CPSC-8650 Data Mining Spring 2019

Final Project

**Title:**

Lightweight Coreset Construction for K-means and K-medoids Clustering and Performance Analysis.

**Team Number: 5**

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1. **Introduction**

Unsupervised cluster analysis groups a set of objects such that the objects in the same group (called a cluster) are more similar to each other than to those in other clusters. It is a common technique for statistical data analysis, and is widely used in many fields, such as machine learning, pattern recognition, image analysis, bioinformatics, information retrieval, data compression, etc.

There are several common clustering approaches, such as partitioning approach, hierarchical approach, density-based approach, grid-based approach, etc. K-means and K-medoids both are partitioning approaches. Briefly, they partition a dataset of N objects into k clusters, to minimize some chosen evaluation metrics, such as the sum of Euclidean distances. K-means represents each cluster by using the mean center of the cluster, and assigns each point to the closest cluster center. K-medoids represents each cluster by the centroid object of this cluster, and also assigns each point to the closest cluster. They are very popular methods for clustering analysis.

Both of them are heuristic methods. K-means method, which runs in O(n) time with a large hidden constant, is more efficient than K-medoids method, which runs in O(n2) time. But K-means is more sensitive to outliers and noisy data.

The recent, unprecedented increase in the size of data sets leads to the big computational challenge for them. Coresets can be employed to speed up the inference.

“Coresets are a proven data summarization approach that can be used to scale clustering problems to massive data sets. Coresets are small, weighted subsets of the original data set such that models trained on the coreset are provably competitive with models trained on the full data set.” [1]

Coresets have been successfully constructed by some researchers and applied for a lot of clustering problems. Here, Olivier Bachem, Mario Lucic and Andreas Krause proposed a novel approach in their paper “Scalable k-Means Clustering via Lightweight Coresets” which is published by KDD 2018.

They prove that the sufficient coreset size is , which is smaller than the which is proved by previous study. A simple and embarrassingly parallel algorithm is proposed too, to construct such lightweight coresets. kmeans++ algorithm is used to solve the clustering problem on subsamples and full dataset.

We reproduce their result using 2 different datasets. We also use the k-medoids method to cluster subsamples and full datasets too.

1. **Subsampling/Coresets construction**

We use 3 construction methods.

1). Uniform

The samples are generated by uniformly choosing m points at random from datasets. It can be shown that the cost evaluated on the uniformly constructed corset is an unbiased estimator of the true objective function. However, since single points can potentially have a large impact on the objective function, this subsampling method does not provide the strong theoretical guarantee required by the definition of a coreset.

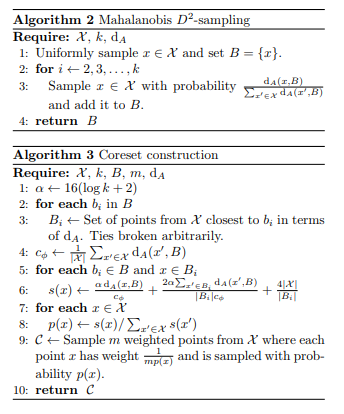
2). CS

The coresets are constructed with following two steps:

Step1. Find a rough approximation of the optimal clustering. This is achieved by sampling the 1st cluster uniformly at random then iteratively sampling additional points with probability proportional to the minimum squared distance to the already sampled cluster centers. See algorithm 2 for details.

Step2. Use importance sampling to construct the corsets. The idea is to sample points with a potentially high impact on the objective more frequently but assign them a lower weight. The impact of a sample point is measure by the upper bound of its sensitivity, the maximum ratio between the cost contribution of that point and the average contribution of all points. See algorithm 3 for details.

It can be proven that the samples generated by this methods form coresets[7].



3). Light weight coresets (LWCS).

The coresets are constructed by sampling m weighted points from datasets. Each point x has weight and is sampled with probability where is the mean of the whole dataset X.

has 2 terms. The intuition behind the second term is that “the points that are far from the mean of the data have a potentially large impact on the quantization error of a clustering.” [1]. The distance used in is the Euclidean distance. Following is the construction algorithm. [1]



1. **Performance analysis.**

The performances are valued by the running time and the relative error vs. full datasets.

Running time includes the time used to construct the coresets and the time used to solve clustering problem on subsamples or full dataset using k-means or k-medoids algorithms.

After we cluster the sample set, we have k clusters. Assign each object in full dataset to these k clusters and compute the quantization error . This sample quantization error is compared with the quantization error given by solving clustering problem on full set. This relative error is employed to evaluate the clustering quality.

1. **Experimental setup**

We choose samples size m {1000, 2000, 5000, 10000, 20000} and clusters k {100, 500}.

Programs are coded using Python. The multi-processing package is used to construct coresets. The sklearn/cluster package is employed to solve the k-means clustering problem. Since we don’t find a k-medoids package which handles weighted points, we write the algorithm ourselves.

Require: subsample X, number of clusters k, max-iteration maxi, tolerance t

1. Randomly choose k medoids from X
2. while iterations < maxi or reduced cost > t：

for each object in X:

assign cluster

for each cluster:

for each object O in this cluster:

cost =

choose the object whose cost is minimum as the new medoid of this cluster

1. Return medoids of k clusters.
2. **Environment**

We use the Clemson University Palmetto Cluster. The simulations for samples/coresets generation and error analysis are performed on single CPUs with 15 to 60GB memory. The lightweight coresets are constructed in parallel, we used 8 cores in order to speed up the construction. For time analysis, all simulations are run on single CPU with 60 GB memory to ensure valid comparisons.

1. **Datasets**

Two datasets are analyzed in this study.

1. KDD — 145’751 samples with 74 features measuring the match between a protein and a native sequence [3].
2. SONG — 90 features from 515’345 songs of the Million Song datasets used for predicting the year of songs [5].

The datasets downloaded from the reference are converted to files containing only feature values separated by whitespace using “awk” first before further analysis such as subsampling or K-means.

Due to time limitations, for SONG dataset, k-medoids with k=500 are not performed.

1. **Results and Discussions**

|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Relative error and speedup of different methods vs. Full for K-means | | | | | | | | |
|  | | | Relative error vs. Full | | | Speedup vs. Full | | |
| k | Data | Method | m = 1000 | m = 2000 | m = 5000 | m = 1000 | m = 2000 | m = 5000 |
| 100 | KDD | UNIFORM | 2.82(1.38) | 2.13(1.02) | 2.67(0.57) | 555 | 334 | 126 |
| CS | 1.25(0.14) | 1.14(0.06) | 1.07(0.01) | 0.1 | 0.1 | 0.1 |
| LWCS | 1.24(0.01) | 1.16(0.01) | 1.09(0.01) | 32 | 32 | 27 |
| SONG | UNIFORM | 1.22(0.01) | 1.16(0.01) | 1.10(0.01) | 1921 | 1251 | 484 |
| LWCS | 1.21(0.009) | 1.16(0.008) | 1.11(0.005) | 30 | 30 | 28 |
| 500 | KDD | UNIFORM | 3.72(0.04) | 2.03(1.46) | 1.66(0.81) | 630 | 417 | 169 |
|  | LWCS | 1.37(0.01) | 1.30(0.01) | 1.19(0.004) | 121 | 110 | 77 |
| SONG | UNIFROM | 1.44(0.02) | 1.32(0.01) | 1.22(0.01) | 516 | 316 | 137 |
|  | LWCS | 1.33(0.007) | 1.26(0.005) | 1.20(0.004) | 29 | 28 | 25 |

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| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Relative error and speedup of different methods vs. Full for K-medoids | | | | | | | | |
|  | | | Relative error vs. Full | | | Speedup vs. Full | | |
| k | Data | Method | m = 1000 | m = 2000 | m = 5000 | m = 1000 | m = 2000 | m = 5000 |
| 100 | KDD | UNIFORM | 2.48(0.69) | 2.05(0.74) | 1.42(0.55) | 82 | 21 | 6 |
| LWCS | 0.76(0.01) | 0.75(0.04) | 0.82(0.12) | 22 | 15 | 6 |
| SONG | UNIFORM |  |  |  |  |  |  |
| CS |  |  |  |  |  |  |
| LWCS |  |  |  |  |  |  |
| 500 | KDD | UNIFORM | 2.40(1.04) | 2.60(0.93) | 1.35(0.55) | 2594 | 1038 | 203 |
|  | LWCS | 0.67(0.01) | 0.65(0.01) | 0.65(0.01) | 39 | 23 | 10 |

* With all three subsampling methods, the relative errors are all considerably large.
* The CS method takes a long time to generate the coresets which largely limits its usage in practice. It might still be useful when memory is the bottleneck for performing clustering methods. A potential improvement can be implement CS algorithm in parallel. Due to time limitations, we didn’t do that in this project.
* The UNIFORM method provides the best speedup.
* The LWCS gives the best performance in general. It gives noticeable speedup compared with full dataset. And the relative errors are smaller than UNIFORM.

1. **References**
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8. Mario Lucic, Olivier Bachem, and Andreas Krause. Strong Coresets for Hard and Soft Bregman Clustering with Applications to Exponential Family Mixtures. arXiv e-prints, page arXiv:1508.05243, Aug 2015.