# Sets: Medical Testing Example

#### Video companion

## 1 Example using set theory

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VBS: "very bad syndrome"
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X = set of people in a clinical trial

$$S = \{x \in X : x \text{ has VBS}\}$$
  
$$H = \{x \in X : x \text{ does not have VBS}\}$$

$$X = S \cup H$$
 (you either have VBS or you don't)  
 $S \cap H = \emptyset$  (no one both has and doesn't have it)

Point of medical testing to figure out whether a person is in S or in H

### 2 Test

$$P \neq \{x \in X : x \text{ tests positive for VBS}\}\$$
  
 $N = \{x \in X : x \text{ tests negative for VBS}\}$ 

$$P \cup N = X$$
 (you either test positive or negative)  
 $P \cap N = \emptyset$  (no one tests both positive and negative)

In a perfect world, S would equal P—the sick people would always test positive, and H would equal N—the healthy people would always test negative.

...but this is not always the case.

$$S \cap P$$
 true positive |  $H \cap N$  |  $S \cap N$  |  $H \cap P$  true positive | false negative | false positive | real life outcomes

## 3 Cardinality

 $\frac{|S|}{|X|}$  = proportion of people in the study who do genuinely have VBS

 $\frac{|H|}{|X|}$  = proportion of people in the study without VBS

$$\frac{|S|}{|X|} + \frac{|H|}{|X|} = 1$$

careful in choosing a representative sample, not a biased one, to represent the total population

$\frac{ S \cap P }{ S }$	true positive rate	would like to be close to 1
$\frac{ H {\cap} P }{ H }$	false positive rate	would like to be as small as possible
$\frac{ S \cap N }{ S }$	false negative rate	would like to be as small as possible
$\frac{ H \cap N }{ H }$	true negative rate	would like to be close to 1