

15-1 (D) 15-2 (B) 15-3 (B) 15-4 (C) 15-5 (C)

15-8 由 $\lambda_m T = b$ 得 $\lambda_m = 2.57 \times 10^{-7} \text{ m}$

15-9 $M(T) = \sigma T^4$ 得 $T = 1416.1 \text{ K}$

15-10. $M(T) \cdot 4\pi d^2 = M_{\text{表}}(T) \cdot 4\pi r^2$

且 $M_{\text{表}}(T) = \sigma T^4$ 得 $T = 5802.7 \text{ K}$

15-11 $W = h\nu$ 得 $\nu_{\text{红}} = 1.092 \times 10^{15} \text{ Hz}$, $\nu_{\text{蓝}} = 6.04 \times 10^{14} \text{ Hz}$

15-12 $h\nu = h\nu_0 = \frac{1}{2} m_0 v_0^2$ $\nu = \frac{c}{\lambda}$ 得 $v_0 = 5.74 \times 10^5 \text{ m/s}$

15-13. 能量守恒 $h\frac{c}{\lambda} = h\frac{c}{\lambda'} + (m - m_0)c^2$. $m = \frac{m_0}{\sqrt{1 - \frac{v^2}{c^2}}}$

得 且有 $\Delta\lambda = \lambda' - \lambda = \lambda_c (1 - \cos\theta)$

得 $\lambda' = 4.35 \times 10^{-3} \text{ nm}$, $\theta = 63.6^\circ$.

15-14 $E = h\nu$ 得 $\nu = 2.41 \times 10^{18} \text{ Hz}$, $\lambda_0 = \frac{c}{\nu} = 0.124 \text{ nm}$
 (1) $\Delta\lambda = \lambda - \lambda_0 = \lambda_c (1 - \cos\theta)$ 得 $\Delta\lambda = 1.22 \times 10^{-3} \text{ nm}$

$\Delta\nu = \frac{c}{\lambda} - \frac{c}{\lambda_0} = \frac{c}{\lambda_0 + \Delta\lambda} - \frac{c}{\lambda_0} = \frac{-c\Delta\lambda}{(\lambda_0 + \Delta\lambda)\lambda_0} = -2.3 \times 10^{16} \text{ Hz}$

$\Delta E = h\nu - h\nu_0 = h\Delta\nu = -95.3 \text{ eV}$

(2) 电子动能 $E_k = \Delta E = 95.3 \text{ eV}$

电子动量 $E^2 = p^2 c^2 + m_0^2 c^4$ 其中 $E = m_0 c^2 + E_k$ 得 $p = 5.27 \times 10^{-24} \text{ kg} \cdot \text{m/s}$

$p \cdot \sin\theta = \frac{h\nu}{c} \sin\phi = 0$ 得 电子运动方向 $\phi = 59.1^\circ$

15-15 (1) 则 $\Delta\lambda = \lambda_c (1 - \cos\theta)$ $\lambda = \lambda_0 + \Delta\lambda = 0.1024 \text{ nm}$

(2) 反冲电子动能 $E_k = \frac{hc}{\lambda_0} - \frac{hc}{\lambda} = 4.66 \times 10^{-17} \text{ J}$

$\frac{h}{\lambda} \sin\theta = \frac{h}{\lambda_0} \sin\phi = 0$ 得 $\phi = 44.05^\circ$

$$15-16 \quad (1) E = h\nu = h\frac{c}{\lambda} \quad p = \frac{h}{\lambda} \quad m_e = \frac{h}{\lambda c}$$

$$E_1 = h\nu_1 = \frac{hc}{\lambda_1} = 1.33 \times 10^{-19} \text{ J}$$

$$p_1 = \frac{h}{\lambda_1} = 4.42 \times 10^{-28} \text{ kg} \cdot \text{m/s}$$

$$m_1 = \frac{h}{\lambda_1 c} = 1.47 \times 10^{-36} \text{ kg}$$

$$(2) E_2 = 3E_1 = 3.99 \times 10^{-19} \text{ J} \quad p_2 = 3p_1 = 1.33 \times 10^{-27} \text{ kg} \cdot \text{m} \cdot \text{s}^{-1} \quad m_2 = 4.41 \times 10^{-36} \text{ kg}$$

$$(3) E_3 = 9.97 \times 10^{-18} \text{ J}, p_3 = 3.31 \times 10^{-26} \text{ kg} \cdot \text{m/s} \quad m_3 = 1.1 \times 10^{-34} \text{ kg}$$

$$(4) E_4 = 1.33 \times 10^{-15} \text{ J} \quad p_4 = 4.42 \times 10^{-24} \text{ kg} \cdot \text{m/s} \quad m_4 = 1.47 \times 10^{-32} \text{ kg}$$

15-18

$$E_n = \frac{E_1}{n^2} \quad E_1 = -13.6 \text{ eV}$$

$$\text{从 } n_i = 5 \text{ 跃迁到 } n_f = 2 \quad h\frac{c}{\lambda} = E_5 - E_2 \quad \text{得 } \lambda = 434 \text{ nm}$$

$$\text{从 } n_f = 2 \text{ 跃迁至游离态} \quad E = -E_2 = 3.4 \text{ eV} \quad \text{提供 } 3.4 \text{ eV}$$

$$15-19 \text{ 知 } E_n - E_1 \leq 12.6 \text{ eV} \quad \text{得 } n \leq 3.68 \quad \text{即 } n \text{ 最大取 } 3$$

故产生 $3 \rightarrow 1, 3 \rightarrow 2, 2 \rightarrow 1$ 谱线

$$15-21. \quad \lambda = \frac{h}{p} \approx \frac{h}{m_0 v} = 1.99 \times 10^{-5} \text{ nm}$$

$$15-22. \quad E^2 = p^2 c^2 + m_0^2 c^4 \quad \lambda = \frac{h}{p} = 1.23 \text{ nm}$$

$$15-23 \quad \text{方均根速率 } \sqrt{\frac{3RT}{M}} \quad \lambda = \frac{h}{p} = \frac{h}{m_i \sqrt{v_i}} = 2.58 \times 10^{-2} \text{ nm}$$

$$15-25. \quad p = \frac{h}{\lambda} \quad p_{\text{电}} = p_{\text{光}} = 3.22 \times 10^{-24} \text{ kg} \cdot \text{m} \cdot \text{s}^{-1}$$

$$\text{光子动能 } E_{\text{光}} = pc = 6.22 \text{ keV}$$

$$\text{电子动能 } E_{\text{电}} = \frac{p^2}{2m} = 37.8 \text{ eV}$$

$$15-27. \quad \Delta x \Delta p \geq \hbar \quad \Delta p = m \Delta v \quad \text{得 } \Delta v = 2.3 \times 10^6 \text{ m} \cdot \text{s}^{-1}$$

15-28 即 $\Delta x = 7.2 \times 10^{-5} \text{ m}$.

$\Delta x \cdot \Delta p \geq \frac{h}{2\pi}$ 得 $\Delta p = 2.93 \times 10^{-20} \text{ kg} \cdot \text{m/s}$, $\Delta v = \frac{\Delta p}{m} = 1.75 \times 10^{-7} \text{ m/s}$

15-29 (1) $\lambda = \frac{h}{mv} = 1.66 \times 10^{-35} \text{ m}$ (2) $\Delta x \cdot m \cdot \Delta v \geq \frac{h}{2\pi}$ $\Delta v = 2.64 \times 10^{-29} \text{ m/s}$

15-30 (1) $\Delta x = b = 0.1 \text{ nm}$ $\Delta x \Delta p_y \geq \frac{h}{2\pi}$ 得 $\Delta p_y = 1.06 \times 10^{-24} \text{ kg} \cdot \text{m/s}$

15-34 (1) $E_1 = \frac{h^2}{8ma^2} = 1.51 \times 10^{-18} \text{ J}$

(2) $\psi(x) = \sqrt{\frac{2}{a}} \sin \frac{n\pi}{a} x$ $\psi(x) = \sqrt{\frac{2}{a}} \sin \frac{2\pi}{a} x$

$|\psi(x)|^2 = \frac{2}{a} \sin^2 \frac{2\pi}{a} x$

$\frac{d|\psi(x)|^2}{dx} = 0$ 得 $\frac{4}{a^2} \pi \sin \frac{4\pi}{a} x = 0$ 得 $x=0, x=\frac{a}{2}, x=a$ 时

即 $x=0, x=0.1 \text{ nm}, x=0.2 \text{ nm}$ 时概率最小为0.

15-36. (i) $E_n = \frac{n^2 h^2}{8ma^2}$ $E = E_2 - E_1 = 112 \text{ eV}$.

(2) $\psi_1(x) = \sqrt{\frac{2}{a}} \sin \frac{\pi}{a} x$ $P_1 = \int_{x_1}^{x_2} |\psi_1(x)|^2 dx = 3.8 \times 10^{-3}$

(3) $\psi_2(x) = \sqrt{\frac{2}{a}} \sin \frac{2\pi}{a} x$ $P_2 = \int_{x_1}^{x_2'} |\psi_2(x)|^2 dx = 0.25$

15-37. (1) l 可能值 0, 1, 2, 3, 4

(2) $m_l = 0, \pm 1, \pm 2, \pm 3, \pm 4, \pm 5$ (3) n 最小为 5

(4) $n=3$ 时 可能有 $2n^2 = 18$ 种状态.