

Subject :

No. :

Date :/...../.....

1. $Q = f(L, K) = L^\alpha K^\beta$, $\alpha, \beta > 0$

1) $AP_L = \frac{Q}{L} = \frac{L^\alpha K^\beta}{L} = L^{\alpha-1} K^\beta$

2) $AP_K = \frac{Q}{K} = \frac{L^\alpha K^\beta}{K} = L^\alpha K^{\beta-1}$

3) $MP_L = \frac{dQ}{dL} = \alpha L^{\alpha-1} K^\beta$

4) $MP_K = \frac{dQ}{dK} = \beta L^\alpha K^{\beta-1}$

5) $MRTS = \frac{-dK}{dL} = \frac{MP_L}{MP_K} = \frac{\alpha L^{\alpha-1} K^\beta}{\beta L^\alpha K^{\beta-1}} = \frac{\alpha K}{\beta L}$

6) $\epsilon^L = \frac{\frac{dQ}{Q}}{\frac{dL}{L}} = \frac{\frac{dQ}{dL}}{\frac{Q}{L}} = \frac{MP_L}{AP_L} = \frac{\alpha L^{\alpha-1} K^\beta}{L^{\alpha-1} K^\beta} = \alpha$

7) $\epsilon^K = \frac{\frac{dQ}{Q}}{\frac{dK}{K}} = \frac{\frac{dQ}{dK}}{\frac{Q}{K}} = \frac{MP_K}{AP_K} = \frac{\beta L^\alpha K^{\beta-1}}{L^\alpha K^{\beta-1}} = \beta$

8) $\epsilon^Q = \frac{\frac{dQ}{Q}}{\frac{dK}{K}} = \frac{\frac{dQ}{dK}}{\frac{Q}{K}} = \frac{MP_K}{AP_K} = \frac{\beta L^\alpha K^{\beta-1}}{L^\alpha K^{\beta-1}} = \beta$

9) $\epsilon^{LK} = \epsilon^L + \epsilon^K = \alpha + \beta$

2. 設生產函數 $Q = 3K + 2L$

K : 資本 L : 勞動 Q : 產出

1) 函數呈現固定規模報酬 - ✓

當 L 、 K 增加 n 倍, nL 和 nK , 生產函數

$$\text{為 } F(nL, nK) = 2(nL) + 3(nK)$$

$$= n(2L + 3K) = nQ$$

故呈現固定規模報酬

2) ✗

$$MP_L = \frac{dQ}{dL} = 2, \quad MP_K = \frac{dQ}{dK} = 3$$

資本、勞動的邊際生產力皆固定

故無邊際生產力遞減

3) ✓

$$MRTS = \frac{MP_L}{MP_K} = \frac{2}{3}$$

故技術替代率成固定值。