Indexing

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Outline

- Types of indexes
- B+ trees

Indexes

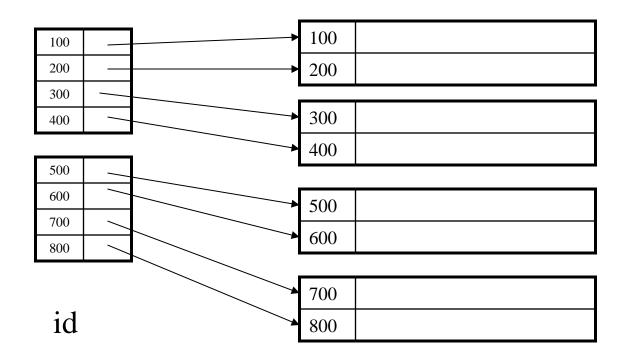
- An <u>index</u> is a data structure that speeds up selections on the <u>search key field(s)</u>
- *Fields* = *attributes*
- Search key = any subset of the fields of a relation
 - Search key is not the same as key (minimal set of fields that uniquely identify a record in a relation).
- Entries in an index: (k, r), where:
 - k =the key
 - r = the record OR record id OR a list of record ids

Index Classification

- Clustered/unclustered
 - Clustered = records sorted & stored in the order of search key
 - Unclustered = records are not sorted in key order
- Dense/sparse
 - Dense = each record has an entry in the index
 - Sparse = only some records have
- B+ tree / hash table / ...

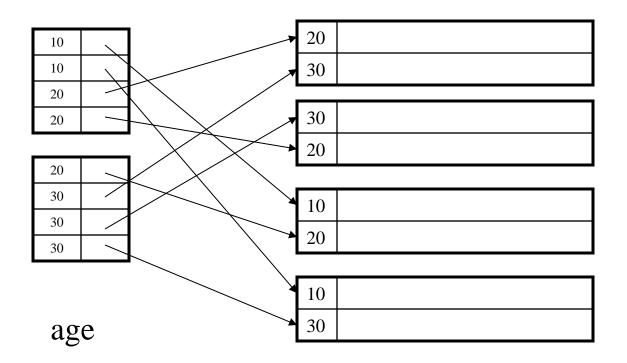
Clustered Index

- Records are sorted on the index attribute
 - Often for index on primary key
 - E.g., employee(<u>id</u>, name, age, salary)



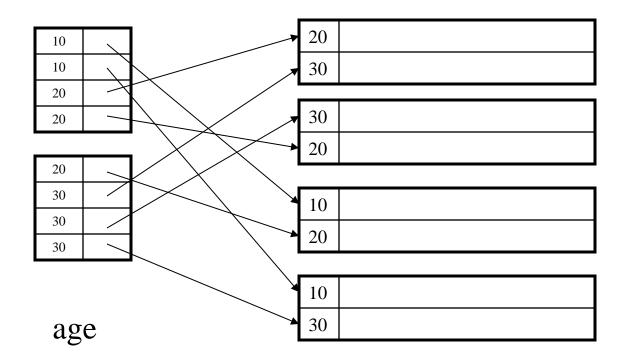
Unclustered Indexes

Often for indexes on attributes other than primary key



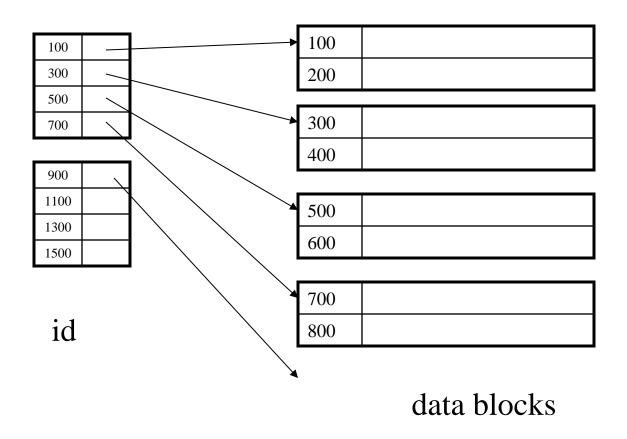
Dense Index

- <u>Dense</u> index: one key per data record
- See Sections 14.1.2 14.1.3 in book [GVW]



Sparse Index

• *Sparse* index: one key per data block



Questions

• Must a unclustered index be dense?

• Can a clustered index be sparse?

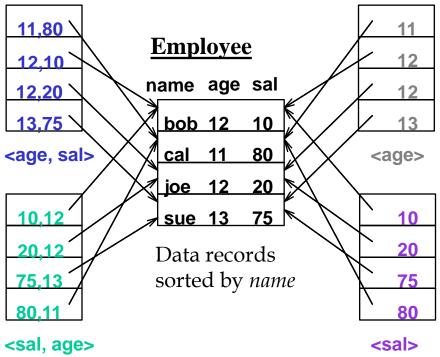
Query Types

- Equality query: <attribute> = <value>
 - E.g., age = 20, sal = 75
- Range query: <attribute> <inequality operator> <value>
 - Inequality operator: <, >, <=, >=
 - E.g., age > 20 or sal <= 75

Composite Search Keys

• *Composite Search Keys*: Search key = a list of fields.

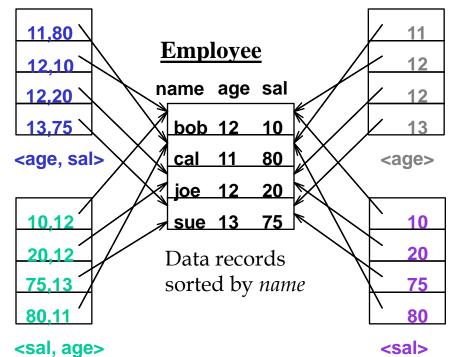
Keys in index sorted by <age,sal>: i.e., first by age; if ties, by sal



Keys sorted by *<sal>*

Questions

- Which index is useful for queries:
 - -Sal > 75
 - Age = 12 and sal > 10
 - -Age > 12



Outline

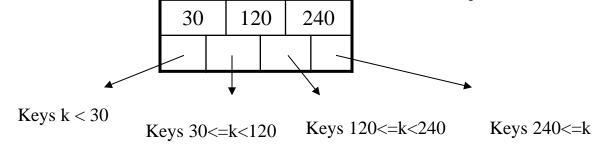
- Types of indexes
- B+ trees

B+ Trees

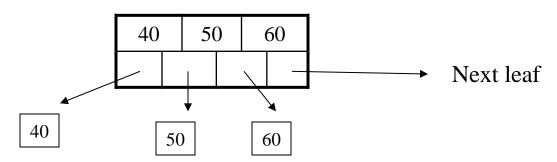
- Search trees
- Idea in B Trees:
 - make 1 node = 1 block
- Idea in B+ Trees:
 - Make leaves into a linked list
 - Efficiently support range queries

B+ Trees Basics

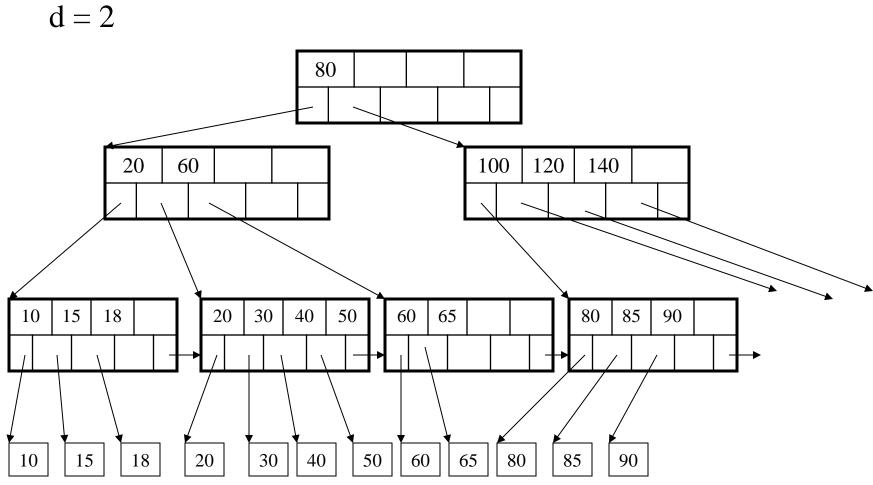
- Parameter d = the **degree** (also called order)
- Each node has $\geq = d$ and $\leq = 2d$ keys (except root)



• Each leaf has >=d and <= 2d keys:



B+ Tree Example



B+ Tree Design

- How large is d?
- Example:
 - Key size = 4 bytes
 - Pointer size = 8 bytes
 - Block size = 4096 byes
- 2d * 4 + (2d+1) * 8 <= 4096
- $d = 170 (\sim 170.33)$

B+ Trees in Practice

- Typical order d = 100.
- Typical fill-factor (minimum in practice): 66.7% (i.e., 2/3) (note minimum fill factor in design: 50%)
 - Minimum # of keys in a node = 133 (200 * 2/3)

• Capacities:

- Height 1 (tree with a single root): 133 records
- Height 2: $133^2 = 17$, 689 records
- Height 3: $133^3 = 2$, 352, 637 records
- Height 4: $133^4 = 312,900,721$ records

B+-tree in Practice

• Can often hold top levels in buffer pool:

```
Level 1 = 1 page = 4KB
Level 2 = 133 pages = 532KB
Level 3 = 17,689 pages = 70, 756KB ~ 70MB
```

Searching a B+ Tree

- Equality search:
 - Start at the root
 - Proceed down, to the leaf

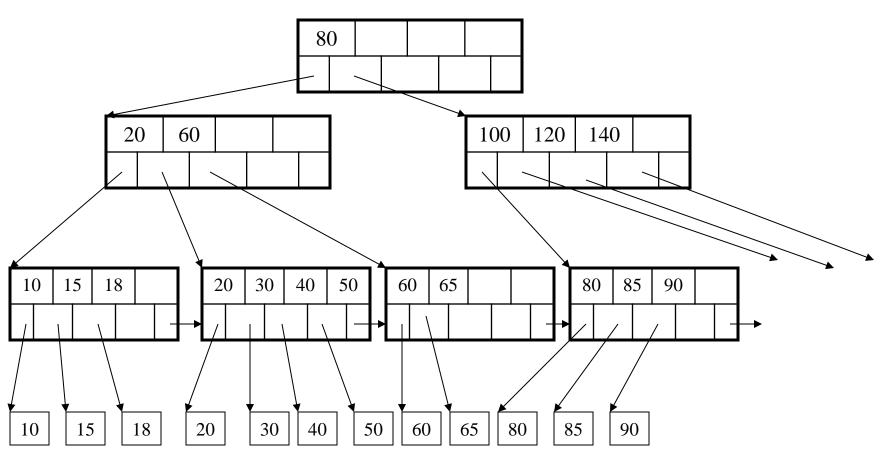
Select name From people Where age = 25

- Range query:
 - Finding the first leaf
 - Then sequential traversal of leaves

Select name
From people
Where 20 <= age
and age <= 30

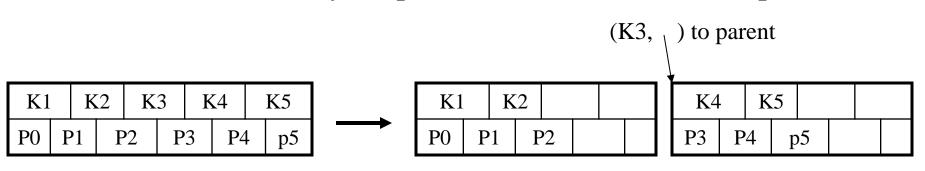
Example

20 <= age and age <= 55



Insert (K, P)

- Find leaf where K belongs, insert
- If no overflow (2d keys or less), stop
- If overflow (2d+1 keys), split node, insert middle into parent:



Notes

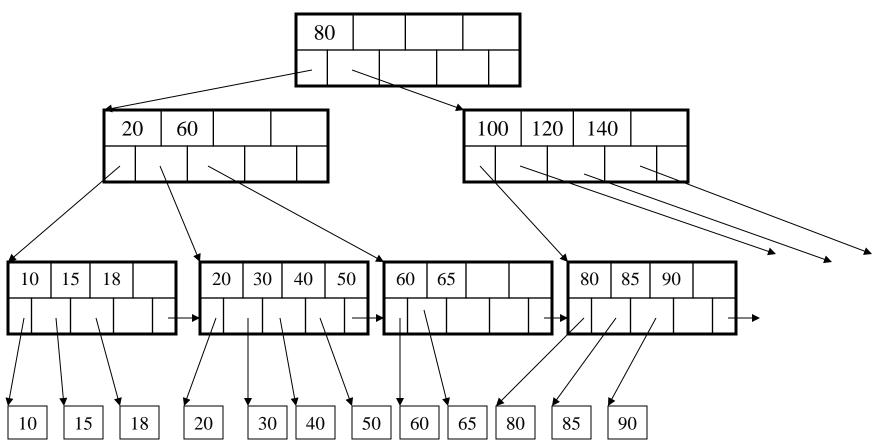
 Splitting of leaf may lead to splitting of its parent and ancestors

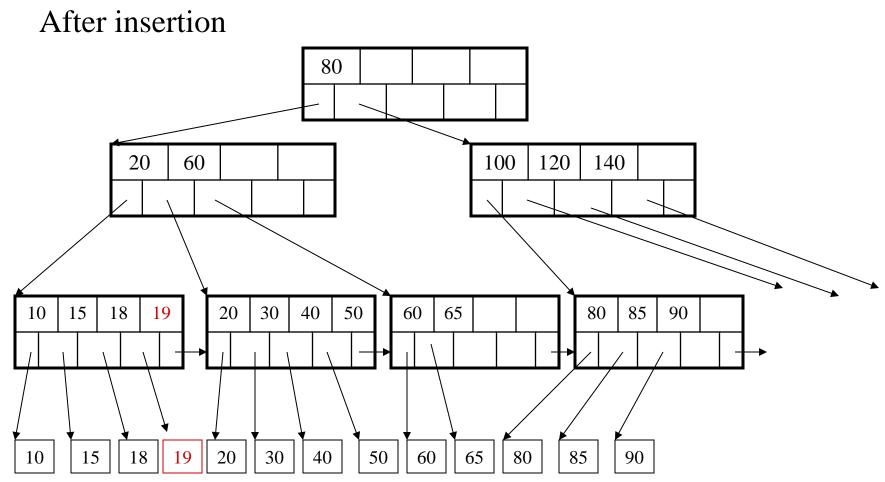
• When splitting a leaf, middle key (e.g., K3) is also kept in the new node on the right

 No need to retain middle key in the split nodes when splitting internal node

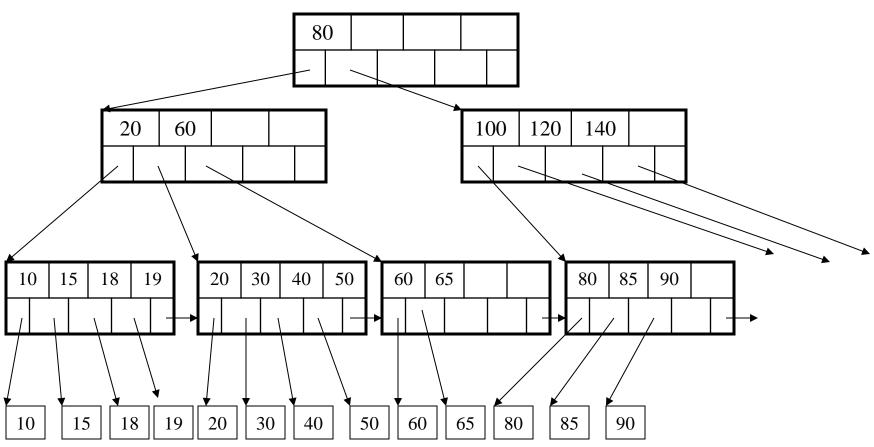
 When root is split, new root has only one key

Insert K=19

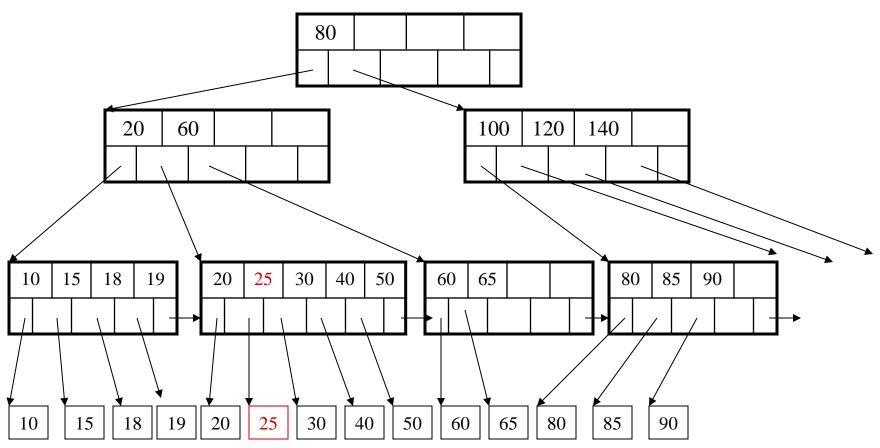




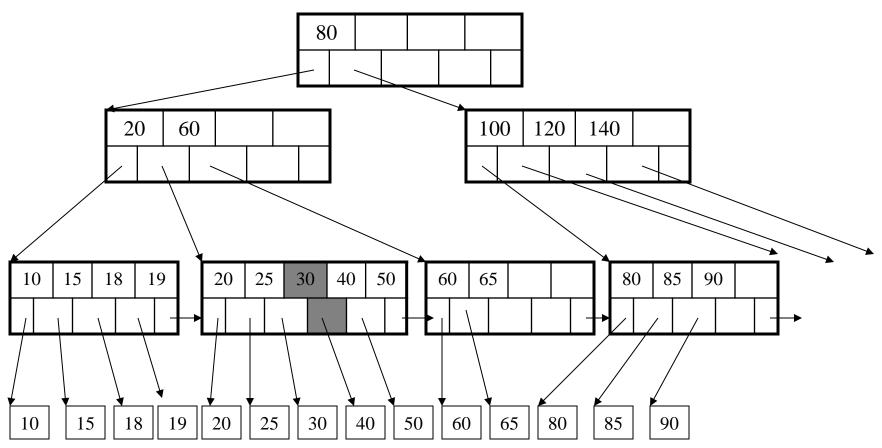
Now insert 25



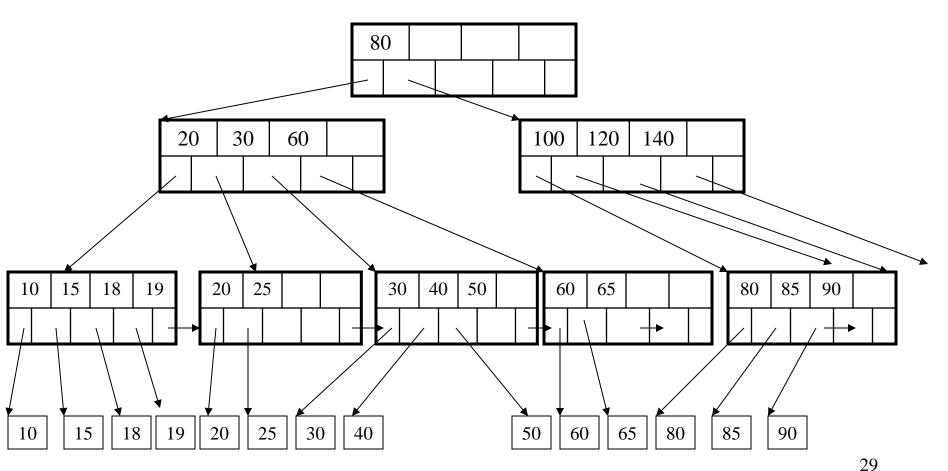
After insertion



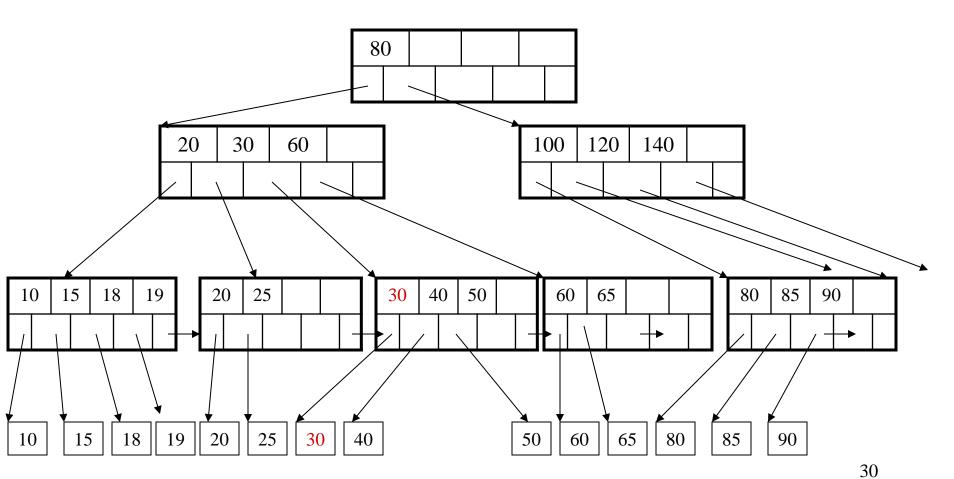
But now have to split!

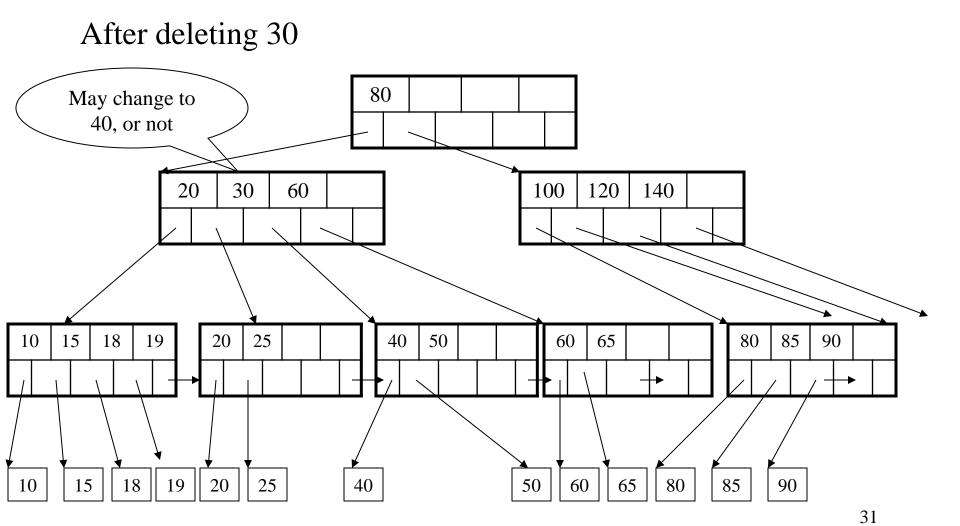


After the split

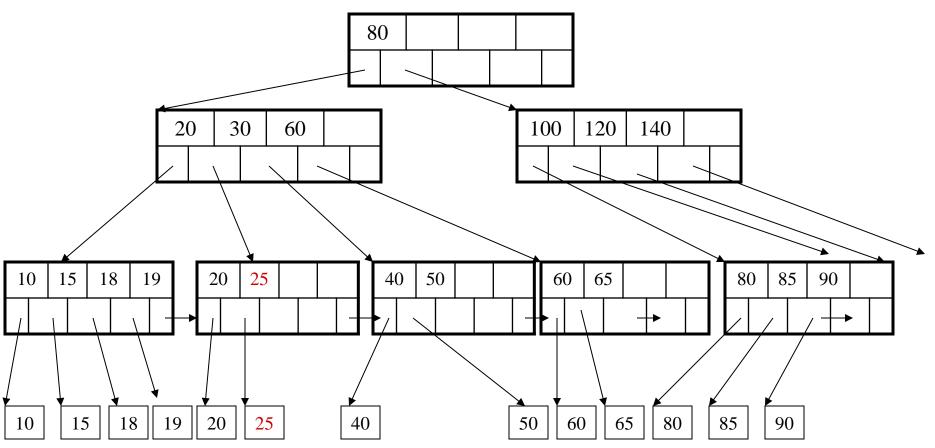


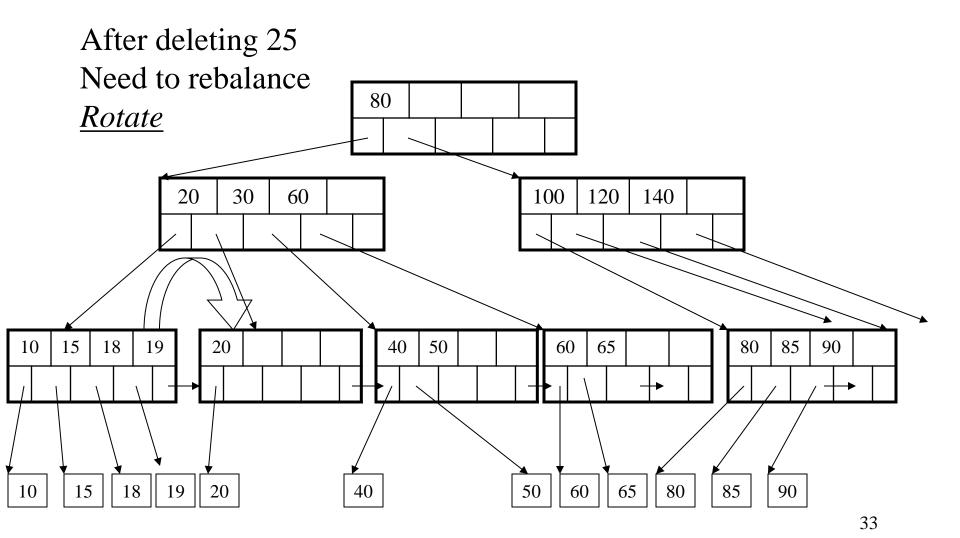
Delete 30



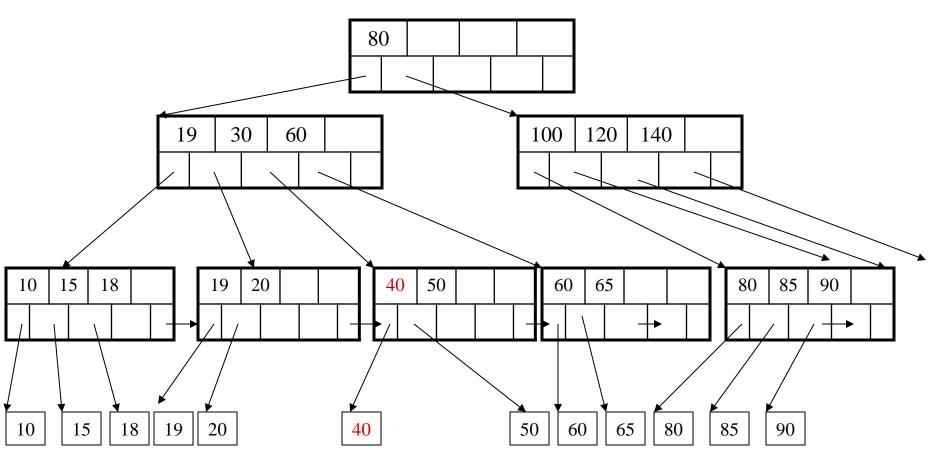


Now delete 25



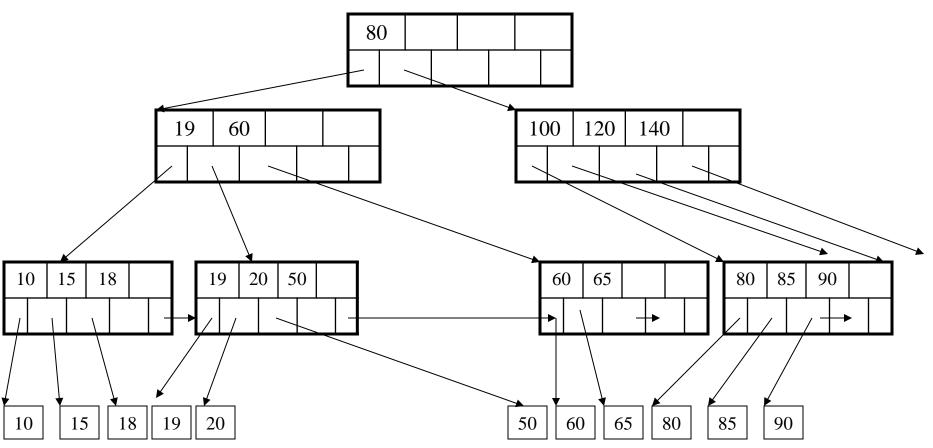


Now delete 40



After deleting 40 Rotation not possible Need to *merge* nodes

Final tree



Deletion Strategy

- If a node is below the min capacity after deletion...
- Try the following in the given order
 - 1. move a key from immediate left sibling;
 - 2. move a key from immediate right sibling;
 - 3. merge with immediate left sibling;
 - 4. merge with immediate right sibling

• Cases 3 and 4 may lead to further removal of key from parent, and more fixing