



## Odds and ends

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Deterministic Encryption  
Constructions:  
SIV and wide PRP

# Deterministic encryption

Needed for maintaining an encrypted database index

- Lookup records by encrypted index

Deterministic CPA security:

- Security if never encrypt same message twice using same key:  
the pair  $(\text{key}, \text{msg})$  is unique

Formally: we defined deterministic CPA security game

# Construction 1: Synthetic IV (SIV)

Let  $(E, D)$  be a CPA-secure encryption.  $E(k, m ; r) \rightarrow c$

Let  $F: K \times M \rightarrow R$  be a secure PRF

Define:  $E_{\text{det}}(k_1, k_2, m) =$

$$\begin{cases} r \leftarrow F(k_1, m) \\ c \leftarrow E(k_2, m ; r) \\ \text{output } r \end{cases}$$

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**Thm:**  $E_{\text{det}}$  is sem. sec. under det. CPA.

Proof sketch: distinct msgs.  $\Rightarrow$  all  $r$ 's are indist. from random

Well suited for messages longer than one AES block (16 bytes)

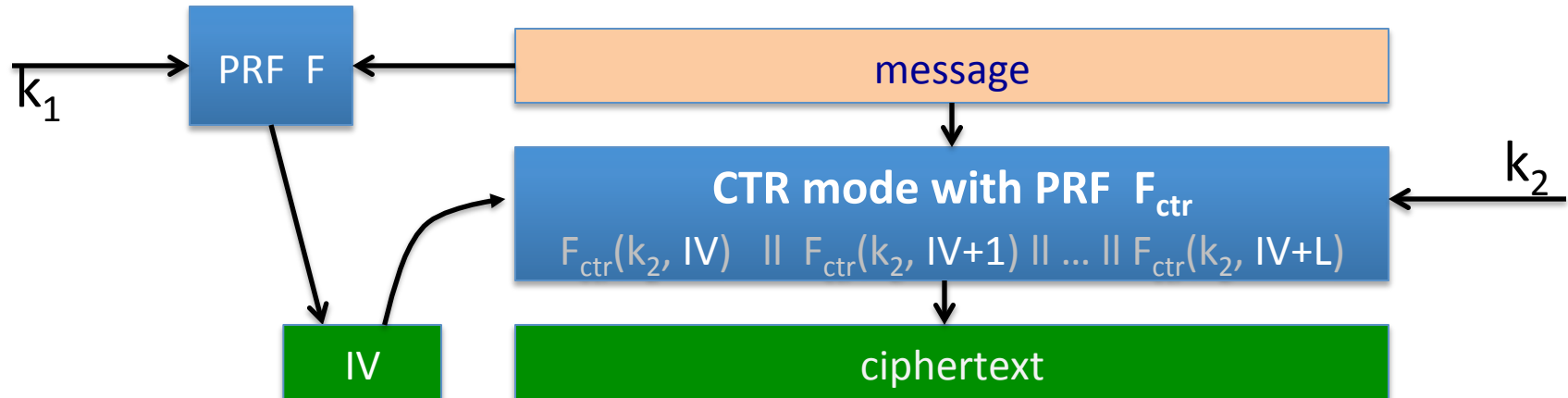
# Ensuring ciphertext integrity

**Goal:** det. CPA security and ciphertext integrity

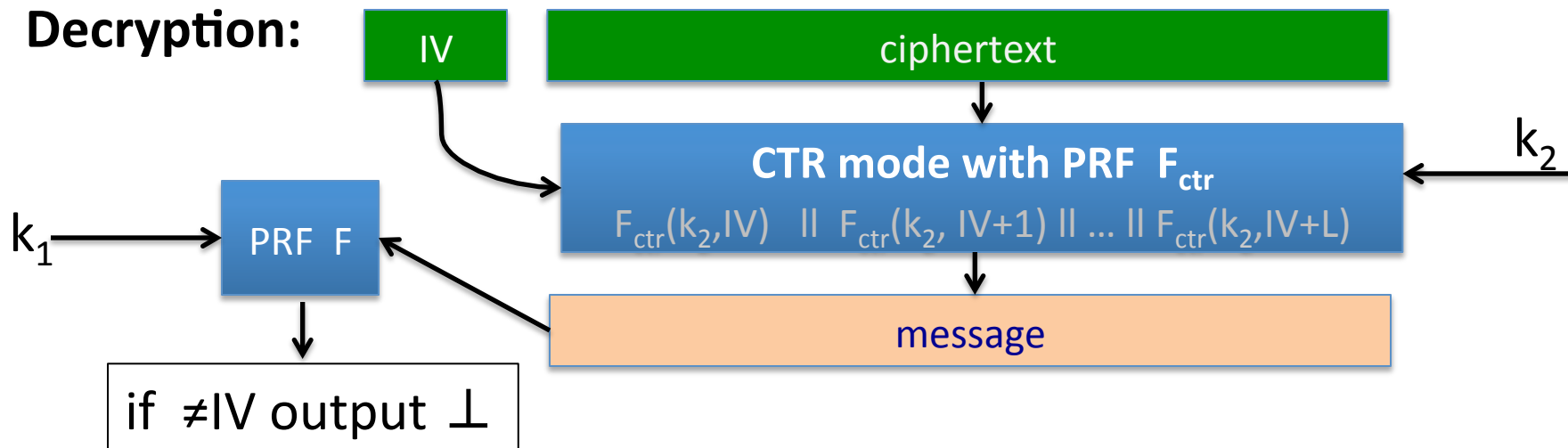
⇒ **DAE: deterministic authenticated encryption**

Consider a SIV special case: SIV-CTR

SIV where cipher is counter mode with rand. IV



# Det. Auth. Enc. (DAE) for free



**Thm:** if  $F$  is a secure PRF and CTR from  $F_{ctr}$  is CPA-secure then SIV-CTR from  $F, F_{ctr}$  provides DAE

# Construction 2: just use a PRP

Let  $(E, D)$  be a secure PRP.  $E: K \times X \rightarrow X$

**Thm:**  $(E, D)$  is sem. sec. under det. CPA .

Proof sketch: let  $f: X \rightarrow X$  be a truly random invertible func.

in  $\text{EXP}(0)$  adv. sees:  $f(m_{1,0}), \dots, f(m_{q,0})$   q random values in X

in  $\text{EXP}(1)$  adv. sees:  $f(m_{1,1}), \dots, f(m_{q,1})$

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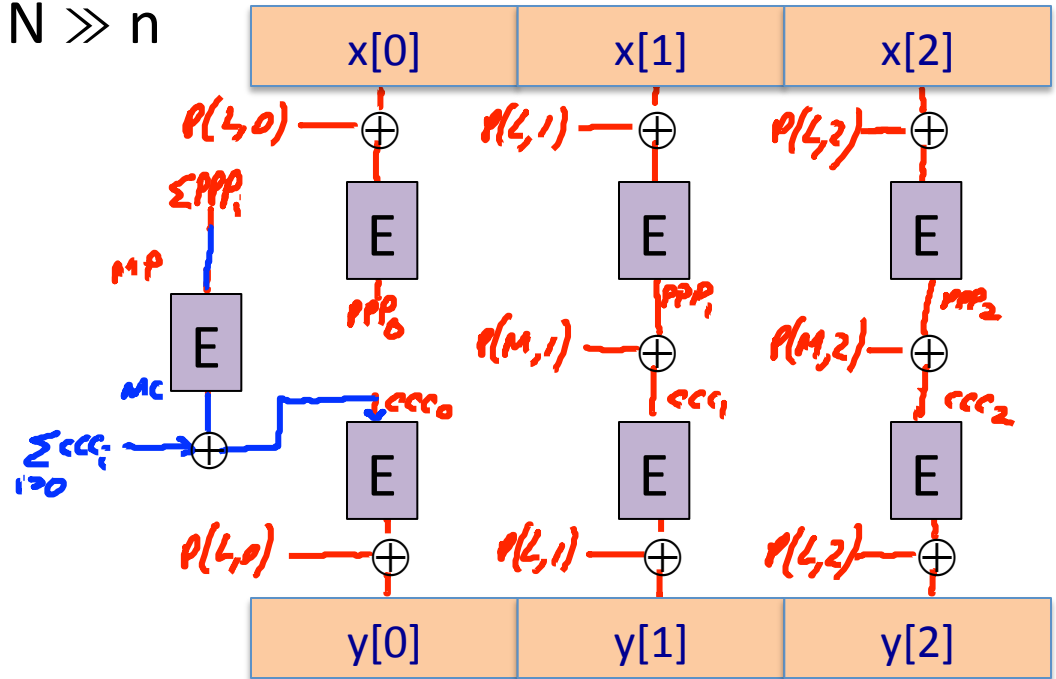
**Using AES:** Det. CPA secure encryption for 16 byte messages.

Longer messages?? Need PRPs on larger msg spaces ...

# EME: constructing a wide block PRP

Let  $(E, D)$  be a secure PRP.  $E: K \times \{0,1\}^n \rightarrow \{0,1\}^n$

**EME:** a PRP on  $\{0,1\}^N$  for  $N \gg n$

$$\text{key} = (K, L)$$
$$M \leftarrow MP \oplus MC$$


## Performance:

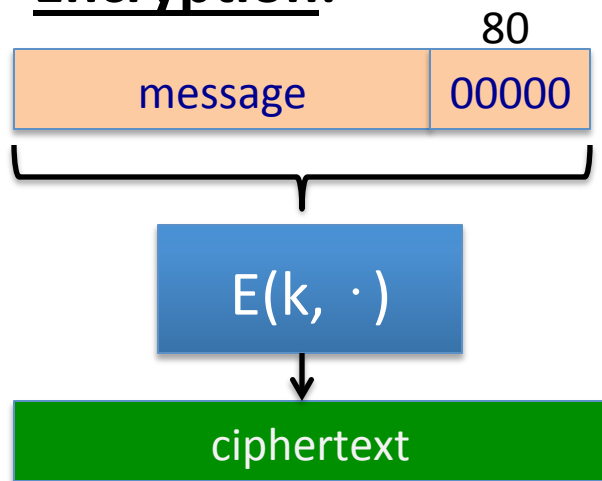
- can be 2x slower than SIV

# PRP-based Det. Authenticated Enc.

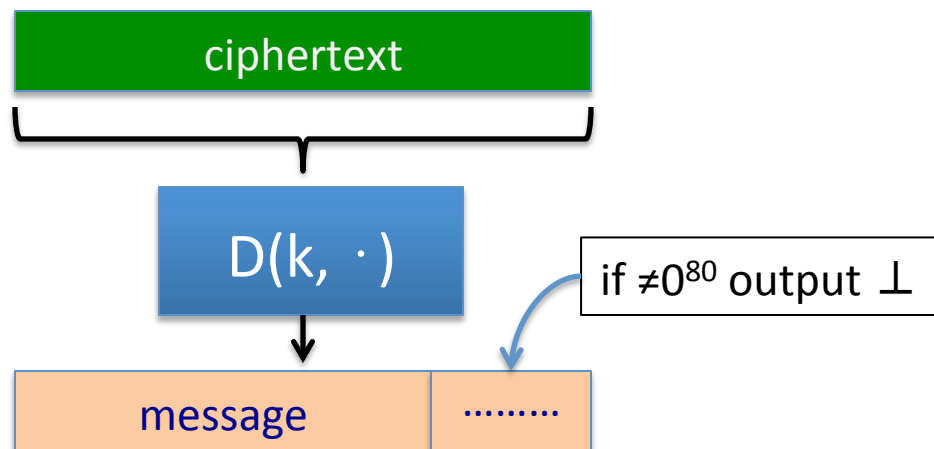
**Goal:** det. CPA security and ciphertext integrity

⇒ **DAE: deterministic authenticated encryption**

## Encryption:



## Decryption:



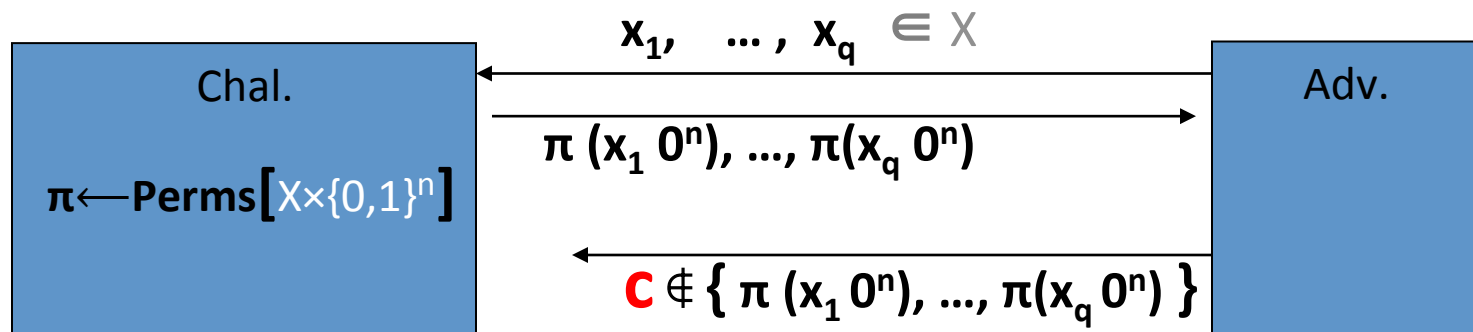


# PRP-based Det. Authenticated Enc.

Let  $(E, D)$  be a secure PRP.  $E: K \times (X \times \{0,1\}^n) \rightarrow X \times \{0,1\}^n$

**Thm:**  $1/2^n$  is negligible  $\Rightarrow$  PRP-based enc. provides DAE

Proof sketch: suffices to prove ciphertext integrity



But then  $\Pr[ \text{LSB}_n( \pi^{-1}(\mathbf{c}) ) = 0^n ] \leq$

End of Segment