

Subject :

No. :

Date :

隨堂 11. $Q = 10L^{0.5}K^{0.5}$ $W = r = 10$

$Q^* = 100LK$

$L^* = \frac{Q^*}{100K}$

1A) 短期成本函數, 變動成本函數, 邊際成本函數

$$STC = 10 \times \frac{Q^*}{100K} + 10K_0 = \frac{Q^*}{10K} + 10K_0$$

$$SAC = \frac{STC}{Q} = \frac{Q}{10K_0} + \frac{10K_0}{Q}$$

$$SMC = \frac{dSTC}{dQ} = 2 \frac{Q}{10K} = \frac{Q}{5K}$$

1B) 反推總成本函數

$$\frac{dSTC}{dK} = \frac{-Q^*}{10K^2} \quad \pi_0 = 0 \Rightarrow K^* = \frac{Q}{10}$$

$$STC(K=K^*) = \frac{Q^*}{10 \frac{Q}{10}} + 10 \frac{Q}{10} = Q + Q = 2Q$$

隨堂 12. 產量 20, AC, AVC 各 10 元

產量 40, AC, AVC 各 ?

$$SAC = AVC + AFC$$

$$AFC = AC - AVC = 10$$

$$TFC = 10 \times 20 = 200$$

$$\frac{TFC}{Q} = AFC \Rightarrow \frac{200}{40} = 5$$

隨堂 13. $MC = 10Q$ $FC = 100$ 10 單位下總成本

$$STC = \int_0^{10} 10Q dQ = 10 \int_0^{10} Q dQ = 10 \frac{1}{2} Q^2 \Big|_0^{10}$$

$$= 5 Q^2 \Big|_0^{10} = 500 - 0 = 500$$

$$STC = TVC + FC = 500 + 100 = 600$$

Subject: 3/31

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隨堂 9. 技術 A: $q = \min\{L/2, K/4\}$ 設 $w=1$
技術 B: $q = \min\{L/4, K/2\}$ $r=2$

(A) 分別購買兩種技術, 總成本函數.

$$A: q = L/2 = K/4 \Rightarrow L = 2q, K = 4q$$

$$C = 1 \times 2q + 2 \times 4q = 10q$$

$$TC_A = 10q + 40$$

$$B: q = L/4 = K/2 \Rightarrow L = 4q, K = 2q$$

$$C = 1 \times 4q + 2 \times 2q = 8q$$

$$TC_B = 8q + 100$$

(B) 若公司生產 20 單位, 應購買.

$$TC_A = 10q + 40 = 10 \times 20 + 40 = 240 \quad \checkmark$$

$$TC_B = 8q + 100 = 8 \times 20 + 100 = 260$$

(C) 若公司生產 40 單位, 應購買.

$$TC_A = 10q + 40 = 10 \times 40 + 40 = 440$$

$$TC_B = 8q + 100 = 8 \times 40 + 100 = 420 \quad \checkmark$$

由在產量低於多少時, 應購買 A.

$$TC_A < TC_B$$

$$10q + 40 < 8q + 100$$

$$2q < 60$$

$$q < 30$$