,
      pre(c)
    )
)
```



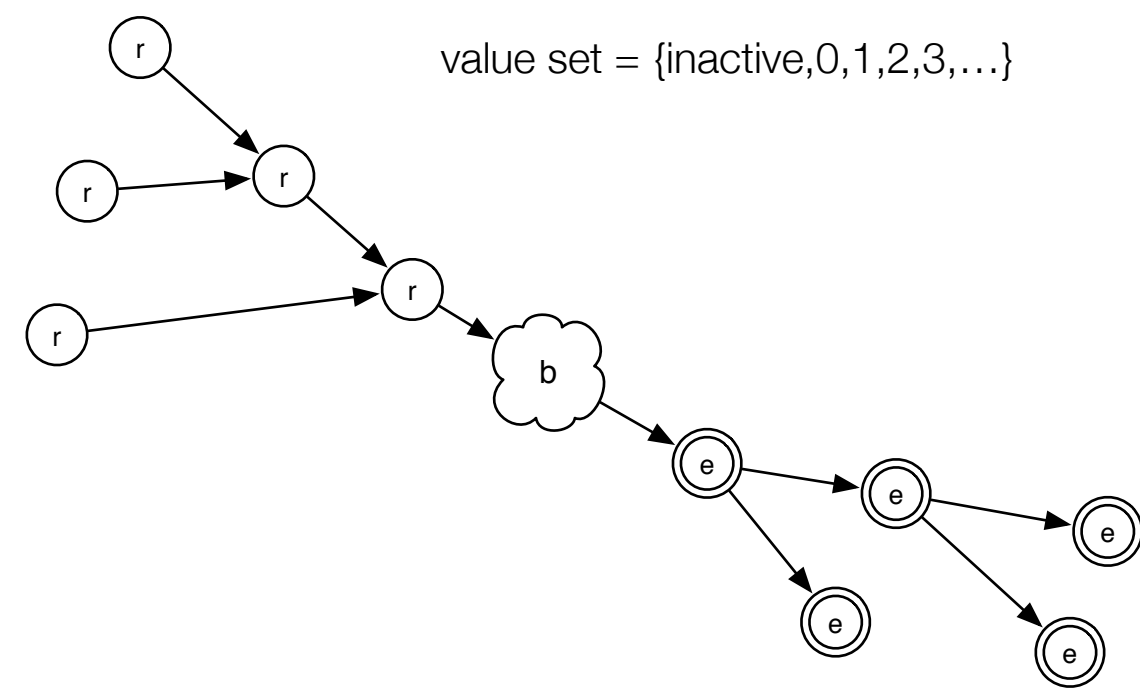


### Transition Function Structure

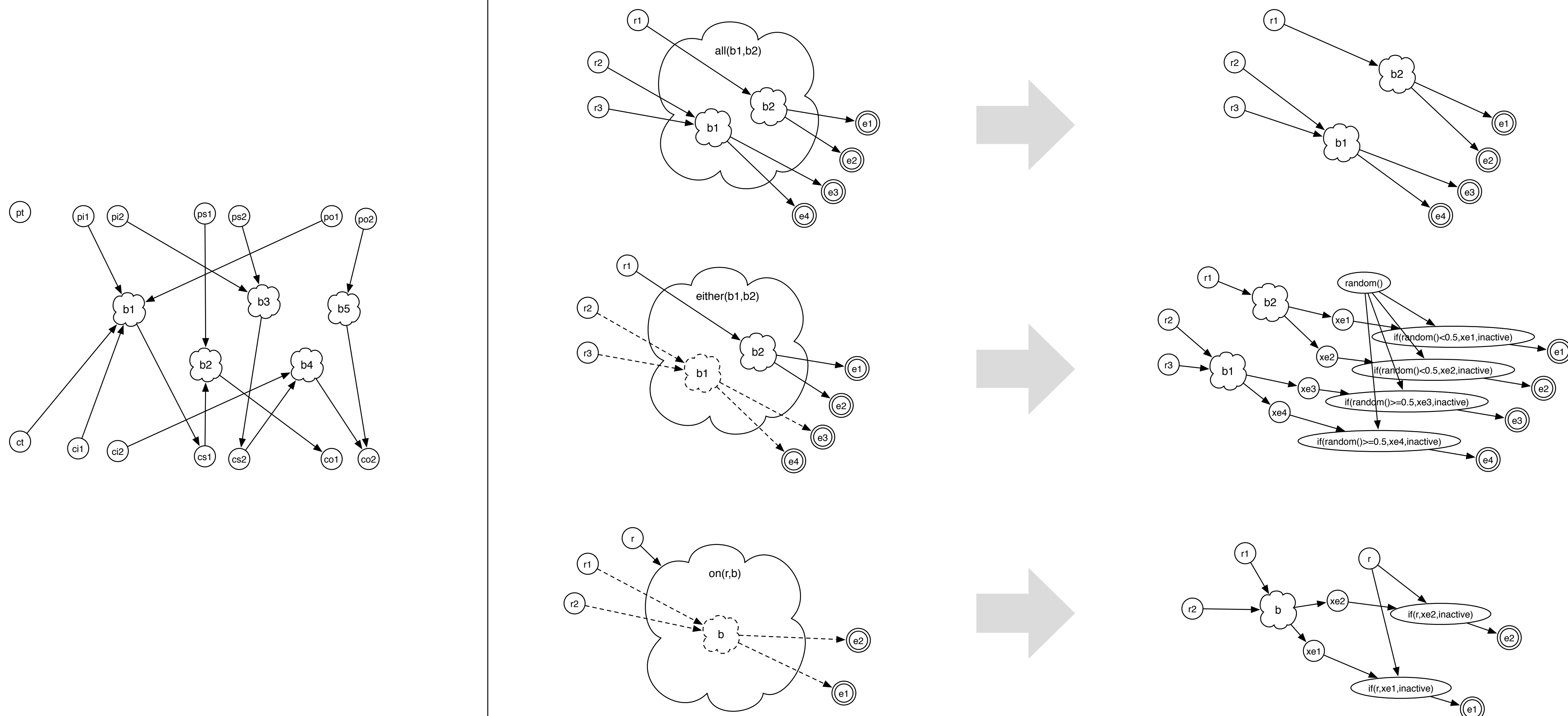


### Transition Function Rules

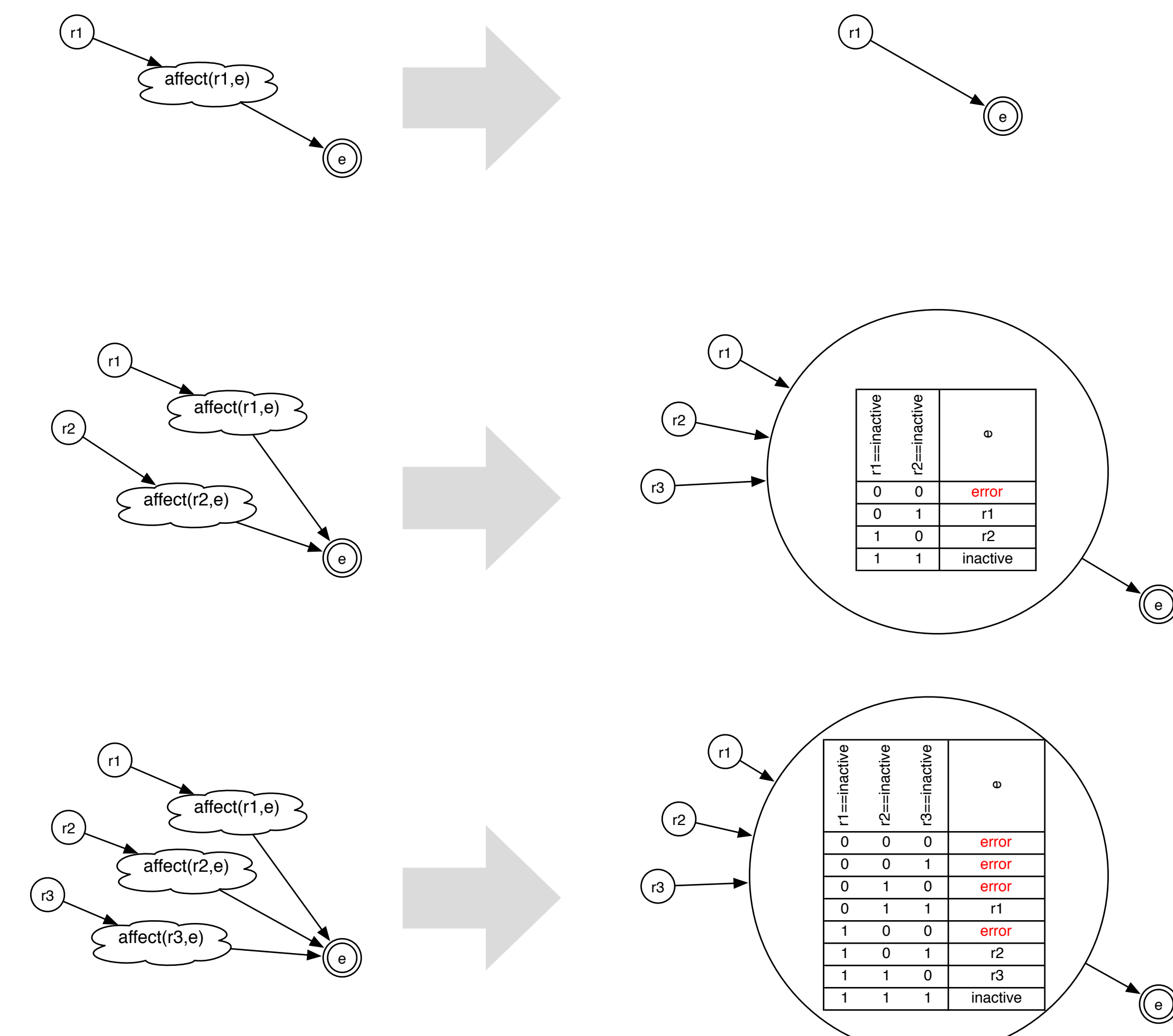
$ct > pt$      $t$  is for time  
 for all  $pi\_n$ , exists  $ci\_n$   
 for all  $ps\_n$ , exists  $cs\_n$   
 for all  $po\_n$ , exists  $co\_n$   
  
 for all  $pi\_n$ ,  $in(pi\_n) = 0$   
 for all  $ps\_n$ ,  $in(ps\_n) = 0$   
 for all  $po\_n$ ,  $in(po\_n) = 0$   
 for all  $ci\_n$ ,  $in(ci\_n) = 0$   
 for all  $cs\_n$ ,  $in(cs\_n) \geq 0$   
 for all  $co\_n$ ,  $in(co\_n) \geq 0$   
  
 for all  $b\_n$ ,  $out(b\_n) \geq 1$   
  
 all nodes are reception node    (noted e)  
 only  $cs\_n$  and  $co\_n$  are emission nodes    (noted r)



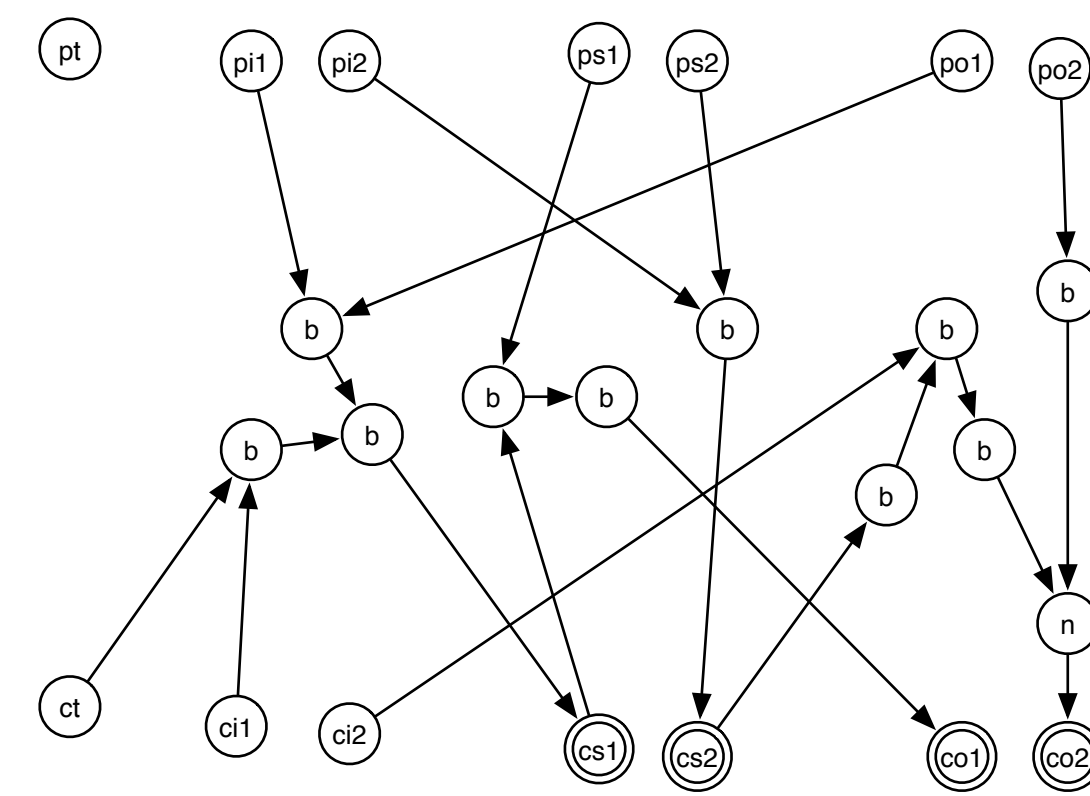
### First transform : Behaviour elimination

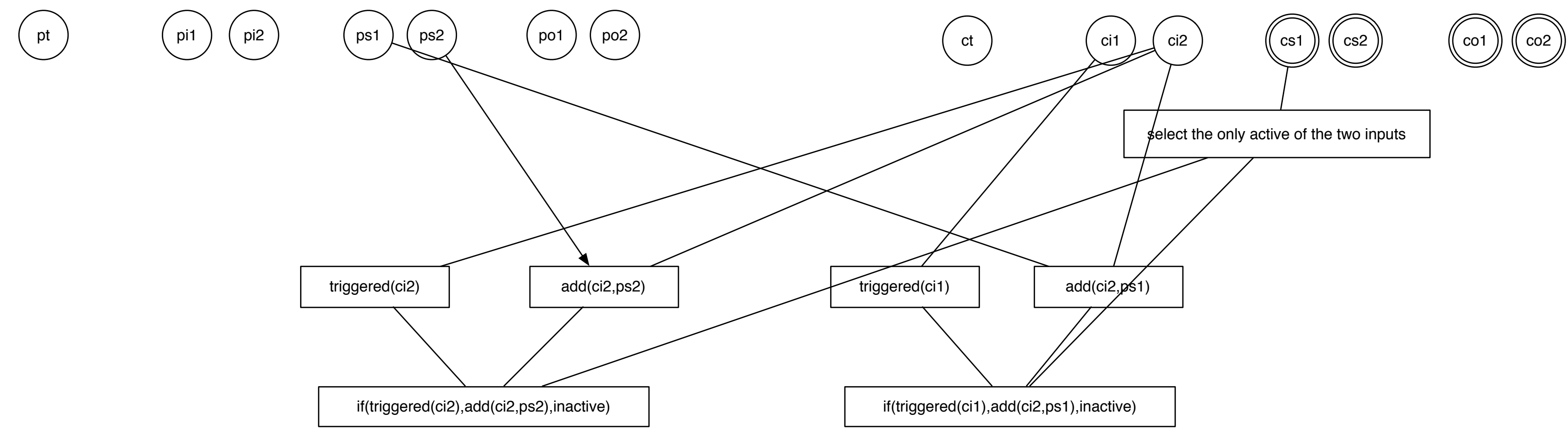
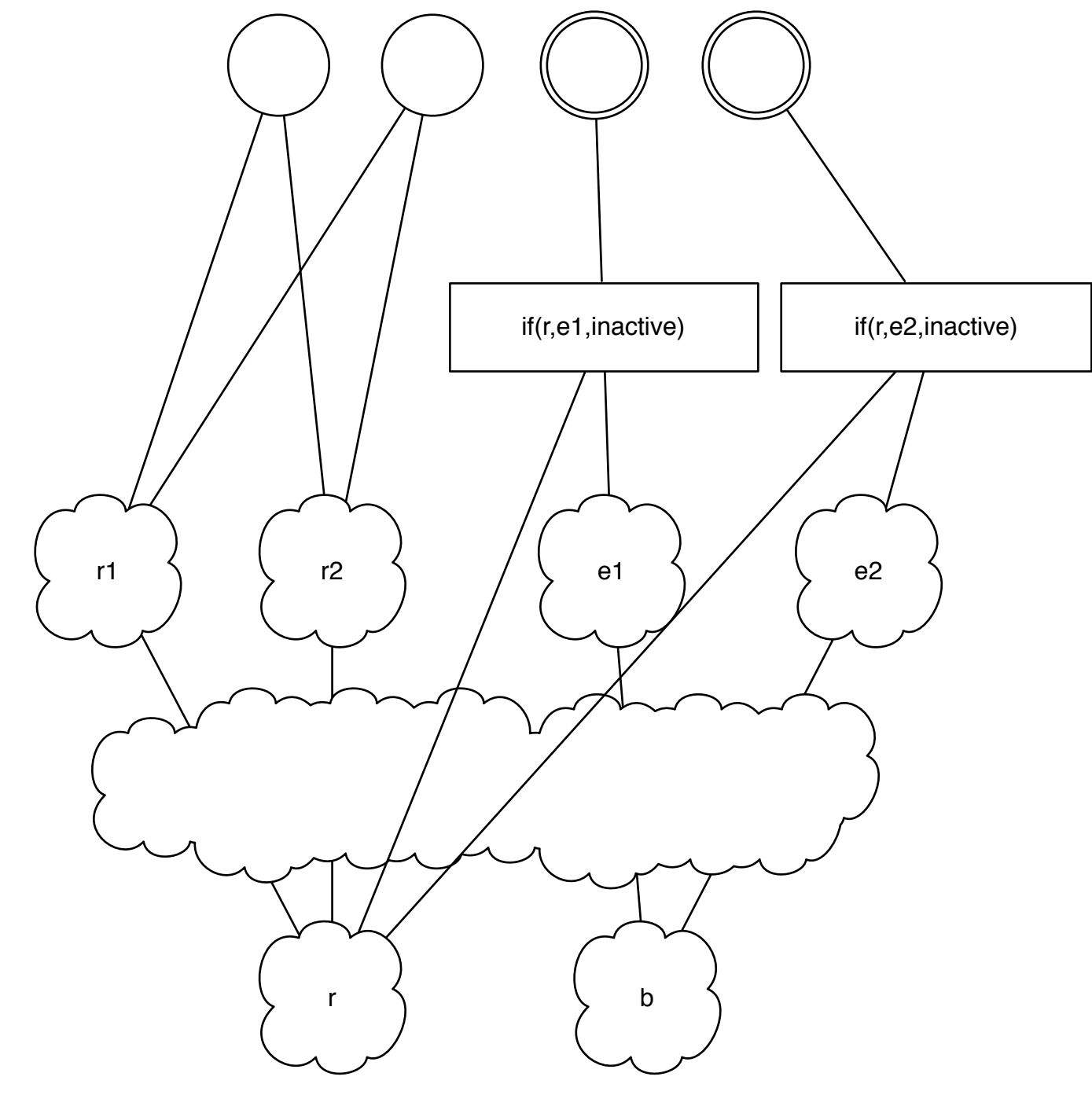
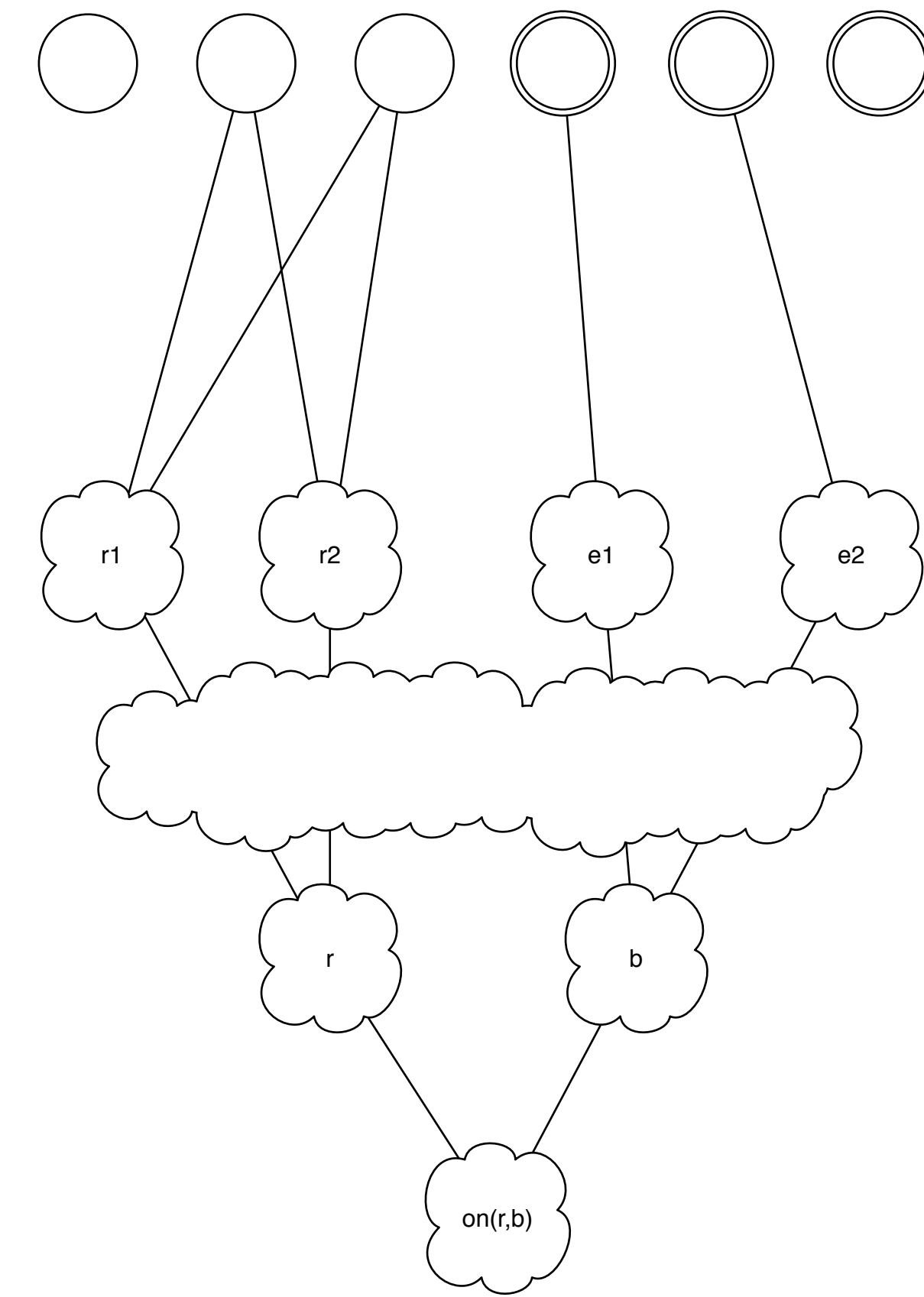
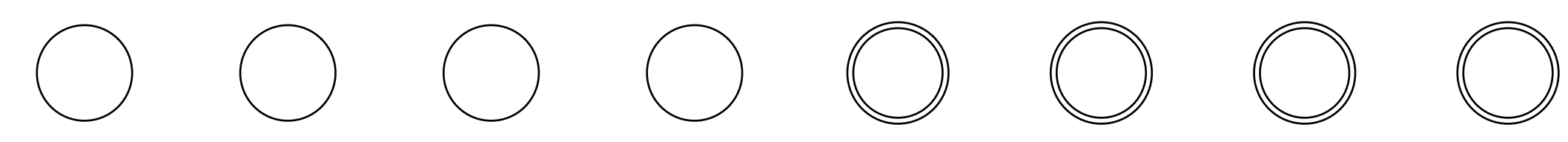
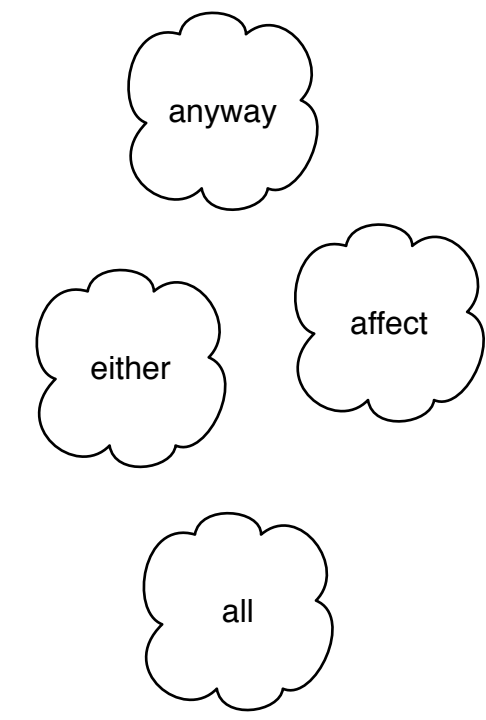
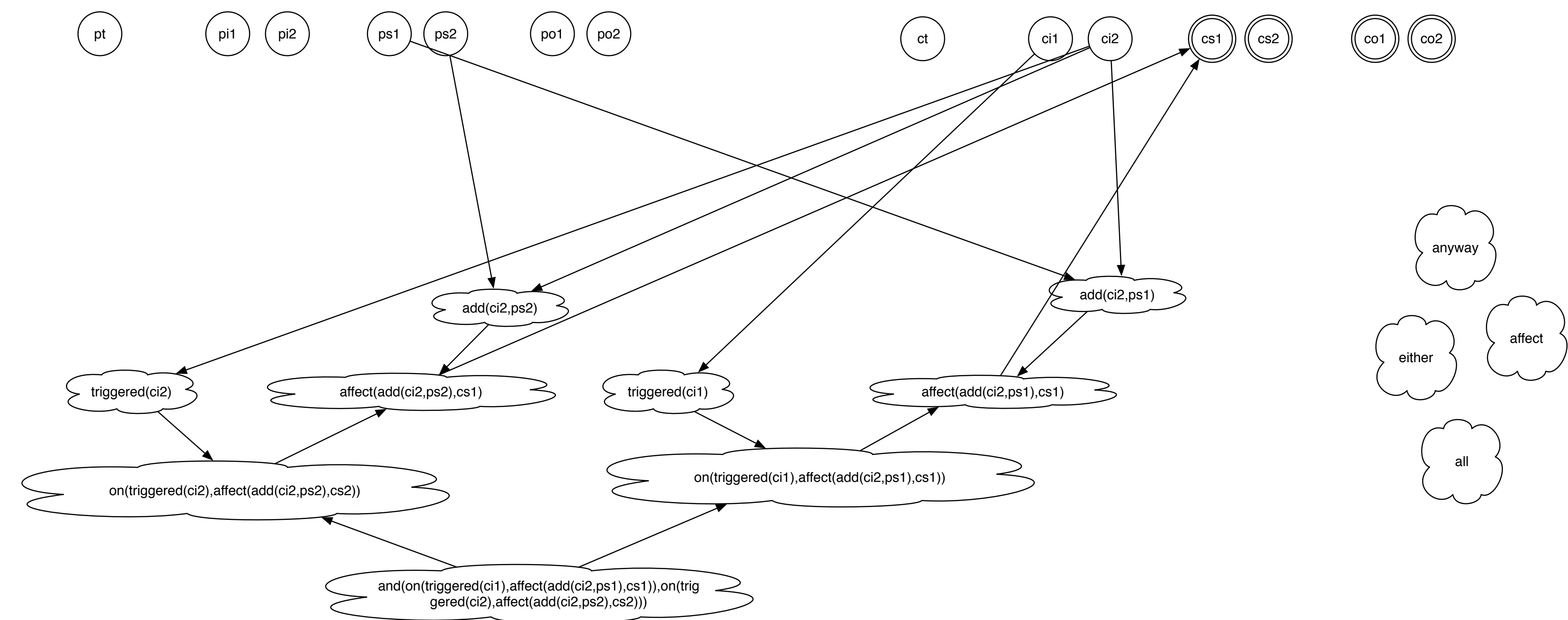


### Second transform : Affectation elimination

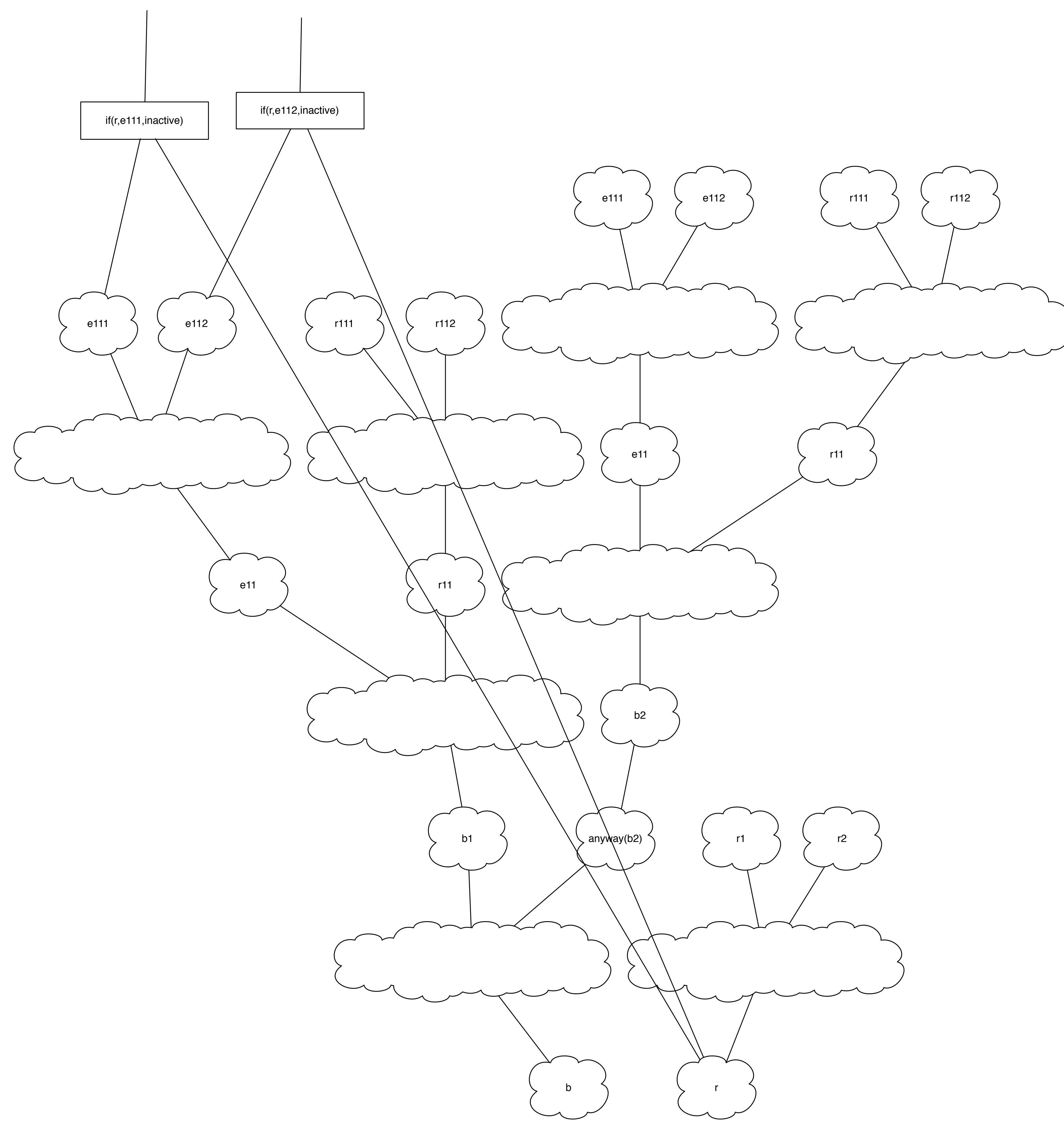
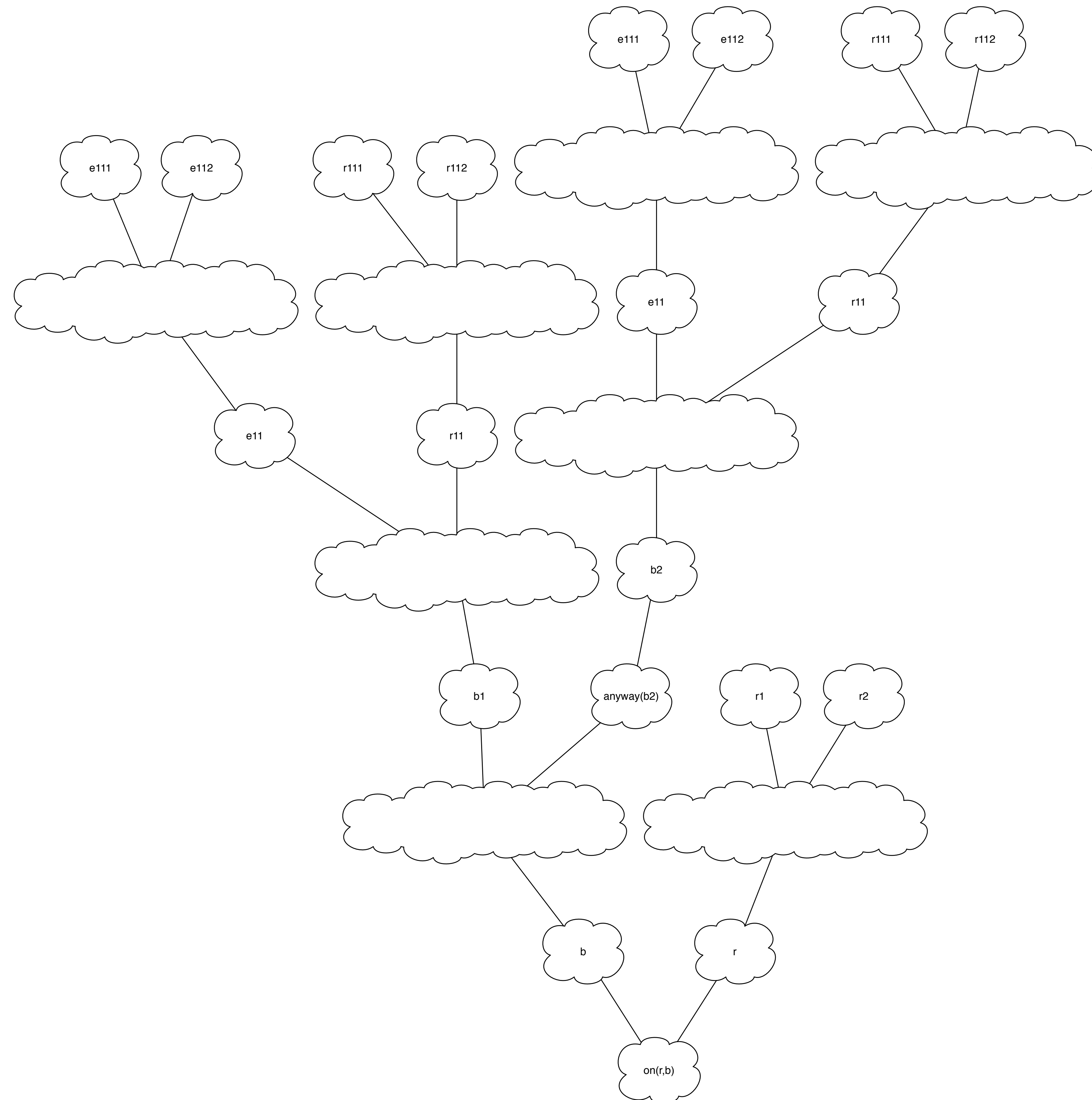


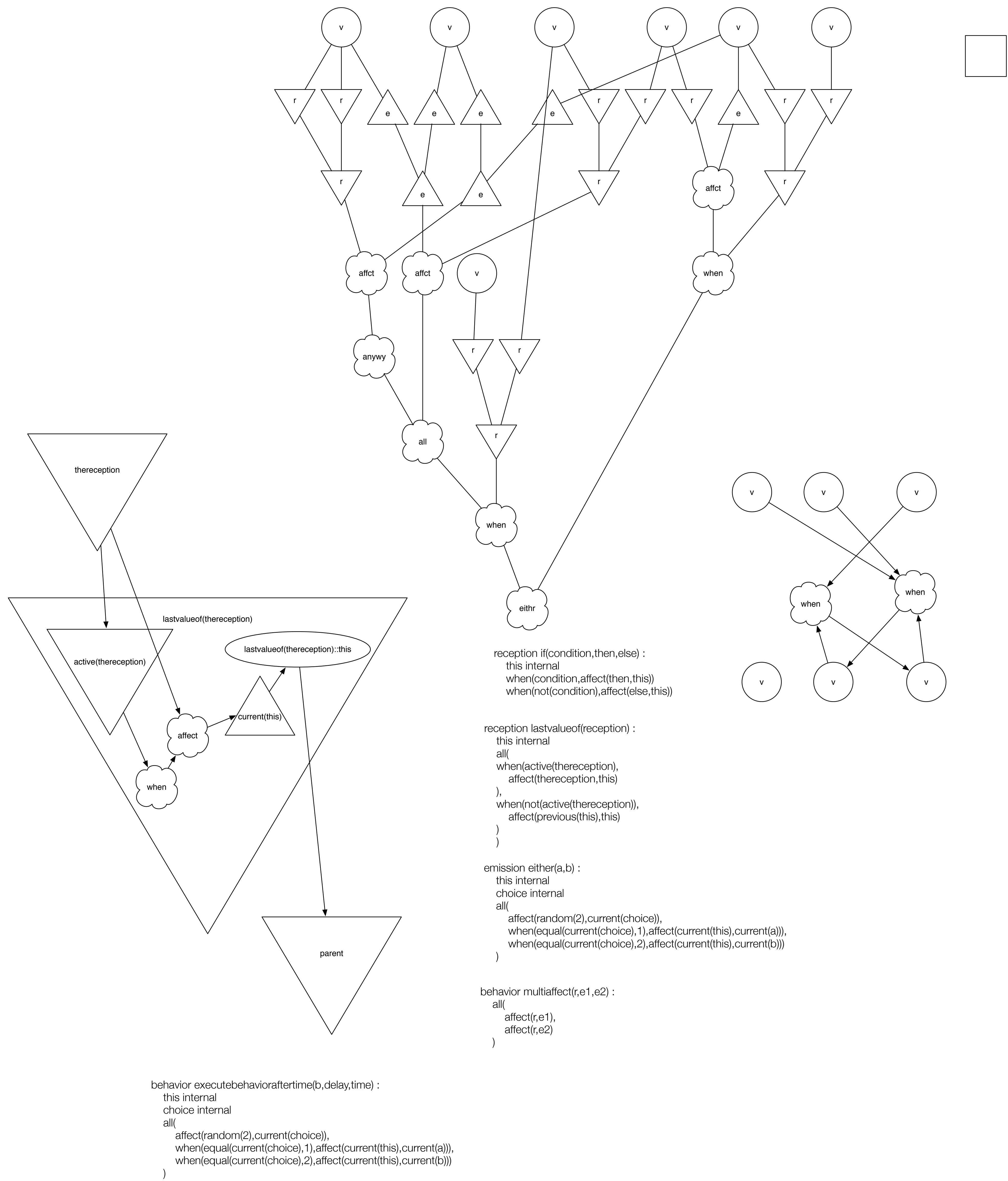
Quand on a plusieurs affectations sur le meme id, il faut prouver avec un solveur SMT que la condition est UNSAT  
 quand il y a un cycle, il faut prouver avec un solveur SMT que la condition de bouclage est UNSAT



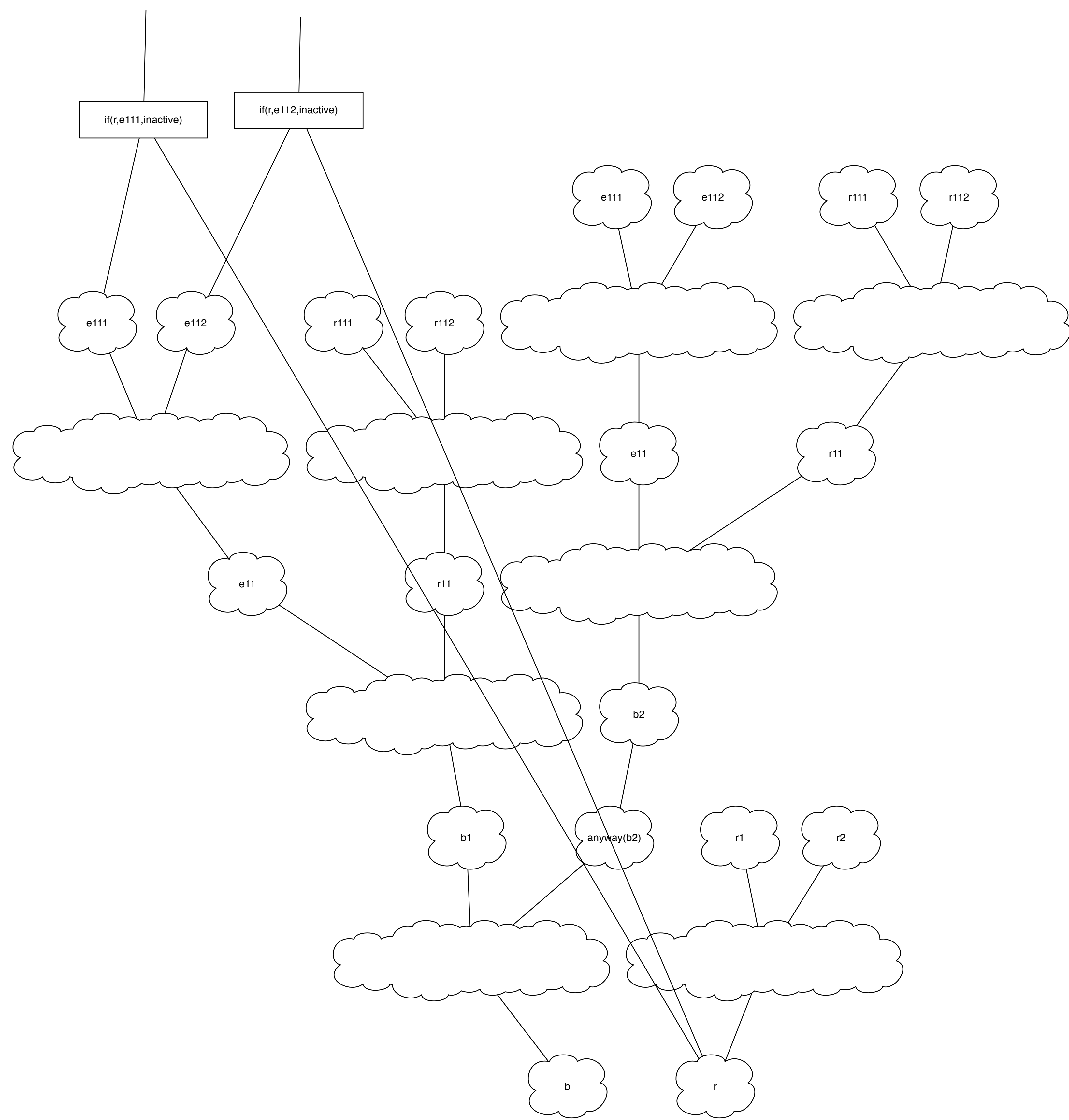
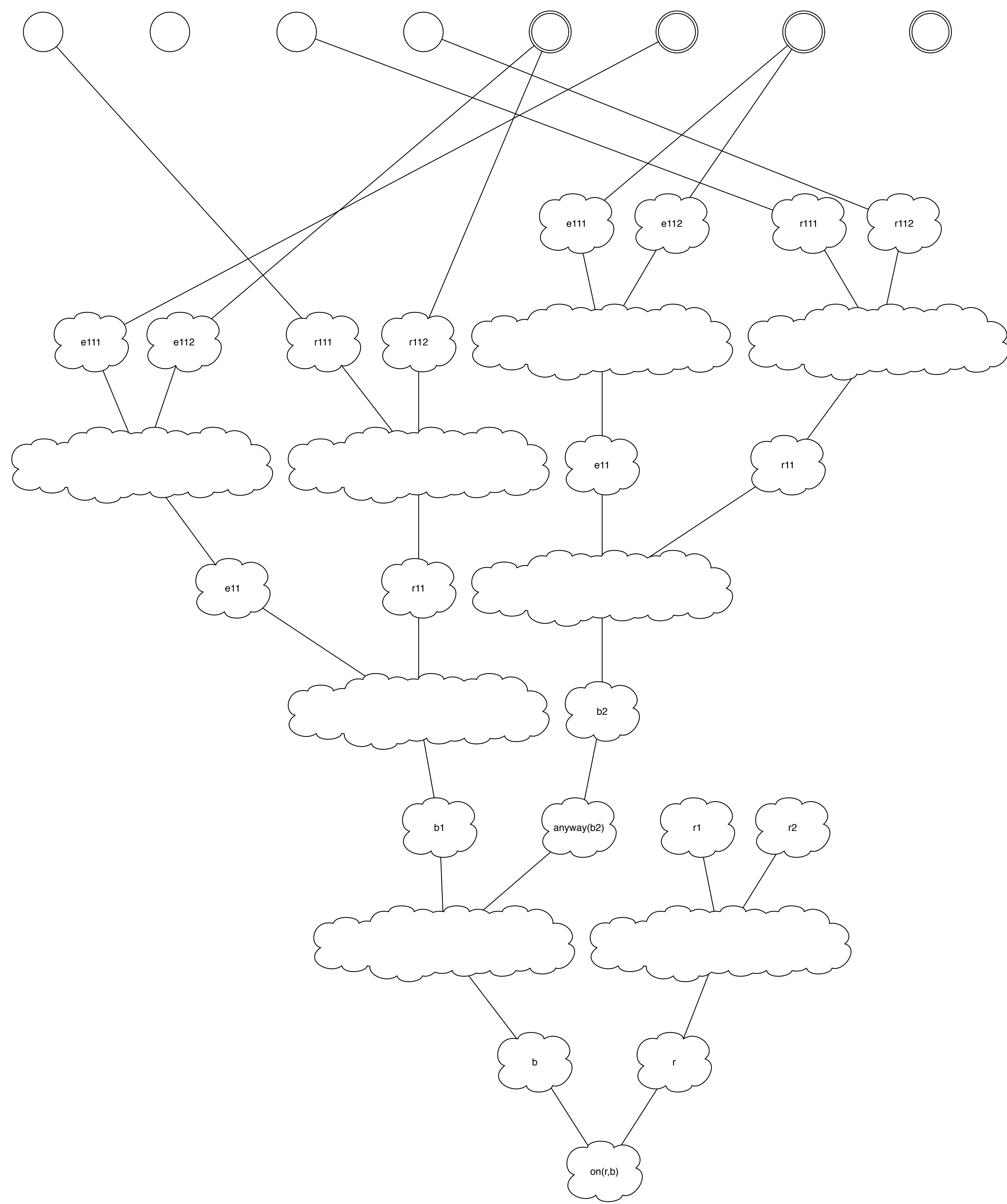


select the only active of the two inputs







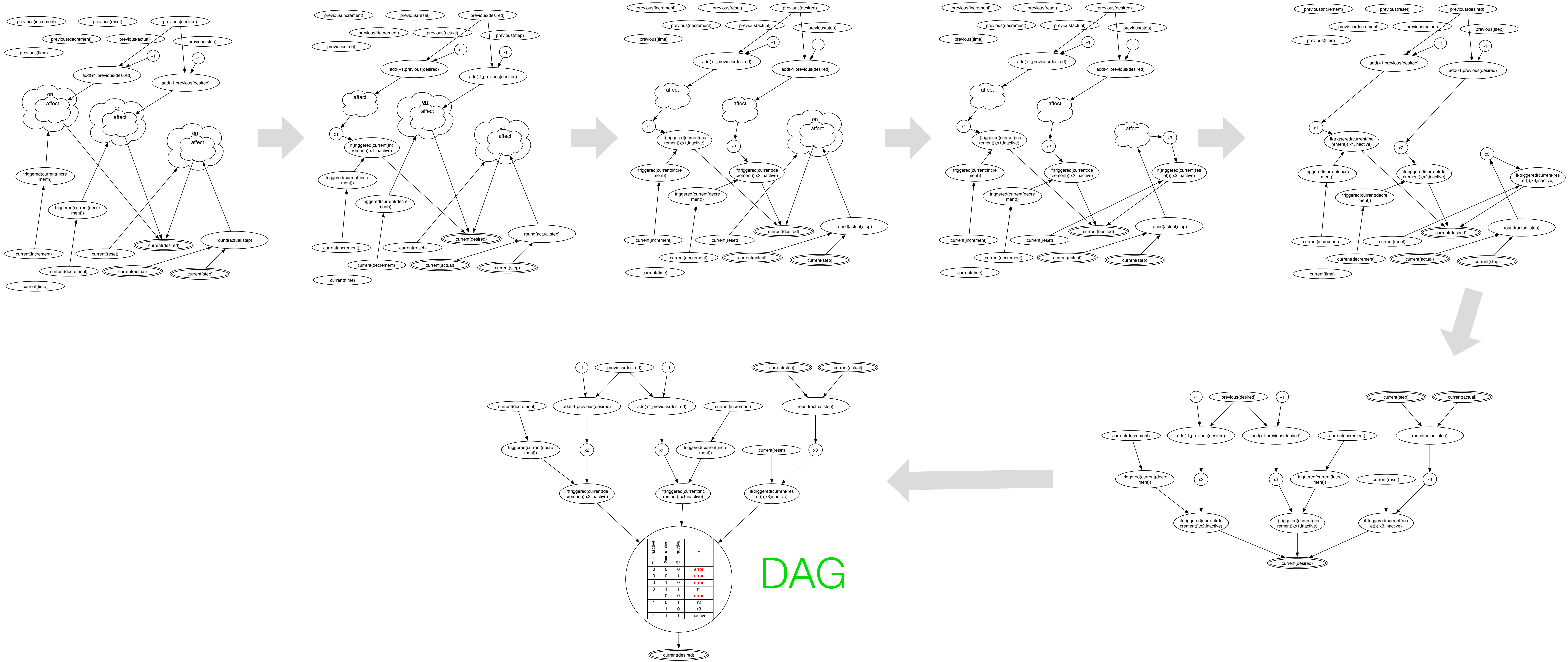




```
increment input
decrement input
reset input
actual output
desired output
step internal

on(triggered(increment),
  affect(add(+1,previous(desired)),current(desired))
)
on(triggered(decrement),
  affect(add(-1,previous(desired)),desired)
)
on(triggered(reset),
  affect(round(actual,step),desired)
)

```

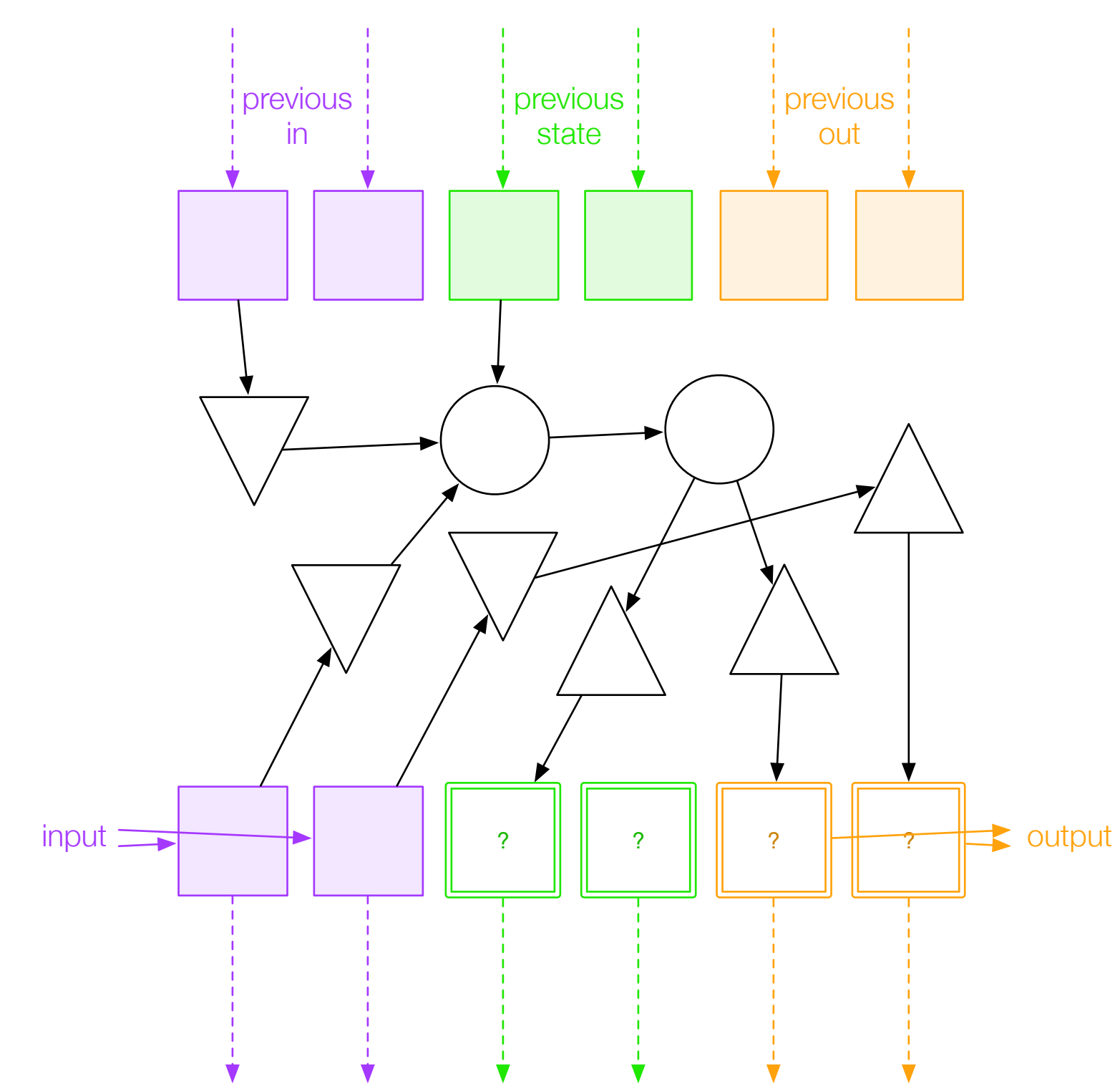
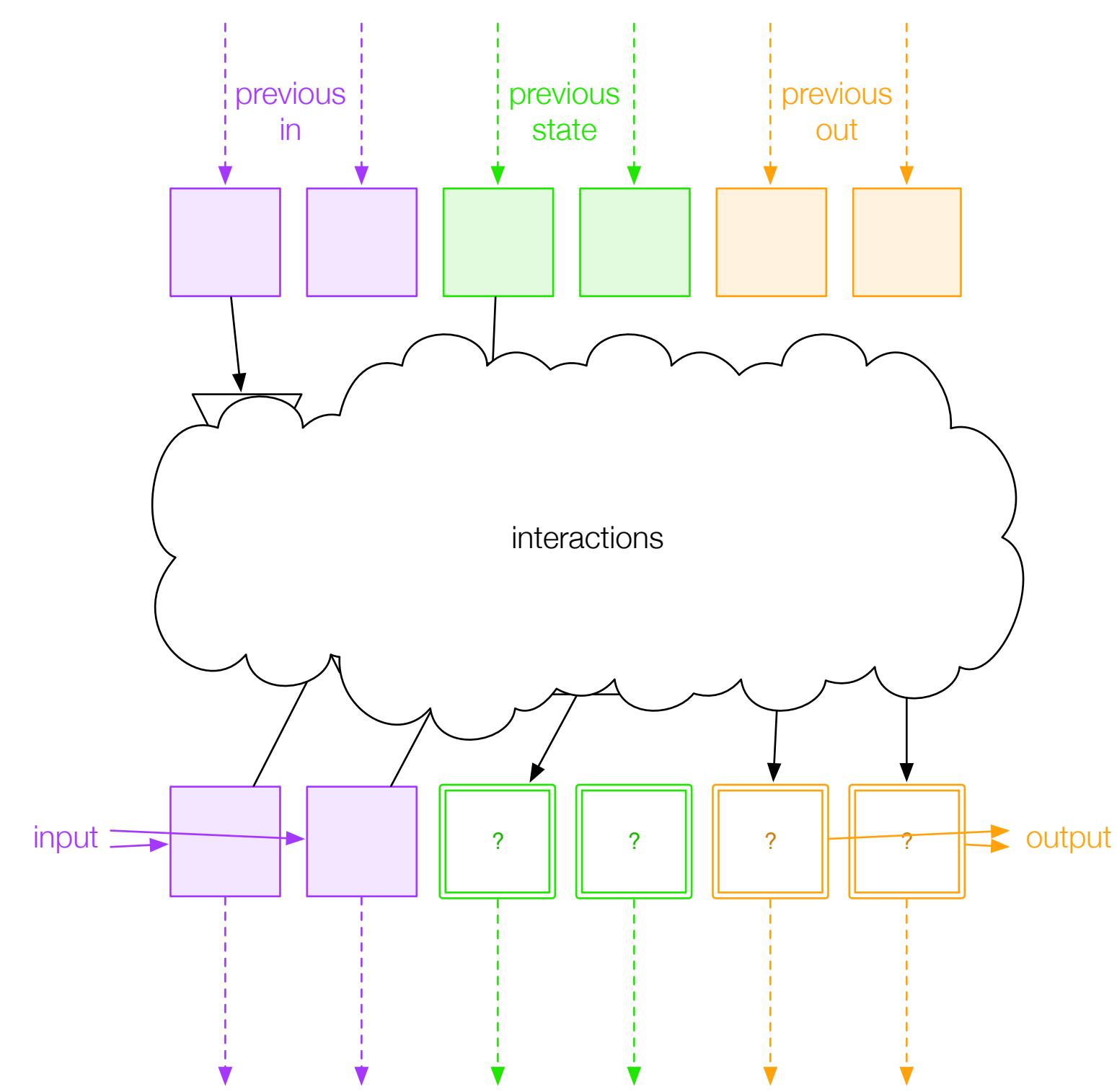
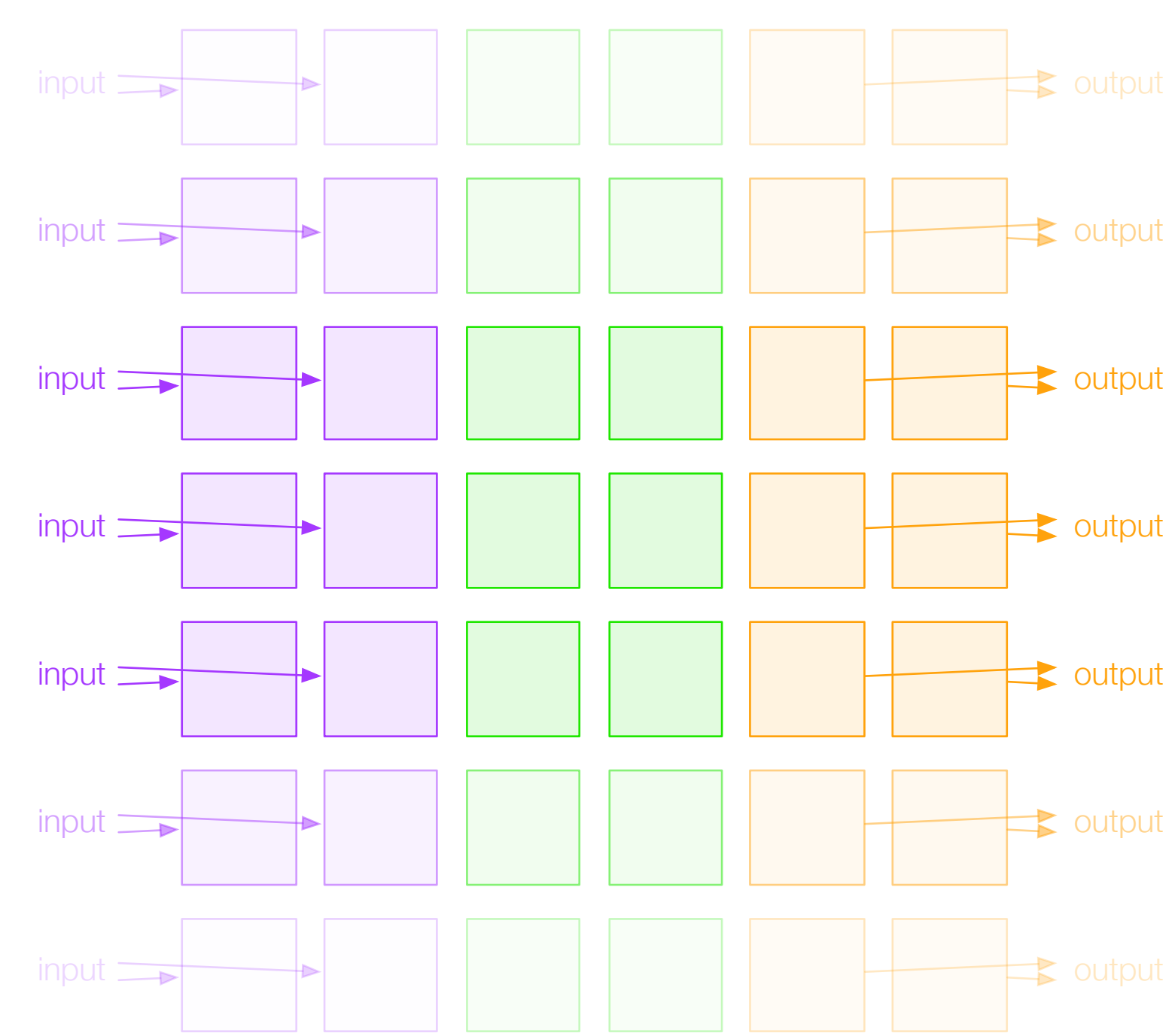


Merge Reception-Emissio-behavior

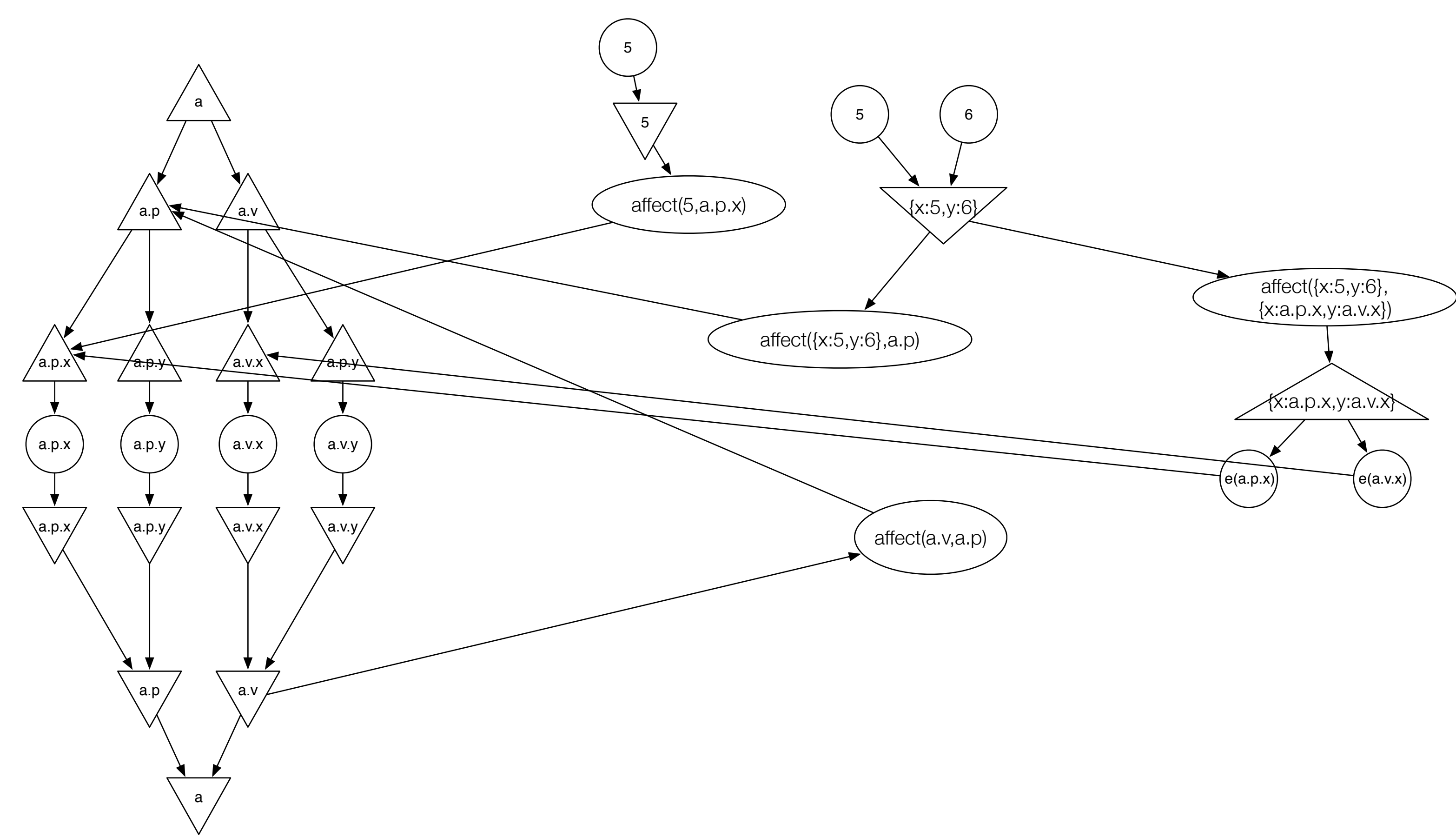
It's all the same thing finally

NO, because we could imagine receptions with side effects for example.

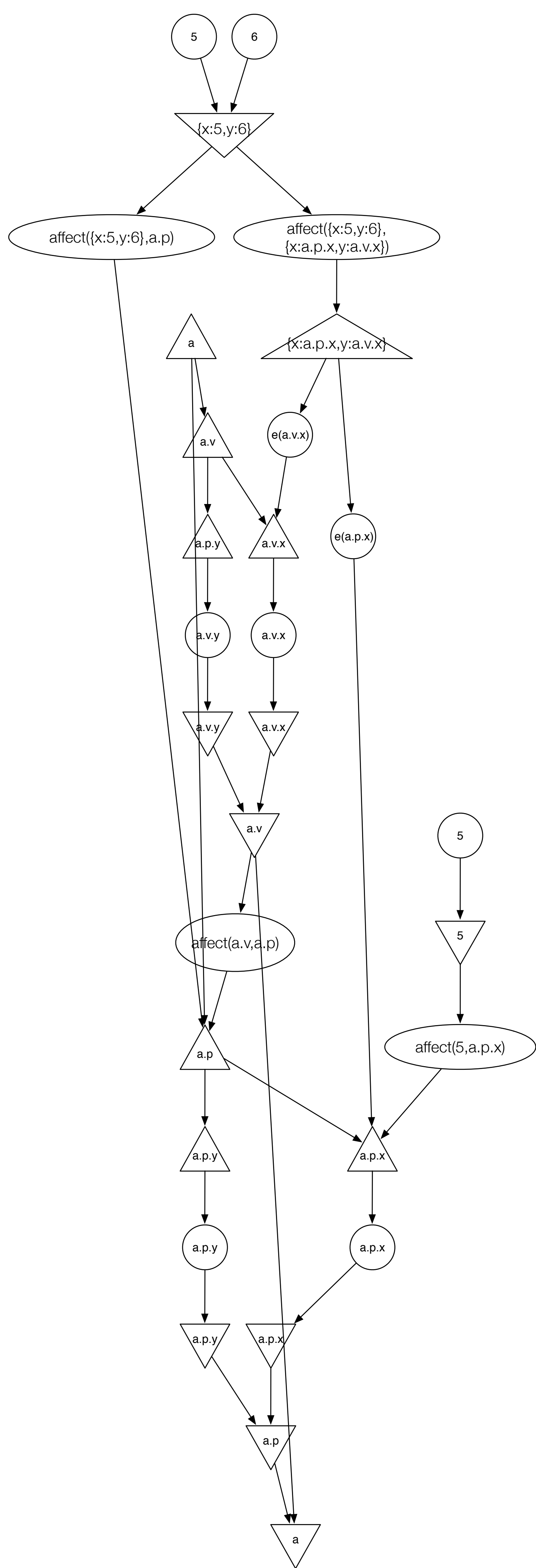
AND this would be wrong, because a reception with a side effect is misleading

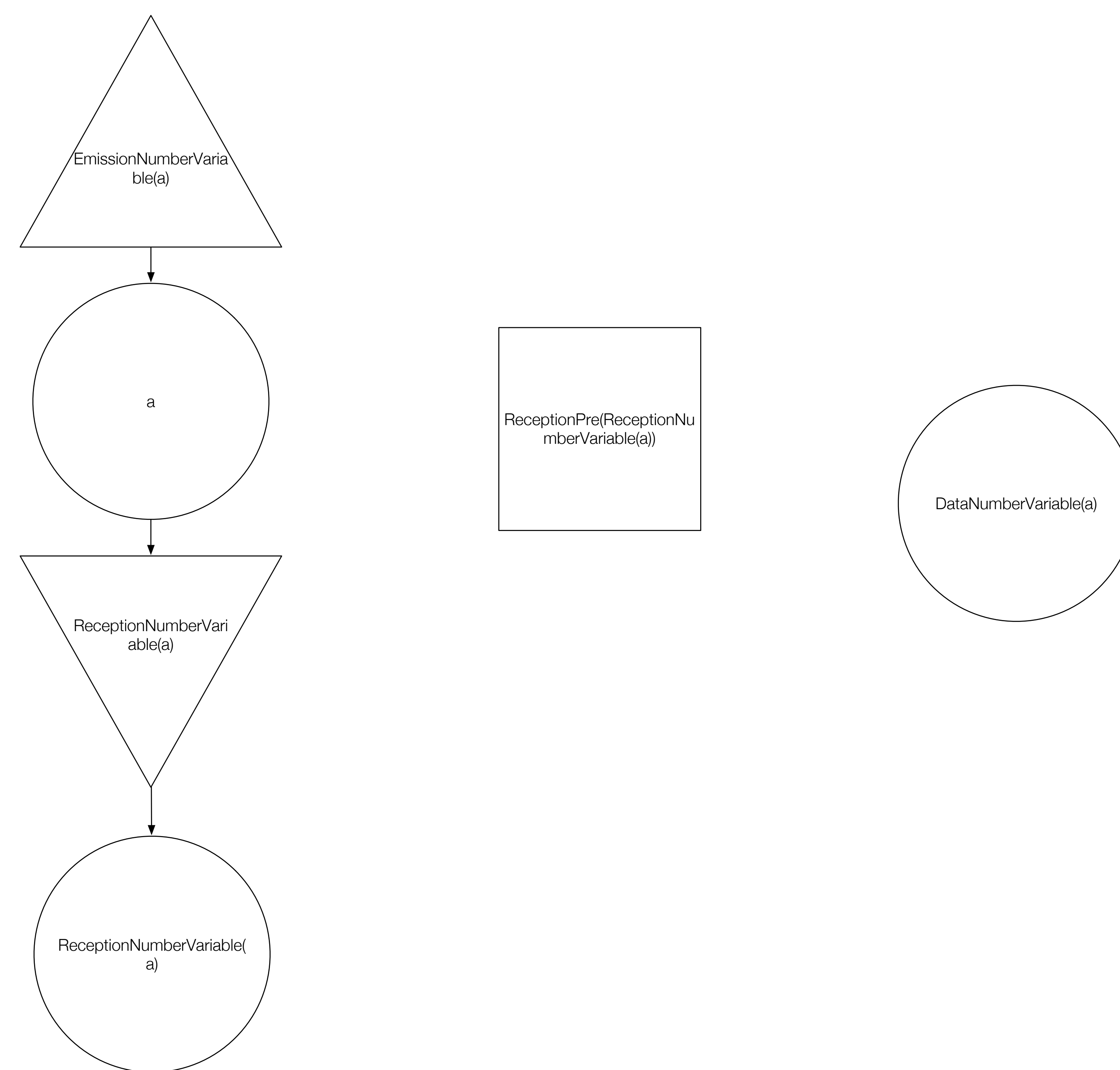


Composed data types :  $a = \{p: \{x: \text{Number}, y: \text{Number}\}, v: \{x: \text{Number}, y: \text{Number}\}\}$





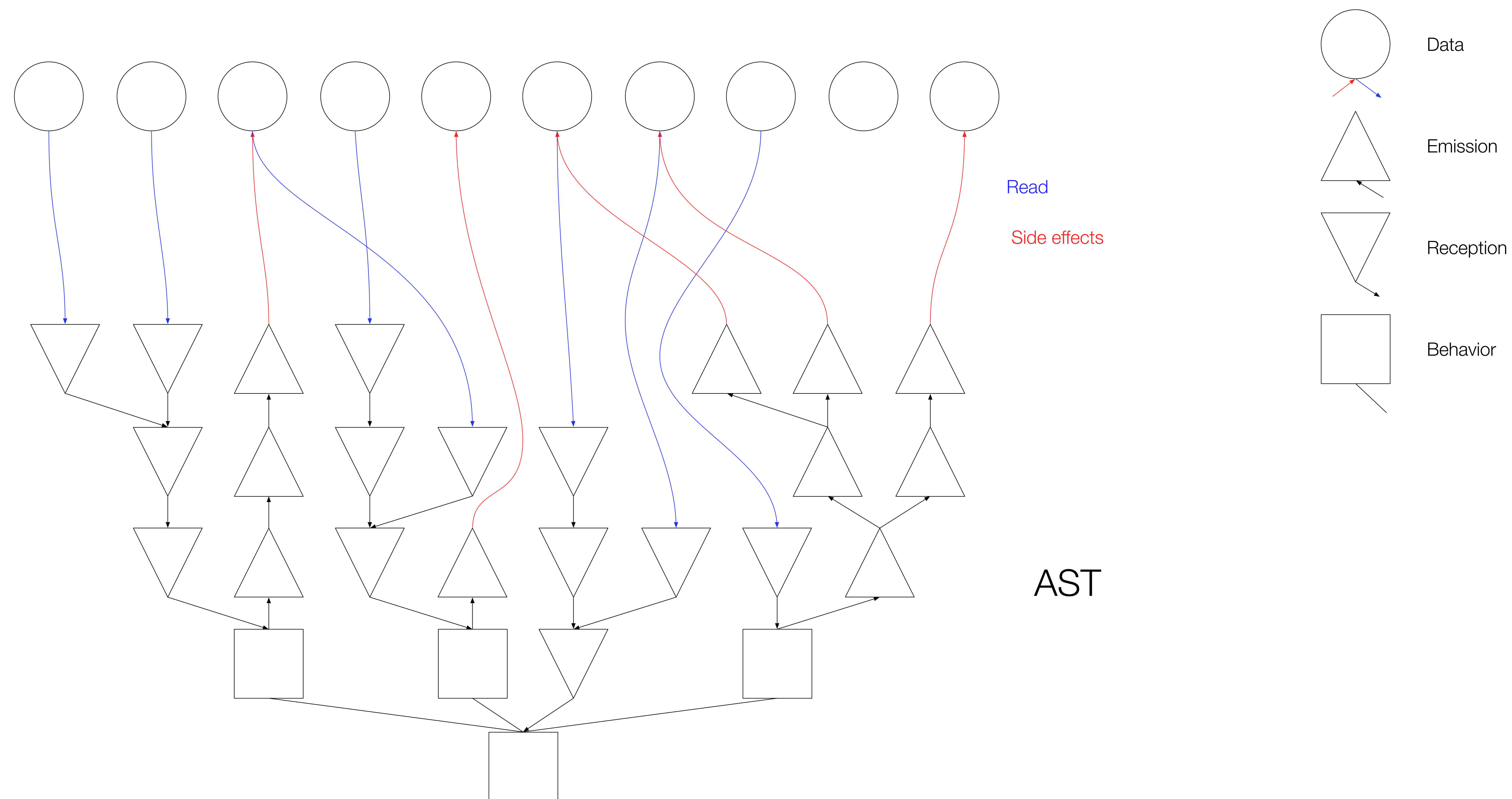




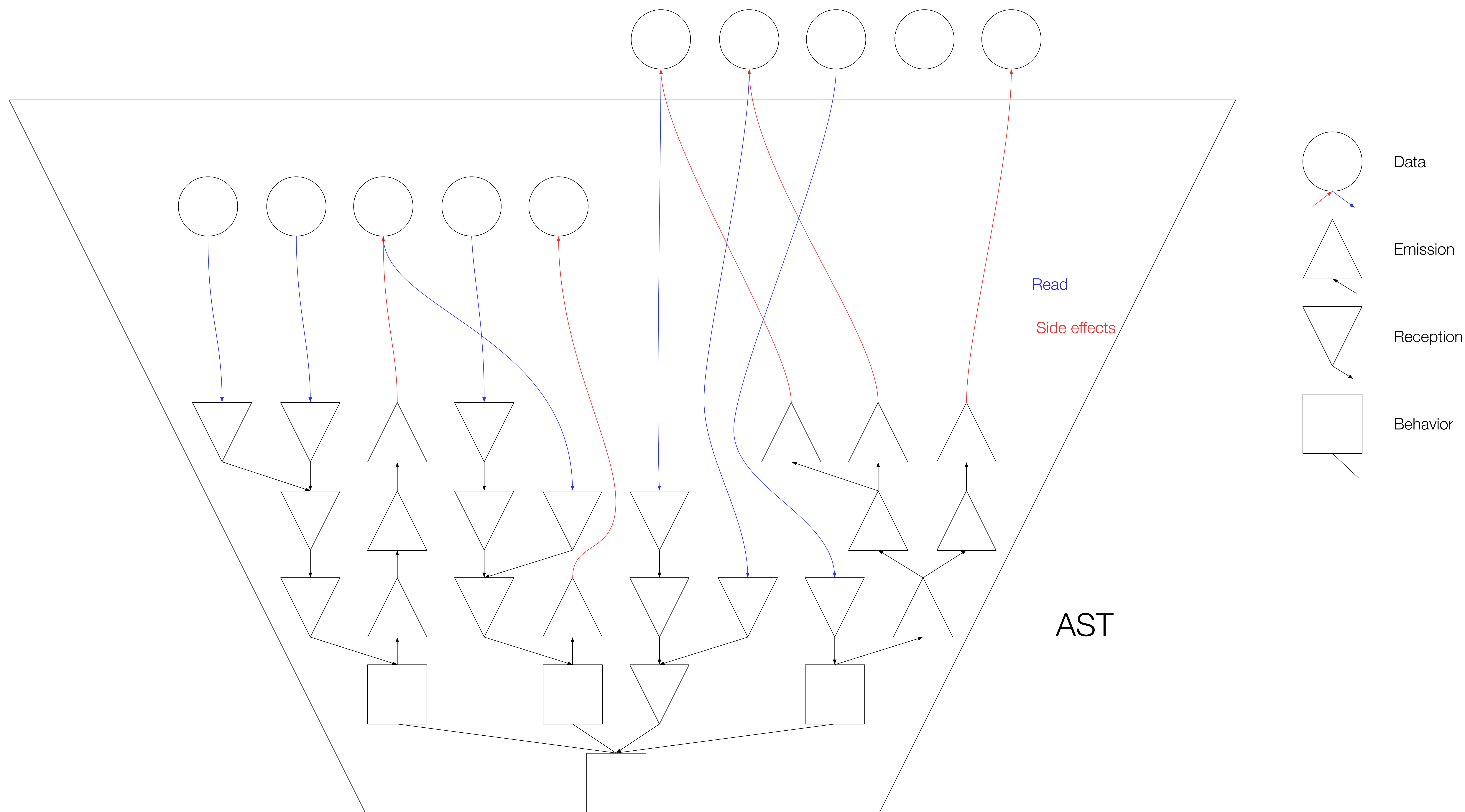
Data -> iii

Computation -> custom iii receptions

Interaction -> iii



- 1 - Unfold custom interactions receptions and emissions
- 2 - Eliminate whens
- 3 - Eliminate anyways
- 4 - Eliminate alls



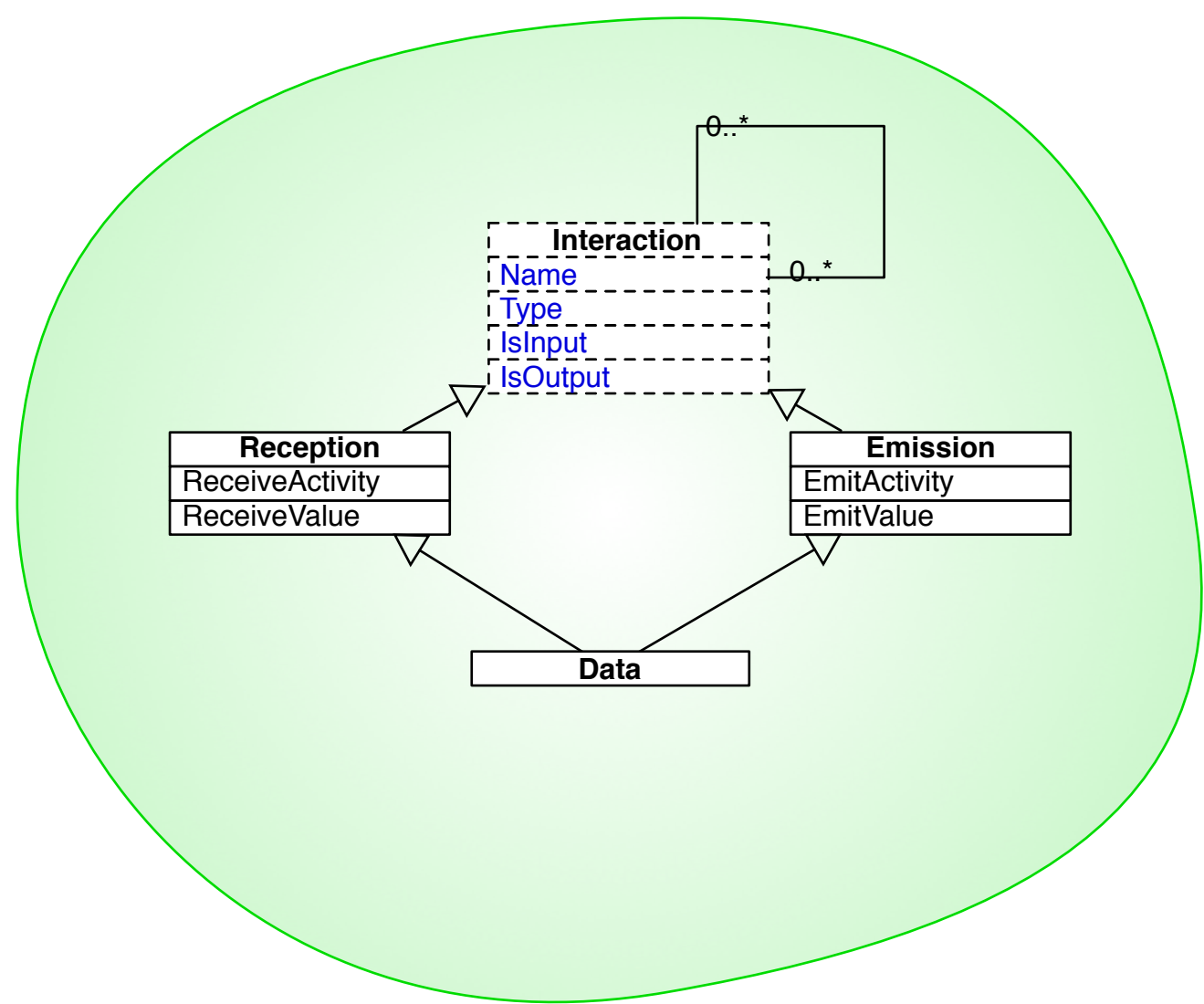
- 1 - Unfold custom interactions receptions and emissions
- 2 - Eliminate whens
- 3 - Eliminate anyways
- 4 - Eliminate alls

ACTIVE FOR ALL ! NOT for the data, but for the actual NODES



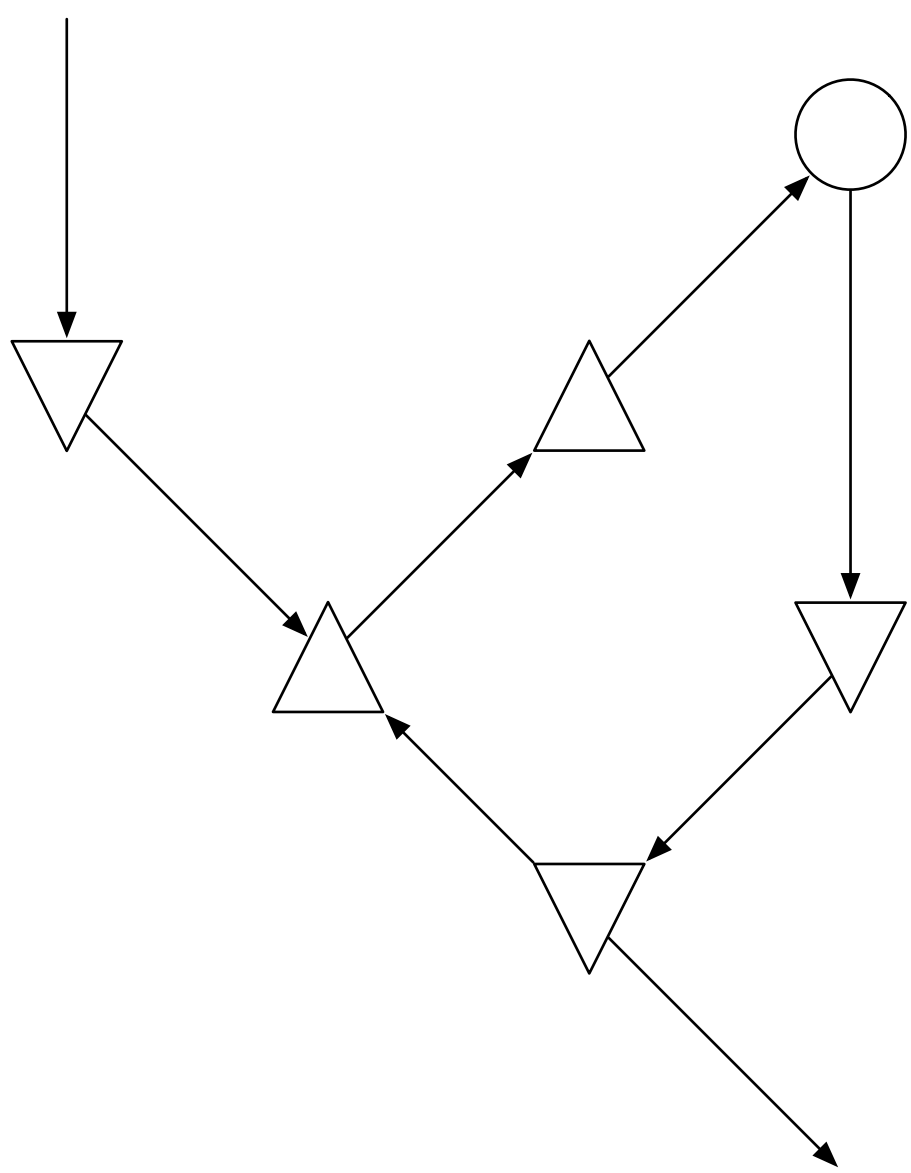
Activity for input = input received  
Activity for output = we send this output  
activity for variable = this thing is defined  
activity for behaviour = execute this now

Unified into node activity



```
emission affectOrFlow(data b):
  affect(
    if(active(this),this,previous(b)),
    b
  )
```

```
void emission affectAfterDelay(time reception delay,reception source, emission destination):
  when(this,
    all(
      affect(firstActive(source,previous(local.value)),local.value),
      affect(firstActive(time,previous(local.time)),local.time),
      anyway(
        when(becameTrue(moreThan(time,add(local.time,delay))),
          affect(local.value,destination)
        )
      )
    )
  )
```



```
boolean reception becameTrue(boolean reception condition) :
  and(condition,not(previous(condition)))
```

```
void reception flow(data a,reception newA):
  affect(if(active(newA),newA,previous(a)),a)
```

```
when(conditionMet(equals(mode,1)),
  all(
    triggerEventsOfQueue(thequeue),
    when(click,
      all(
        addEventToQueue(thequeue,counter),
        affect(add(1,previous(counter)),newcounter),
        anyway(flow(counter,newcounter))
      )
    )
  )
)
```

```
<type> emission flow(<type> data target):
  affect(
    if(active(emitted),emitted,previous(target)),
    target
  )
```

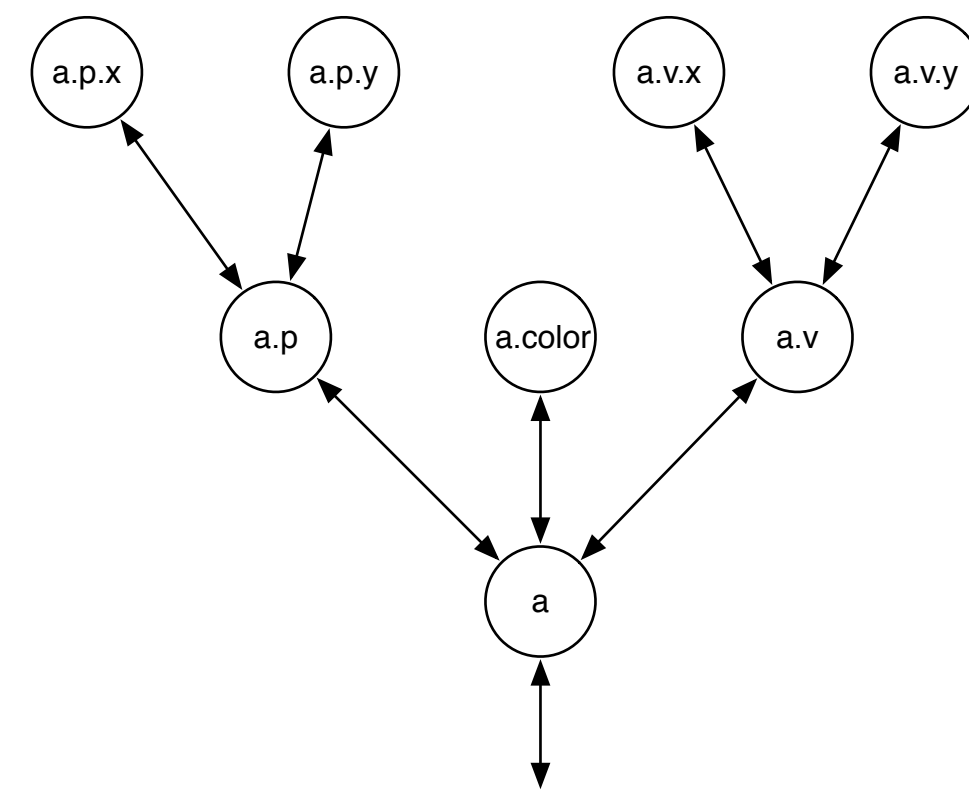
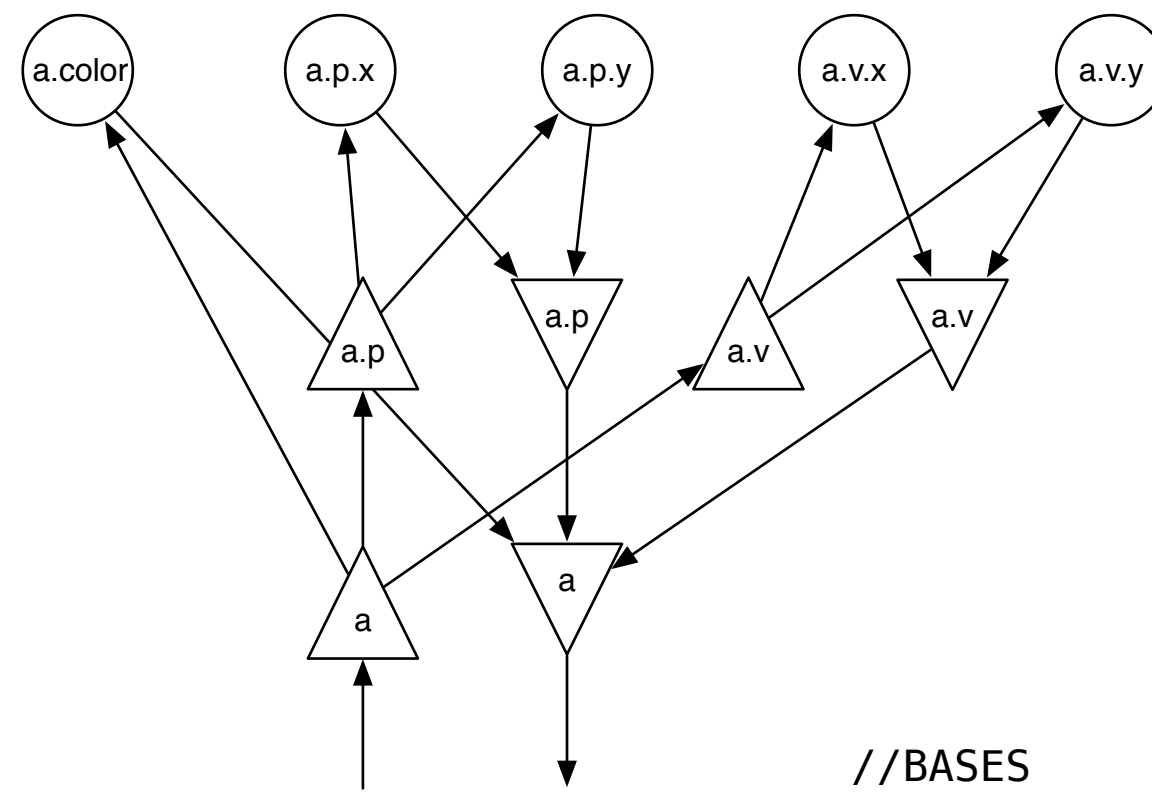
```
mark data mark(color data color, point data p,point data v):
  when(emitted.color,affect(emitted.color,color))
  when(emitted.p,affect(emitted.p,p))
  when(emitted.v,affect(emitted.v,v))

point data point(number data x, number data y):
  when(emitted.x,affect(emitted.x,x))
  when(emitted.y,affect(emitted.y,y))

when(color,affect(color,received.color))
when(p,affect(p,received.p))
when(v,affect(v,received.v))
when(x,affect(x,received.x))
when(y,affect(y,received.y))
```

```
number reception incDec(
  void reception inc, void reception dec, number reception step,
  number reception min, number reception max, number reception actual ) :

  all(
    when(increment,
      affect(add(previous(this),step),desired)
    ),
    when(decrement,
      affect(sub(previous(this),step),desired)
    ),
    when(reset,
      affect(round(actual,step),desired)
    ),
    affect(crop(desired,min,max),this)
  )
```



```
//BASES
void emission all()

void emission when(void reception activation, void emission do)

reception if(boolean reception if, reception then, reception else)

text data text(identifier)

number data number(identifier)

boolean data boolean(identifier)
```

```
void emission affect(<type> reception source, <type> emission destination)

<type> emission all(<type> emission interactions...)

<type> emission either(<type> emission interactions...)

void emission when(void reception activation, void emission interaction)

void emission anyway(void emission interaction)

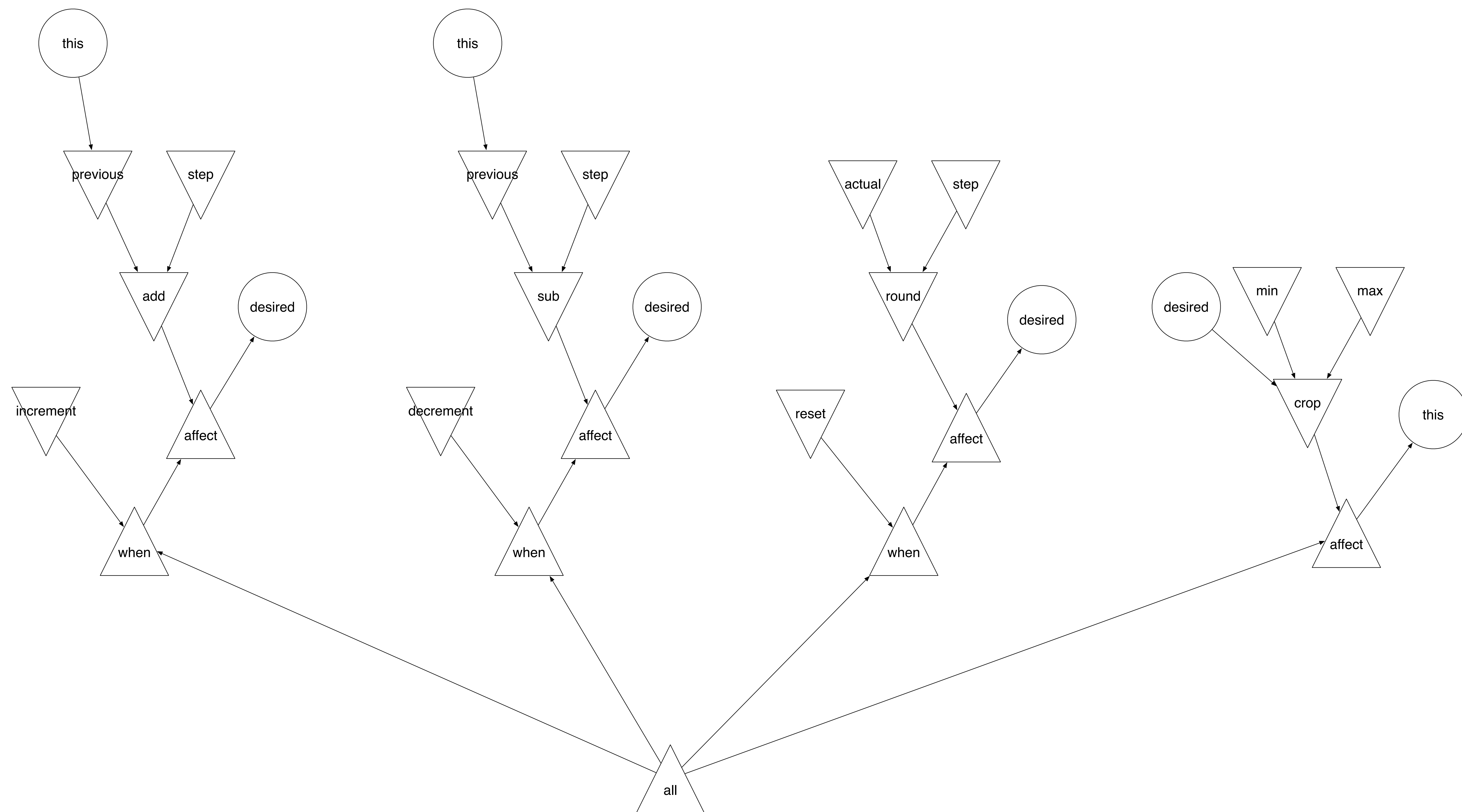
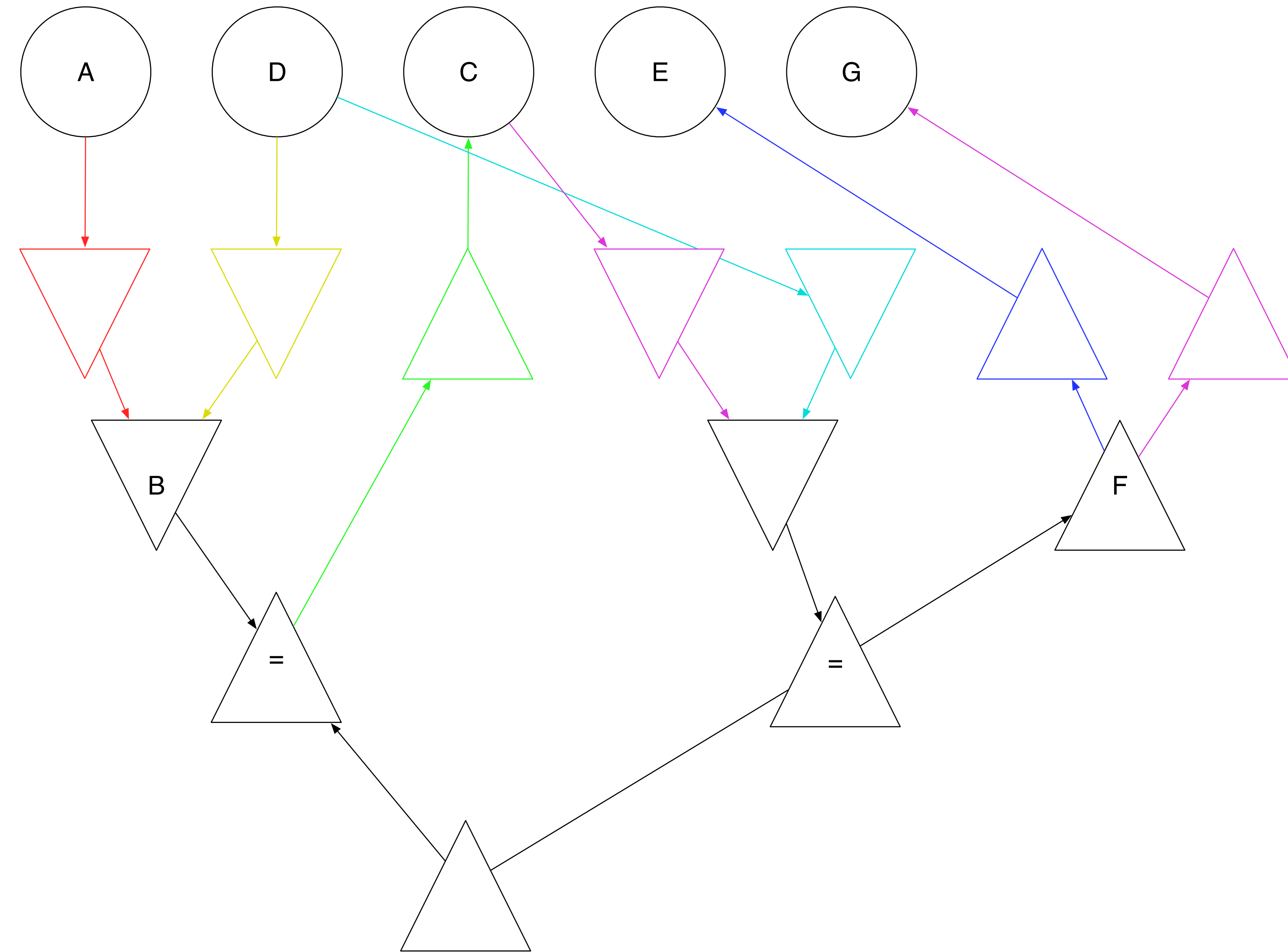
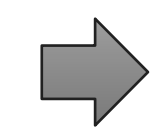
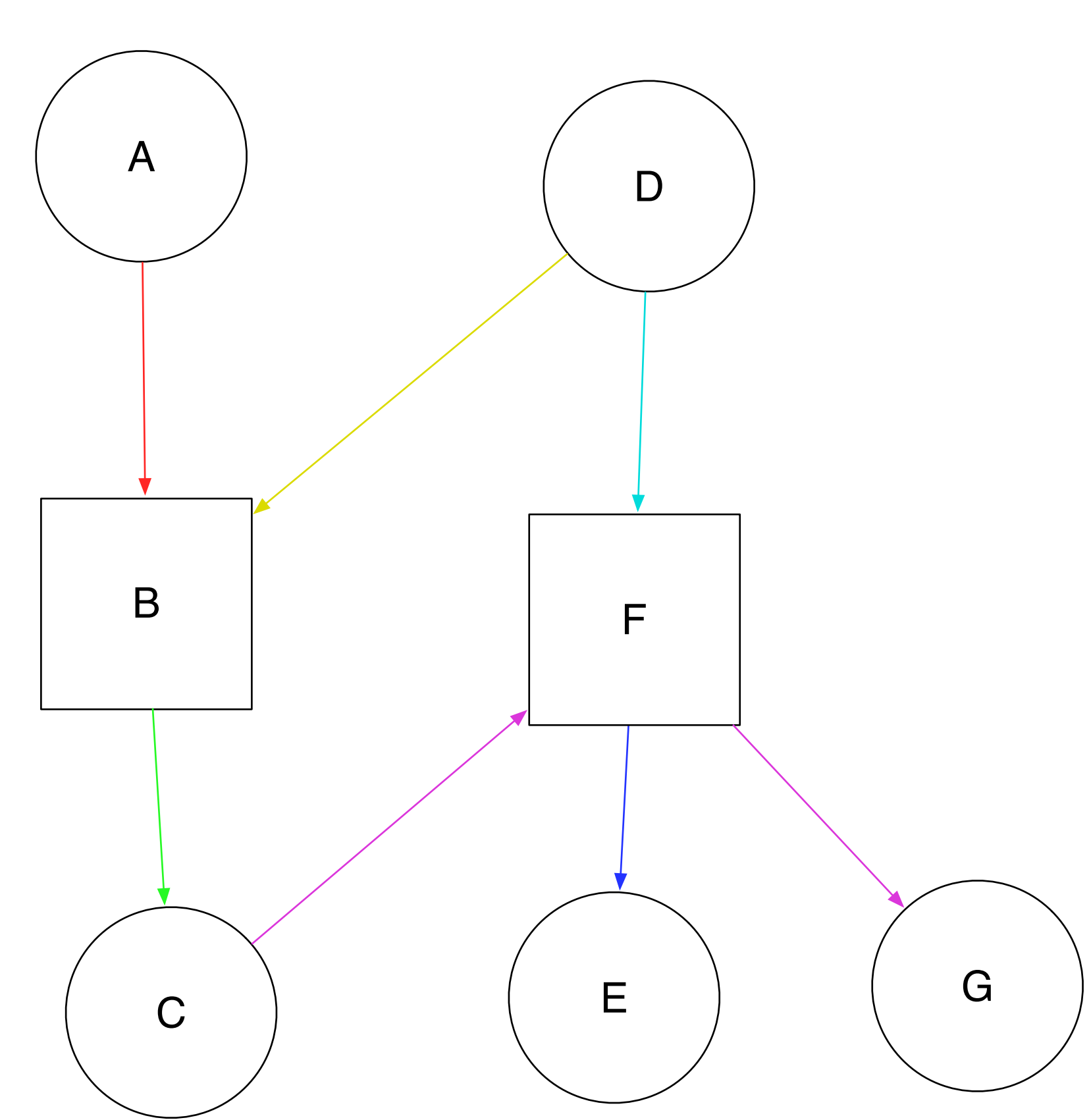
void emission doNot(void emission interaction)

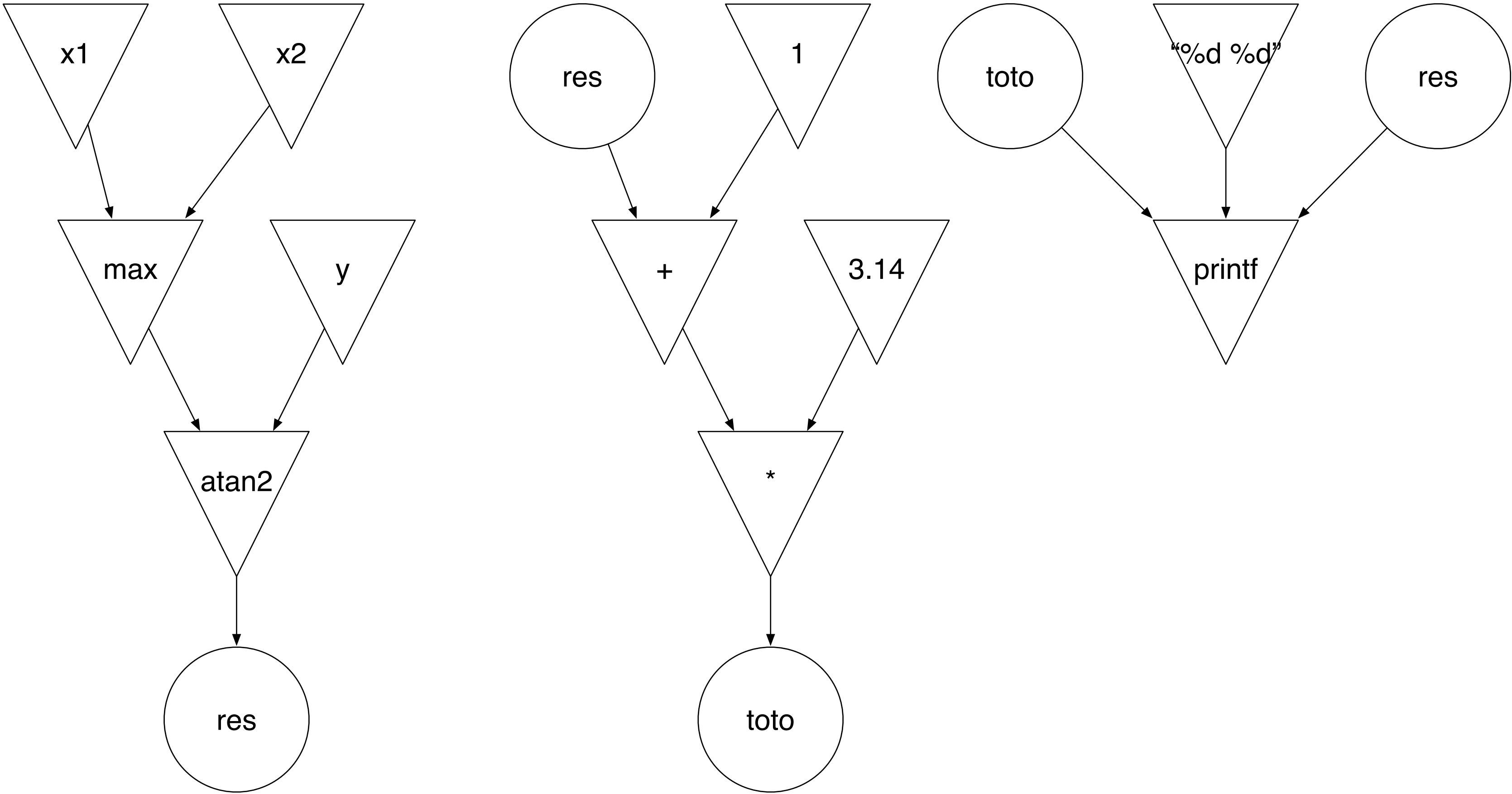
void reception isTrue(boolean reception value)

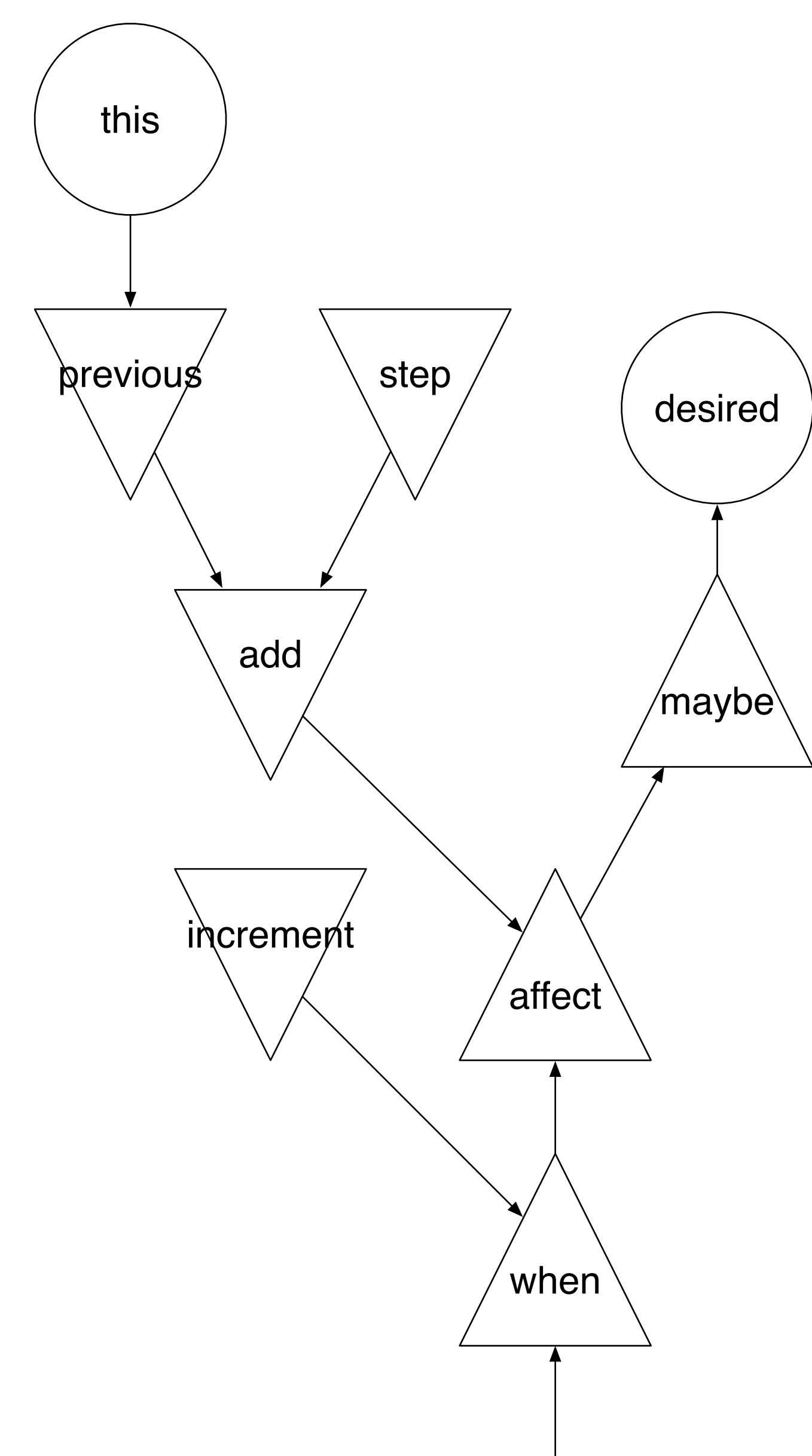
<type> reception previous(<type> reception value)

boolean reception not(boolean reception value)

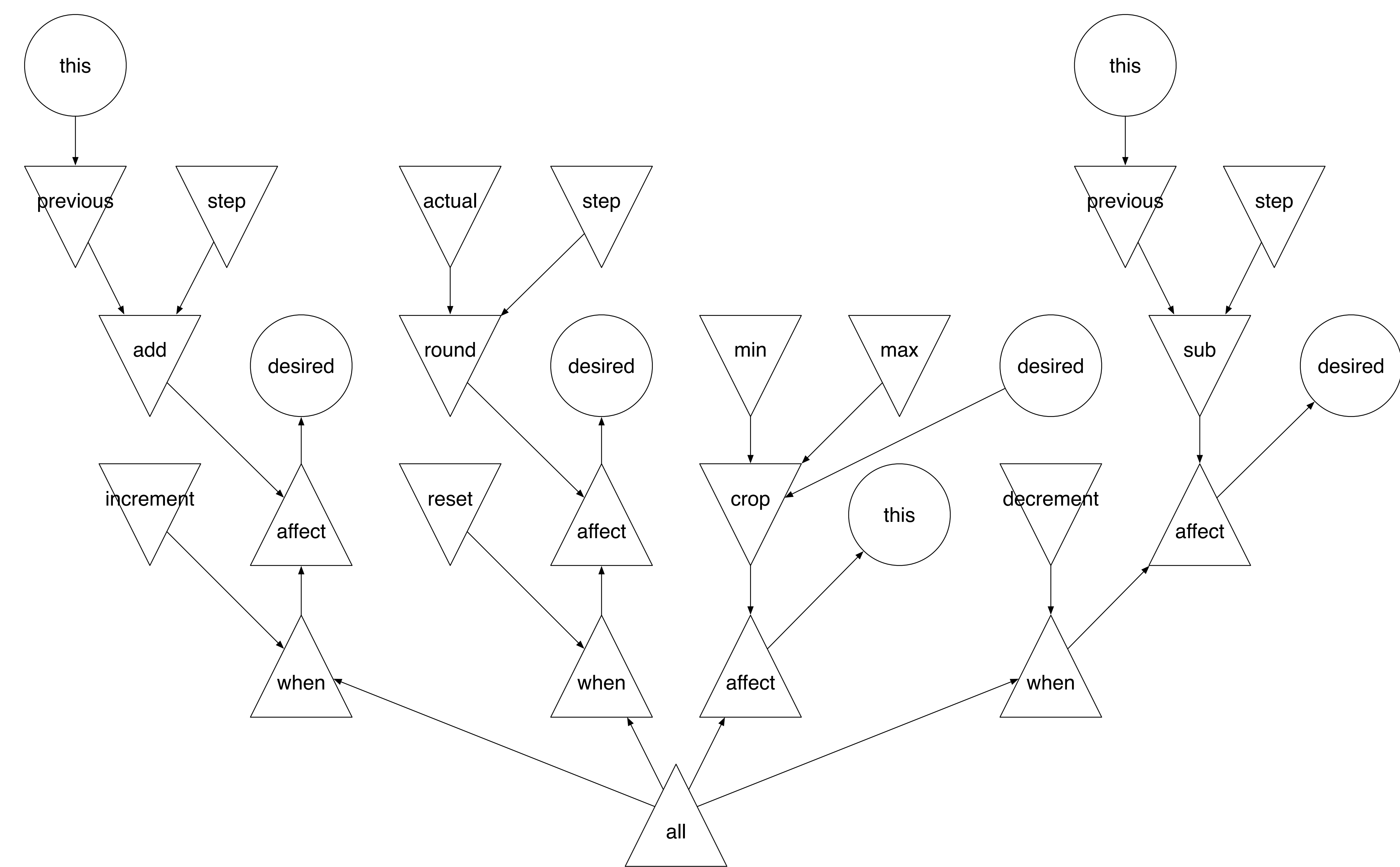
<type> reception if(boolean reception if, <type> reception then, <type> reception else)
```

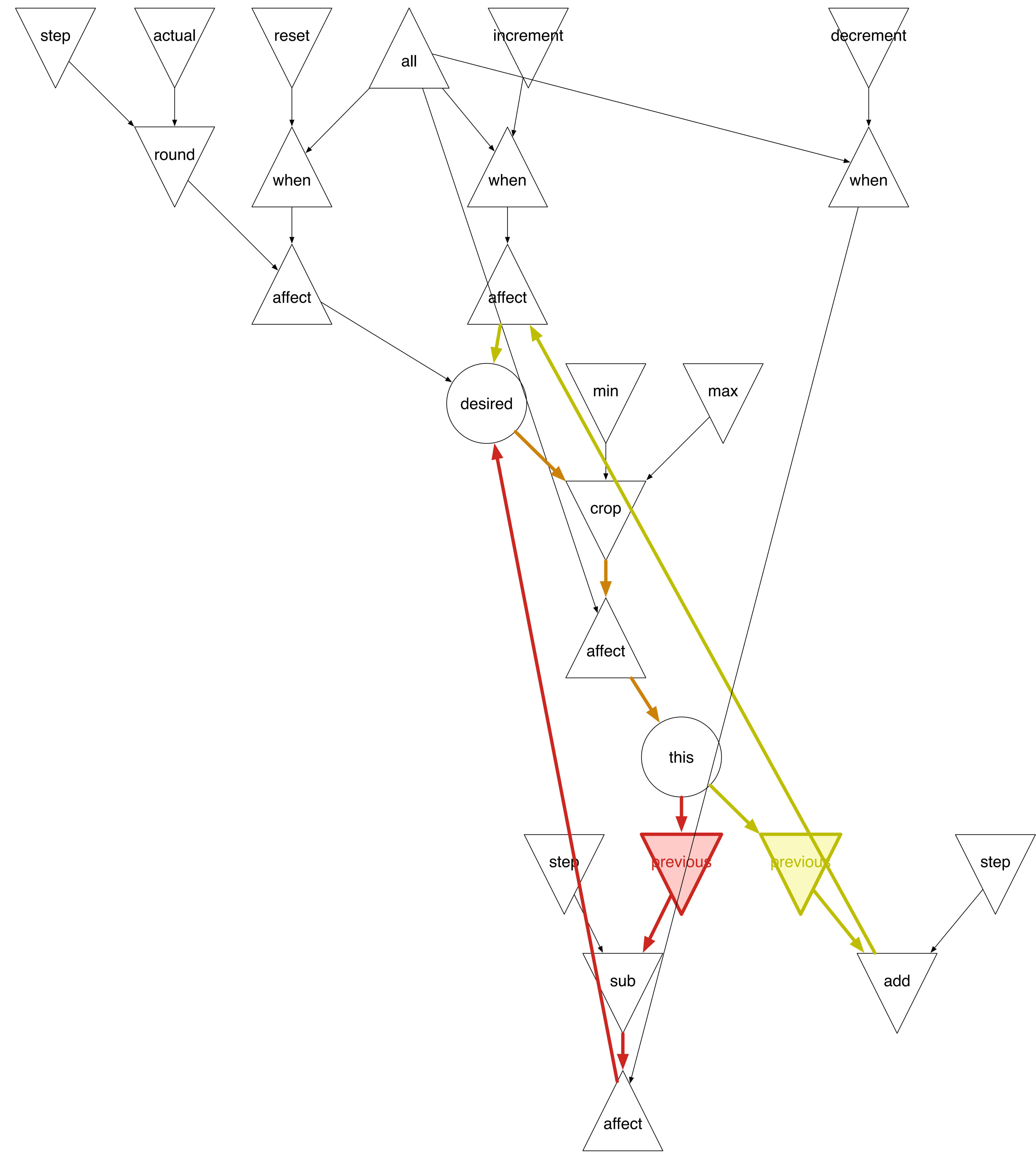


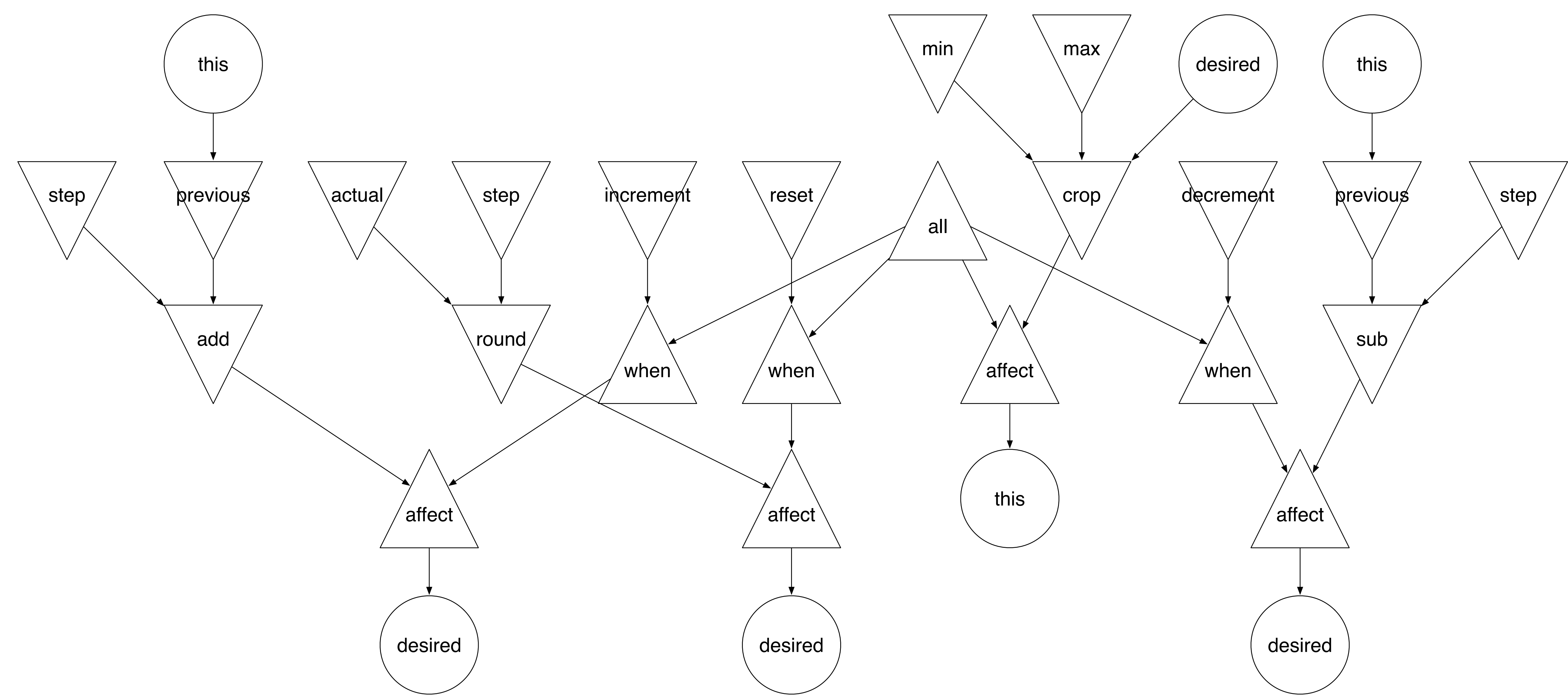


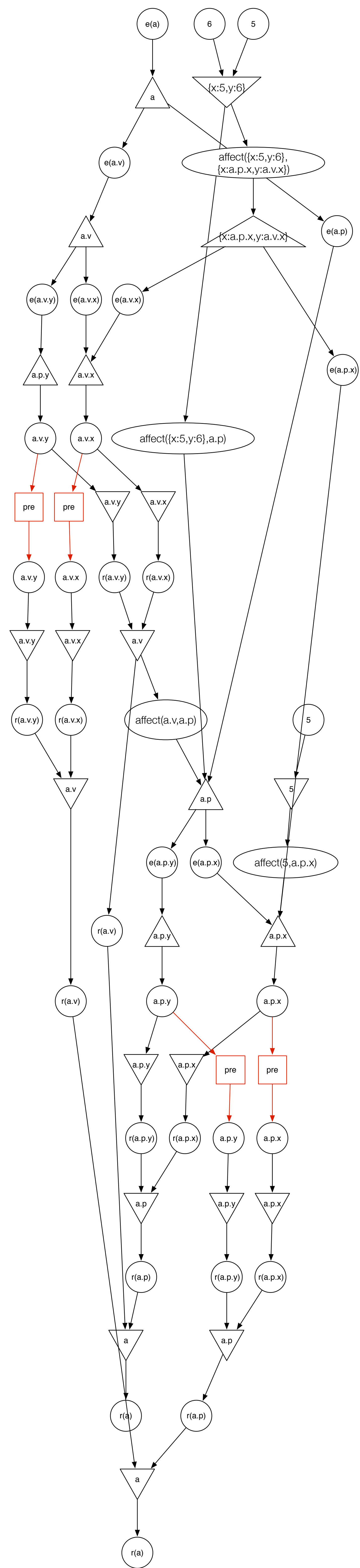




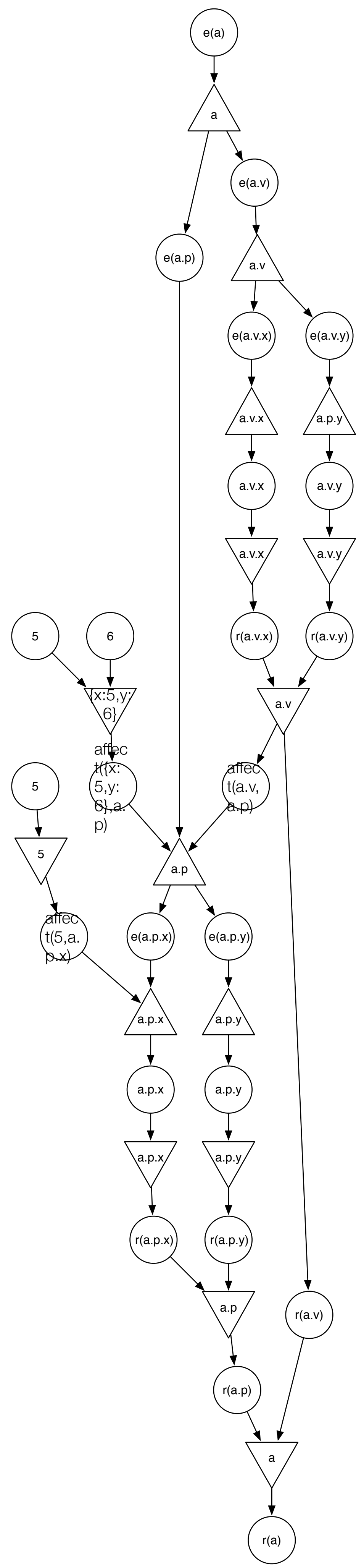




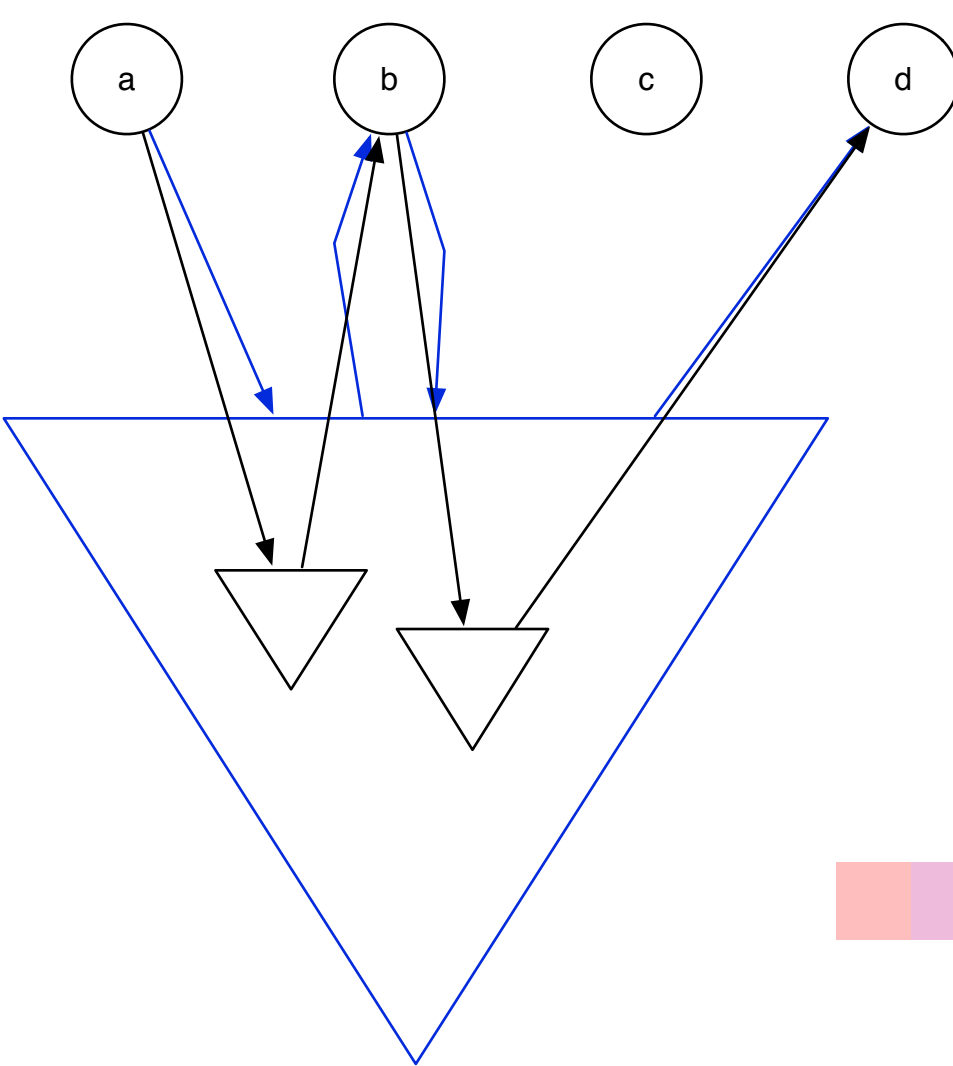






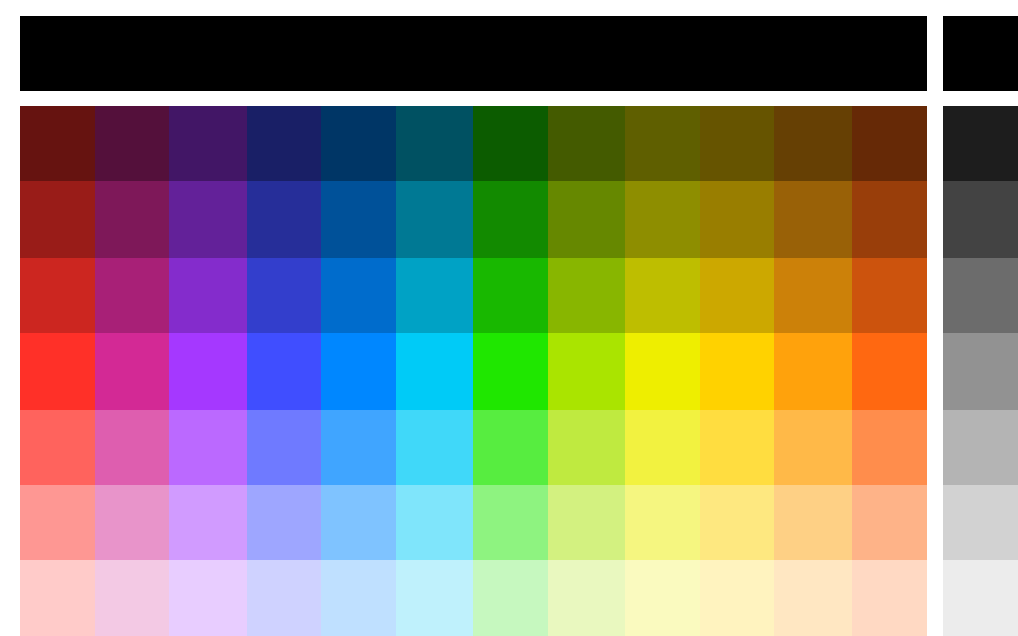
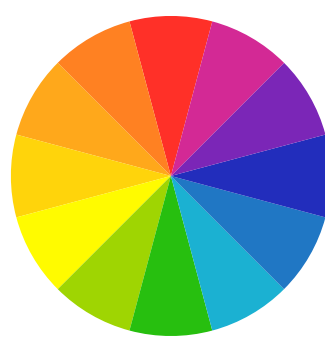
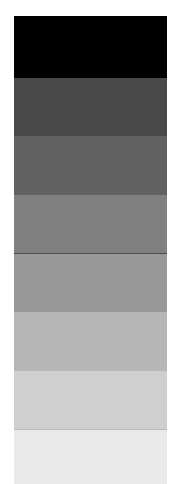
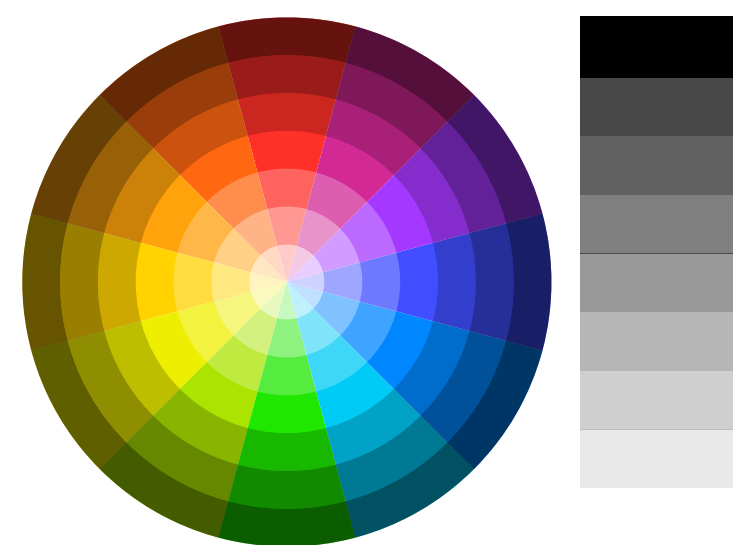
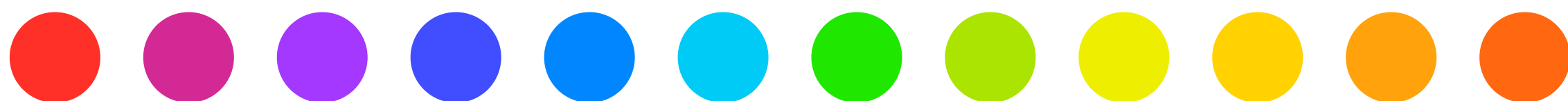
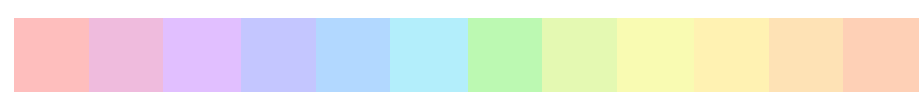


Pathologic



cycle when folded

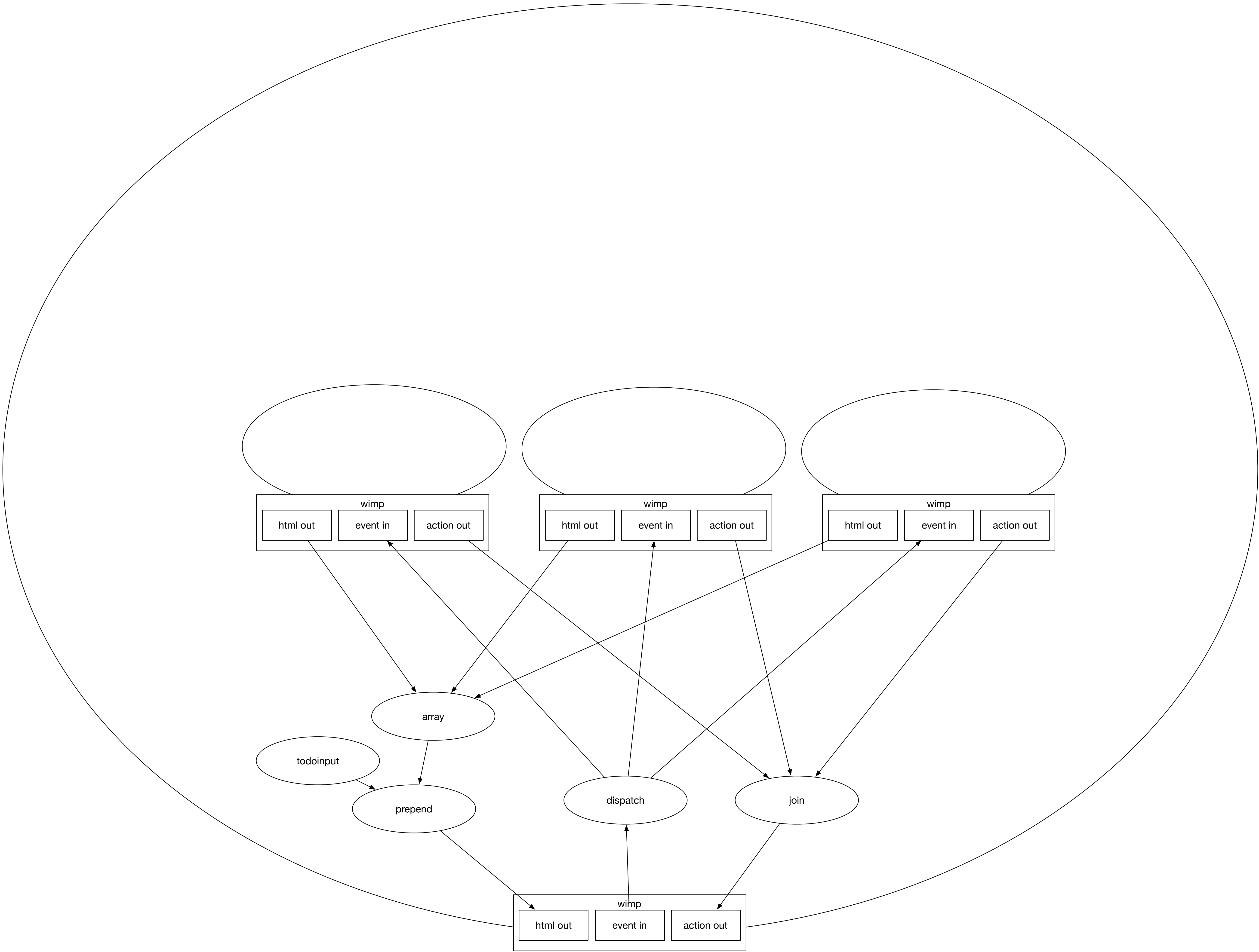
nocycle when unfolded



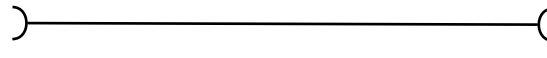
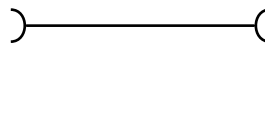
Duck typing

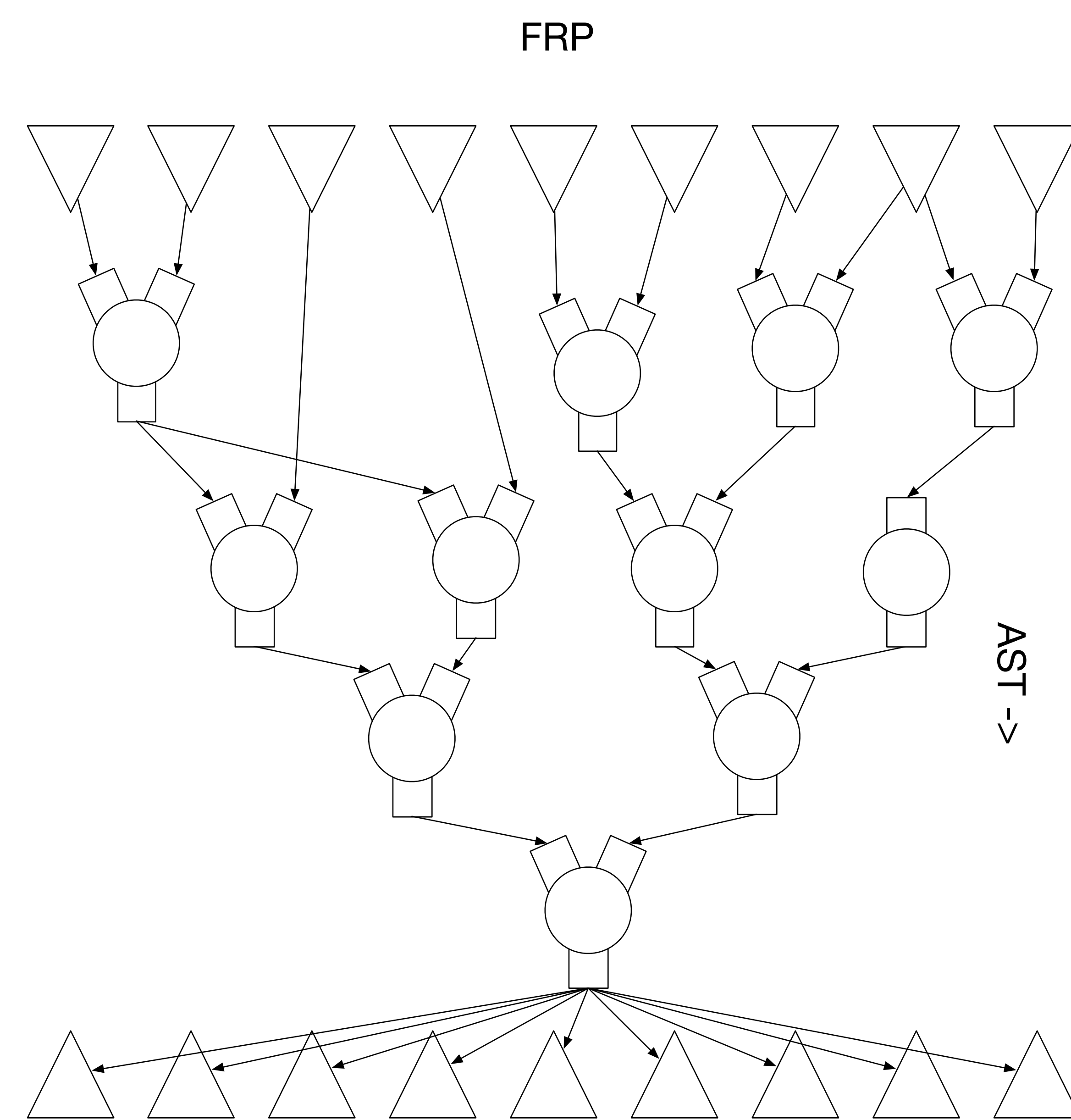
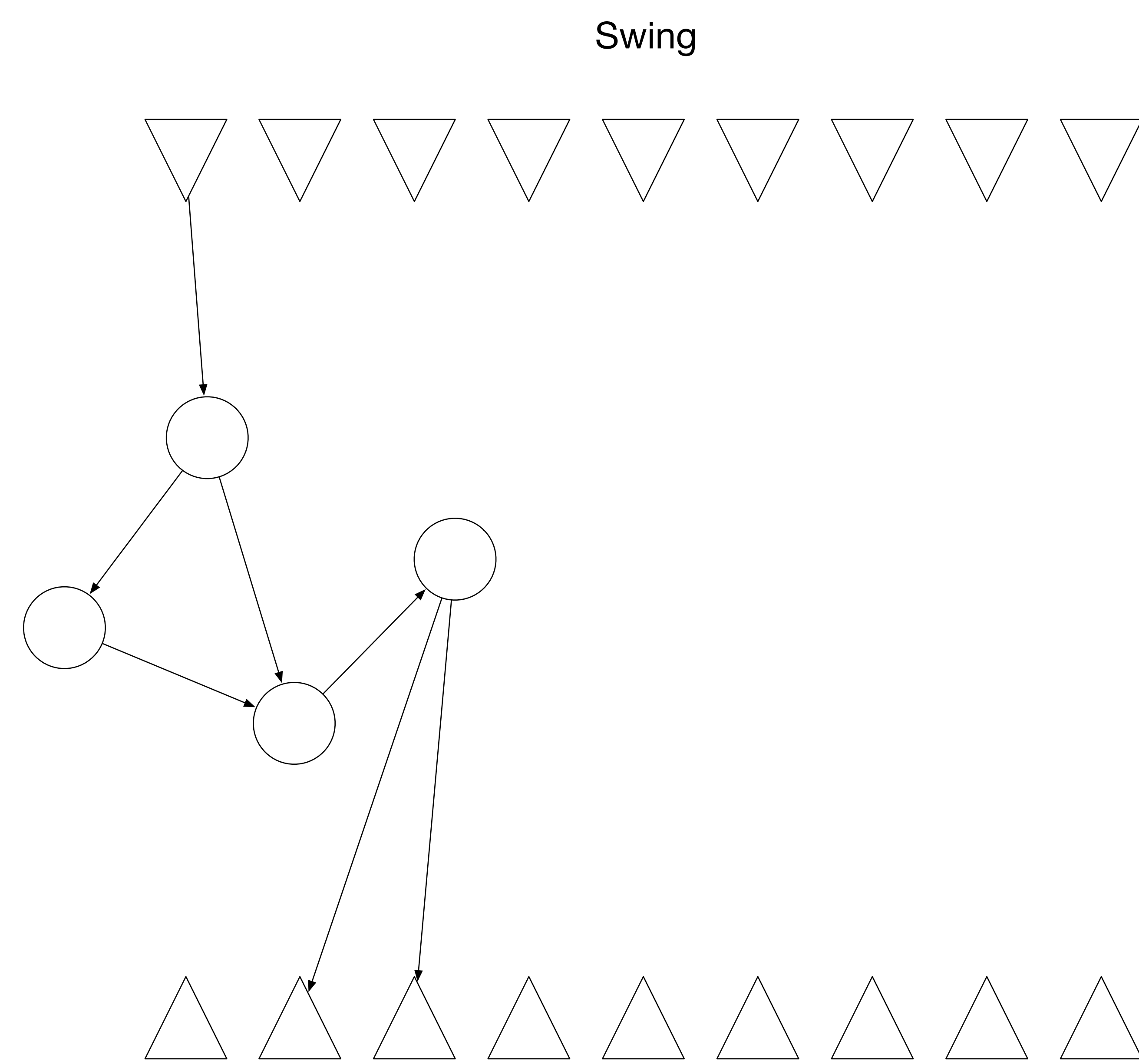
Multiple dispatch

Functional Reactive Programming



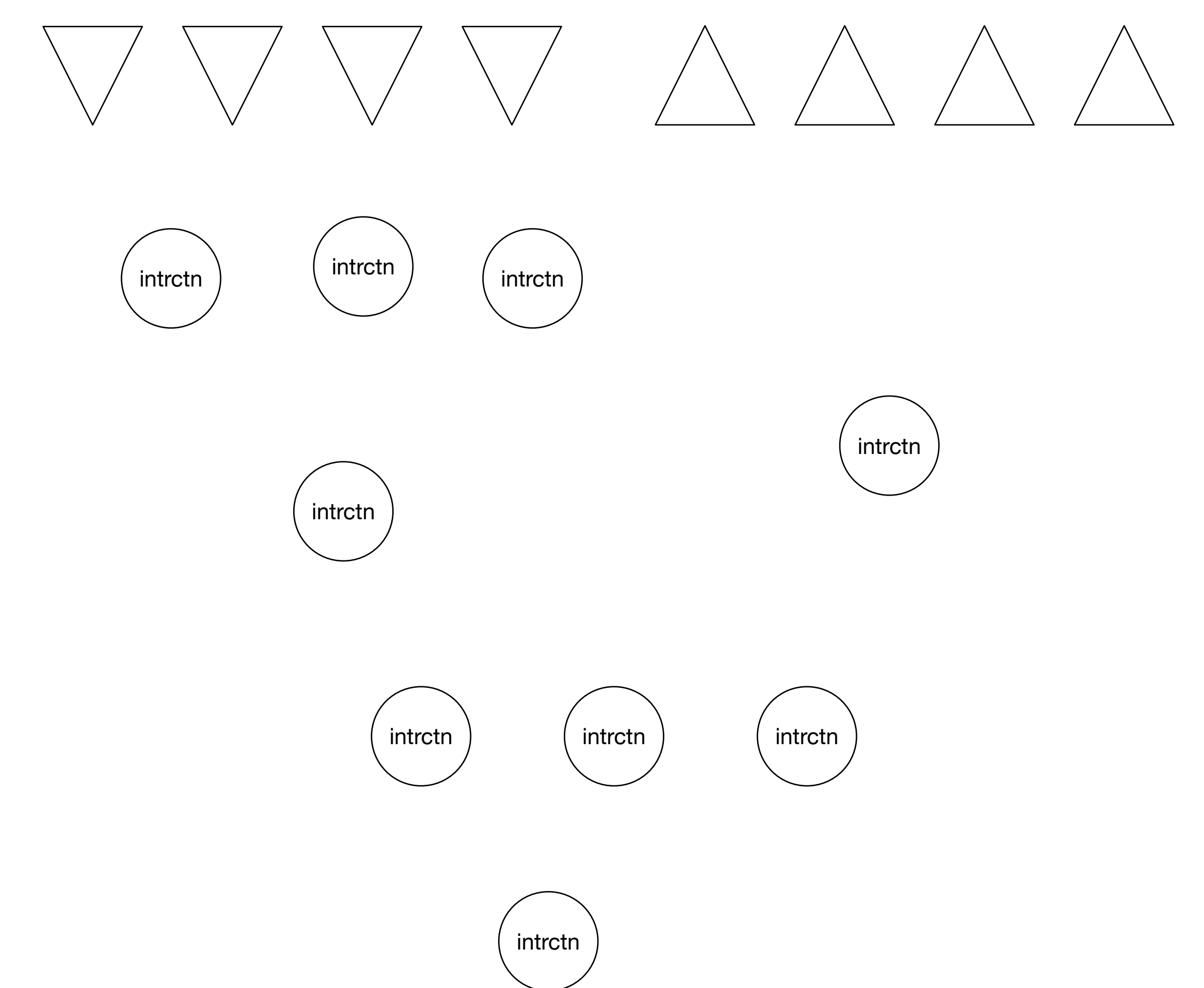
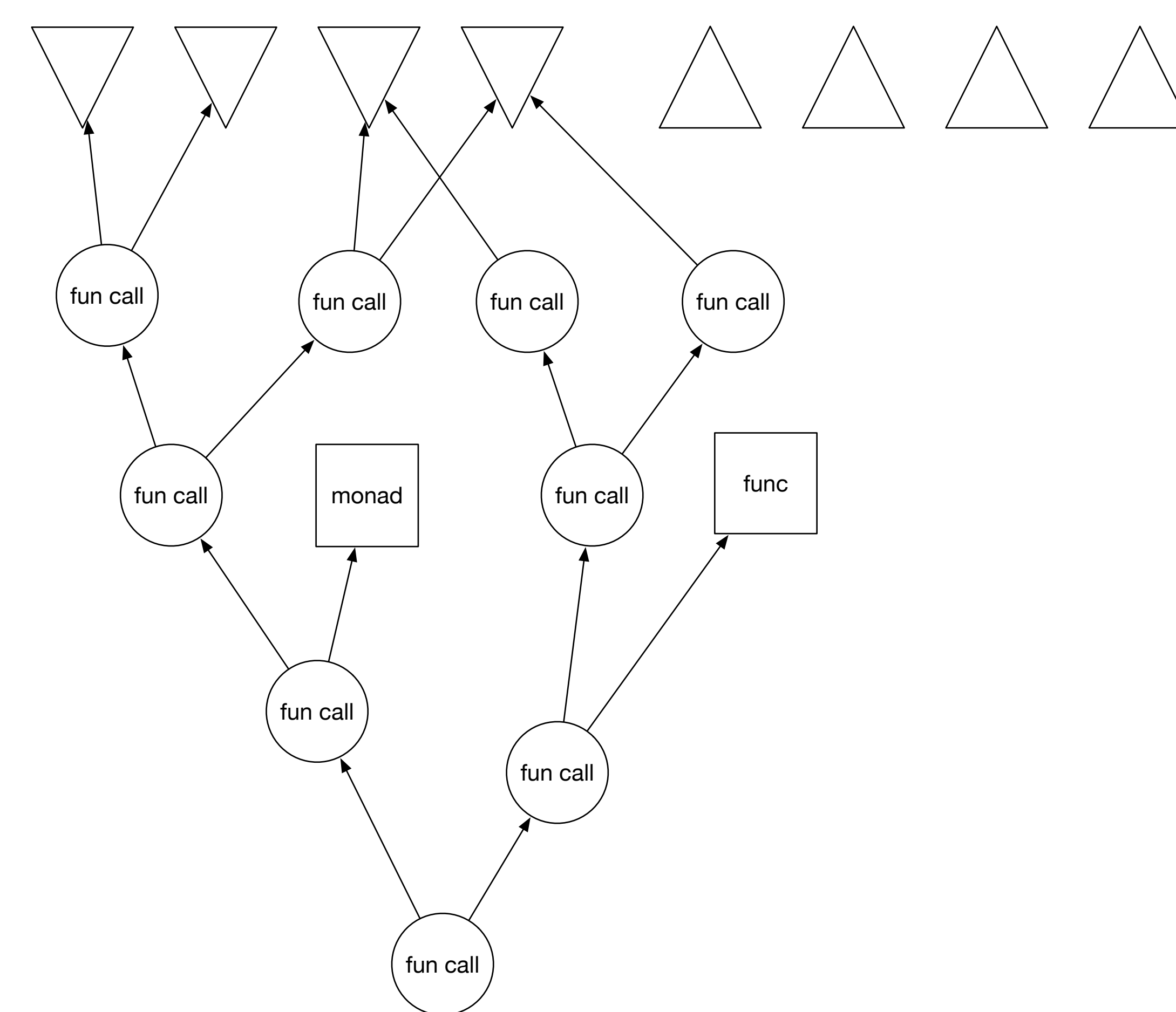
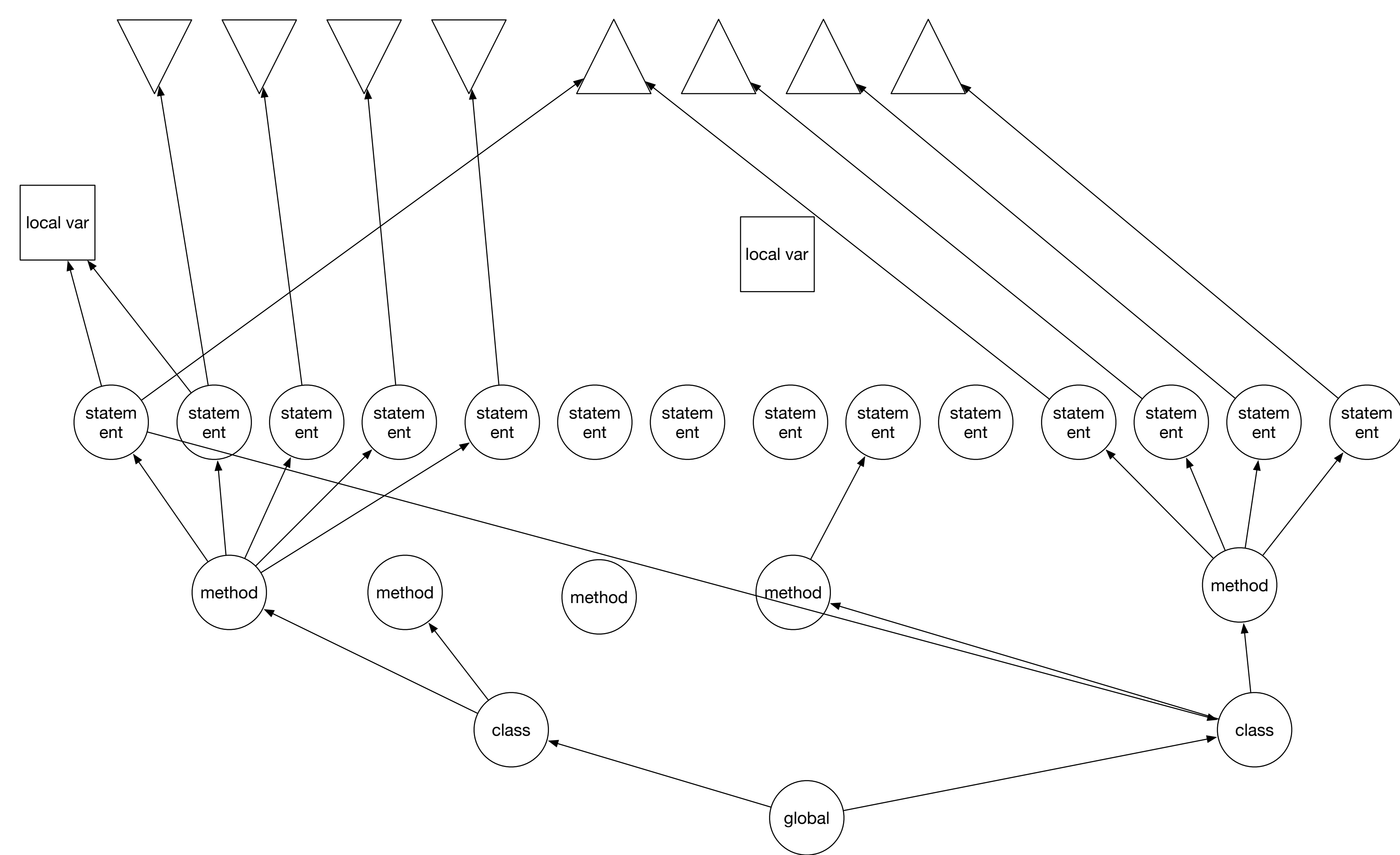
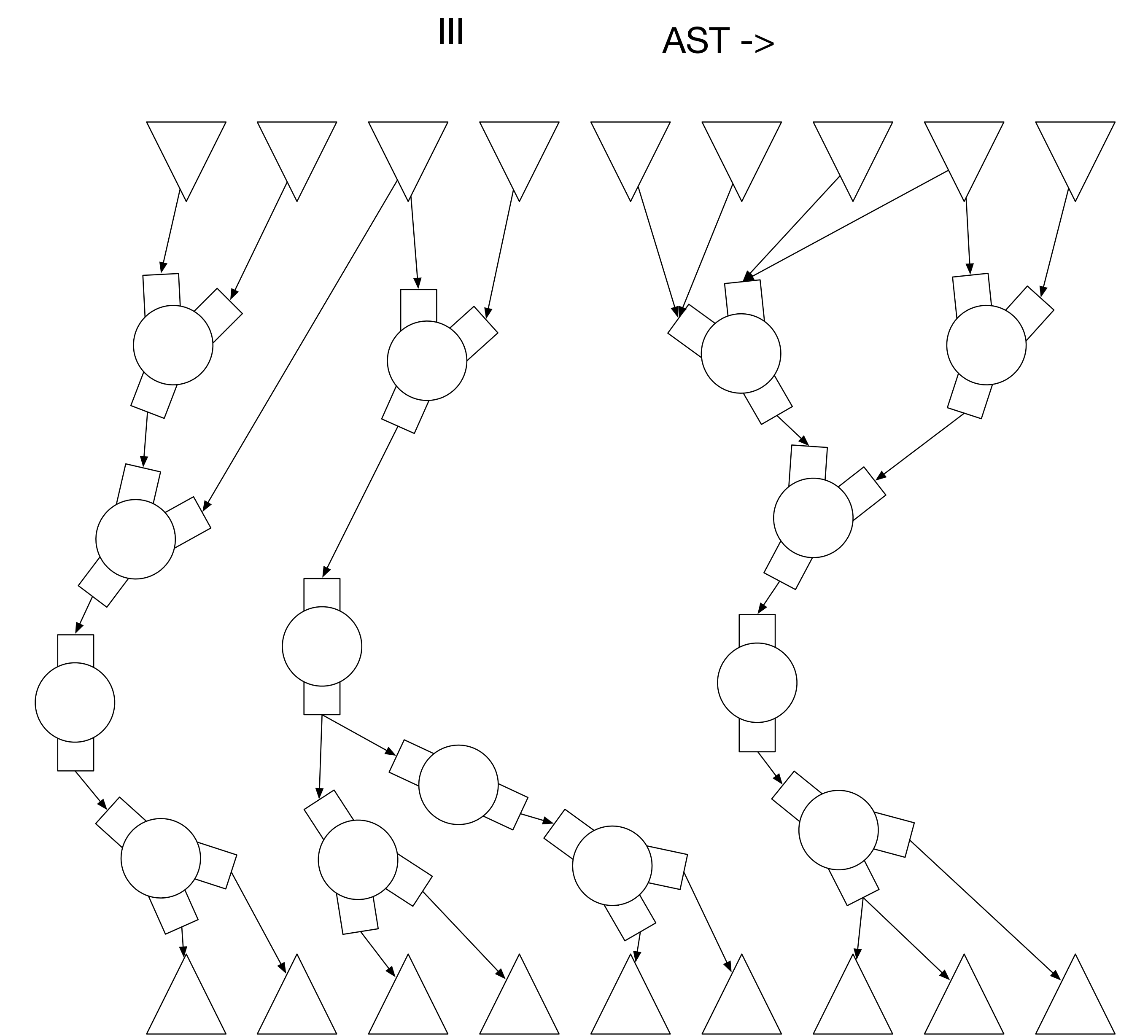
Position philosophique  
Symétrie avec previous et next  
Ou  
Asymétrie du temps avec seulement previous

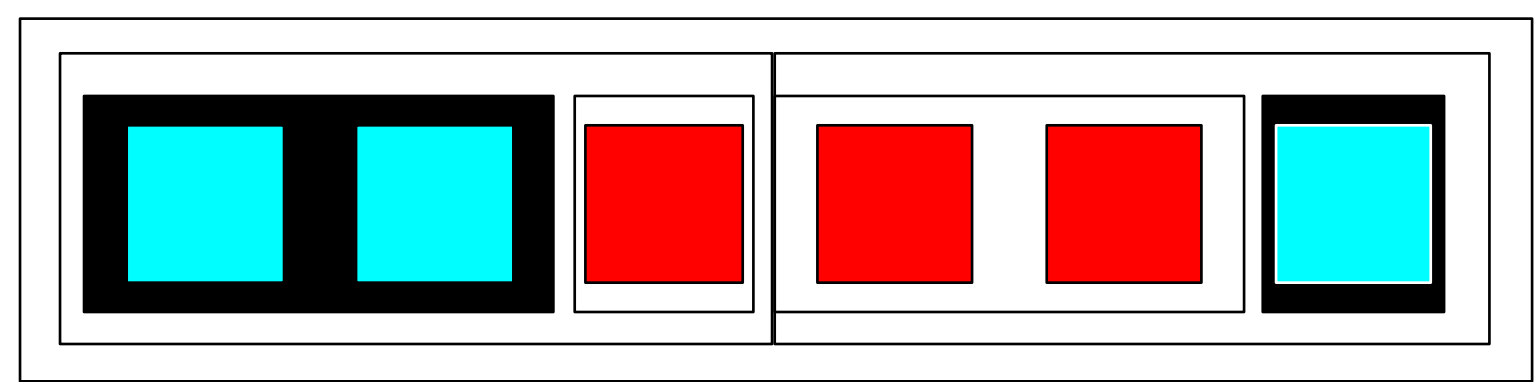
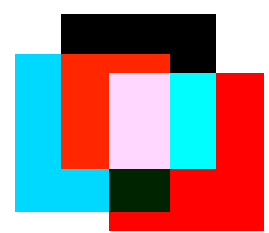
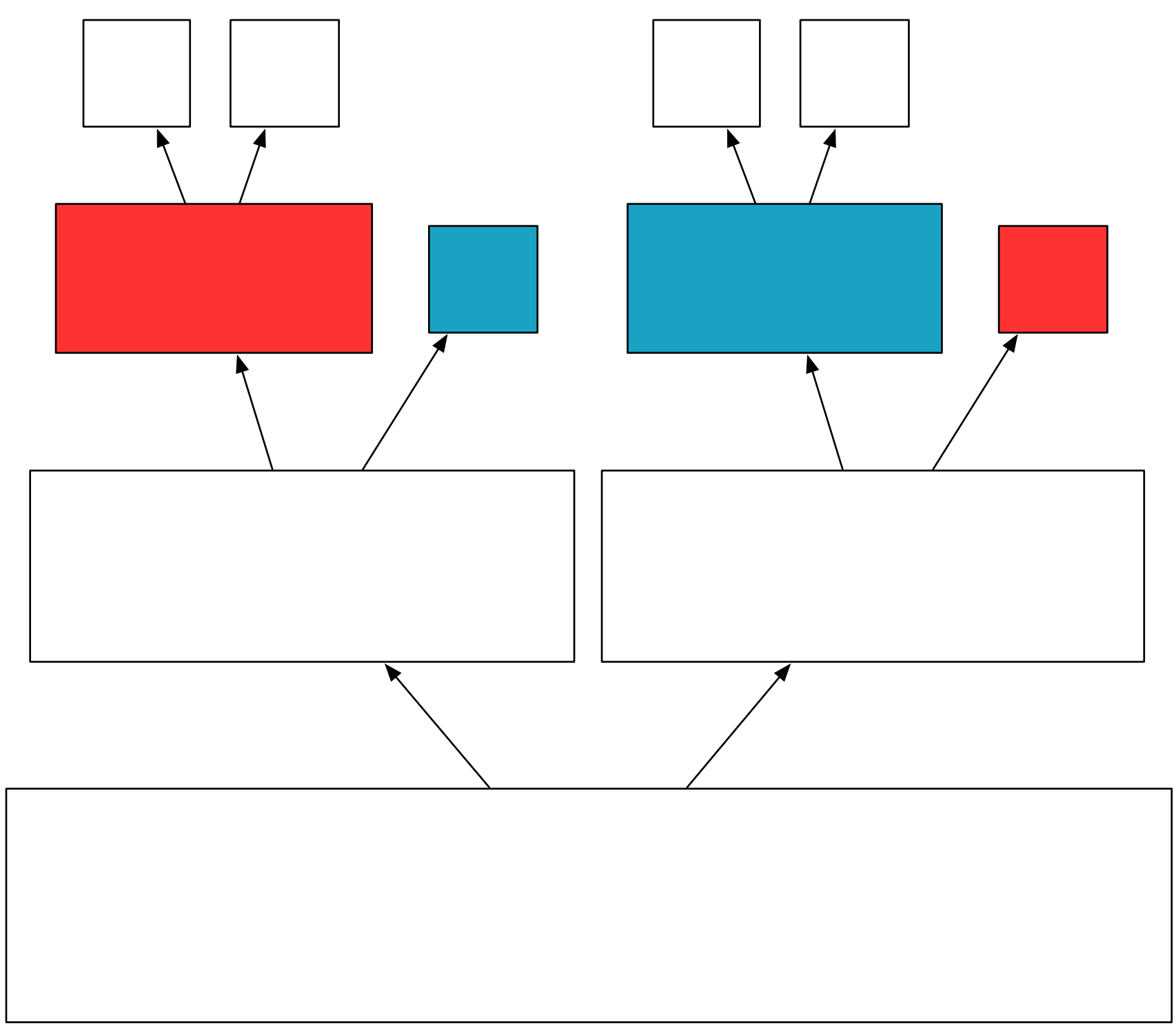
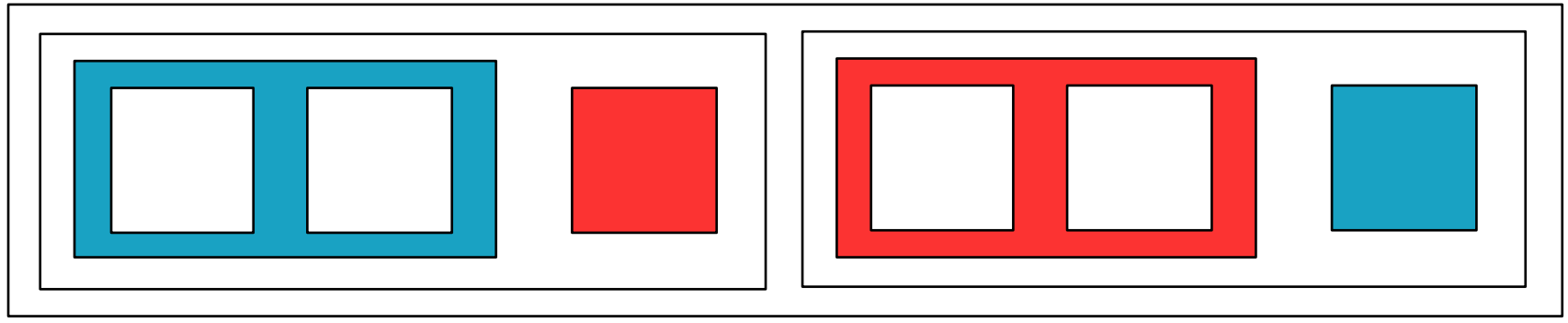


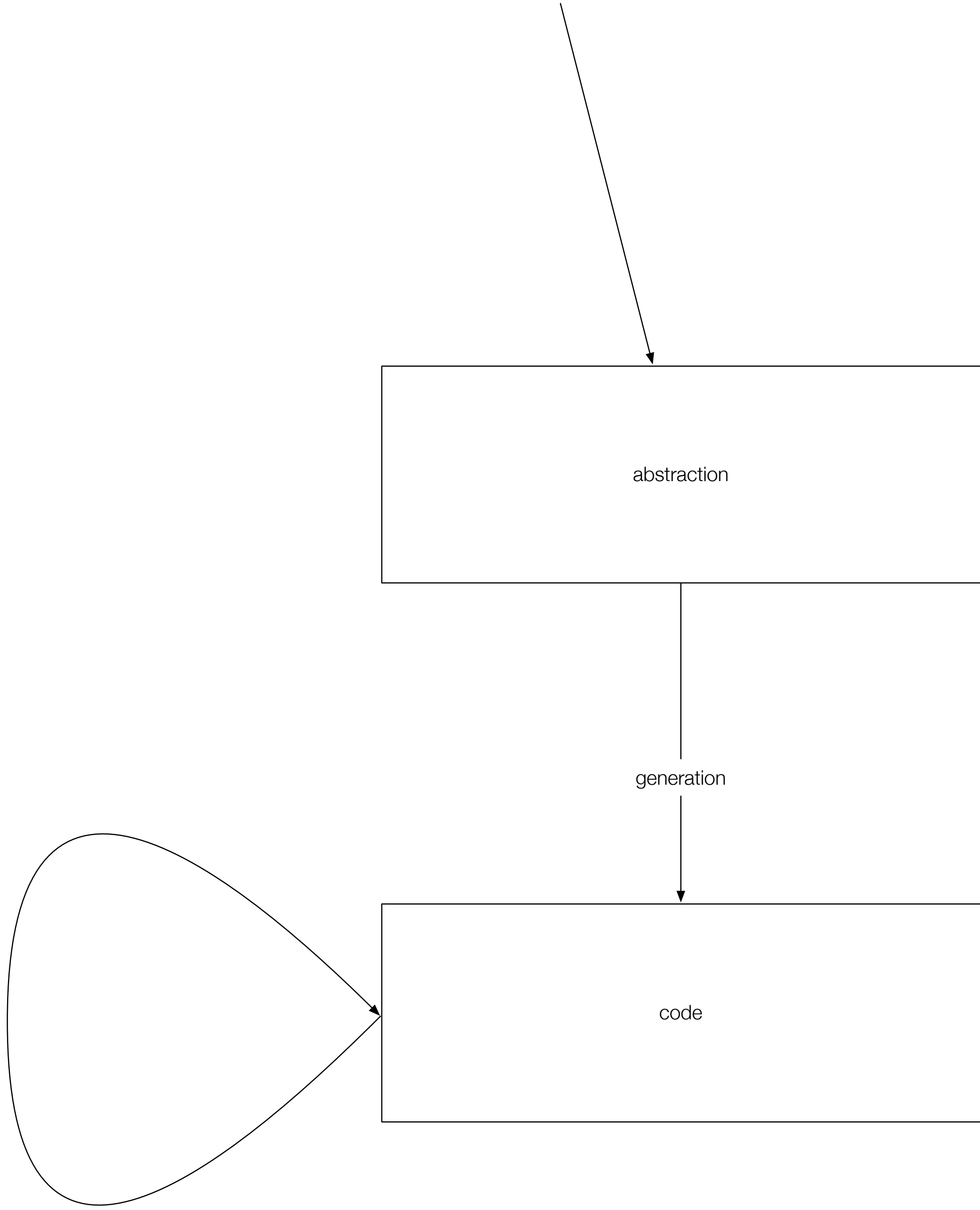


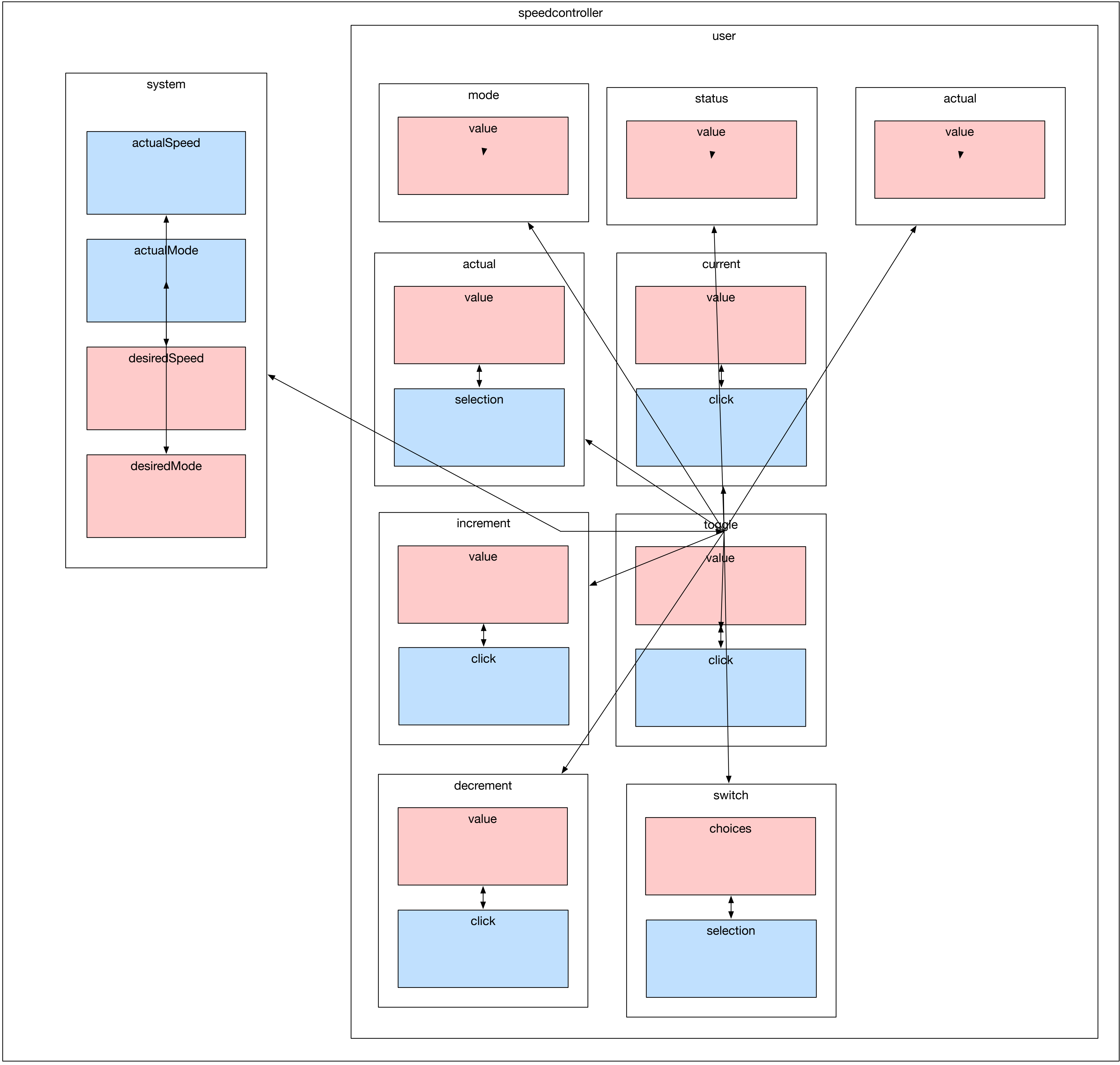
inputs

outputs

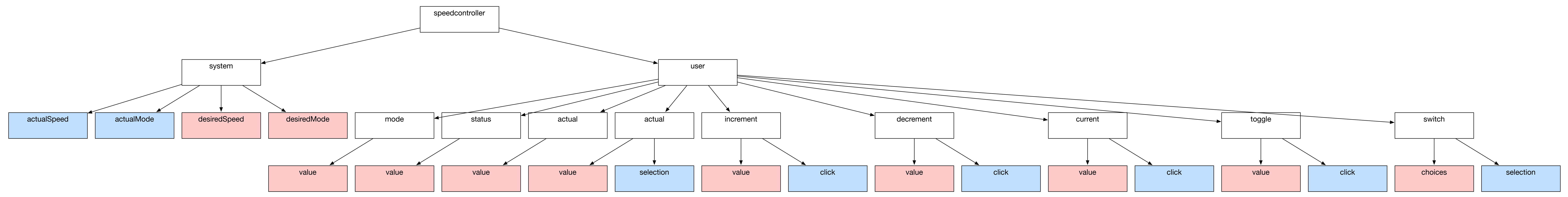


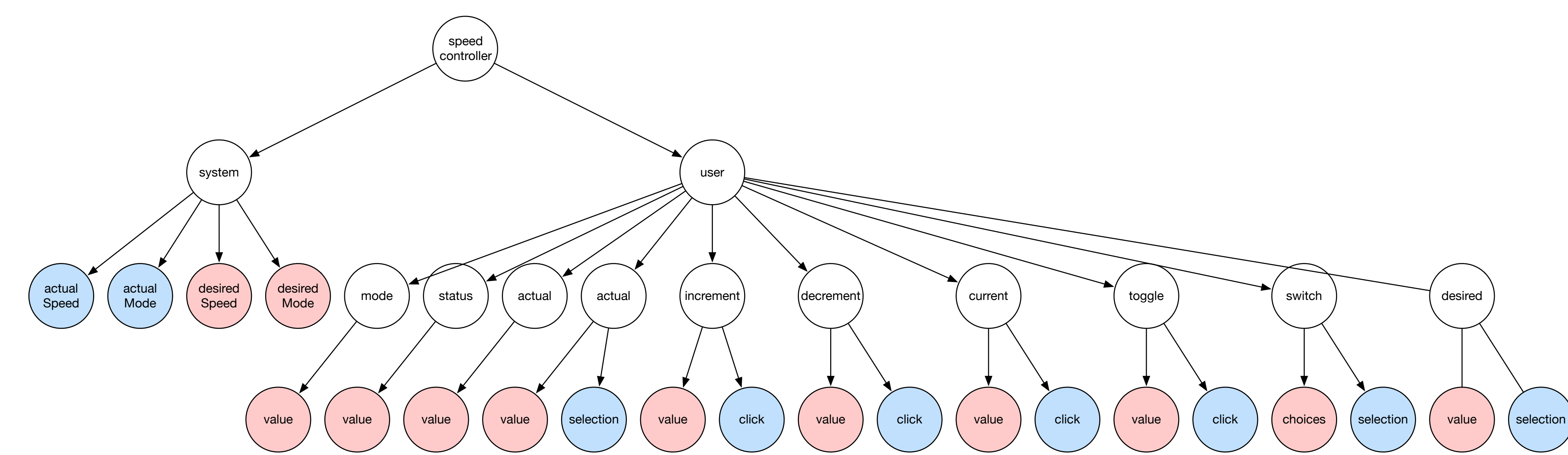






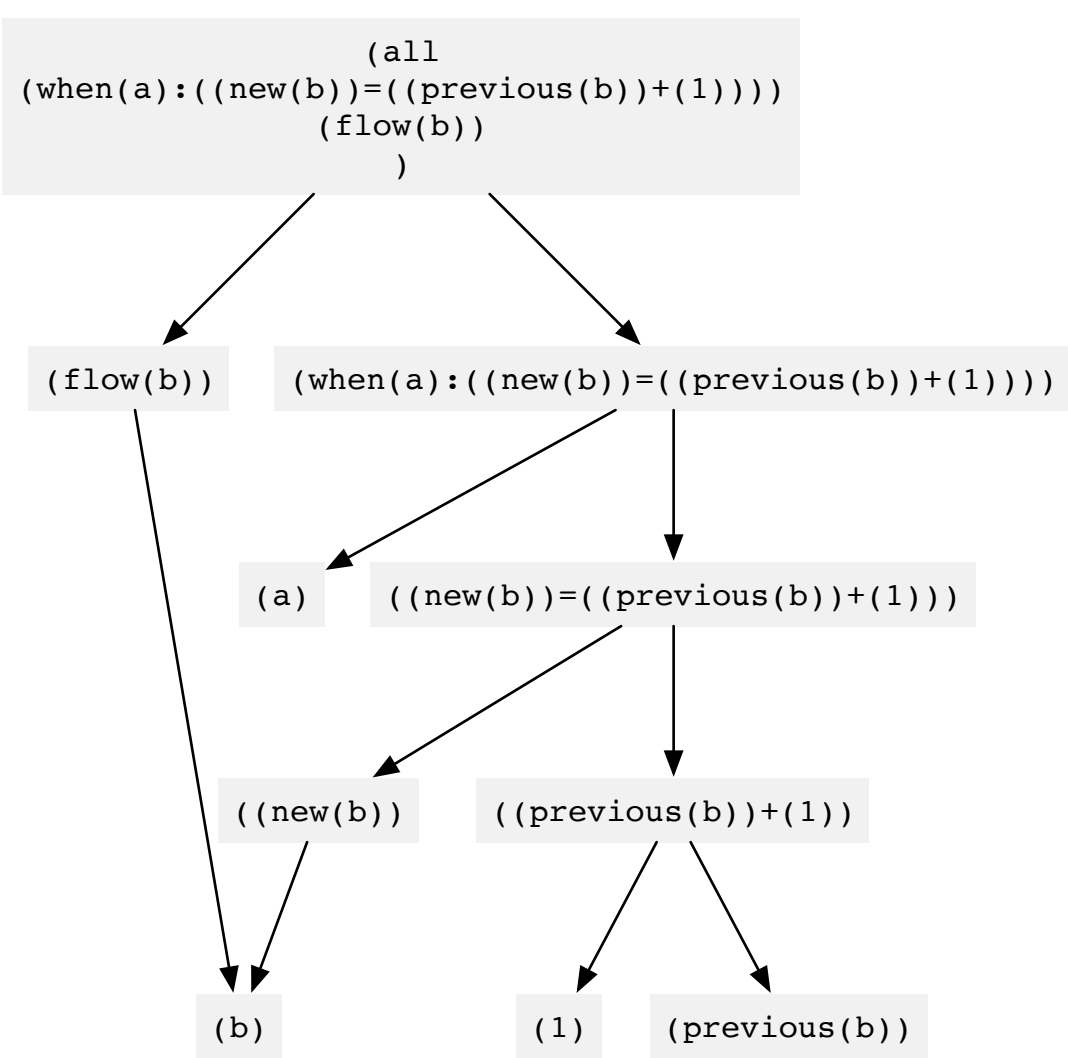




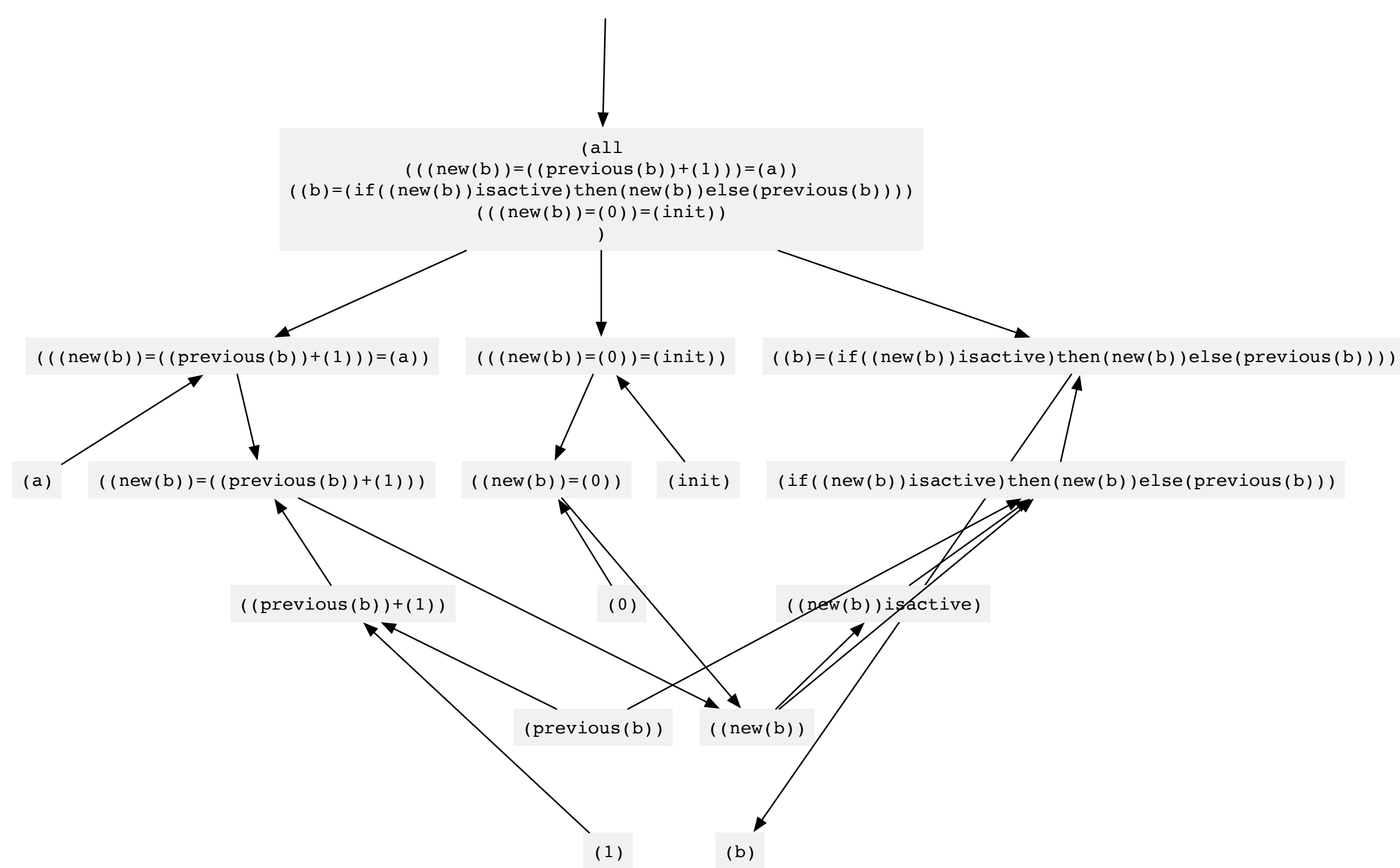




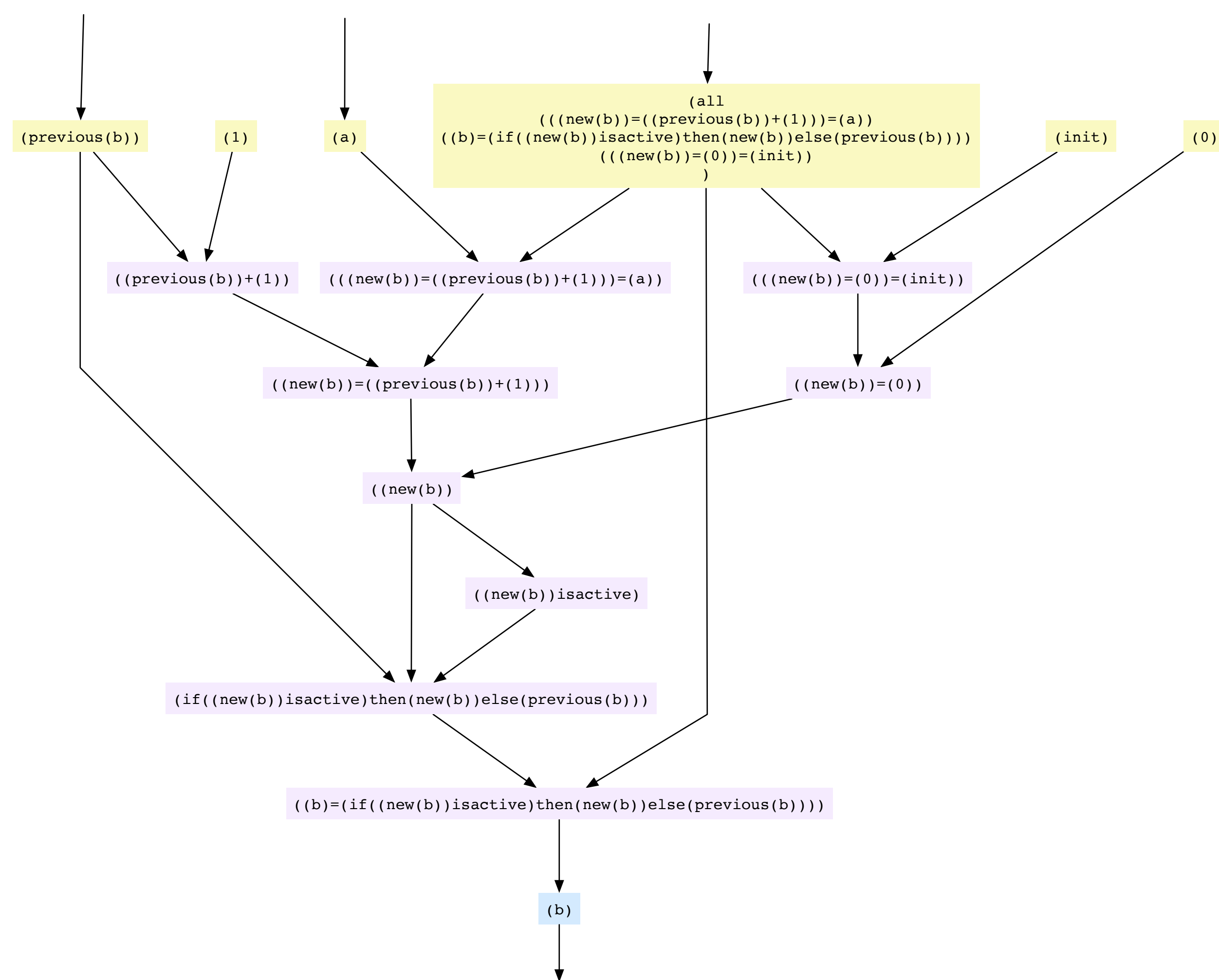
## Parse



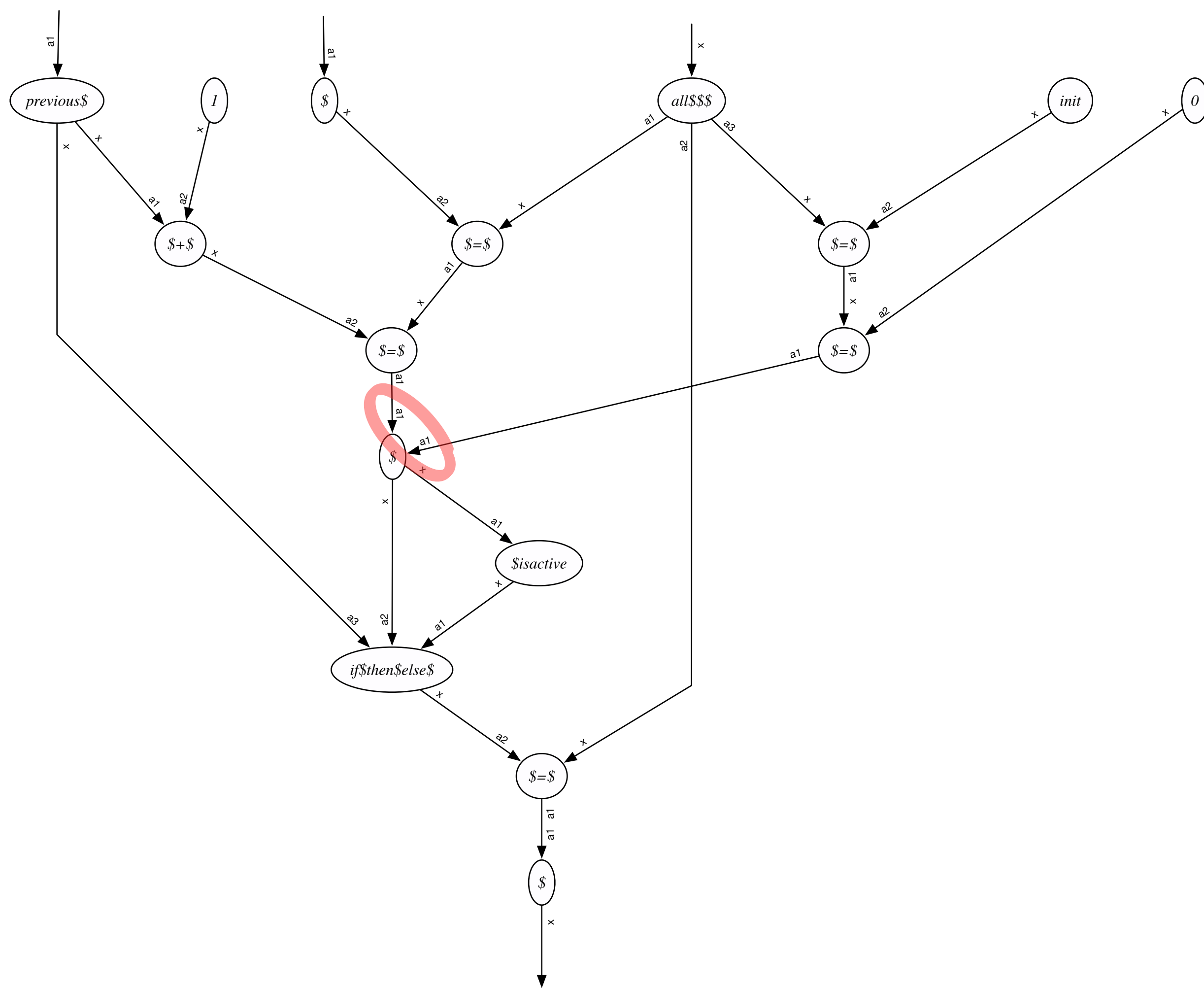
## Expand



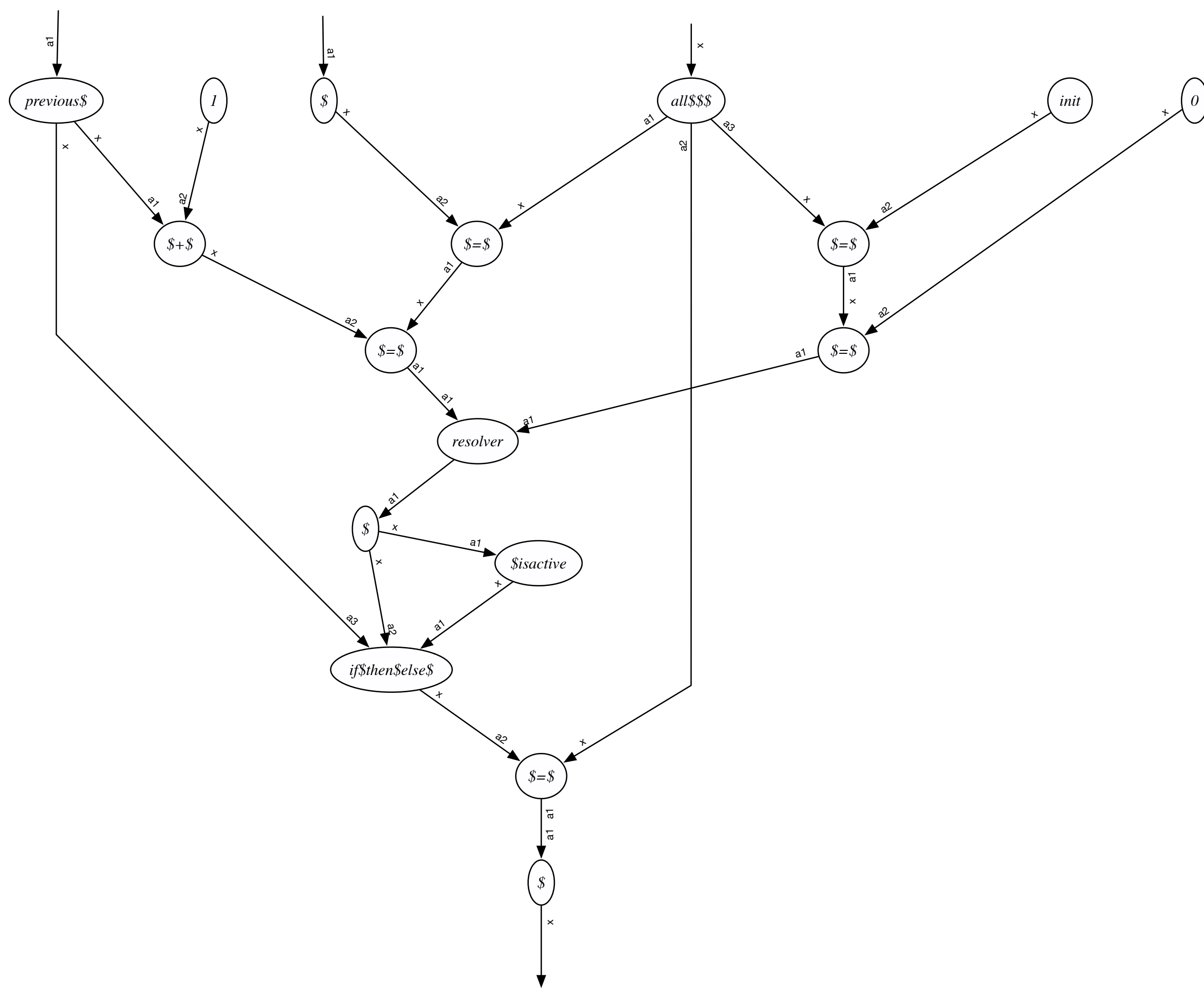
# Order



# Instantiate

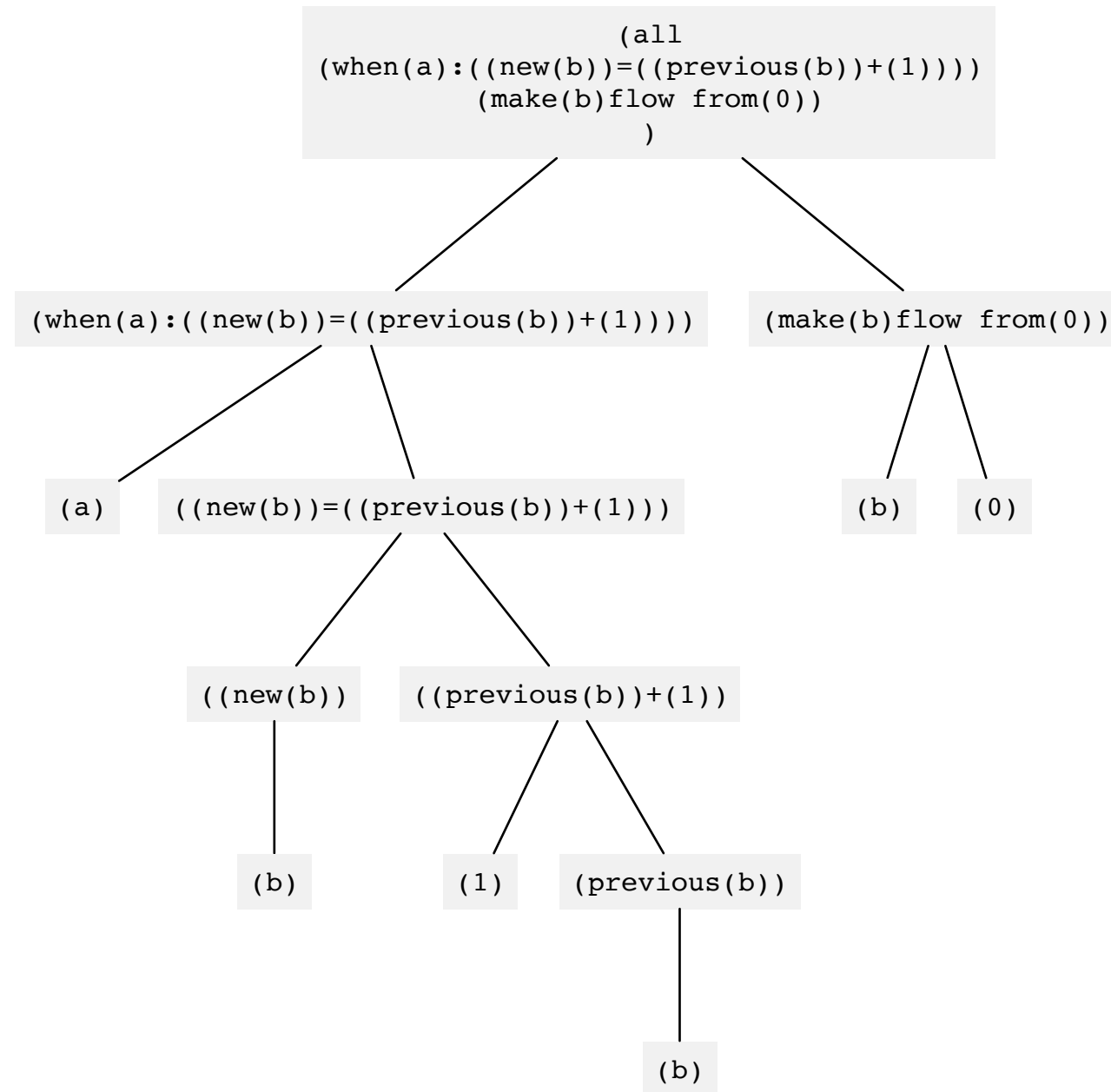


# Resolve



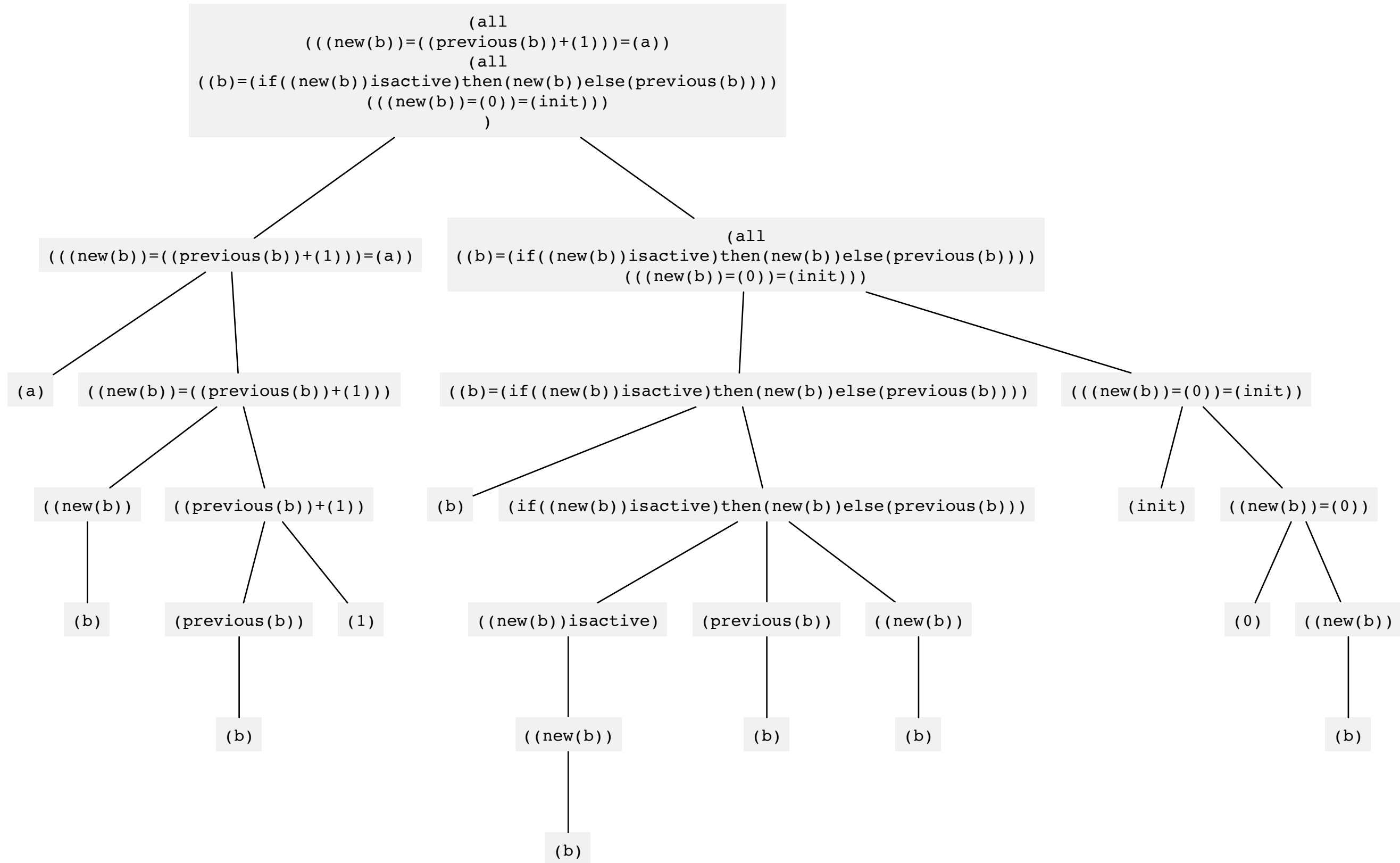
# Parse

Here we parse the code and made the expression tree



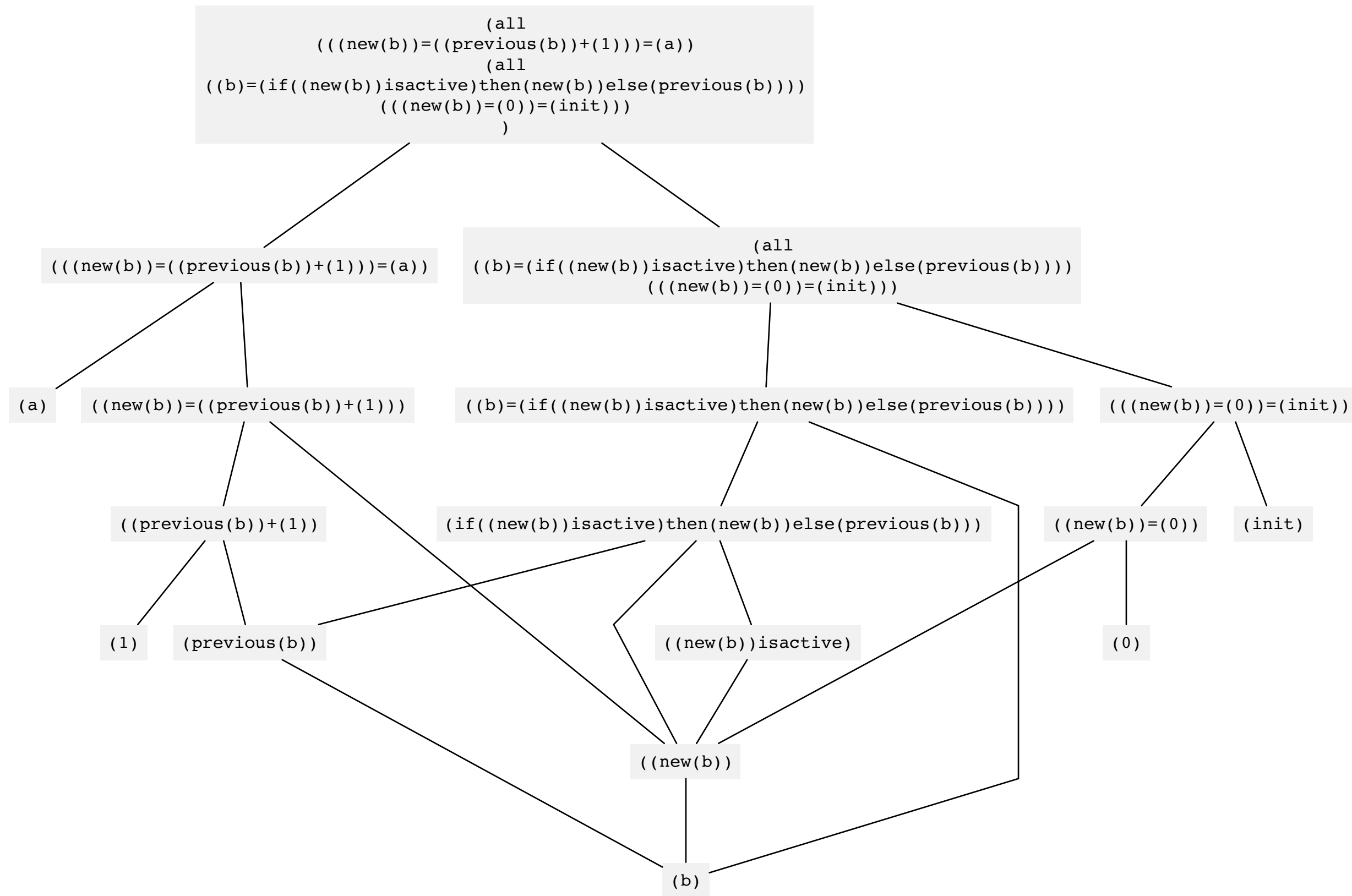
# Expand

Then we expand the tree, using the definitions of interactions, stopping when all interactions are native interactions



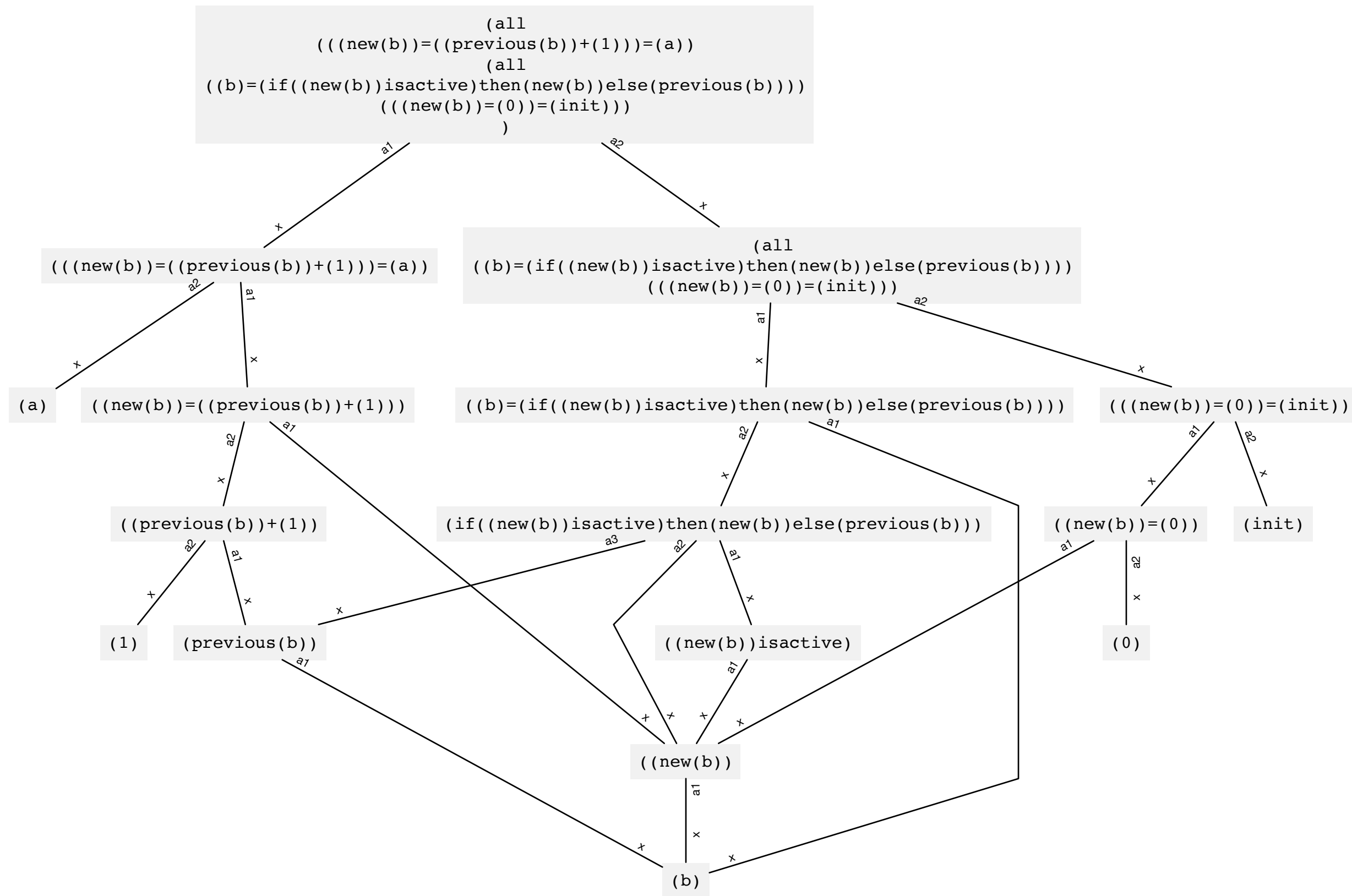
# Link

Here we removed duplicate nodes, effectively linking references to the same node



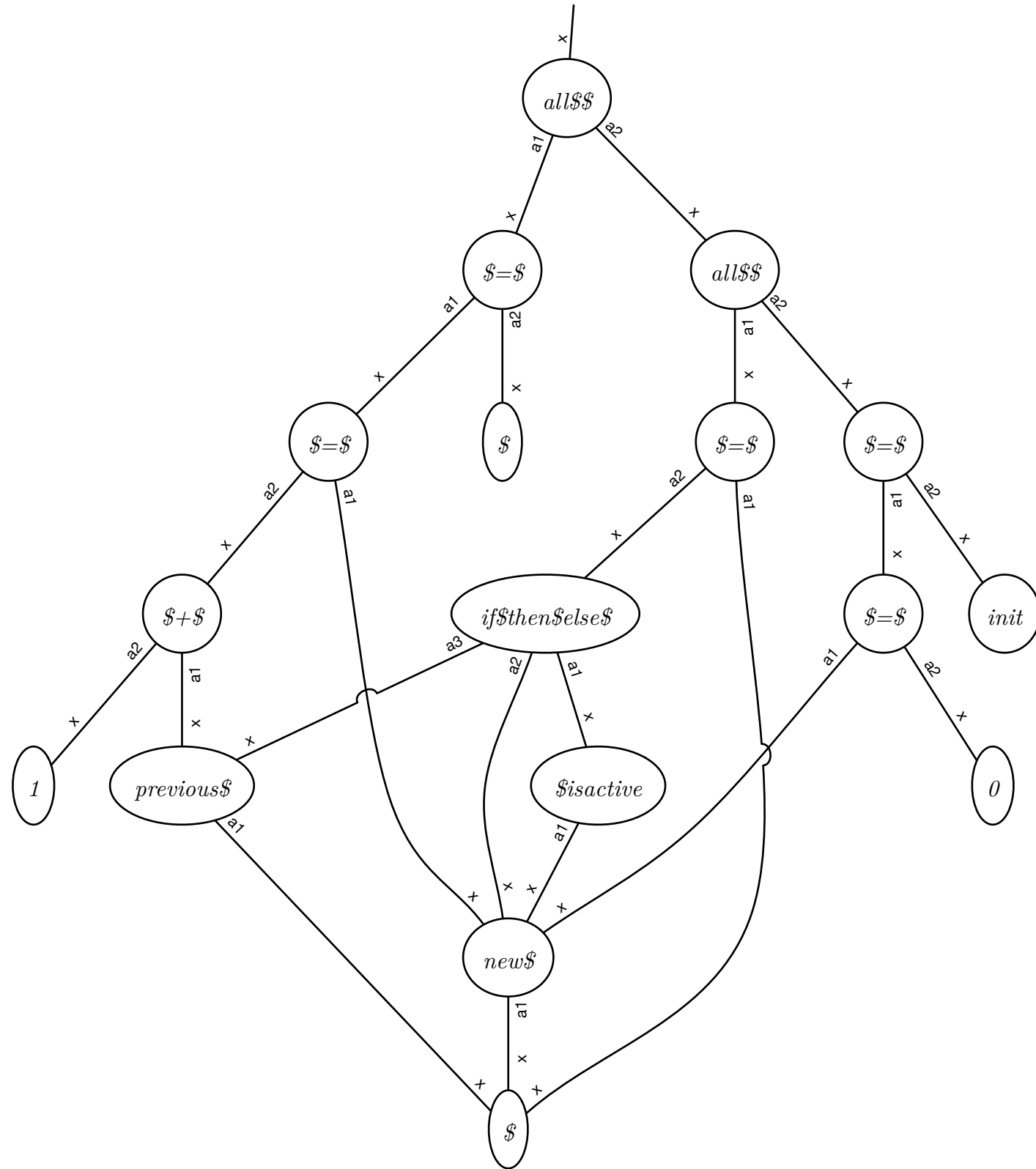
# Annotate

Here we added annotations to the graph edges, these annotations describe the role of each element in the expression  
(a1 for argument1, a2, ..., and x for the expression itself)  
Note that adding annotations is straightforward, as the bottom end of each edge is an “x”, and the top end is an “a” numbered according to the argument number.



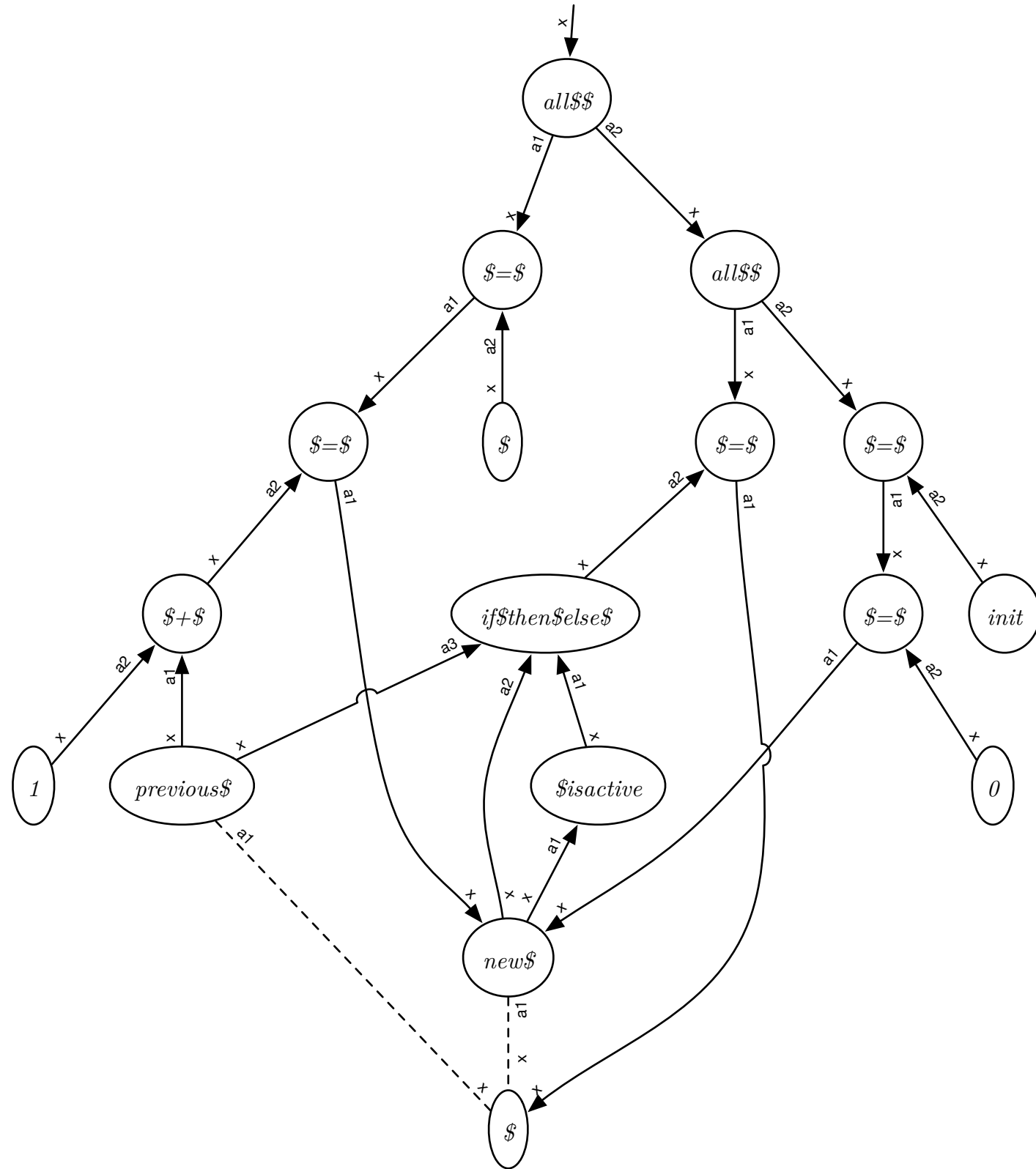


From here we don't need identifiers anymore, we can remove the notion of identifier, and rename nodes according to their operator instead of their identifier



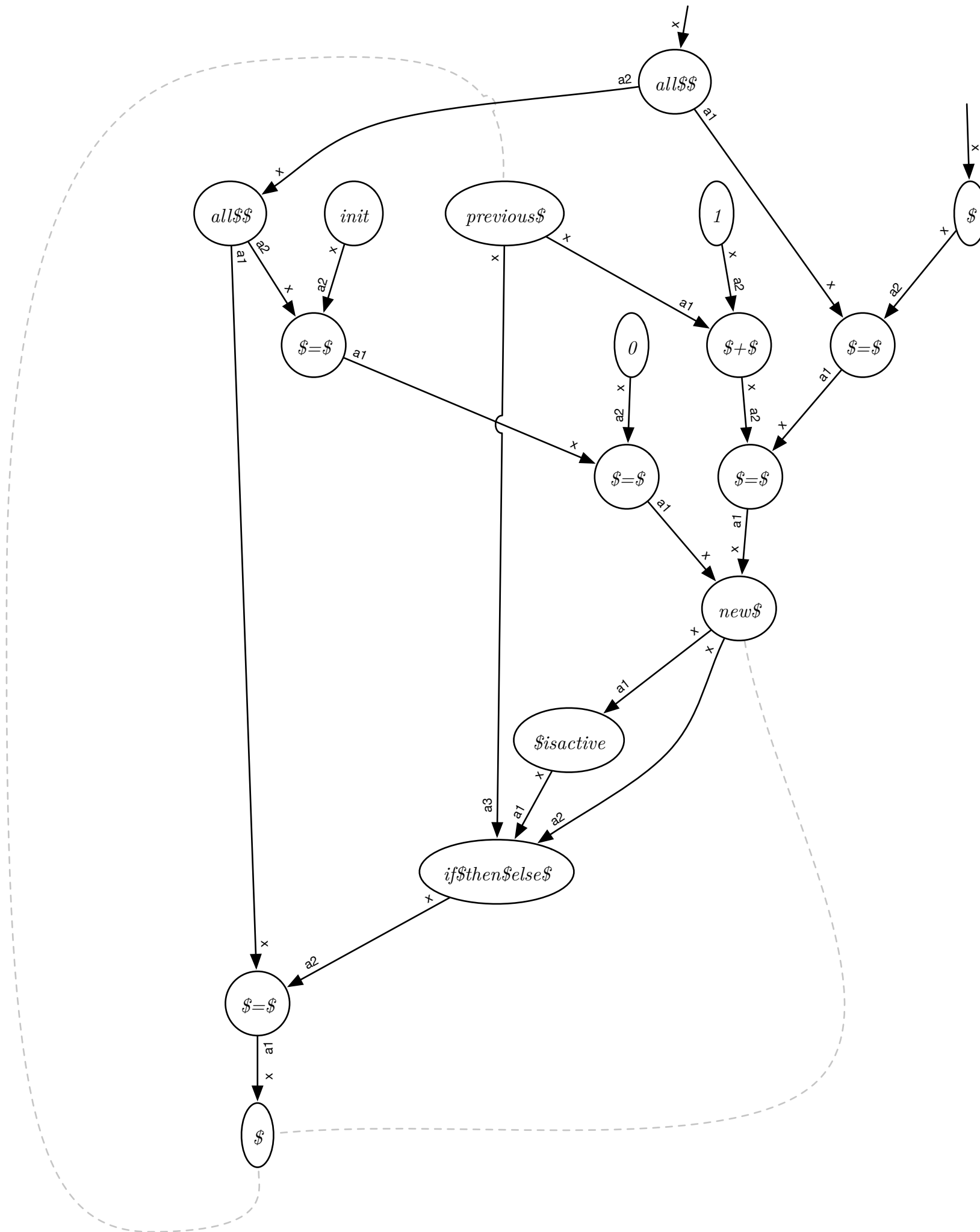
# Direct

Here we keep the same graph, but we give directions to edges, according to the direction of the data flow. For this step to be possible, the program has to be consistent according to interfaces flow directions. (i.e. the OUTs must match the INs)  
Some edges do not denote a data flow, so they are dashed



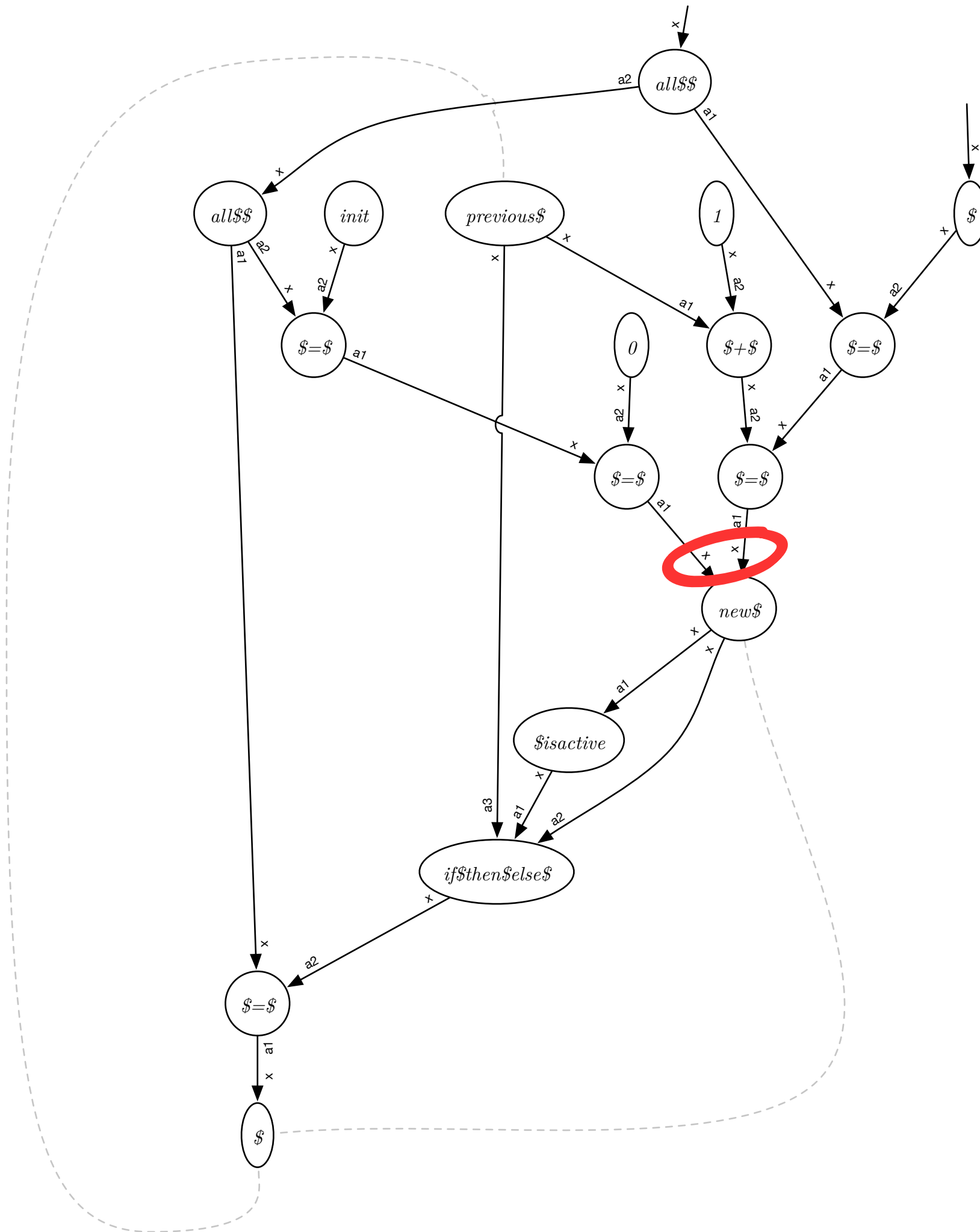
# Order

Again, this is the same graph, but we changed its layout so all arrows go down

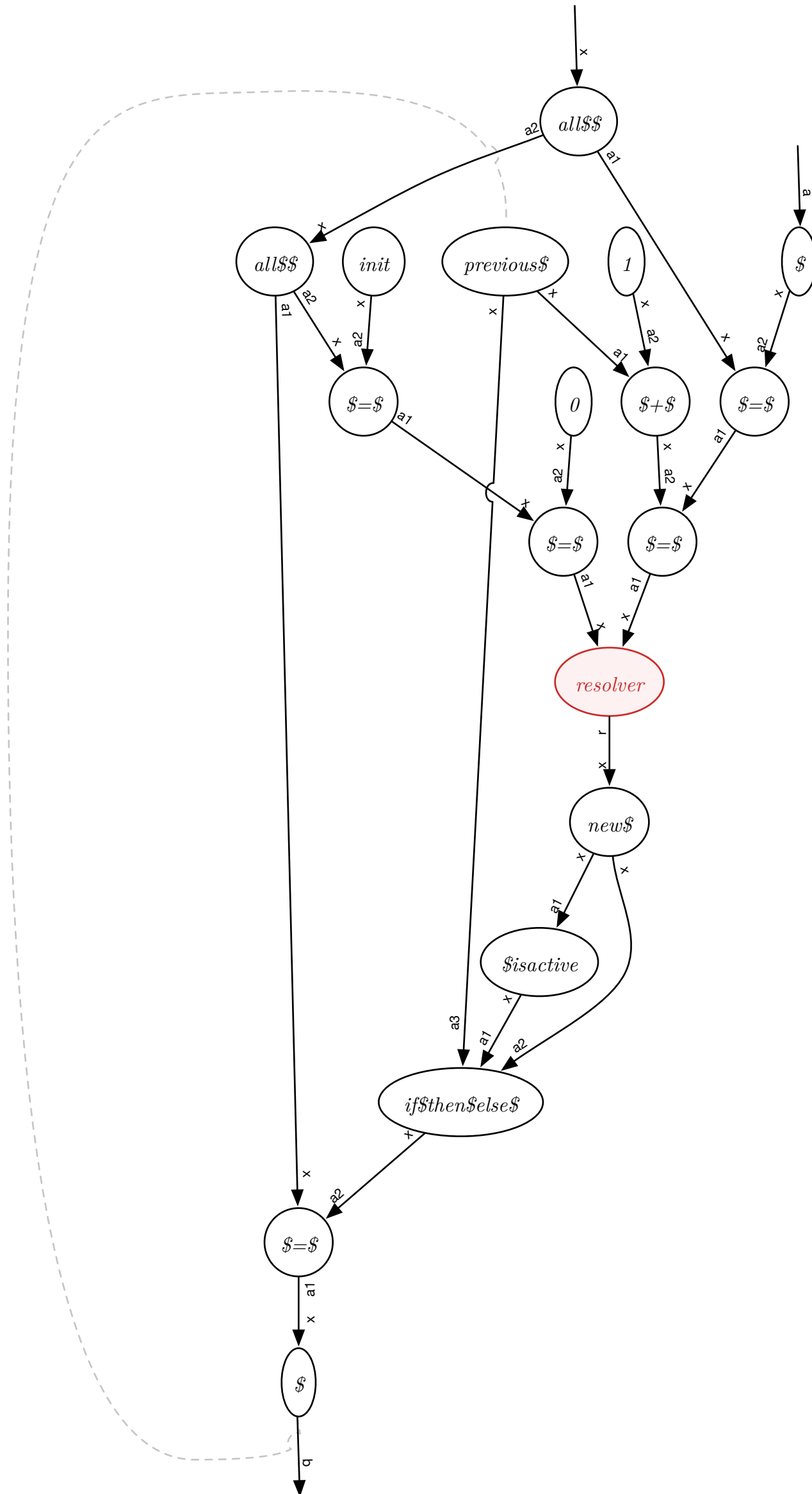


# Detect conflicts

We detect nodes where two incoming edges have the same annotations



## Add a resolver where conflicts exist

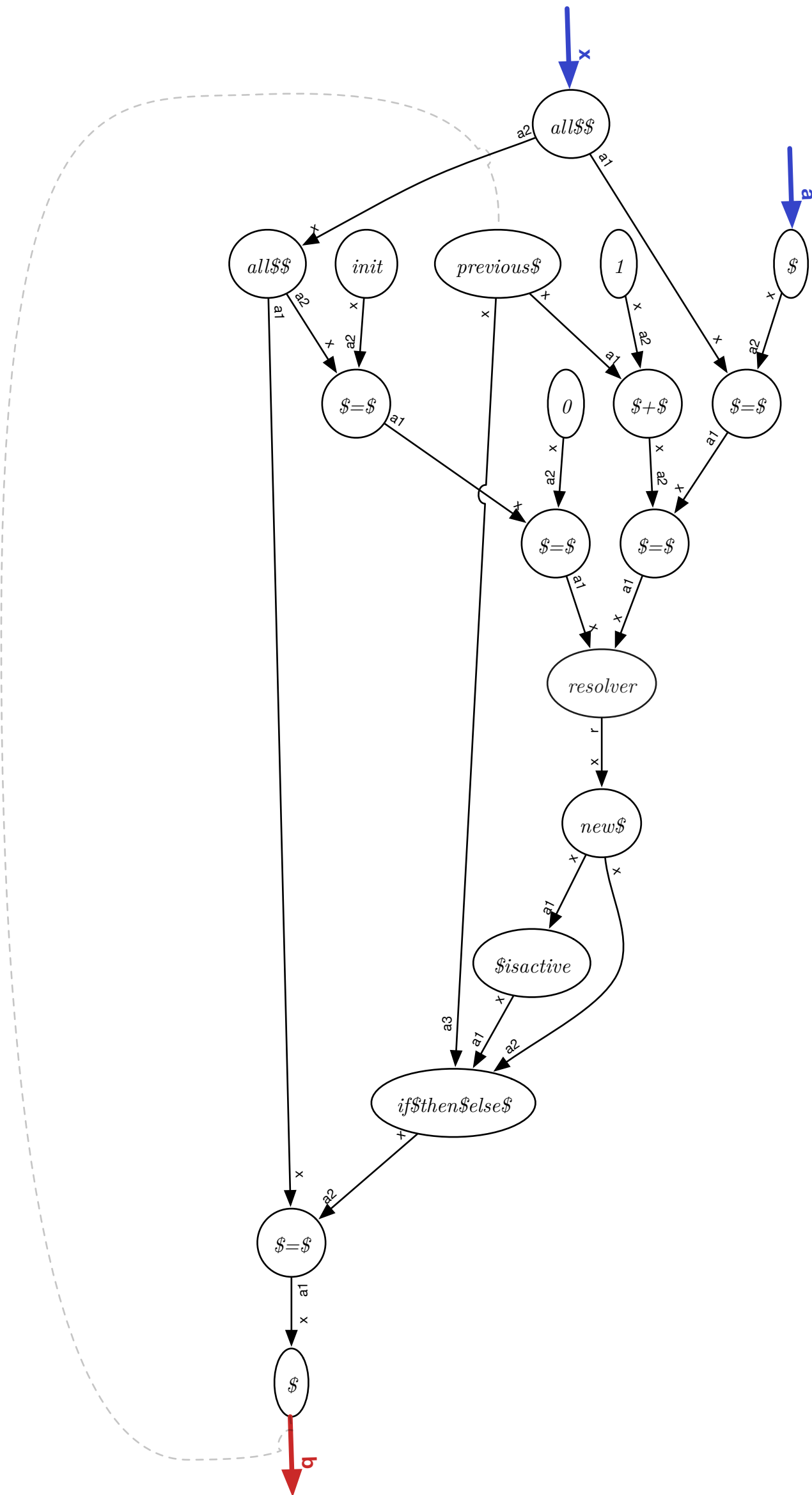


# Execution

From here, the interaction is ready to be executed.  
To execute, assign values to edges, from top to bottom.

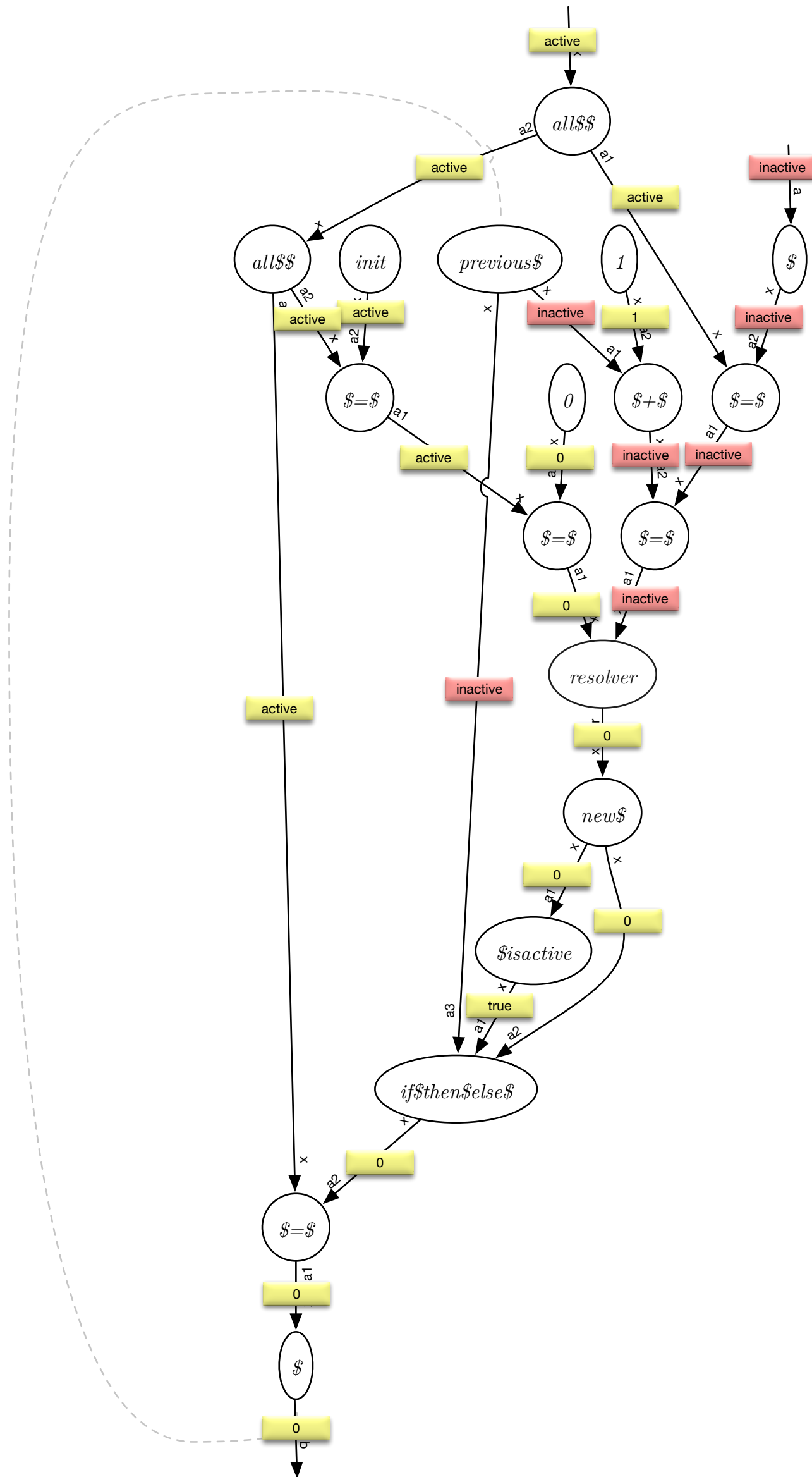
System inputs are incoming edges.

System outputs are outgoing edges.



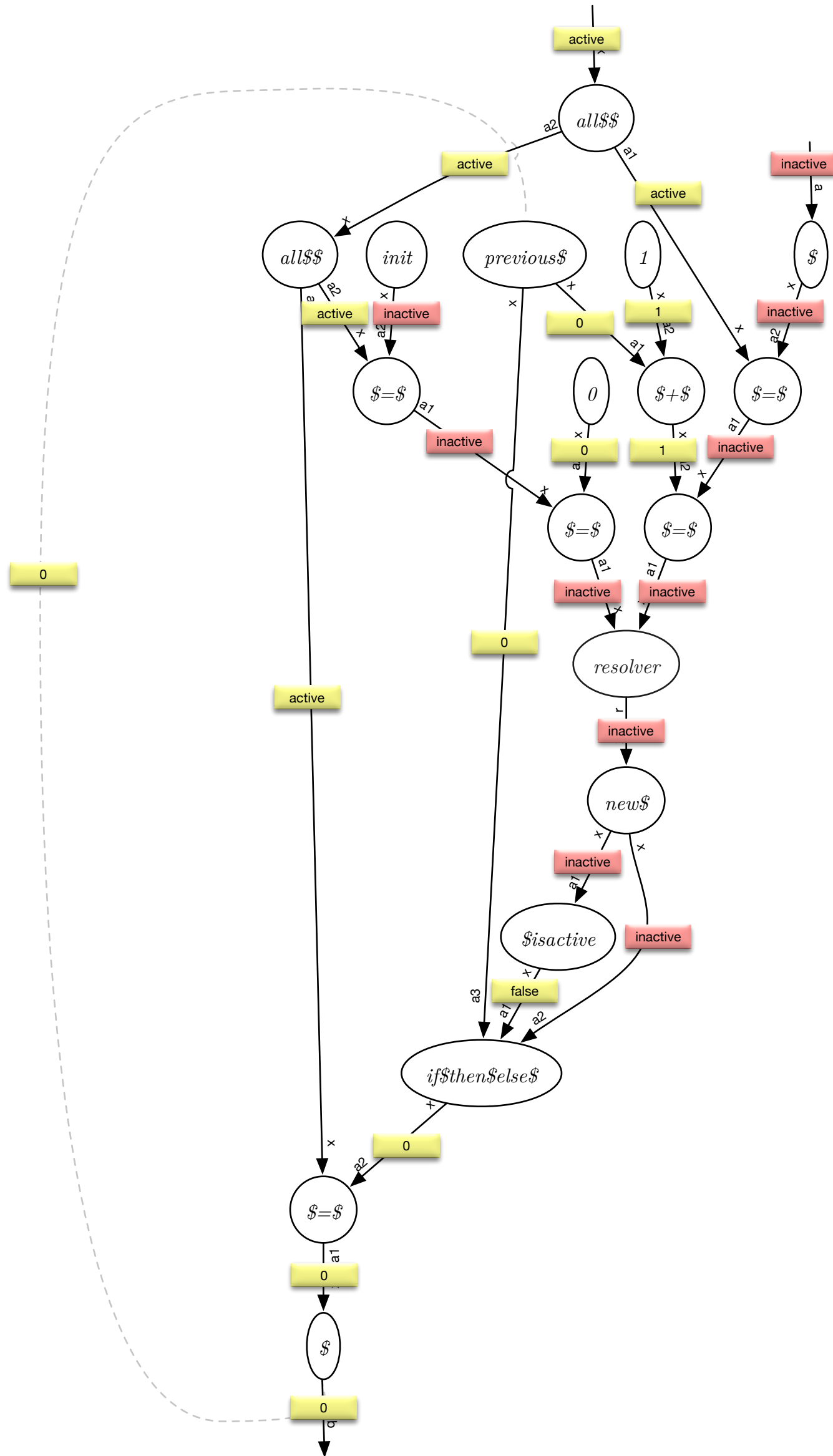
# Execute 0

First execution step, so (init) outputs active  
Inputs :  
a=inactive,  
the root interaction is active



# Execute 1

Second execution step,  
still no input on a,  
But notice how the output is still 0 (not inactive), it “flows”



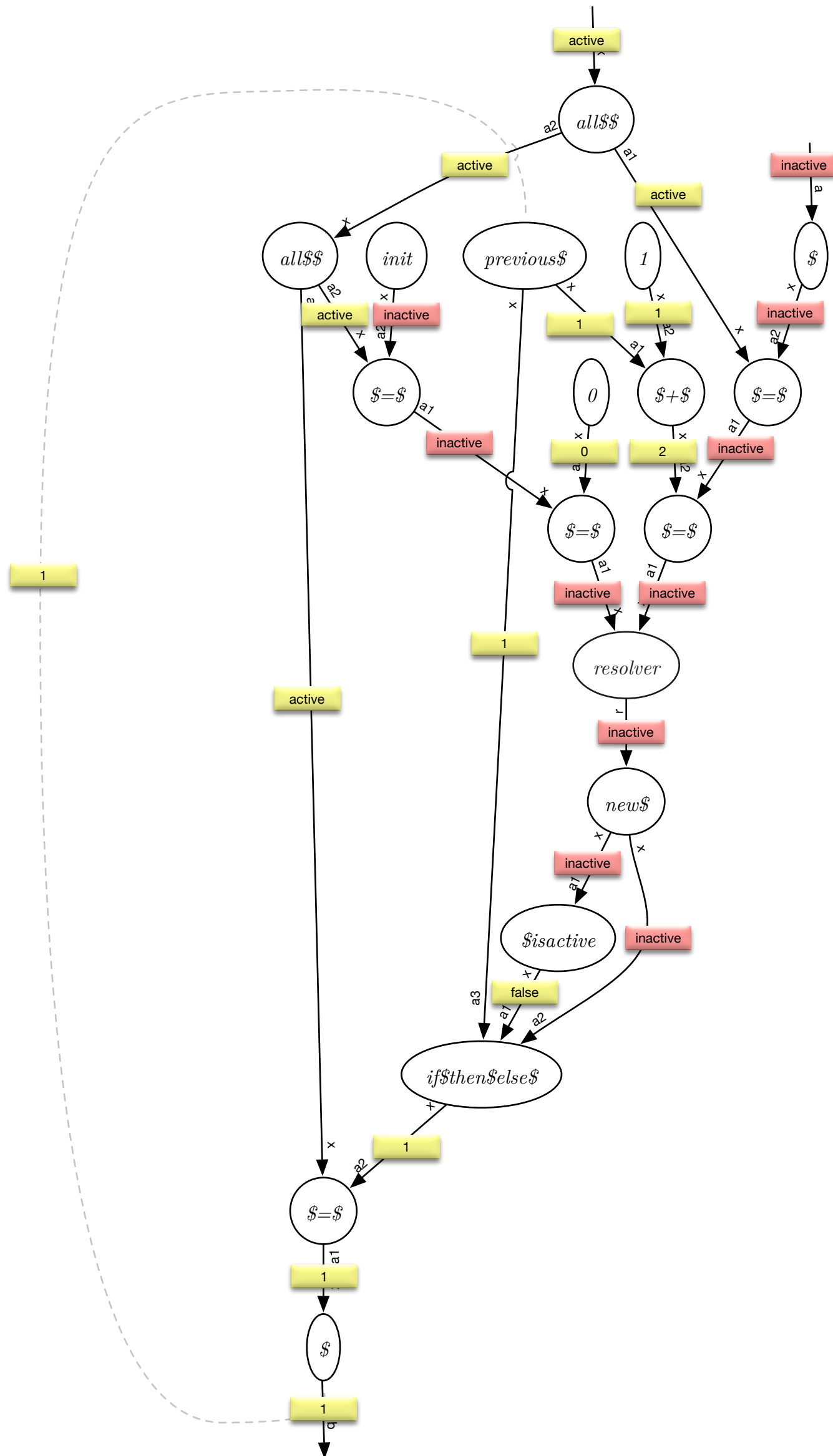






# Execute 4

No input on a, b stays to 1



Another input “active” on a, b is now 2