videos on linear algebra

The Essence of Linear Algebra series (<u>3blue1brown</u>) linked below is an excellent resource for reviewing (or learning) basic concepts of linear algebra. The most important concepts to review are vectors (Chapter 1-2), linear transformations and matrices (Chapter 3), matrix multiplication (Chapter 4), non-square matrices as transformations between dimensions (Chapter 8), and dot products (Chapter 9).

Please review these.

https://www.youtube.com/playlist?list=PLZHQObOWTQDPD3MizzM2xVFitgF8hE_ab

Homework 4

posted on Brightspace due Mon (Oct 3) at 11:59pm*

(pushed back so I'm not lecturing about topics for a homework due two days later) (due late on Mon so people can ask last-minute questions that Mon after class)

Homework4.pdf (written description)
Homework4.ipynb (notebook to use for your solution)
difdata.csv

^{*} most homeworks will continue to be due at class time

download from Brightspace

FileIO.ipynb LogicalIndexing.ipynb

some basic file I/O

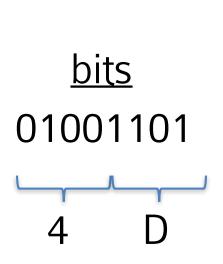
FileIO.ipynb

Every file is a "binary" file in the sense that its contents is merely bits (0s and 1s) and bytes (8 bits).

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```
e.g.,
<u>bits</u>
01001101
```

Every file is a "binary" file in the sense that its contents is merely bits (0s and 1s) and bytes (8 bits).



binary	hex
0000	0
0001	1
0010	2
0011	3
0100	4
0101	5
0110	6
0111	7
1000	8
1001	9
1010	Α
1011	В
1100	C
1101	D
1110	E
1111	F

Every file is a "binary" file in the sense that its contents is merely bits (0s and 1s) and bytes (8 bit).

binary (base 2) bits	hexadecimal (base 16) <u>bytes</u>	ASCII character
01001101	4D	M
01101101	6D	m
00100011	23	#

ASCII "binary" files are interpreted universally (8 bit). Unicode is a 16 or 32 bit extension (non-western characters, emojis, other) - ASCII is a subset of Unicode.

Dec	Н	Oct	Cha	r	Dec	Нх	Oct	Html	Chr	Dec	Нх	Oct	Html	Chr	Dec	Нх	Oct	Html Chr	×
0	0	000	NUL	(null)	32	20	040	6#32;	Space	64	40	100	@	0	96	60	140	a#96;	•
1	1	001	SOH	(start of heading)	33	21	041	%#33 ;	!	65	41	101	«#65;	A	97	61	141	a#97;	a
2				(start of text)	34	22	042	%#34 ;	**	66	42	102	B	В	98	62	142	6#98; 1	0
3	3	003	ETX	(end of text)	35	23	043	%#35 ;	#	67	43	103	<u>4#67;</u>	C	99	63	143	6#99; (0
4	4	004	EOT	(end of transmission)	36	24	044	%#36 ;	ş	68	44	104	«#68;	D	100	64	144	6#100; ¢	4
5	5	005	ENQ	(enquiry)	37	25	045	%#37;	*	69	45	105	%#69;	E	101	65	145	e ¢	2
6	6	006	ACK	(acknowledge)				4#38;					%#70;					a#102; 1	
7	7	007	BEL	(bell)	39			%#39 ;		71			6#71;			-		a#103;	
8		010		(backspace)	40			440;		72			6#72;					4#104; 1	
9	9	011	TAB	(horizontal tab)	41			6#41;		73			6#73;					a#105;	
10		012		(NL line feed, new line)				6#42;					a#74;					a#106;	
11		013		(vertical tab)				6#43;		P 1000			6#75;					a#107; }	
12		014		(NP form feed, new page)				a#44;			1		L					a#108;	
13		015		(carriage return)				a#45;	10. 10.				6#77;					4#109; 1	
14		016		(shift out)				a#46;		1000			N					n 1	
15	_	017		(shift in)				6#47;					O					a#111; (
			DLE	(data link escape)				6#48;					P					6#112; <u>1</u>	
				(device control 1)				a#49;					Q					a#113; (
			DC2	(device control 2)				%#50 ;					R					6#114; 1	
		023		(device control 3)	1000			6#51;					S					6#115;	
				(device control 4)				6#52;	_				«#8 4 ;					a#116; t	
				(negative acknowledge)				%#53 ;					U					6#117; \	
				(synchronous idle)				4#54;	_				V					6#118; V	
				(end of trans. block)				%#55 ;					W					6#119; T	
				(cancel)				%#56 ;					X					6#120; >	
		031		(end of medium)	57			%#57 ;					«#89;					y <u>}</u>	
		032		(substitute)				%#58 ;					6#90;			-		z 2	
		033		(escape)	59			%#59 ;					[6#123;	
		034		(file separator)				«#60;					6#92;					«#124;	
		035		(group separator)				4#61;					6#93;	-				a#125;	
		036		(record separator)				«#62;					6#94;					~ ·	
31	1F	037	US	(unit separator)	63	3F	077	?	?	95	5F	137	6#95;	_				%#127; <mark>I</mark>	

Source: www.LookupTables.com

ASCII files are read by every operating system and many many programs exactly the same way.

text files (.txt)

the extension (.txt) by itself doesn't make it a "text file" (ASCII), but can give a clue to the O/S about what default program to use to read the file

configuration files (.ini)

batch files (.bat)

scripts and source code (.m, .c, .py)

notebooks (.ipynb)

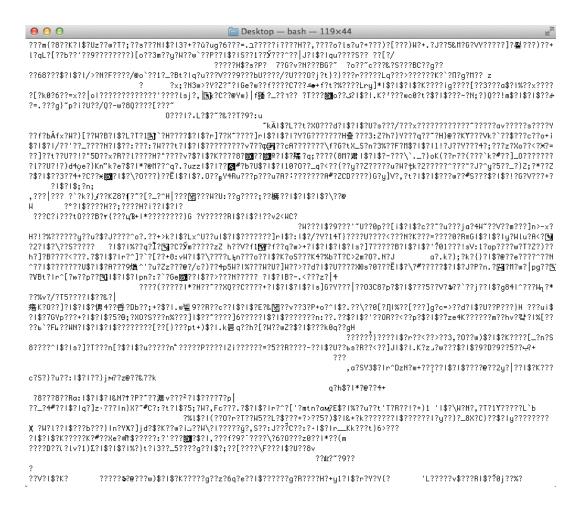
if you have a data file (or program code) that is in ASCII format you are guaranteeing it can be read by anyone anywhere in the world (likely "forever")

binary files are also made of bits and bytes but the way those bits and bytes are interpreted depends on the particular O/S and program

you either need to have the program (and perhaps the O/S) that created the file or hope that a newer version (or a different program) can read those files

e.g., I have some analysis files from graduate school created by a program that hasn't existed for a decade e.g., I couldn't read Microsoft Word files created 15 years ago in Microsoft Word by Microsoft Word now

If you open a binary file in an application that doesn't understand it, it probably defaults to an ASCII interpretation, which could be garbage ...



basic File I/O in Python

(and a bit on iterators and navigating arrays)

variety of file I/O approaches in Python

human-readable

 CSV file (ASCII text, comma-delimited) general-purpose

human-readable

- JSON file (ASCII text, more complex) general-purpose
- numpy.save/numpy.load create/read.npy files (binary)
 Python-specific
- pickle and marshal (binary)
 Python-specific
- HDF5 format (binary) general-purpose

of course there are other binary, general-purpose file formats for images (.jpg, .gif, .tif, etc.), audio (.mp3, .wav, etc.), and video (.mp4, .mov, etc.)

CSV = "Comma*-Separated Value" format

* a different delimiter can be specified

```
TP, JA, WO, WM, KL, WS, BB, EC, VB
0.89, 0.91, 0.78, 0.82, 0.74, 0.81, 0.88, 0.92, 0.83
0.71, 0.73, 0.81, 0.73, 0.76, 0.83, 0.7, 0.72, 0.83
451, 515, 574, 614, 550, 643, 634, 514, 613
723, 689, 712, 613, 812, 743, 690, 719, 772
```

file needs to be read row by row and parsed (following the delimiters) into the right data structures with the right types

spreadsheets (Excel, Numbers) can read/write CSV format many analysis programs read/write CSV format

** lose formulas and formatting when doing so

CSV = "Comma-Separated Value" format

critically, they're also ASCII (text) file format (can be read by any program that can read text files) - raw text files, JSON, XML are other ASCII formats

Best Practices: always avoid saving important information (only) in binary (non-ASCII) format (especially data)

binary files can only be read by the applications that created them (and those applications might stop working)

e.g., I recently accessed data (text) files I collected 30 years ago

can save 1-dimensional and 2-dimensional data in a CSV file (easily)

```
import csv
                                 opens file
                                 for writing
a robust way to open files in Python (prevent
issues if they are not closed properly)
with open('sinit.csv', 'w') as fp: fp is the "file pointer"
      csvwriter = csv.writer(fp)
                                              creates a "writer" object to fp
      csvwriter.writerow(sinit)
                                               writes 1D object to a row in fp
not using with, you would need to call fp.close()
with open('acc.csv', 'w') as fp:
      csvwriter = csv.writer(fp)
      csvwriter.writerows(acc)
                                               writes 2D object to rows in fp
```

with in Python for file I/O

```
with in Python (for files) does opening and closing of files and takes care of exception handling gracefully (if file not found, or an error) with open('sinit.csv', 'w') as fp:
```

stuff here

stuff here

- •
- •
- •

files are external resources with respect to Python (with works with other kinds of resources) - they do a lot of things out of your control (e.g., writing is often buffered, and if you fail to properly close a file, information buffered but not written will

not be added to the file) - with takes care of that for you

https://realpython.com/python-with-statement/

read data in a CSV file

```
opens file
for reading

with open('sinit.csv', 'r') as fp:
    csvreader = csv.reader(fp, delimiter=',')
    for row in csvreader: iterates rows of file
        Sinit = row
        row is a list of strings (that were separated by the delimiter)
```

```
Best Practices
Nsubj = len(Sinit)
                                  meaningful variable names
Ncond = 2
                                   parameterize dimensions
Acc = np.zeros((Ncond, Nsubj))
                                    of arrays rather than
Rts = np.zeros((Ncond, Nsubj))
                                      hard-code them
with open('acc.csv', 'r') as fp:
    csvreader = csv.reader(fp, delimiter=',')
    for i, row in enumerate(csvreader):
         for j in range(Nsubj):
             Acc[i,j] = float(row[j])
```

```
Nsubj = len(Sinit)
Ncond = 2
Acc = np.zeros((Ncond, Nsubj))
Rts = np.zeros((Ncond, Nsubj))
with open('acc.csv', 'r') as fp:
    csvreader = csv.reader(fp, delimiter=',')
    for i, row in enumerate(csvreader):
        for j in range(Nsubj):
            Acc[i,j] = float(row[j])
```

```
Nsubj = len(Sinit)
Ncond = 2
Acc = np.zeros((Ncond, Nsubj))
Rts = np.zeros((Ncond, Nsubj))
with open('acc.csv', 'r') as fp:
    csvreader = csv.reader(fp, delimiter=',')
    i = 0
                                     this all does
    for row in csvreader:
                                    the same thing
        for j in range(Nsubj):
             Acc[i,j] = float(row[j])
        i += 1
```

```
Nsubj = len(Sinit)
Ncond = 2
Acc = np.zeros((Ncond, Nsubj))
Rts = np.zeros((Ncond, Nsubj))
with open('acc.csv', 'r') as fp:
    csvreader = csv.reader(fp, delimiter=',')
    for i, row in enumerate(csvreader):
         for j in range(Nsubj):
             Acc[i,j] = float(row[j])
    enumerate() returns the index and the next item
```

```
with open('acc.csv', 'r') as fp:
opens/closes file gracefully
      csvreader = csv.reader(fp, delimiter=',')
      creates an "iterator" (like a little engine) that will read file line-by-line
      for i, row in enumerate(csvreader):
      0.89, 0.91, 0.78, 0.82, 0.74, 0.81, 0.88, 0.92, 0.83
      0.71,0.73,0.81,0.73,0.76,0.83,0.7,0.72,0.83
      first pass through, row contains the first line of the file
            for j in range(Nsubj):
                   Acc[i,j] = float(row[j])
                   0.89, 0.91, 0.78, 0.82, 0.74, 0.81, 0.88, 0.92, 0.83
                   0.71,0.73,0.81,0.73,0.76,0.83,0.7,0.72,0.83
                   float(row[j]) returns jth element on the row as a float
                  Acc[i,j] is building a numpy array containing accuracy data
                   indexed by subject i and condition j
```

```
with open('acc.csv', 'r') as fp:
opens/closes file gracefully
      csvreader = csv.reader(fp, delimiter=',')
      creates an "iterator" (like a little engine) that will read file line-by-line
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indexed by subject i and condition j

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      0.89, 0.91, 0.78, 0.82, 0.74, 0.81, 0.88, 0.92, 0.83
      0.71,0.73,0.81,0.73,0.76,0.83,0.7,0.72,0.83
     first pass through, row contains the first line of the file
            for j in range(Nsubj):
                  Acc[i,j] = float(row[j])
                  0.89, 0.91, 0.78, 0.82, 0.74, 0.81, 0.88, 0.92, 0.83
                  0.71,0.73,0.81,0.73,0.76,0.83,0.7,0.72,0.83
                  float(row[j]) returns jth element on the row as a float
```

Acc[i,j] is building a numpy array containing accuracy data indexed by subject i and condition j

can write out all the data structures to one file

```
with open('data.csv', 'w') as fp:
    csvwriter = csv.writer(fp)
    csvwriter.writerow(sinit)
    csvwriter.writerows(acc)
    csvwriter.writerows(rts)
```

```
data.csv — Edited
```

```
TP, JA, WO, WM, KL, WS, BB, EC, VB
0.89, 0.91, 0.78, 0.82, 0.74, 0.81, 0.88, 0.92, 0.83
0.71, 0.73, 0.81, 0.73, 0.76, 0.83, 0.7, 0.72, 0.83
451, 515, 574, 614, 550, 643, 634, 514, 613
723, 689, 712, 613, 812, 743, 690, 719, 772
```

file needs to be read row by row and parsed into the right data structures with the right types

```
need to read them in the same way as written out
with open('data.csv', 'r') as fp:
                                                   if file other than CSV format, you
    csvreader = csv.reader(fp, delimiter=',') would not use csv.reader()
    Sinit = next(csvreader)
                                next() returns the next item of an iterator
    Nsubj = len(Sinit)
    Ncond = 2
    Acc = np.zeros((Ncond, Nsubj))
    Rts = np.zeros((Ncond, Nsubj))
    for i in range(Ncond):
        row = next(csvreader)
         for j in range(Nsubj):
             Acc[i,j] = float(row[j])
    for i in range(Ncond):
        row = next(csvreader)
         for j in range(Nsubj):
             Rts[i,j] = float(row[j])
```

Homework 4

Q1 first **(a)** asks you to save HDR(t) and t (plus some other things) from Homework 3^{*} as a CVS file (in a particular format) using the techniques I just went over and second **(b)** asks you to read in that CSV file into the appropriate variables and plot it (using your code from Homework 3^{*}).

Your CSV file should have the follow structure:

 $1^{\rm st}$ line should be an informative note (< 50 characters) about what the file contains.

 2^{nd} line is the <u>number of time steps</u> in *HDR(t)*.

3rd line should be the <u>names</u> of the parameters of the HDR (from Homeworks 2 and 3), separated by commas.

4th line should be the <u>values</u> of the parameters (from Homeworks 2 and 3), separated by commas.

The remaining lines should be each value of t and its corresponding HDR(t), separated by commas (in other words, if you had 1000 values of t and HDR(t) in your numpy arrays, these should be 1000 lines in the CSV file).

^{*} if your code from Homework 3 did not work, you should correct it based on the comments from Jason (seeing me or Jason if you need help)

an example of reading and analyzing some behavioral data using numpy arrays

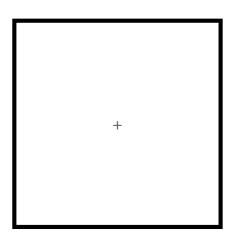
operations on numpy arrays

numpy arrays contain "data" (of the same type); in the context of psychology and neuroscience, these could be

- behavioral data (e.g., choices, response times, as a function of subjects, conditions, trials) from an experiment
- 1D signal (time-series) (e.g., intracellular, extracellular, scalp voltage as a function of time) from neural recordings
- 2D signal (time-series) (e.g., N electrical channels x T time steps), 3D signal (e.g., S subjects x N channels x T time)
- 3D eye movements with (x, y) gaze direction by time
- 2D B/W image with (x, y) intensity, 3D color images with (x,y) intensity for R, G, and B color channels
- 3D functional or anatomical brain scan (x, y, z)
- 4D functional or anatomical brain scan (x, y, z) by time steps

a simple experiment (visual search)

Trial 1

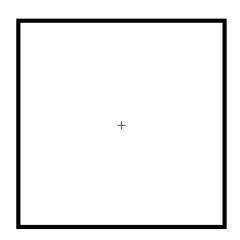


time



a simple experiment (visual search)

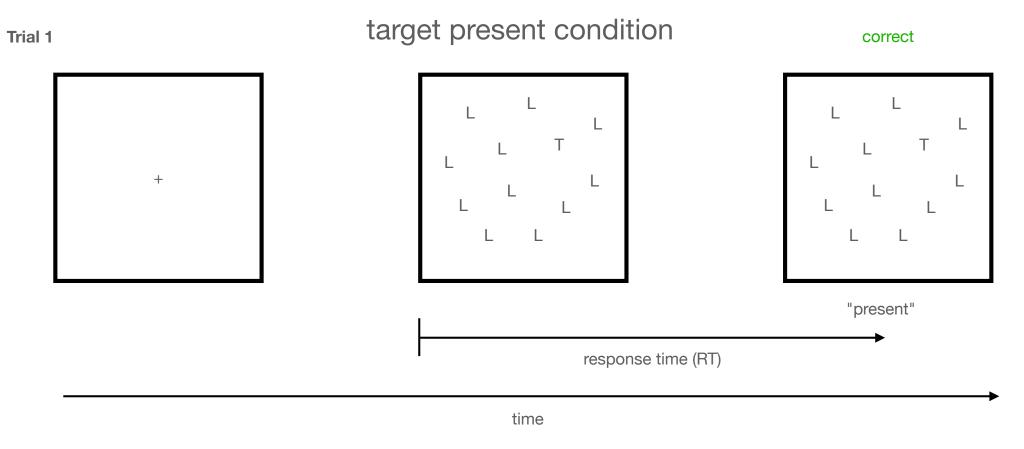
Trial 1



time

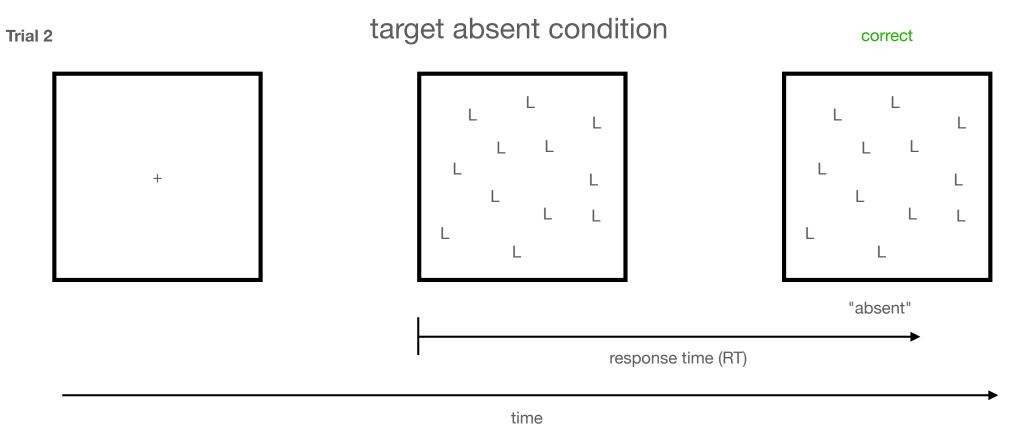


a simple experiment (visual search)



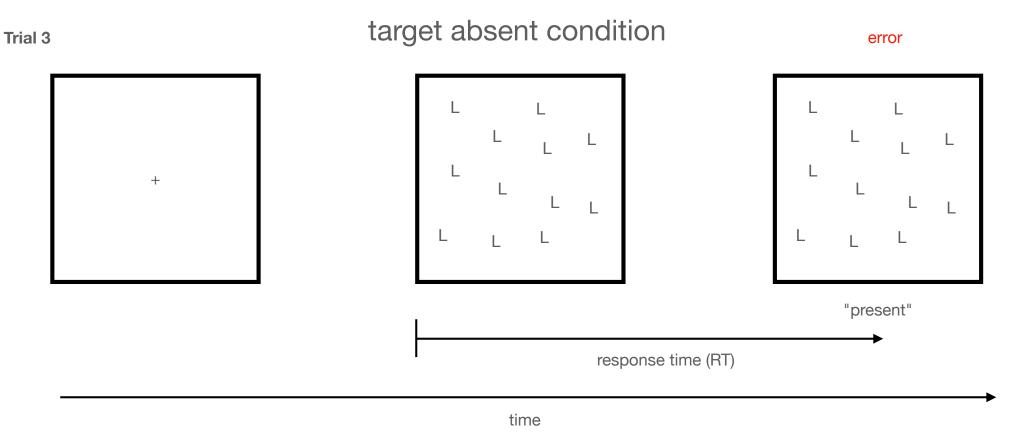


a simple experiment (visual search)





a simple experiment (visual search)





(simulated) data from an experiment with 2 conditions

difdata.csv (ASCII text file in CSV format)

one subject's data

correct (1) error (0) trial # each line (except first) condition response time (1 or 2)(in sec) present absent # trials 1000 0,1,0,0.386 1,1,1,0.520 2,1,0,0.388 3,2,1,0.419 4,1,1,0.530 5,1,0,0.416 6,1,1,0.393 7,2,1,0.661 8,2,1,1.095 9,1,1,0.514

how to write code that processes this file difdata.csv (ASCII text file)

(0) get csv

(1) open file for reading

correct (1)
trial # error (0)

each line
(except first)

condition response time
(1 or 2)

contract (1)
trial # error (0)

condition response time
(1 or 2)

trials

1000
0,1,0,0.386
1,1,1,0.520
2,1,0,0.388
3,2,1,0.419
4,1,1,0.530
5,1,0,0.416
6,1,1,0.393
7,2,1,0.661
8,2,1,1.095
9,1,1,0.514

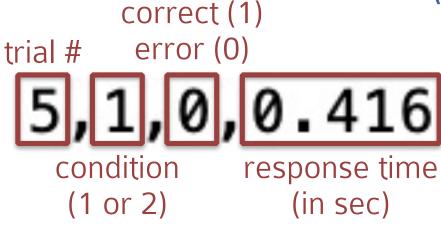
(2) read # trials

how to write code that processes this file difdata.csv (ASCII text file)

(0) get csv

(1) open file for reading

each line (except first)



trials

0,1,0,0.386
1,1,1,0.520
2,1,0,0.388
3,2,1,0.419
4,1,1,0.530
5,1,0,0.416
6,1,1,0.393
7,2,1,0.661
8,2,1,1.095

(2) read # trials

(3) read each line, filling arrays with condition, response, RT

later, we'll do more

see FileIO.ipynb

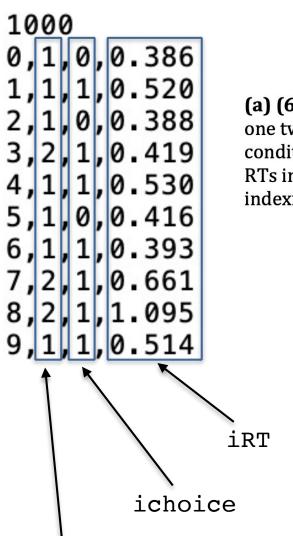
```
import csv
                            import numpy as np
                            with open('difdata.csv', 'r') as fp:
                                # create the "reader" object
                                csvreader = csv.reader(fp, delimiter=',')
                                # get a line of the file
1000
                             row = next(csvreader)
                                # that first line is the # trials
                                Ntrials = int(row[0])
                                # using # trials, preallocate np arrays to hold condition, choice, and RT
                                icondition = np.zeros(Ntrials, dtype=int)
                                ichoice = np.zeros(Ntrials, dtype=int)
                                iRT
                                           = np.zeros(Ntrials, dtype=float)
                                # loop over all trials (all remaining lines in the file)
                                for i, row in enumerate(csvreader):
                                    icondition[i] = int(row[1])
                                    ichoice[i]
                                                 = int(row[2])
                                    iRT[i]
                                                  = float(row[3])
```

read in the data

icondition

ichoice

iRT



icondition

Homework 4

(a) (6 points) Following the discussion from class, I want you to partition the data so that one two-dimensional array that holds the choices in condition 1 and the choices in condition 2 and another two-dimensional array that holds the RTs in condition 1 and the RTs in condition 2. First, do this using for loops. Second, do this using logical (Boolean) indexing.

one thing we might want to do is divide up the choice and RT data by condition, creating separate arrays for condition 1 and for condition 2 - how to do that?

logical (Boolean) indexing

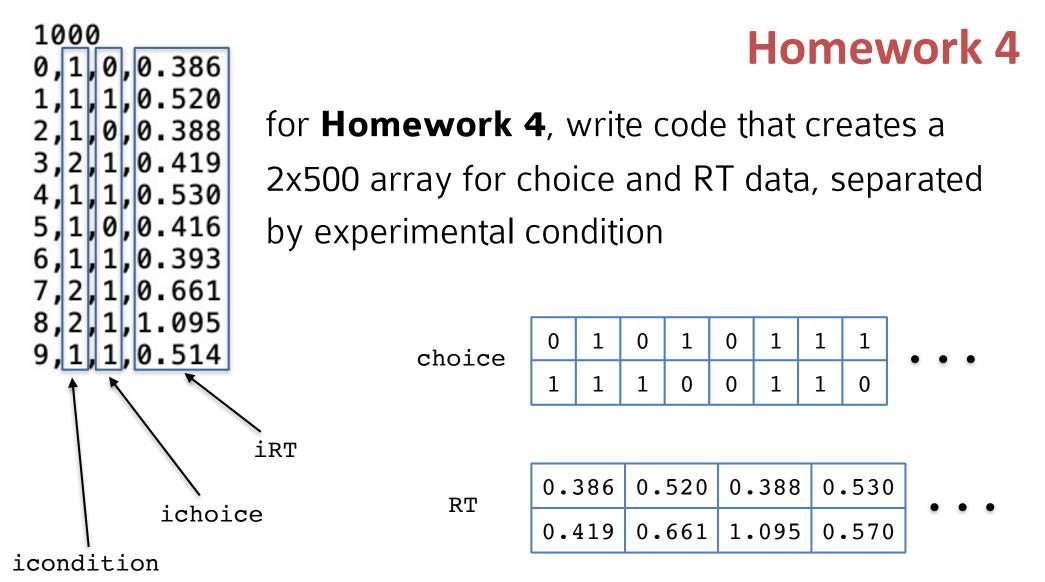
```
a = np.array([1, 2, 3, 4, 5])
b = np.array([False, True, False, False, True])
print(a[b]) a and b need to be the same size
```

see LogicalIndexing.ipynb

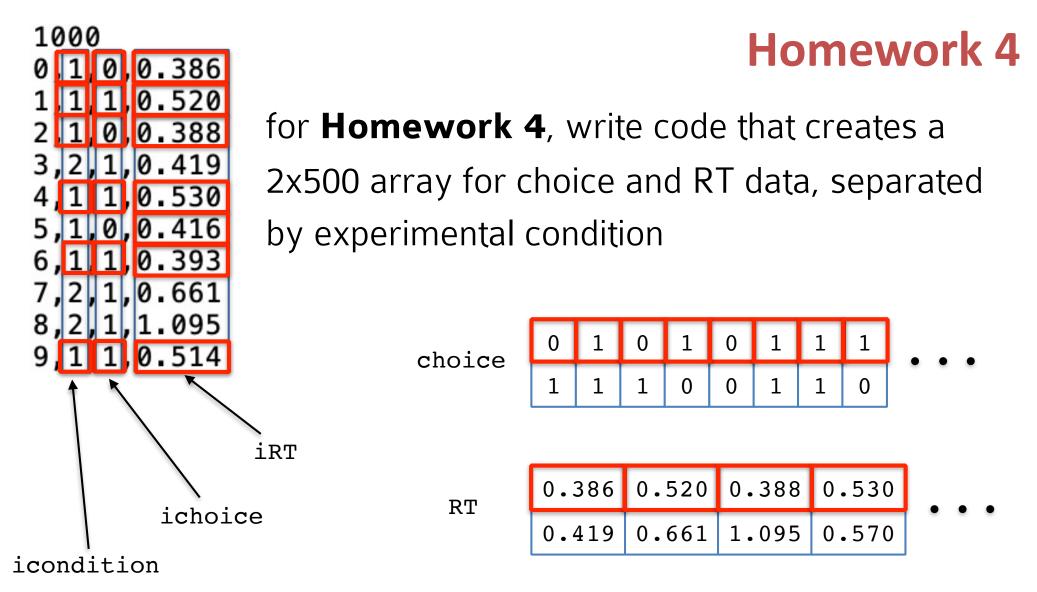
1000 0.386 iRT ichoice icondition

one thing we might want to do is divide up the choice and RT data by condition, creating separate arrays for condition 1 and for condition 2 - how to do that?

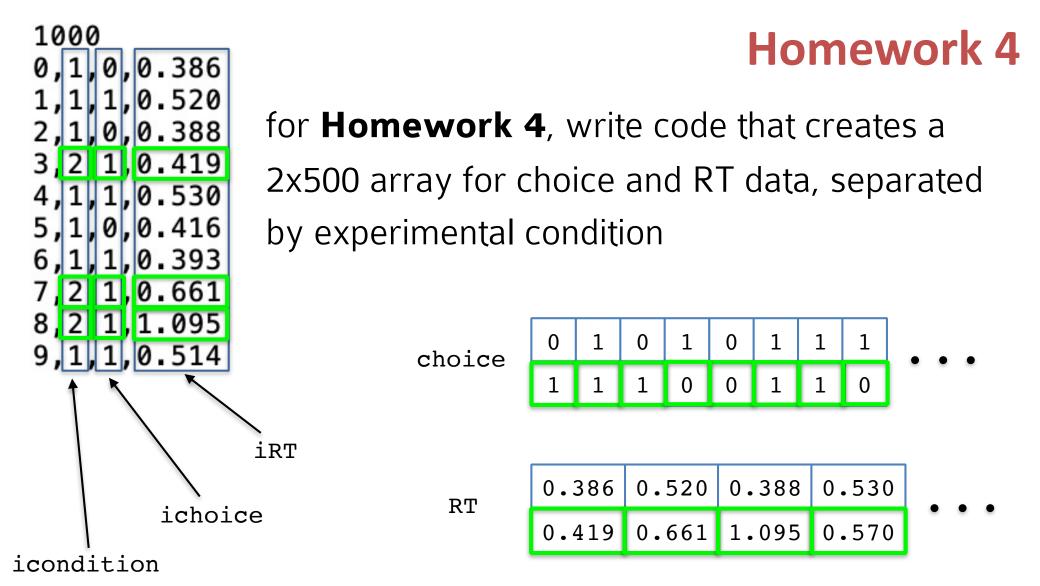
Homework 4



one thing we might want to do is divide up the choice and RT data by condition, creating separate arrays for condition 1 and for condition 2 - how to do that?



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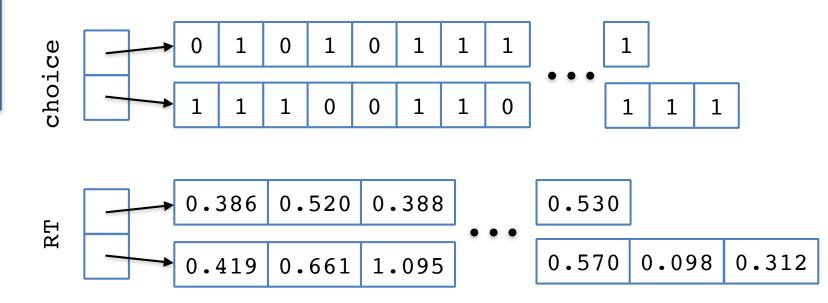


one thing we might want to do is divide up the choice and RT data by condition, creating separate arrays for condition 1 and for condition 2 - how to do that?

1000 0, 1, 0, 0.386 1, 1, 1, 0.520 2, 1, 0, 0.388 3, 2, 1, 0.419 4, 1, 1, 0.530 5, 1, 0, 0.416 6, 1, 1, 0.393 7, 2, 1, 0.661 8, 2, 1, 1.095 9, 1, 1, 0.514

Homework 4

how would you remove "outliers", for example trials where RT was outside some bound (e.g., RT<0.100 or RT>1.000)



one thing we might want to do is divide up the choice and RT data by condition, creating separate arrays for condition 1 and for condition 2 - how to do that?

1000 0,1,0,0.386 1,1,1,0.520 2,1,0,0.388 3,2,1,0.419 4,1,1,0.530 5,1,0,0.416 6,1,1,0.393 7,2,1,0.661 8,2,1,1.095 9,1,1,0.514

Homework 4

(b) (6 points) Following the discussion from class, I want you to remove "outliers" based on RT, in this case trials where RT is outside some bound (RT<0.100 or RT>1.000). This will result in a list of arrays for the choices with outlier trials removed and a list of arrays for the RTs with the outlier trials removed. **First**, do this using for loops. **Second**, do this using logical (Boolean) indexing. Remember from discussion in class that here you will not be able to use a 2x500 numpy array because the number of resulting trials after removing outliers will be unequal (instead, use a list of numpy arrays).

Command-Line Input

command-line input

```
input a string
name = input('Enter Name :')

entering a non-string requires a type conversion
SubjN = int(input('Enter the Subject Number: '))
SessN = int(input('Enter the Session Number: '))
```