

$$\vec{GA} + \vec{GB} + \vec{GC} = \vec{0}$$

in triangle, GBC we have:

$$\vec{GB} + \vec{GC} = 2\vec{GM} \quad (\text{Midpt } [BC])$$

Then $\vec{GA} + \vec{GB} + \vec{GC} = \dots$

$$= 2\vec{GM} + 2\vec{GM} = \vec{0} \quad \text{Proved}$$

the parallel through G to (AB) cuts $[BM]$ at E then $GE \parallel AB$. Compare \vec{EG} and \vec{AB}

Take 2 Δ s MGE and MAB , are similar Δ s

Cor angle \hat{A} , and $GE \parallel AB$.

Ratio of similarity:

$$\frac{MG}{MA} = \frac{ME}{MB} = \frac{GE}{AB}$$

but $\frac{MG}{MA} = \frac{1}{3}$ (property of Centroid divides the median in a $\frac{1}{2}$ ratio)

Then $\frac{GE}{AB} = \frac{1}{3}$ Then $\vec{AB} = 3\vec{GE}$