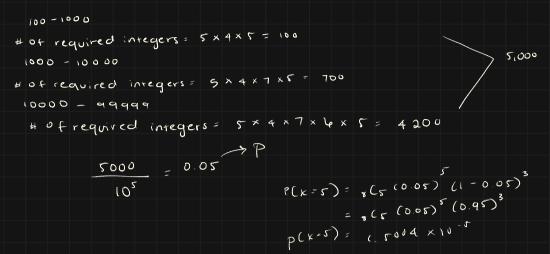
i) A professor has 15 students and during lecture will (uniformly) at random choose a student to answer a question. The professor asks 8 questions during the lecture. What is the probability no student will have to answer more than one question?

An integer from the range 00000 - 99999 is generated uniformly at random. We are interested only in even integers that start with 2 odd digits where all digits are unique. If we randomly generate 8 of these numbers in succession, what is the probability we get exactly 5 numbers that meet our criteria?



You roll 3 six-sided, fair dice. Let A be the event that at least 2 dice show 4 or above. Let B be the event that all 3 dice show the same value. Are A and B independent?

$$P = \frac{4 \times 1365}{4 \times 1287} = \frac{4 \times 1287}{2.54896 \times 10^{6}} = \frac{5148}{2598960} = 0.001980$$

$$E[x7 = \frac{1}{P} = 504.8486]$$

A basketball team has a superstar. When their superstar plays, they win 70% of the time. When their superstar does not play they win 60% of the time. Entering a 5 game stretch, the superstar had been recovering from an injury and said the chance they would play the next 5 games was 75%. You go on a trip to the jungle (no internet access). When you return you find out the team won 4 of the 5 games. What is the probability the superstar played those 5 games? You may assume the superstar doesn't get injured during those games (either they play all or none of the 5).

P (win | superstar) = 0.7 p (superstar) = 0.75 p(win | no superstar) = 0.5

P(4/5 | superstay plays) = C(5,4) × 0.74 × 0.3 5 × 0.2401 × 0.3 = 0.36015

P (415 | no superstay) = c (5,4) × 0.55 5 × 0.03125 = 0.15 625

 $P(win 4.15) = 0.15625 \times 0.25 + 0.36015 \times 0.75 = 0.309175$ $P(superstar | win 4.15) = 0.36015 \times 0.75 = 0.8137$ 0.309175