

# Solutions

$$1) \frac{-4-5}{|-5+3|} = \frac{-9}{|-2|} = \boxed{-\frac{9}{2}}$$

$$3) \frac{1}{2}x - \frac{1}{3}x + \frac{1}{3} = \frac{1}{6}x + 5$$

$$\frac{3}{6}x - \frac{2}{6}x - \frac{1}{6}x = \frac{15}{3} - \frac{1}{3}$$

$$0 = \frac{14}{3}$$

no solution

$$5) x^2 = 9 \quad \boxed{x = \pm 3}$$

$$6) x^2 - 3x - 4 = 0$$

$$(x-4)(x+1) = 0$$

$$\boxed{x=4, x=-1}$$

$$8) |x-10| < 5$$

$$-5 < x-10 < 5$$

$$+10 \quad +10 \quad +10$$

$$\boxed{5 < x < 15}$$

$$11) \boxed{\frac{-2x^2}{y^4}}$$

$$13) \ln 2 + \ln(x^2)^5 - \ln(y)^{\frac{1}{2}}$$

$$\ln(2 \cdot x^{10}) - \ln(y)^{\frac{1}{2}}$$

$$\boxed{\ln\left(\frac{2x^{10}}{\sqrt{y}}\right)}$$

$$14) \boxed{\frac{3}{2} \ln x + 2 \ln y - \ln \sqrt{3z}}$$

17) undefined - can't take  $\sqrt{\quad}$  of a negative #

$$18) \boxed{-2}$$

$$20) \frac{1}{x(x-3)} + \frac{2x}{(x+3)(x-3)} = \frac{(x+3)}{x(x-3)(x+3)} + \frac{2x(x)}{x(x+3)(x-3)}$$

$$= \boxed{\frac{2x^2 + x + 3}{x(x-3)(x+3)}}$$

$$2) -\frac{2}{3}x - \frac{8}{3} = 6 + x$$

$$-\frac{2}{3}x - \frac{3}{3}x = \frac{18}{3} + \frac{8}{3}$$

$$-\frac{5}{3}x = \frac{26}{3} \cdot \frac{3}{-5}$$

$$\boxed{x = -\frac{26}{5}}$$

$$4) aK = bK + b$$

$$(a-b)K = b$$

$$\boxed{K = \frac{b}{a-b}} \quad a \neq b$$

$$7) x^2 + 4x + 4 = 0$$

$$(x+2)^2 = 0$$

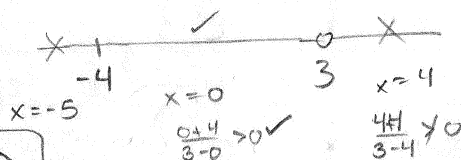
$$\boxed{x = -2}$$

$$9) (e^{5x} + 3)(e^{5x} + 3)$$

$$\boxed{e^{10x} + 6e^{5x} + 9}$$

$$10) \boxed{64x^{12}y^2}$$

$$12) x \neq 3$$



$$\boxed{x \in (-4, 3)}$$

$$15) \frac{13}{(x-2)(x+2)} = \frac{2(x+2)}{(x-2)(x+2)} - \frac{3(x-2)}{(x+2)(x-2)}$$

$$13 = 2x + 4 - 3x + 6$$

$$3 = -x \Rightarrow \boxed{x = -3}$$

$$16) (49)^{\frac{1}{2}} = -(7)^3 = \boxed{-343}$$

$$19) \frac{2^{1/2} \cdot 2^n}{2^2} = \boxed{2^{n-\frac{3}{2}}}$$

$$21) \frac{y(x+y)}{x(x-y)(x+y)} - \frac{y}{(x-y)(x+y)} \cdot x = \frac{xy+y^2}{x(x-y)(x+y)} - \frac{xy}{x(x-y)(x+y)}$$

$$= \frac{y^2}{x(x^2-y^2)}$$

$$22) \frac{\frac{x^2+1}{\frac{x-1}{x}} - \frac{x^2+1}{\frac{x+1}{x}}}{\frac{x^2+1}{x}} = \left( \frac{x^2+1}{1} \cdot \frac{x}{x-1} - \frac{x^2+1}{1} \cdot \frac{x}{x+1} \right) \cdot \frac{x}{x^2+1}$$

$$= \left[ \frac{x}{x-1} - \frac{x}{x+1} \right] x = \left( \frac{x(x+1)}{(x-1)(x+1)} - \frac{x(x-1)}{(x-1)(x+1)} \right) x$$

$$= \frac{(x^2+x-x^2+x)x}{(x-1)(x+1)} = \frac{(2x)(x)}{(x-1)(x+1)} = \frac{2x^2}{x^2-1}$$

$$23) e^{\ln 2} \cdot e^{\ln \frac{1}{2}} = 2 \cdot \frac{1}{2} = \boxed{1}$$

$$24) y = \frac{x}{x-1} + 1$$

$$y-1 = \frac{x}{x-1}$$

$$xy - x - y + 1 = x$$

$$xy - 2x = y - 1$$

$$x(y-2) = y-1$$

$$\boxed{x = \frac{y-1}{y-2}}$$

$$25) x^2 - x - 2 \geq 0$$

$$(x-2)(x+1) \geq 0$$

$$\boxed{x \in (-\infty, -1) \cup (2, \infty)}$$

$$x = -2 \quad x = 0 \quad x = 3$$

indikator  
so cant =

$$26) m = \frac{\Delta y}{\Delta x} = \frac{1-3}{-13} = \frac{2}{13}$$

$$3 = \frac{2}{13}(2) + b \Rightarrow b = \frac{39}{13} - \frac{4}{13} = \frac{35}{13}$$

$$\boxed{y = \frac{2}{13}x + \frac{35}{13}}$$

$$27) \begin{array}{l} 2x+5y=7 \\ -2(x+3y)=-4 \end{array}$$

$$-y = 15$$

$$y = -15$$

$$x = -4 - 3(-15) = 41$$

$$\boxed{\begin{array}{l} x=41 \\ y=-15 \end{array}}$$

$$28) \frac{(-3)^{\frac{3}{5}} x^{\frac{10}{6}} y^{-7}}{-9 x^3 y^6} = \frac{3^3 x^7}{y^{13}} = \frac{27x^7}{y^{13}}$$

$$29) 4x^{\frac{4}{3}} y^{\frac{4}{5}} (-3)^2 y^{-\frac{6}{5}} x^{-\frac{1}{6}}$$

$$= 36 x^{\frac{3}{6}} y^{-\frac{2}{5}} = \frac{36x^{\frac{1}{2}}}{y^{\frac{2}{5}}}$$

$$30) \frac{x(x-2)}{(x+2)(x-2)} \cdot \frac{(x-3)(x+2)}{x^2(x-3)} = \boxed{\frac{1}{x}}$$

$$31) \frac{a^2(a-2b)}{a(a^2-4b^2)} \cdot \frac{(a-b)(a+2b)}{a^3(a+3b)} = \frac{a^2(a-2b)}{a(a-2b)(a+2b)} \cdot \frac{(a-b)(a+2b)}{a^2(a+3b)}$$

$$= \boxed{\frac{a-b}{a^2(a+3b)}}$$

$$32) \frac{(6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1)(3 \cdot 2 \cdot 1)}{(5 \cdot 4 \cdot 3 \cdot 2 \cdot 1)(1)} = 6 \cdot 6 = \boxed{36}$$

$$33) \frac{[(n+1)(n)(n-1) \cdots 1] [(n-1)(n-2) \cdots 1]}{[n(n-1) \cdots 1] [(n+2)(n+1)(n)(n-1) \cdots 1]} = \boxed{\frac{1}{(n+2)(n)}}$$

$$34) x^2 - 4x + \frac{4}{1} + y^2 + 6y + \frac{9}{1} = 12 + 4 + 9$$

$$(x-2)^2 + (y+3)^2 = 25$$

center (2, -3)  
radius 5

$$35) \frac{\frac{1}{\cos x} \cdot \cos^2 x \cdot \sin x}{\sin x \cdot \frac{\cos^2 x}{\sin^2 x} \cdot \frac{1}{\sin^3 x}} = \frac{\sin x}{1} \cdot \frac{\sin^4 x}{\cos^2 x} = \boxed{\frac{\sin^5 x}{\cos^2 x}}$$

$$36) \begin{array}{c} 7 \\ \diagup \\ \text{triangle} \\ \diagdown \\ 3 \end{array} \quad \sqrt{3^2 + 7^2} = \boxed{\sqrt{58}}$$

$$37) \tan^{-1}(1) = \boxed{\frac{\pi}{4}}$$

$$38) \tan^{-1}(\sqrt{3}) = \boxed{\frac{\pi}{3}}$$

$$\frac{\sin}{\cos} \sqrt{3} = \frac{\frac{\sqrt{3}}{2}}{\frac{1}{2}}$$

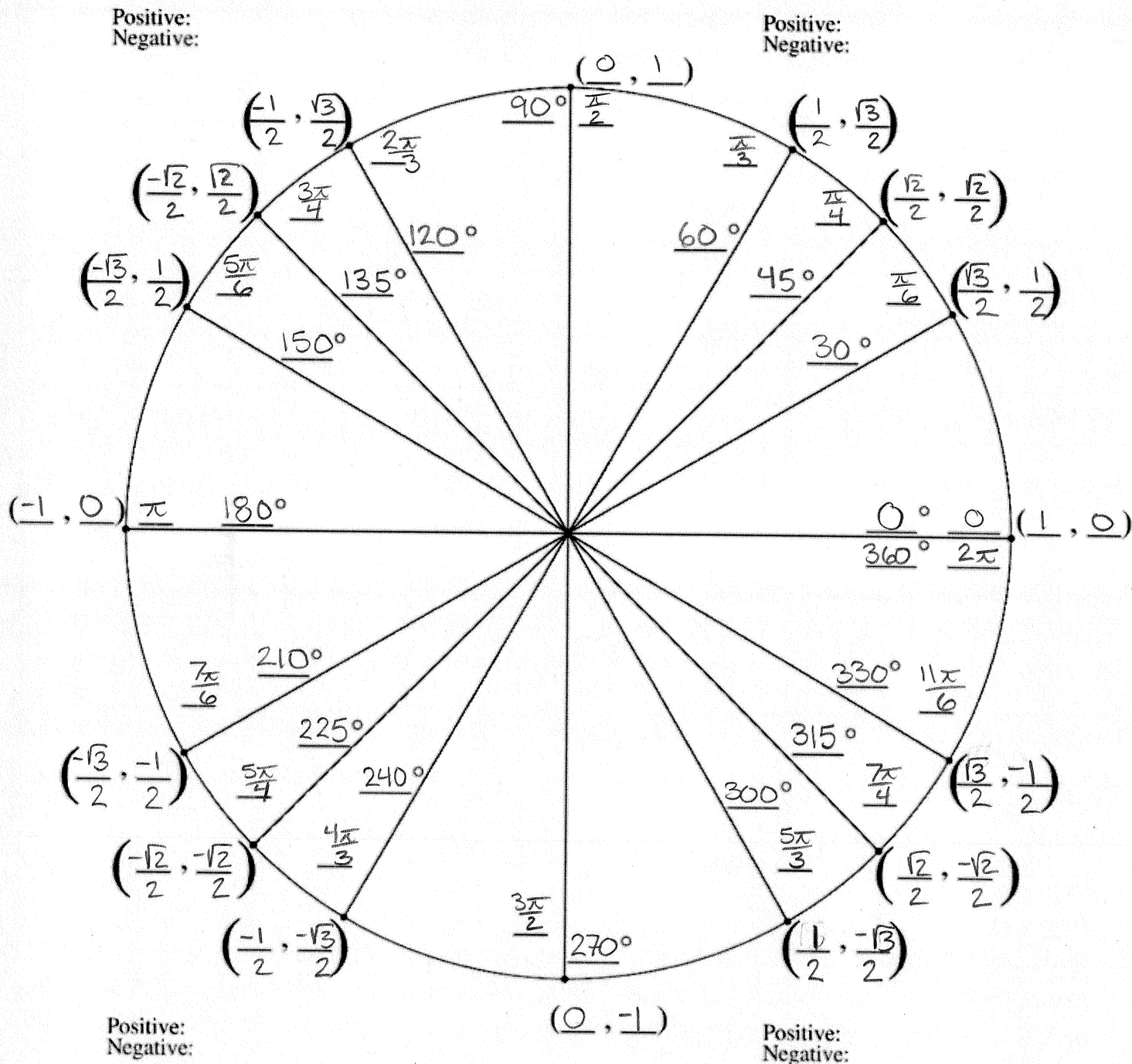
39) next page

$$40) \lim_{x \rightarrow 0} \frac{\sin(3x) - \sin(5x)}{\sin(2x)} = \frac{0}{0} \Rightarrow \lim_{x \rightarrow 0} \frac{3\cos(3x) - 5\cos(5x)}{2\cos(2x)} = \frac{3-5}{2} = \boxed{-1}$$

$$41) \lim_{x \rightarrow \infty} \frac{4x + \sqrt{x^2 + 1}}{3x + 7} = \frac{\infty}{\infty} \Rightarrow \lim_{x \rightarrow \infty} \frac{4 + \frac{2x}{2\sqrt{x^2 + 1}}}{3} = \frac{4}{3} + \lim_{x \rightarrow \infty} \frac{x}{3\sqrt{x^2 + 1}} = \frac{\infty}{\infty}$$

$$= \frac{4}{3} + \lim_{x \rightarrow \infty} \frac{x \cdot \frac{1}{\sqrt{x^2}}}{3\sqrt{1 + \frac{1}{x^2}}} = \frac{4}{3} + \lim_{x \rightarrow \infty} \frac{1}{3\sqrt{1 + \frac{1}{x^2}}} = \frac{4}{3} + \frac{1}{3} = \boxed{\frac{5}{3}}$$

# Fill in The Unit Circle



$$42) \lim_{h \rightarrow 0} \frac{(x+h)^{50} - x^{50}}{h} = \frac{0}{0} \Rightarrow \lim_{h \rightarrow 0} \frac{50(x+h)^{49} - 0}{1} = \boxed{50x^{49}}$$

$$43) \lim_{n \rightarrow \infty} \frac{n(n-1) \cdots 1}{(n+1)(n)(n-1) \cdots 1} = \boxed{0}$$

$$44) \lim_{n \rightarrow \infty} \frac{3^n(n^5 - 16)}{3^{n+1}(n^4 - n^5)} \quad \begin{array}{l} \text{same powers} \\ \text{take coeff in front} \\ \text{of biggest} \end{array} \quad \boxed{\frac{1}{-9}}$$

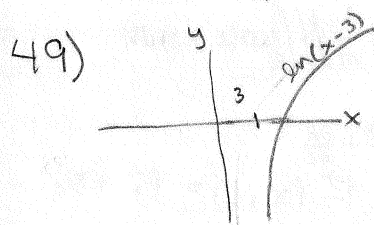
$$45) \lim_{x \rightarrow 4} \frac{(x-4)(x+1)}{(x+4)(x-4)} = \boxed{\frac{5}{8}}$$

$$46) \lim_{x \rightarrow 4^+} \sqrt{16-x^2} \quad \boxed{\text{does not exist}}$$

$$47) \lim_{x \rightarrow 4^-} \frac{1}{\sqrt{16-x^2}} = \boxed{\infty}$$

$$48) \lim_{x \rightarrow 2} \frac{x^2-4}{\frac{1}{5}-\frac{1}{x+3}} = \frac{0}{\frac{1}{5}-\frac{1}{5}} \Rightarrow \lim_{x \rightarrow 2} \frac{x^2-4}{x+3-5} = \lim_{x \rightarrow 2} \frac{5(x+3)(x^2-4)}{x-2} = \frac{0}{0}$$

$$\lim_{x \rightarrow 2} \frac{5(x^3+3x^2-4x-12)}{x-2} \xrightarrow{\text{L'Hopital's}} \lim_{x \rightarrow 2} \frac{5(3x^2+6x-4)}{1} = 5(12+12-4) = \boxed{100}$$



$$\lim_{x \rightarrow 3^+} \ln(x-3) = \boxed{-\infty}$$

$$50) \lim_{x \rightarrow 3^-} \ln(x-3) \Rightarrow \boxed{\text{does not exist}}$$

$$51) \lim_{x \rightarrow 3} \ln(x-3) \quad \boxed{\text{does not exist}}$$

$$52) \int_1^3 x^2 dx = \left. \frac{x^3}{3} \right|_1^3 = 9 - \frac{1}{3} = \boxed{\frac{26}{3}}$$

$$53) \int_0^1 e^{3x} dx = \left. \frac{e^{3x}}{3} \right|_0^1 = \boxed{\frac{e^3-1}{3}}$$

$$54) \int_0^2 x^2 e^{x^3} dx \quad \begin{array}{l} u = x^3 \\ du = 3x^2 dx \end{array} \quad \int \frac{1}{3} e^u du = \frac{1}{3} e^u$$

$$= \left. \frac{1}{3} e^{x^3} \right|_0^2 = \boxed{\frac{e^8-1}{3}}$$

$$55) \int \frac{1}{y} dy = \boxed{\ln|y| + C}$$

$$56) \int \frac{1}{y^2} dy = \int y^{-2} dy = \boxed{-\frac{1}{y} + C}$$

$$57) \int \frac{1}{2-x} dx = \boxed{-\ln|2-x| + C}$$

$$58) \int \frac{x}{2-x^2} dx \quad u = 2-x^2 \quad du = -2x dx \quad \int -\frac{1}{2} \frac{1}{u} du = -\frac{1}{2} \ln|u|$$

$$= \boxed{-\frac{1}{2} \ln|2-x^2| + C}$$

$$59) \int \frac{1}{x^2+1} dx = \boxed{\tan^{-1} x + C}$$

$$60) \int \frac{1}{2(1+(\frac{x}{\sqrt{2}})^2)} dx \quad u = \frac{x}{\sqrt{2}} \quad du = \frac{1}{\sqrt{2}} dx \quad \frac{1}{2} \int \frac{\sqrt{2}}{1+u^2} du = \frac{\sqrt{2}}{2} \tan^{-1} u$$

$$= \boxed{\frac{\sqrt{2}}{2} \tan^{-1}\left(\frac{x}{\sqrt{2}}\right) + C}$$

$$61) \int (e^{4x} + 2e^{5x} + e^{6x}) dx = \boxed{\frac{e^{4x}}{4} + \frac{2e^{5x}}{5} + \frac{e^{6x}}{6} + C}$$

$$62) \int \frac{7x}{1+x^2} + \frac{3}{1+x^2} dx \quad u = 1+x^2 \quad du = 2x dx \quad \int \frac{7}{2} \frac{1}{u} du = \frac{7}{2} \ln|u|$$

$$= \boxed{\frac{7}{2} \ln|1+x^2| + 3 \tan^{-1} x + C}$$

$$63) \int \frac{2x+3}{(x+1)^4} dx \quad u = x+1 \Rightarrow x = u-1$$

$$\int \frac{2(u-1)+3}{u^4} du = \int \frac{2u+1}{u^4} du = \int 2u^{-3} + u^{-4} du$$

$$= \frac{2u^{-2}}{-2} + \frac{u^{-3}}{-3} = -\frac{1}{(x+1)^2} - \frac{1}{3(x+1)^3} + C$$

$$64) \int \frac{e^{2x}}{1+e^{2x}} dx \quad u = 1+e^{2x} \quad du = 2e^{2x} dx \quad \int \frac{1}{2} \frac{1}{u} du = \frac{1}{2} \ln|u|$$

$$= \boxed{\frac{1}{2} \ln|1+e^{2x}| + C}$$

$$\begin{aligned}
 65) \quad \int \frac{(3\ln x)^2 + 1}{x} dx & \quad u = 3\ln x \\
 & \quad du = \frac{3}{x} dx \quad \int \frac{1}{3} u^2 du + \int \frac{1}{x} dx \\
 & \quad \frac{1}{3} \frac{u^3}{3} + \ln|x| \\
 & = \frac{(3\ln x)^3}{9} + \ln|x| + C = \boxed{3\ln^3(x) + \ln|x| + C}
 \end{aligned}$$

$$\begin{aligned}
 66) \quad \int \cos x \sin x dx & \quad u = \sin x \\
 & \quad du = \cos x dx \quad \int u du = \frac{u^2}{2} \\
 & = \boxed{\frac{\sin^2 x}{2} + C}
 \end{aligned}$$

$$\begin{aligned}
 67) \quad \int \frac{\cos x dx}{\sin^2 x + 2\sin x + 1} & \quad u = \sin x \\
 & \quad du = \cos x dx \\
 & \quad \int \frac{du}{u^2 + 2u + 1} = \int \frac{du}{(u+1)^2} = \int (u+1)^{-2} du \\
 & \quad = \frac{(u+1)^{-1}}{-1} \\
 & = \boxed{-\frac{1}{\sin x + 1} + C}
 \end{aligned}$$

$$\begin{aligned}
 68) \quad \int \frac{x^2 + x}{(2 - 3x^2 - 2x^3)^{1/3}} dx & \quad u = 2 - 3x^2 - 2x^3 \\
 & \quad du = -6x - 6x^2 dx \\
 & \quad = -6(x + x^2) dx \\
 & \quad = -\frac{1}{6} \int u^{-1/3} = -\frac{1}{6} \cdot \frac{3}{2} u^{2/3} \\
 & = \boxed{-\frac{1}{4} (2 - 3x^2 - 2x^3)^{2/3} + C}
 \end{aligned}$$

$$69) \quad \int \sec x \tan x dx = \boxed{\sec x + C}$$

$$\begin{aligned}
 70) \quad \int \frac{(\sec x^{1/3})^2}{x^{2/3}} dx & \quad u = x^{1/3} \\
 & \quad du = \frac{1}{3} x^{-2/3} dx \quad \int 3 \sec^2 u du = 3 \tan u \\
 & = \boxed{3 \tan(x^{1/3}) + C}
 \end{aligned}$$

$$\begin{aligned}
 71) \quad \int_0^{182} 12 + \sin\left(\frac{\pi}{182} t\right) dt & = 12t - \cos\left(\frac{\pi}{182} t\right) \Big|_0^{182} \\
 & = 12(182) - \frac{182}{\pi} \cos(\pi) - 0 + \frac{182}{\pi} \cos(0) \\
 & = 12(182) + \frac{2(182)}{\pi} \\
 & = \boxed{182 \left(12 + \frac{2}{\pi}\right)}
 \end{aligned}$$

$$72) \int_0^1 \frac{x \ln(x^2+1)}{1+x^2} dx$$

$$u = x^2 + 1$$

$$du = 2x dx$$

$$\int \frac{1}{2} \frac{\ln u}{u} du$$

$$v = \ln u$$

$$dv = \frac{1}{u} du$$

$$\int \frac{1}{2} v dv$$

$$= \frac{v^2}{4}$$

$$\left( \frac{(\ln(x^2+1))^2}{4} \right) \Big|_0^1$$

$$= \left[ \frac{\ln^2(2)}{4} \right]$$

$$\leftarrow \frac{(\ln u)^2}{4} \leftarrow$$

$$73) \int (x+1) e^{(x^2+2x+5)} dx$$

$$u = x^2 + 2x + 5$$

$$du = (2x+2) dx$$

$$= 2(x+1) dx$$

$$\int \frac{1}{2} e^u du = \frac{1}{2} e^u$$

$$= \left[ \frac{1}{2} e^{x^2+2x+5} + C \right]$$

$$74) \int \frac{1}{e^{2x} \sqrt{1-e^{-2x}}} dx \cdot \frac{e^{-2x}}{e^{-2x}} = \int \frac{e^{-2x}}{\sqrt{1-e^{-2x}}} dx$$

$$u = 1 - e^{-2x}$$

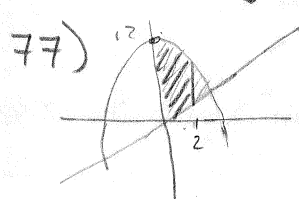
$$du = 2e^{-2x} dx$$

$$\int \frac{1}{2} \frac{du}{\sqrt{u}} = \int \frac{1}{2} u^{-1/2} du = \frac{1}{2} \cdot 2 u^{1/2}$$

$$= \left[ \sqrt{1-e^{-2x}} + C \right]$$

75) It makes no sense for dy to be in a denominator.

$$76) \frac{d(\ln y)}{dy} = \frac{1}{y} \text{ not the integral}$$



$$77) \int_0^2 (12-x^2) - (x) dx = 12x - \frac{x^3}{3} - \frac{x^2}{2} \Big|_0^2$$

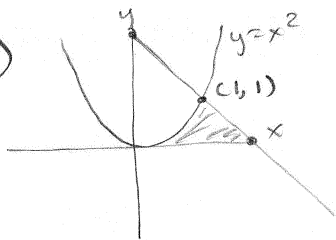
$$= 24 - \frac{8}{3} - 2$$

$$= 22 - \frac{8}{3}$$

$$= \frac{58}{3}$$



78)



$$x^2 = 2 - x$$

$$x^2 + x - 2 = 0$$

$$(x+2)(x-1) = 0$$

$$x = -2$$

$$x = 1$$

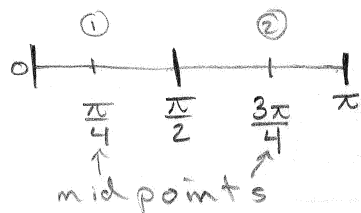
$$\int_0^1 x^2 dx + \int_1^2 2-x dx$$

$$\left. \frac{x^3}{3} + 2x - \frac{x^2}{2} \right|_0^2$$

$$\frac{1}{3} + 4 - 2 - 2 + \frac{1}{2}$$

$$\frac{2}{6} + \frac{3}{6} = \boxed{\frac{5}{6}}$$

79)



base of each rectangle =  $\frac{\pi}{2}$

$$\text{height of ①} = \left( \frac{\pi}{4} - \sin \frac{\pi}{4} \right)^2$$

$$\text{height of ②} = \left( \frac{3\pi}{4} - \sin \frac{3\pi}{4} \right)^2$$

$$\text{Area} \approx \frac{\pi}{2} \left( \frac{\pi}{4} - \frac{\sqrt{2}}{2} \right)^2 + \frac{\pi}{2} \left( \frac{3\pi}{4} - \frac{\sqrt{2}}{2} \right)^2$$

$$\frac{\pi}{2} \left[ \left( \frac{\pi^2}{16} - \frac{2\sqrt{2}\pi}{8} + \frac{2}{4} \right) + \left( \frac{9\pi^2}{16} - \frac{6\sqrt{2}\pi}{8} + \frac{2}{4} \right) \right]$$

$$\boxed{\frac{\pi}{2} \left( \frac{5\pi^2}{8} - \sqrt{2}\pi + 1 \right)}$$