4.0 Receiver Software

4.1 Program Structure

The software has two major sections, the main routine and an interrupt service routine. This description will go from the general to more specific in terms of objects, the state transitions for each object, and timing diagrams:

Figure 4-1 illustrates the program object structure. The 3 major objects are the GPS RCVR, the Channel, and the Satellite. The satellite interacts with the channel through the RF signal. There is a one-to-one correspondence of each channel with one satellite. There can be as many as 32 satellites (not counting other satellites using the same PRN family) but the GP2021 has only 12 channels. With a 24 satellite constellation the maximum number of satellites in view of a receiver on the ground is 12. With a larger constellation some will not be tracked if more than 12 are in view. The channels interact with the GPS RCVR through the GPS ISR (Interrupt Service Routine).

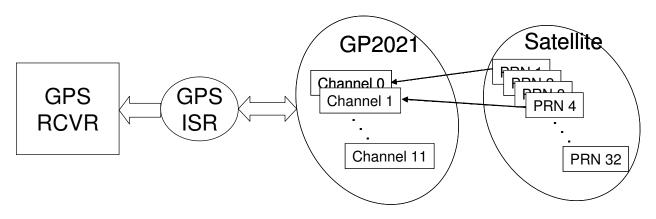


Figure 4-1
OpenSourceGPS Object Structure

More detail of the interactions between GPS RCVR and GPS ISR are shown in figure 4-2. The GPS ISR communicates directly with flags that tell the main program when to compute a navigation fix, when satellite visibility should be checked and when a new frame of data is ready. The navigation data and transmission time is provided in common memory.

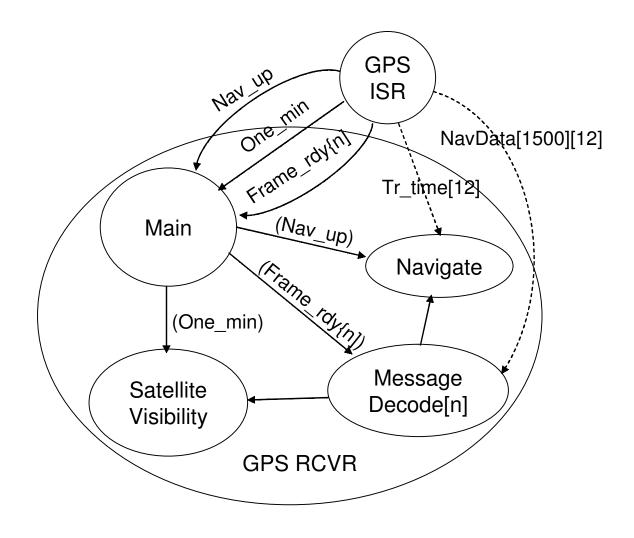


Figure 4-2
GPS Receiver Software Collaboration Diagram

The receiver state diagram is shown in figure 4-3. The most complex part is determining how to start. From then on it is either navigating or re-starting. The cold start is a bootstrap operation. If the receiver does not know enough information to determine which satellites are in view it must search every PRN code to see if it is available. In addition, since the position or receiver clock is not known the range of Doppler to be searched is also very wide. A warm start can be performed if an almanac is available and a rough idea of the receiver's location is available. The Doppler search can be narrowed. The last starting algorithm is the hot start. This is when the data needed for a warm start is available along with valid clock and ephemeris data. As soon as the start of a subframe is found the range measurements from the satellite can be used.

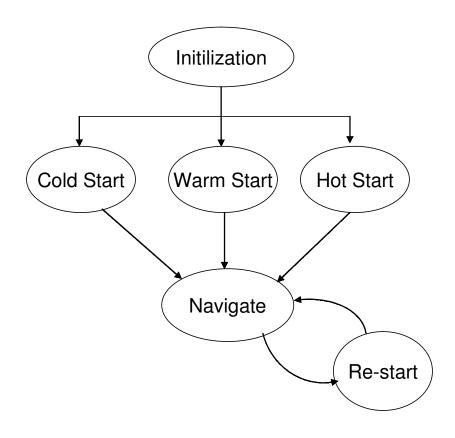


Figure 4-3 GPS RCVR State Diagram

The channel state diagram is the most complex. The prompt and dither magnitudes are the root sum squared value of the I and Q components of the two correlators which are separated by ½ chip. The state numbers are the ones seen on page 1 of the display. When fully tracking the satellite the channel is in state 4.

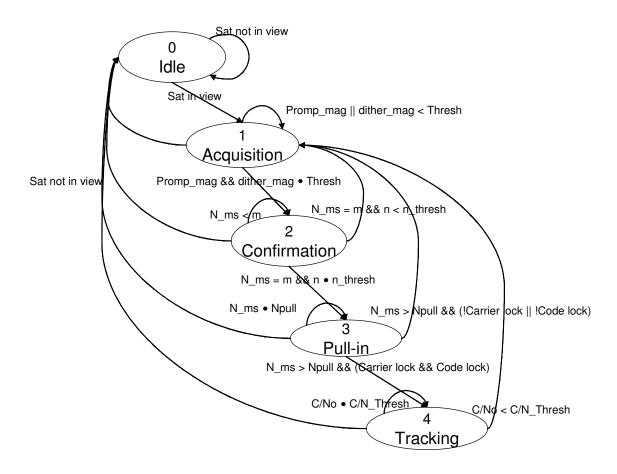


Figure 4-4 Channel State Diagram

The state of the satellite is shown in figure 4-5. We start out not knowing the almanac or ephemeris. Whatever data becomes available has the possibility of showing the satellite as healthy or unhealthy. Ultimately the satellite is declared usable only if the current ephemeris data says it is healthy.

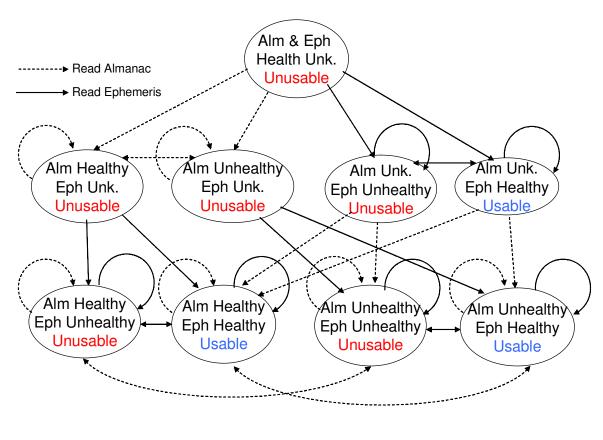


Figure 4-5 Satellite State Diagram

In figure 4-6 the major startup actions are depicted. Since GPS is such an accurate source of time the computer clock and clock interrupt routine are taken over. The computer clock is set to interrupt every few hundred micro-seconds and the IRQ 0 of the real time clock is re-directed to the GPS ISR. After the GP2021, the interrupt controller and PC clock are configured the program alternates between the GPS RCVR and GPS ISR code.

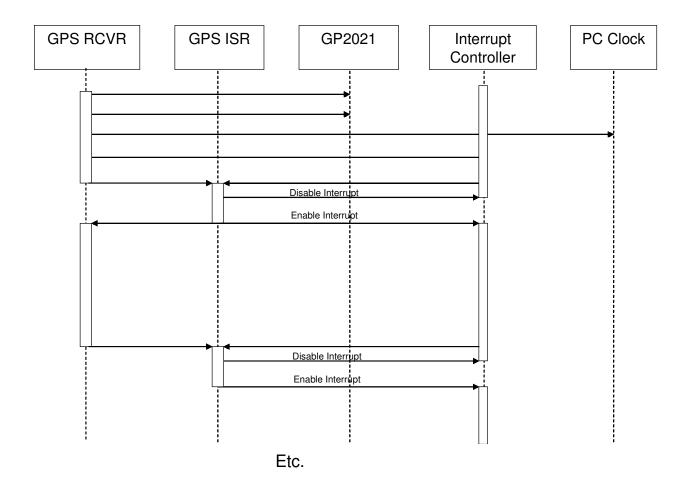


Figure 4-6
Receiver Startup Sequence Diagram

Figure 4-7 provides some more detail on the GPS interrupt service routine. The PC clock is set to wake up the interrupt controller after a few hundred micro-seconds. The first thing the ISR must do is to latch the channel correlation data. After reading the correlator and TIC status it reads the correlators and gets the measurement data. At this point it loops through all of the channels with data to be processed and either slews the correlator (during acquisition), or sets the carrier and code DCOs to track the signal. In order to avoid writing an ISR to be re-entrant the PC clock is reset after all of the channels are processed. This avoids more than 1 interrupt request being active at any time.

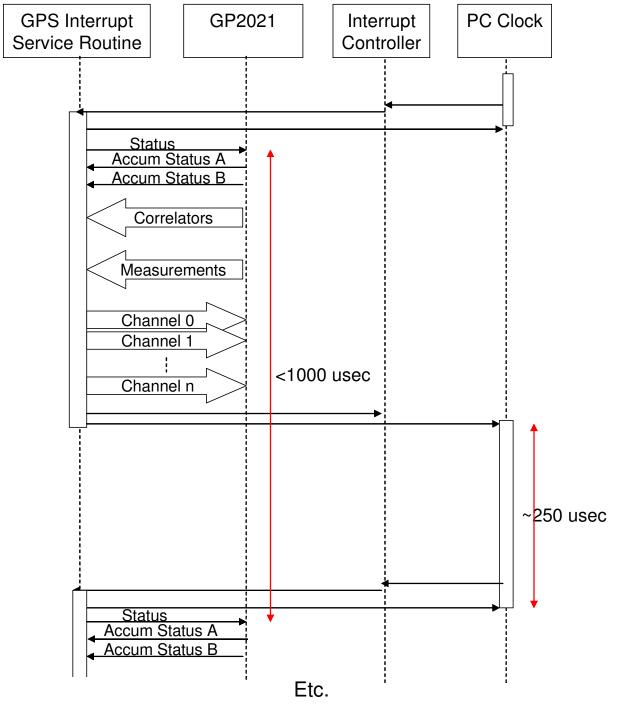


Figure 4-7
GPS Interrupt Service Routine Sequence Diagram

4.1.1 Constants.h

Only a few constants such as pi, the speed of light etc. are defined.

```
double const pi=3.1415926535898E0,r_to_d=57.29577951308232;
double const c=2.99792458e8,omegae=7.2921151467E-5;
// WGS-84 speed of light m/sec and earth rotation rate rad/sec
double const lambda=0.1902936728; // L1 wavelength in meters
long const SCALED_PI_ON_2 = 25736L; // used for fixed point Atan function long const SCALED_PI = 51472L; // used for fixed point Atan function
```

4.1.2 Globals.h

Globals.h is set up with 2 sections. The first is the definition of the globals with their corresponding initialization and is only used by MAIN which is defined only in gpsrcvr.cpp. The second section is the same set of globals but without initialization which is included when needed by other parts of the program.

```
#ifdef MAIN
channel chan[12];
int a missed, n chan, chmax=11, display page=0;
unsigned test[16]=
\{0x0001,0x0002,0x0004,0x0008,0x0010,0x0020,0x0040,0x0080,
  0 \times 0100, 0 \times 0200, 0 \times 0400, 0 \times 0800, 0 \times 1000, 0 \times 2000, 0 \times 4000, 0 \times 8000};
unsigned int tr_ch[13];
int prn_code[37]={0,0x3f6,0x3ec,0x3d8,0x3b0,0x04b,0x096,0x2cb,0x196,0x32c,
                 0x3ba, 0x374, 0x1d0, 0x3a0, 0x340, 0x280, 0x100, 0x113, 0x226,
                 0x04c,0x098,0x130,0x260,0x267,0x338,0x270,0x0e0,0x1c0,
                 0x380,0x22b,0x056,0x0ac,0x158,0x058,0x18b,0x316,0x058};
int out_debug, out_pos, out_vel, out_time, out_kalman;
hms cur_lat, cur_long;
#define IROLEVEL
                        0 // IRO Line
char Version[40]; // NMEA
// These are arrays for debugging
// they can be written into while running and dumped to a
// file at the end of the run
//long qdither[6][1500];
//long qprompt[6][1500];
//long idither[6][1500];
//long iprompt[6][1500];
//int qdither0[30000];
//int qprompt0[30000];
```

```
//int idither0[30000];
//int iprompt0[30000];
  long store_code, store_carrier;
// definitions with default values which can be overridden in
// file rcvr par.dat
int nav tic, search max f=30, search min f=0, cold prn=1, ICP CTL=0;
long rms=312,acq_thresh=650,code_corr,time_on=0;
long pull_code_k=111,pull_code_d=7,pull_carr_k=-12,pull_carr_d=28;
long trk_code_k=55, trk_code_d=3, trk_carr_k=-9, trk_carr_d=21;
long cc_scale=1540;
float nav_up=1.0;
double speed, heading;
int pull_in_time=1000,phase_test=500;
long d_freq=4698,d_tow,trk_div=19643;
      confirm_m=10, n_of_m_thresh=8, key, tic_count=0, hms_count=0;
int
      nav_count,min_flag,nav_flag,sec_flag,n_track;
unsigned int interr_int=512;
float clock_offset=-0.6;
ecef rec_pos_ecef;
long i_TIC_dt;
double m_time[3], delta_m_time, m_error, TIC_dt;
long TIC_cntr,old_TIC_cntr,TIC_ref=571427L,TIC_sum;
int
bit_pat[12]={0x2,0x4,0x8,0x10,0x20,0x40,0x80,0x100,0x200,0x400,0x800,0x1000};
int last hi carr[12], last hi code[12], ch status;
char last_address;
int ms_count;
int astat, mstat;
unsigned int ComOBaud; // NMEA
unsigned int Com1Baud;
unsigned int GPGGA;
unsigned int GPGSV;
unsigned int GPGSA;
unsigned int GPVTG;
unsigned int GPRMC;
unsigned int GPZDA;
char tzstr[40];// = "TZ=PST8PDT";
time_t thetime;
FILE *stream, *debug, *in, *out, *kalm;
almanac gps_alm[33];
      SVh[33], ASV[33];
float b0,b1,b2,b3,a10,a11,a12,a13; // broadcast ionospheric delay model
float a0, a1, tot, WNt, dtls, WNlsf, DN, dtlsf; //broadcast UTC data
ephemeris qps eph[33];
pvt rpvt;
```

```
state receiver;
float gdop,pdop,hdop,vdop,tdop,alm_toa;
unsigned long clock tow;
llh rec pos llh;
llh current_loc,rp_llh;
eceft track_sat[13];
ecef rec_pos_xyz;
int alm_gps_week,gps_week,almanac_valid,almanac_flag,handle;
unsigned long sf[6][11];
int p_error[6], status;
enum {off,acquisition,confirm,pull_in,track};
    0 1 2 3 4
enum {cold_start,warm_start,hot_start,tracking,navigating};
         0
              1
                                      3
unsigned long test_1[33] = \{0x00000000L,
                                                  // single bit set numbers
  0x00000001L,0x00000002L,0x00000004L,0x00000008L, // for testing bit positions
  0x0000010L,0x00000020L,0x00000040L,0x00000080L,
  0x00000100L,0x00000200L,0x00000400L,0x00000800L,
  0x00001000L, 0x00002000L, 0x00004000L, 0x00008000L,
  0x00010000L, 0x00020000L, 0x00040000L, 0x00080000L,
  0x00100000L, 0x00200000L, 0x00400000L, 0x00800000L,
  0x01000000L, 0x02000000L, 0x04000000L, 0x08000000L,
  0x10000000L, 0x20000000L, 0x40000000L, 0x80000000L};
float mask_angle;
char header[45], trailer;
double meas_dop[13];
ecef d_sat[13];
long carrier_ref=0x1f7b1b9L,code_ref=0x016ea4a8L;
double dt[13],cbias;
int m_tropo, m_iono, align_t; // flags for using tropo and iono models
satvis xyz[33];
#else
extern channel chan[12];
extern int a_missed, n_chan, chmax, display_page;
extern unsigned test[16];
extern unsigned int tr_ch[13];
extern int prn_code[37];
extern int out_debug,out_pos,out_vel,out_time,out_kalman;
extern hms cur lat, cur long;
```

```
extern char Version[40]; // NMEA
// These are arrays for debugging
// they can be written into while running and dumped to a
// file at the end of the run
// long far i_prompta[4500], far q_prompta[4500];
// long far i dithera[4500], far g dithera[4500];
// long far car freg[4500], far chip freg[4500];
// int far data_bit[4500];
//extern long qdither[6][1500];
//extern long qprompt[6][1500];
//extern long idither[6][1500];
//extern long iprompt[6][1500];
//extern int qdither0[30000];
//extern int qprompt0[30000];
//extern int idither0[30000];
//extern int iprompt0[30000];
extern long store_code, store_carrier;
// definitions with default values which can be overridden in
// file rcvr_par.dat
extern int nav_tic,search_max_f,search_min_f,cold_prn,ICP_CTL;
extern long rms, acq_thresh, code_corr, time_on;
extern long pull_code_k,pull_code_d,pull_carr_k,pull_carr_d;
extern long trk_code_k, trk_code_d, trk_carr_k, trk_carr_d;
extern long cc scale;
extern float nav up;
extern double speed, heading;
extern int pull_in_time,phase_test;
extern long d_freq,d_tow,trk_div;
extern int confirm_m,n_of_m_thresh,key,tic_count,hms_count;
extern int nav_count,min_flag,nav_flag,sec_flag,n_track;
extern unsigned int interr int;
extern float clock_offset;
extern ecef rec_pos_ecef;
extern long i TIC dt;
extern double m_time[3],delta_m_time,m_error,TIC_dt;
extern long TIC_cntr,old_TIC_cntr,TIC_ref,TIC_sum;
extern int bit pat[12];
extern int last_hi_carr[12], last_hi_code[12], ch_status;
extern char last address;
extern int ms_count;
extern int astat, mstat;
extern unsigned int Com0Baud; // NMEA
extern unsigned int Com1Baud;
extern unsigned int GPGGA;
extern unsigned int GPGSV;
extern unsigned int GPGSA;
extern unsigned int GPVTG;
extern unsigned int GPRMC;
extern unsigned int GPZDA;
```

```
extern char tzstr[40];// = "TZ=PST8PDT";
extern time_t thetime;
extern FILE *stream, *debug, *in, *out, *kalm;
extern almanac gps_alm[33];
extern int SVh[33], ASV[33];
extern float b0,b1,b2,b3,a10,a11,a12,a13; // broadcast ionospheric delay model
extern float a0,a1,tot,WNt,dtls,WNlsf,DN,dtlsf; //broadcast UTC data
extern ephemeris qps_eph[33];
extern pvt rpvt;
extern state receiver;
extern float gdop, pdop, hdop, vdop, tdop, alm_toa;
extern unsigned long clock_tow;
extern llh rec_pos_llh;
extern llh current_loc,rp_llh;
extern eceft track_sat[13];
extern ecef rec_pos_xyz;
extern int alm_gps_week,gps_week,almanac_valid,almanac_flag,handle;
extern unsigned long sf[6][11];
extern int p_error[6], status;
enum {off,acquisition,confirm,pull_in,track};
// 0 1 2 3 4
enum {cold_start,warm_start,hot_start,tracking,navigating};
         0 1 2 3
extern unsigned long test_1[33];
extern float mask_angle;
extern char header[45], trailer;
extern double meas dop[13];
extern ecef d_sat[13];
extern long carrier_ref, code_ref;
extern double dt[13],cbias;
extern int m_tropo, m_iono, align_t; // flags for using tropo and iono models
extern satvis xyz[33];
#endif
```

4.2 Data Structures

The following section describes the data and data structures used in the software and are defined in structs.h.

4.2.1 Channel data structures:

```
struct channel
 int state;
 carrier_freq, // commanded carrier DCO setting
                   // estimated Doppler in Hz
      doppler,
      carrier_corr; // carrier DCO correction for clock error
 char message[1500], // a frame of navigation data
      tow_sync, // flag to indicate time sync
                    // PRN assigned to this channel
      prn,
                   // number of data bits into message
      bit,
      frame_ready; // flag to indicate frame of data is ready to
                    // be processed
                 // Bit number of start of nav message in the
 int
     offset,
                  // circular bit register
      codes,
      n freq,
                 // frequency delta in search pattern
      del_freq;
                 // delta frequency used in search
 int t_count,
      ms count,
                 // number of ms into state 3
      ms set,
                 //
      i_confirm;
  int ms_epoch,
      n frame,
      ch_time,
      i count;
  int con_thresh, // threshold
      n thresh, // number of times above threshold in confirm
      sfid,
      missed,
      page5;
             // binary number from correlator I dither
  int i_dith,
      q_dith,
                 // binary number from correlator Q dither
      i_prompt, // binary number from correlator I prompt
                 // binary number from correlator Q prompt
      q_prompt;
  long sum,
      avg,
      old_theta,
      old q sum,
      th_rms;
 long dfreq,
      dfreq1,
      dcarr1,
```

```
dcarr,
       cycle_sum;
  long old_carr_dco_phase;
  long q_dith_20, // Q dither coherently integrated for 20 ms
       q_prom_20, // Q prompt coherently integrated for 20 ms
       i_dith_20, // I dither coherently integrated for 20 ms
       i_prom_20; // I prompt coherently integrated for 20 ms
  long prompt_mag, // RSS of I and Q of prompt correlator
         dith_mag; // RSS of I and Q of dither correlator
  long tr_bit_time, // GPS time when signal left satellite
       meas_bit_time, // number of bits into the GPS week at
                      // measurement time
       TOW.
                     // Time of Week from nav message
                    // Telemetry word from nav message
       TLM;
  long carrier_counter;
  long d carr phase;
  double int carr phase;
 unsigned long fifo0, // fifo used for message synchronization
                fifo1;
 unsigned int carr_dco_phase,
               carr_cycle_l,
               carr_cycle_h;
  unsigned int epoch,
               code_phase,
               code dco phase;
  float CNo; // Estimated signal carrier to noise ratio dB-Hz
};
        4.2.2
                Satellite Data Structures:
struct almanac
                          // Approximate orbital parameters
                // orbit angular velocity
  float w,
        ety,
                // eccentricity
        inc,
                // inclination
        rra,
                // rate of right ascension
                // square root of semi-major axis
        sqa,
        lan,
                // longitude of ascending node
               // argument of perigee
        aop,
                // mean anomaly
       ma,
                // time of almanac
       toa,
        af0,
                // satellite clock offset
                // satellite clock rate
        af1;
  char text message[23];
  int health, // is satellite usable?
       week,
                //
       sat file;
```

};

```
struct ephemeris // Precise orbital parameters
int iode,
    iodc,
     ura,
     valid,
     health,
     week;
double dn,
       tgd,
        toe,
        toc,
        omegadot,
        idot,
        cuc,
        cus,
        crc,
        crs,
        cic,
        cis;
        ma,
        e,
        sqra,
        w0,
        inc0,
        W,
        wm,
        ety,
        af0,
        af1,
        af2;
};
        4.2.3
                Receiver Data Structures:
float b0,b1,b2,b3, // Klobuchar Ionospheric
      al0, al1, al2, al3; // delay model parameters
float a0, a1, tot, WNt, dtls, WNlsf, DN, dtlsf; // GPS -> UTC conversion data
struct ecef
 double x,y,z;
};
struct eceft
 double x, y, z, tb;
```

float az,el;

```
};
struct llh
                  // Latitude, Longitude, Height above Ellipsoid
 double lat, lon, hae;
};
                  // Position Velocity Time
struct pvt
  double x, y, z, dt;
  double xv, yv, zv, df;
};
float gdop,pdop,hdop,vdop,tdop,alm_toa;
unsigned long clock_tow;
int alm_gps_week,
   gps_week,
   almanac_valid,
   almanac flag,
   handle;
int m_tropo, m_iono; // flags for using tropo and iono models
                     // flag for turning on the algorithm to align
int align_t;
                     //the receiver measurements to GPS time
struct velocity
 double east, north, up;
 double clock_err;
 ecef
       х,у, z;
};
struct dms
                   // angle in degrees, minutes, seconds
int deg, min;
float sec;
};
dms cur lat,
   cur_long;
struct state
 velocity vel;
 eceft
          pos;
           loc; // location in lat, long, hae
 llh
};
// These are arrays for debugging
// they can be written into while running and dumped to a
```

```
// file at the end of the run
  long far i_prompta[4500],
       far q_prompta[4500];
  long far i_dithera[4500],
       far q_dithera[4500];
  long far car_freg[4500],
       far chip_freq[4500];
  int far data_bit[4500];
  long store_code,
       store carrier;
// definitions with default values which can be
// overridden in file rcvr par.dat
int nav_tic,
     search_max_f=30,
     search min f=0,
    cold prn=1;
long rms=312,
                     // the standard deviation of noise in correlation
                     // counts
     acg thresh=650,
     code_corr,
    time_on=0;
long pull_code_k=111,
    pull_code_d=7,
    pull carr k=-12,
    pull_carr_d=28;
long trk_code_k=55,
    trk code d=3,
    trk carr k=-9,
    trk_carr_d=21;
long cc_scale=1540; // number of carrier cycles in a CA chip
float nav_up=1.0; // navigation update interval (sec)
                    // horizontal speed in meters/sec
double speed,
       heading; // horizontal heading deg from north->east
    pull_in_time=1000, // number of ms for pull in
int
                       // number of ms at end of pull in to
     phase test=500;
                        // measure phase error
long d_freq=4698,
      d tow,
      trk_div=19643;
int
     confirm_m=10,
      n_of_m_thresh=8,
      key,
      tic count=0,
     hms_count=0;
int
     nav_count,
      min flag,
      nav_flag,
      sec_flag,
      n_track;
unsigned int interr_int=512; // approx number of micro sec to delay next
                              // interrupt
```

```
float clock_offset=-0.6; // extimate of clock freq error in
                         // ppm (parts per million
ecef rec_pos_ecef;
                        // receiver position in ecef
long i_TIC_dt;
double m_time[3],
delta_m_time,
m_error,
TIC_dt;
     TIC_cntr,
long
       old_TIC_cntr,
       TIC\_ref=571427L, // nominal TIC setting for 100 ms tic
                         // intervals
       TIC_sum;
int debug_counter;
Matrix classes:
typedef class CMatrix Matrix;
typedef class CMatrix ColumnVector;
typedef class CMatrix DiagonalMatrix;
typedef class CMatrix SymmetricMatrix;
struct matrep
     double
                **Mat;
     int r;
                           // number of rows in the matrix
                           // number of columns in the matrix
     int c;
};
```

4.3 Receiver Control Algorithms

4.3.1 Introduction

The main routine of course manages the entire program. Only truly time critical functions are part of the interrupt routine. Other functions such as decoding the navigation message and computing the position and velocity fixes are called from the main loop. The overall timing is referenced from the 100 ms "tic".

4.3.2 Main

```
void main()
  char ch;
  self_test();
 io config(0x301);
 test control(0);
 system_setup(0);
 reset_cntl(0x0);
// delay(100);
  reset_cntl(0x1fff);
  ch_status=1;
  read rcvr par();
  rec_pos_xyz.x=0.0;
  rec_pos_xyz.y=0.0;
  rec_pos_xyz.z=0.0;
  if (out_kalman==1) kalm
                           =fopen("gpskalm.log","w+");
  if (out_pos==1 || out_vel==1 ||out_time==1) stream=fopen("gpsrcvr.log","w+");
  if (out_debug==1) debug=fopen("debug.log", "w+");
  read_initial_data();
  current loc=receiver loc();
  rec pos llh.lon=current loc.lon;
  rec_pos_llh.lat=current_loc.lat;
  rec_pos_llh.hae=current_loc.hae;
  nav_tic=nav_up*10;
 old TIC cntr=TIC cntr=TIC ref;
// program_TIC(TIC_cntr);
 code_corr=clock_offset*24.0;
  for (ch=0;ch<=11;ch++) chan[ch].state=off;</pre>
  time(&thetime); // set up thetime so it can be taken over by this program
#ifdef VCPP
 _setbkcolor(1);
 _displaycursor( _GCURSOROFF);
 _clearscreen( _GCLEARSCREEN); // PGB MS
#endif
#ifdef BCPP
  clrscr();
#endif
  if ( status != cold start ) chan allocate();
  else if (status==cold_start ) cold_allocate();
 m_time[1]=clock_tow;
```

```
read_ephemeris();
  int err;
  open_com( 0, Com0Baud, 0, 1, 8, &err ); // NMEA
  Interrupt Install();
//
  do
    if (kbhit()) key = getch();
                kev = ' \setminus 0';
    for (ch=0;ch<=11;ch++)
      if (chan[ch].frame_ready==1 )
           navmess(chan[ch].prn,ch);  // decode the navigation message
           chan[ch].frame_ready=0;  // for this channel
    if (sec_flag==1)
        SendNMEA();
        almanac_flag=0;
        thetime++;
#ifdef BCPP
        stime(&thetime);
#endif
        clock tow=(++clock tow)%604800L;
        time on++;
        sec_flag=0;
        for (ch=0;ch<=11;ch++)
            if (chan[ch].state==track)
      // Estimate C/No
               if (chan[ch].avg>0)
                    chan[ch].CNo=10.*log10(chan[ch].avg/1395.*
                                                 chan[ch].avg/1395.*25.*1.7777);
               else chan[ch].CNo=0.0;
               if (chan[ch].CNo<25.0)
      // calculate carrier clock and doppler correction
                   chan[ch].carrier corr=(-xyz[chan[ch].prn].doppler-
                                       clock_offset*1575.42)/42.57475e-3;
      // calculate code clock and doppler correction
                   code_corr=clock_offset*24.+xyz[chan[ch].prn].doppler/65.5;
                   chan[ch].code_freq=code_ref+code_corr;
                   ch_code(ch,chan[ch].code_freq); // 1.023 MHz chipping rate
                   chan[ch].state=acquisition;
                   chan[ch].t_count=0;
                   chan[ch].n_frame=0;
                   chan[ch].codes=0;
                   chan[ch].n freq=search min f;
                   chan[ch].tow sync=0;
                   chan[ch].del freq=1;
                   chan[ch].carrier_freq=carrier_ref+chan[ch].carrier_corr+
```

```
d_freq*chan[ch].n_freq; // set carrier
                                                               // select carrier
                   ch_carrier(ch,chan[ch].carrier_freq);
             }
         }
    nav fix once every X seconds
    if (nav_flag==1)
     nav_fix();
     nav_flag=0;
    channel allocation once every minute
    if (min_flag==1)
       if ( status != cold_start ) chan_allocate();
       else if (status==cold start ) cold allocate();
      min flag=0;
#ifdef BCPP
      clrscr();
#endif
#ifdef VCPP
      _clearscreen( _GCLEARSCREEN); // PGB MS
#endif
    display();
    if (key =='p' || key=='P')
      display_page++;
       display_page=display_page % 4;
#ifdef BCPP
       clrscr();
#endif
#ifdef VCPP
      _clearscreen( _GCLEARSCREEN); // PGB MS
#endif
  } while (key != 'x' && key != 'X');/*Stay in loop until 'X' key is pressed.*/
// Remove our interrupt and restore the old one
 Interrupt_Remove();
 close_com(); // NMEA
// Update the Almanac Data file
 if (almanac_valid==1) write_almanac();
// Update the Ephemeris Data file
 write_ephemeris();
// Update the ionospheric model and UTC parameters
 write_ion_utc();
// Update the curloc file for the next run
 if ( status==navigating )
    out=fopen("curloc.dat", "w+");
     fprintf(out, "latitude %f\n", rec pos llh.lat*r to d);
    fprintf(out, "longitude %f\n", rec pos llh.lon*r to d);
    fprintf(out, "hae
                       %f\n", rec_pos_llh.hae);
     fclose(out);
```

```
}
 fcloseall();
           4.3.2.1 Display
/*******************************
FUNCTION display()
RETURNS None.
PARAMETERS None.
PURPOSE
     This function displays the current status of the receiver on the
     computer screen. It is called when there is nothing else to do
WRITTEN BY
     Clifford Kelley
***********************************
void display(void)
 char ch;
#ifdef VCPP
 _settextposition(1,1);
#endif
#ifdef BCPP
 gotoxy(1,1);
#endif
 printf("
                              OpenSource GPS Software Version 1.13\n");
 printf("%s", ctime(&thetime));
 printf("TOW %6ld\n",clock_tow);
 printf("meas time %f error %f delta %f\n",m_time[1],m_error,delta_m_time);
 cur_lat.deg=rec_pos_llh.lat*r_to_d;
 cur_lat.min=(rec_pos_llh.lat*r_to_d-cur_lat.deg)*60;
 cur lat.sec=(rec pos llh.lat*r to d-cur lat.deg-cur lat.min/60.)*3600.;
 cur_long.deg=rec_pos_llh.lon*r_to_d;
 cur_long.min=(rec_pos_llh.lon*r_to_d-cur_long.deg)*60;
 cur_long.sec=(rec_pos_llh.lon*r_to_d-cur_long.deg-cur_long.min/60.)*3600.;
 printf("
          latitude
                     longitude
                                        HAE
                                                  clock error (ppm) \n");
 printf(" %4d:%2d:%5.2f %4d:%2d:%5.2f %10.2f %f\n",
 cur_lat.deg,abs(cur_lat.min),fabs(cur_lat.sec),cur_long.deg,abs(cur_long.min),
 fabs(cur_long.sec), rec_pos_llh.hae, clock_offset);
 printf(" Speed Heading TIC_dt\n");
 printf(" %lf %lf %lf\n", speed, heading*r_to_d, TIC_dt);
 printf(" \n");
 printf("tracking %2d status %1d almanac valid %1d gps week %4d\n",
 n_track, status, almanac_valid, qps_week%1024);
 if (display_page==0)
" ch prn state n_freq az el doppler t_count n_frame sfid ura page missed
CNo\n");
      for (ch=0; ch<=11; ch++)
```

```
{
           printf(
                    %4.0f %3.0f %6.0f %4d %4d %2d %3d %3d%5d
         %2d %3d
" %2d %2d
%4.1f\n",
           ch, chan[ch].prn, chan[ch].state, chan[ch].n_freq,
           xyz[chan[ch].prn].azimuth*57.3,xyz[chan[ch].prn].elevation*57.3,
     xyz[chan[ch].prn].doppler,chan[ch].t_count,chan[ch].n_frame,chan[ch].sfid,
     qps_eph[chan[ch].prn].ura,chan[ch].page5,chan[ch].missed,chan[ch].CNo);
 printf(" GDOP=%6.3f HDOP=%6.3f VDOP=%6.3f
TDOP=%6.3f\n", qdop, hdop, vdop, tdop); }
 else if (display_page==1)
  {
      printf( " ch prn state TLM
                                       TOW Health Valid TOW sync offset\n");
      for (ch=0; ch<=11; ch++)
           printf(" %2d %2d %2d %6ld %6ld
                                                %2d
                                                        82d
                                                                %2d
                                                                      %4d\n",
           ch, chan[ch].prn, chan[ch].state, chan[ch].TLM, chan[ch].TOW,
     qps_eph[chan[ch].prn].health,qps_eph[chan[ch].prn].valid,chan[ch].tow_sync
            chan[ch].offset);
      }
 else if (display page==2)
      printf(" ch prn state n_freq az el
                                                tropo
                                                              iono\n");
      for (ch=0;ch<=11;ch++)
                                       %4.0f %3.0f %10.4lf %10.4lf\n",
           printf(" %2d %2d %2d %3d
           ch, chan[ch].prn, chan[ch].state, chan[ch].n_freq,
           xyz[chan[ch].prn].azimuth*57.3, xyz[chan[ch].prn].elevation*57.3,
           chan[ch].Tropo*c, chan[ch].Iono*c);
 else if (display page==3)
      printf(" ch prn state
                                 Pseudorange
                                                 delta Pseudorange\n");
      for (ch=0; ch<=11; ch++)
           printf(" %2d %2d %2d %20.10lf %15.10lf\n",
           ch, chan[ch].prn, chan[ch].state, chan[ch].Pr, chan[ch].dPr);
 else if (display_page==4)// can be used for debugging purposes
  {
 }
}
```

4.3.2.2 Channel Allocation

The GP2021 has 12 channels and so is capable of tracking up to 12 satellites. The 24 satellite constellation can put from 5 to 12 satellites into view of a receiver on the surface of the earth. Thus for every satellite in view a channel is available to track it. This makes the software much easier than that required if a smaller number of channels is available. There are two allocation algorithms needed. The first, Cold Allocation is used when there is not enough information to to compute what satellites are in view, the second is used when there is.

4.3.2.2.1 Cold Allocation

Cold Allocation is a boot strap algorithm for channel allocation. It tries every PRN code in groups of 12 and searches a very wide Doppler region since we are not sure of the clock error or our velocity or position.

```
/*****************************
FUNCTION cold_allocate()
RETURNS None.
PARAMETERS None.
PURPOSE To allocate the PRNs to channels for a cold start, start by searching
       for PRN 1 through 12 and cycling through all PRN numbers skipping
channels
       that are tracking
WRITTEN BY
     Clifford Kelley
***********************************
void cold allocate()
  satvis dummy;
  char ch, i, alloc;
  search_max_f=50;
                         // widen the search for a cold start
  dummy=satfind(0);
  almanac_valid=1;
  reset_cntl(0x1fff);
  for (i=1; i \le 32; i++)
     if (gps_alm[i].inc>0.0 && gps_alm[i].week!=gps_week%1024) almanac_valid=0;
  if (al0==0.0 && b0==0.0)almanac valid=0;
  for (ch=0;ch<=chmax;ch++) // if no satellite is being tracked
                           // turn the channel off
   {
     if ( chan[ch].CNo<30.0 )// if C/No is too low turn the channel off
       chan[ch].state=off;
       chan[ch].prn=0;
  for (i=0;i<=chmax;i++)</pre>
     alloc=0;
     for (ch=0; ch<=chmax; ch++)</pre>
```

```
{
         if (chan[ch].prn==cold_prn)
            alloc=1;// satellite is already allocated a channel
            break;
      if (alloc==0) // if not allocated find an empty channel
        for (ch=0; ch<=chmax; ch++)</pre>
          if (chan[ch].state==off)
             chan[ch].carrier_corr=-clock_offset*1575.42/42.57475e-3;
             chan[ch].carrier_freq=carrier_ref+chan[ch].carrier_corr;// compute
                                                                      // carrier
             ch_carrier(ch, chan[ch].carrier_freq);
                                                                // select carrier
             chan[ch].code_freq=code_ref;
             ch_code(ch,chan[ch].code_freq); // 1.023 MHz chipping rate
             ch_cntl(ch,prn_code[cold_prn]|0xa000);// 0xa000 for late select
                                                   // satellite
             chan[ch].prn=cold_prn;
             ch_on(ch);
             chan[ch].state=acquisition;
             chan[ch].codes=0;
             chan[ch].n_freq=search_min_f;
             chan[ch].del freq=1;
             cold_prn=cold_prn%32+1;
             break;
        }
      }
    }
}
```

4.3.2.2.2 Warm/Hot Allocation

The Warm/Hot Allocation routine uses the current time, location, and satellite almanac to predict what satellites are in view and what doppler will be observed.

```
void chan_allocate()
   char ch, prnn, alloc;
  int i;
  almanac_valid=1;
   for (prnn=1;prnn<=32;prnn++)</pre>
      xyz[prnn] = satfind(prnn);
      if (gps_alm[prnn].inc>0.0 && gps_alm[prnn].week!=gps_week%1024)
         almanac_valid=0;
   if (al0==0.0 && b0==0.0)almanac_valid=0;
   for (ch=0;ch<=11;ch++) // if the sat has dropped below mask angle
                           // turn the channel off
      if (xyz[chan[ch].prn].elevation < mask_angle ||</pre>
                    gps_alm[chan[ch].prn].ety == 0.0)
      {
         chan[ch].state=off;
         chan[ch].tow_sync=0;
         chan[ch].prn=chan[ch].offset=0;
         chan[ch].CNo=0.0;
         chan[ch].n_freq=chan[ch].t_count=chan[ch].n_frame=chan[ch].sfid=0;
         chan[ch].Pr=chan[ch].dPr=chan[ch].Tropo=chan[ch].Iono=0.0;
         chan[ch].TOW=chan[ch].TLM=0;
         for (i=0;i<1500;i++) chan[ch].message[i]=0;
   for (prnn=1;prnn<=32;prnn++)</pre>
      if (xyz[prnn].elevation > mask_angle && gps_alm[prnn].health==0 &&
                   gps_alm[prnn].ety != 0.00)
         alloc=0;
         for (ch=0;ch<=11;ch++)
             if (chan[ch].prn==prnn)
                   alloc=1;// satellite already allocated a channel
                   break;
         if (alloc==0) // if not allocated find an empty channel
            for (ch=0;ch<=11;ch++)
               reset_cntl(0x1fff);
               if (chan[ch].state==off)
      // calculate carrier clock and doppler correction
                   chan[ch].carrier corr=(-xyz[prnn].doppler-
                                          clock offset*1575.42)/42.57475e-3;
      // calculate code clock and doppler correction
                   code_corr=clock_offset*24.+xyz[prnn].doppler/65.5;
                   chan[ch].code freq=code ref+code corr;
```

```
chan[ch].prn=prnn;
             chan[ch].state=acquisition;
             chan[ch].codes=0;
             chan[ch].n_freq=search_min_f;
             chan[ch].del_freq=1;
             chan[ch].carrier_freq=carrier_ref+chan[ch].carrier_corr+
                           d_freq*chan[ch].n_freq; // set carrier
                                               // select carrier
             ch_carrier(ch,chan[ch].carrier_freq);
             break;
        }
       }
    }
  }
}
```

4.4 GPS Interrupt Service Routine (GPS ISR)

4.4.1 Main

The main interrupt routine checks for correlation and measurement data, retrieves these data and then branches to the routine for the state each channel is in.

```
/**********************************
FUNCTION GPS_Interrupt()
RETURNS None.
PARAMETERS None.
PURPOSE
    This function replaces the current IRQO Interrupt service routine with
    our GPS function which will perform the acquisition - tracking functions
WRITTEN BY
    Clifford Kelley
*******************************
#ifdef VCPP
void __interrupt _far GPS_Interrupt(void) // MS
#endif
#ifdef BCPP
void interrupt GPS_Interrupt(...)
#endif
//
     int astat, mstat;
     unsigned int add;
     char ch;
     to_gps(0x80,0);
                           // tell 2021 to latch the correllators
     a_missed=from_gps(0x83); // did we miss any corellation data
                            // get info on what channels have data ready
     astat=from_gps(0x82);
     for (ch=0;ch<=chmax;ch++)</pre>
         if (astat & test[ch])
      add=0x84+(ch<<2);
      add++;
      add++;
      chan[ch].i_prompt=from_gps(add); // inphase prompt
      chan[ch].q prompt=from qps(add); // quadrature prompt
      if (a missed & test[ch])
```

```
chan[ch].missed++;
          ch_accum_reset(ch);
       }
      for (ch=0;ch<=chmax;ch++)</pre>
          if (astat & test[ch])
     switch(chan[ch].state)
       case acquisition:
           ch_acq(ch);
           break;
       case confirm
           ch_confirm(ch);
           break;
       case pull_in
           ch_pull_in(ch);
           break;
       case track
           ch_track(ch);
           break;
      mstat=a missed & 0x2000; // has a tic occurred?
      if (mstat)
          tic_count=(++tic_count)%10;
          if (tic_count==0) sec_flag=1;
                                         // one second has passed
          hms_count=(++hms_count)%600;
          if (hms_count==0) min_flag=1;
                                         // one minute has passed
          nav count=(++nav count)%nav tic;
          if (nav_count==0) nav_flag=1;
          TIC_sum+=TIC_cntr+1;
          add=1;
          for (ch=0; ch<=chmax; ch++)</pre>
       {
           add++;
           // computing
      add++;
           chan[ch].carr_dco_phase=from_gps(add); // delta-pseudorange
      add+=3;
           chan[ch].carr_cycle_h=from_gps(add);
           add+=3;
chan[ch].cycle_sum=chan[ch].carr_cycle_1+65536L*chan[ch].carr_cycle_h;
        {
            add=1;
            for (ch=0; ch<=chmax; ch++)</pre>
               chan[ch].code_phase=from_gps(add); // get code data for
computing
```

```
add+=3;
                                                      // pseudorange
                 chan[ch].epoch=from_gps(add);
                 chan[ch].code_dco_phase=from_gps(add);
                 add+=4:
                 chan[ch].meas bit time=chan[ch].tr bit time;
                 chan[ch].doppler=chan[ch].carrier freq;
                 chan[ch].carrier counter=chan[ch].cycle sum;
                 chan[ch].d_carr_phase=chan[ch].carr_dco_phase -
chan[ch].old_carr_dco_phase;
                 chan[ch].old_carr_dco_phase=chan[ch].carr_dco_phase;
               i_TIC_dt= TIC_sum+old_TIC_cntr-TIC_cntr;
               TIC_sum=0;
             }
             for (ch=0; ch<=chmax; ch++)</pre>
          chan[ch].old_carr_dco_phase=chan[ch].carr_dco_phase;
// reset the interrupt
#ifdef VCPP
       _outp( 0x20,0x20 ); // MS
#endif
#ifdef BCPP
       outportb (0x20, 0x20);
#endif
}
```

4.4.2 Search State

The process of tracking a satellite begins by searching for the signal. This process starts by doing trial correlations and checking the correlation results to determine if the signal is present. As illustrated in figure 4-8 the search is conducted in code and frequency space. The GP2021 has the ability to add N½ chip intervals to the correlation time. This is called slewing the code. Starting at frequency where the signal is expected the rss of the inphase and quadrature values are checked for the promt and dither correlators every millisecond. Every millisecond the code is slewed 1 chip and thus every ½ chip in code space is searched.

The values are compared to a threshold. If both the prompt and dither magnitudes are above this threshold the channel transitions to the confirmation state.

As seen in figure 4-9 the sample distribution has Rayleigh distribution when a signal is not present and Ricean when a signal is present.

$$p_n(z) = \frac{z}{\sigma_n^2} e^{-\left(\frac{z^2}{2\sigma_n^2}\right)}$$

$$p_s(z) = \frac{z}{\sigma_n^2} e^{-\left(\frac{z^2 + A^2}{2\sigma_n^2}\right)} I_0\left(\frac{zA}{\sigma_n^2}\right)$$

$$P_{d} = \int_{V_{t}}^{\infty} \frac{z}{\sigma_{n}^{2}} e^{-\left(\frac{z^{2} + A^{2}}{2\sigma_{n}^{2}}\right)} I_{0}\left(\frac{zA}{\sigma_{n}^{2}}\right) dz$$

$$P_{fa} = \int_{0}^{V_t} \frac{z}{\sigma_n^2} e^{-\left(\frac{z^2}{2\sigma_n^2}\right)} dz$$

$$P_{fa} = e^{-\left(\frac{V_t^2}{2\sigma_n^2}\right)}$$

$$V_{t} = \sigma_{n} \sqrt{-2 \ln(P_{fa})}$$

This example, is for a 1 ms integration interval, the 1 sigma value of noise is 312 and the signal to noise ratio shown is 3. The process of searching is a classic example of the trade-off between the false alarm rate and the probability of detection

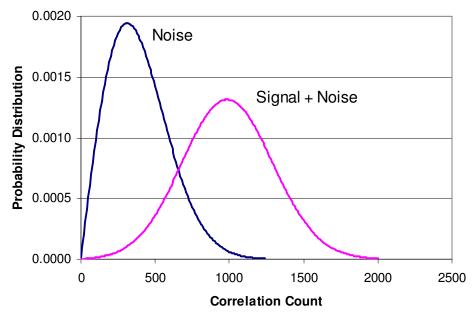


Figure 4-8 Acquisition Distributions

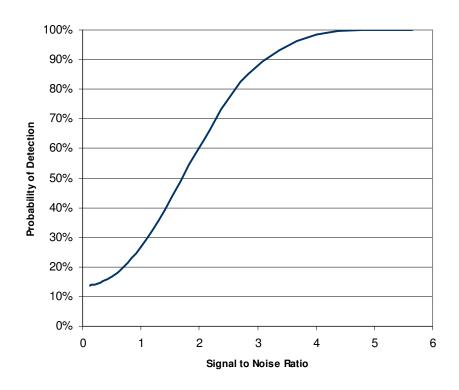


Figure 4-9
Probability of Detection vs Signal to Noise Ratio for Threshold of 630

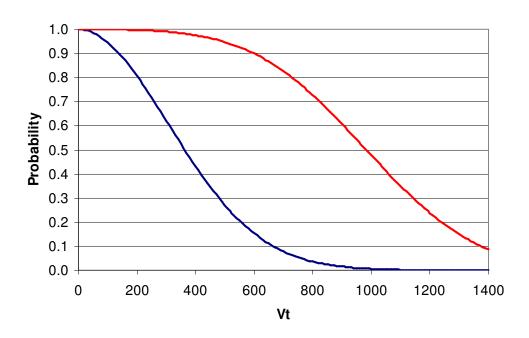


Figure 4-10 Probability of Detection/False alarm vs Vt

In this algorithm both the prompt and dither correlation values must be above the threshold. This keeps the probability of detection high while greatly reducing the false alarm rate.

```
/************************
FUNCTION ch_acq(char ch)
RETURNS None.
PARAMETERS
               ch char
PURPOSE to perform initial acquisition by searching code and frequency space
               looking for a high correllation
WRITTEN BY
     Clifford Kelley
********************************
void ch_acq(char ch)
 long prompt_mag, dith_mag;
 if (abs(chan[ch].n_freq) <= search_max_f) // search frequencies</pre>
      prompt_mag=rss(chan[ch].i_prompt,chan[ch].q_prompt);
      dith_mag =rss(chan[ch].i_dith,chan[ch].q_dith);
      if ((dith_mag > acq_thresh) && (prompt_mag > acq_thresh))
           ch_code_slew(ch,2044);
                                      // slew back 1 chip so we can
                                   // confirm the signal
           chan[ch].state=confirm;
           chan[ch].i_confirm=0;
           chan[ch].n_thresh=0;
      }
      else
      {
          ch_code_slew(ch,2);
          chan[ch].codes+=2;
      if (chan[ch].codes==2044)
          chan[ch].n_freq+=chan[ch].del_freq;
          chan[ch].del_freq=-(chan[ch].del_freq+sign(chan[ch].del_freq));
          chan[ch].carrier_freq=carrier_ref+chan[ch].carrier_corr+
     d_freq*chan[ch].n_freq; // set carrier
          chan[ch].codes=0;
      }
 }
 else
 {
           chan[ch].n_freq=search_min_f;
                                                     // keep looping
           chan[ch].del_freq=1;
```

4.4.3 Confirmation State

In order to keep the probability of detection high the acquisition state produces a high false alarm rate. The purpose of the confirmation state is to maintain this high probability of detection while decreasing the false alarm rate. In this state we keep the code and carrier settings constant and collect M correlation time samples. If either the prompt or delay results are above the threshold it is counted and if this count is greater than or equal to N then the channel transitions to the pull-in state. If not we transition back to the acquisition state.

The probability of detection at this point is:

MORE STUFF NEEDED

While the probability of false alarm at this point is:

```
void ch_confirm(char ch)
 long prompt_mag, dith_mag;
 prompt_mag = rss(chan[ch].i_prompt,chan[ch].q_prompt);
 dith_mag = rss(chan[ch].i_dith,chan[ch].q_dith);
 if ((prompt mag > acg thresh) || (dith mag > acg thresh))
              chan[ch].n thresh++;
 if (chan[ch].i_confirm==confirm_m) // have we got m samples?
     if (chan[ch].n_thresh >= n_of_m_thresh) // are enough > threshold?
         chan[ch].ch time=0;
                                  // initialize variables for pull-in
         chan[ch].sum=0;
         chan[ch].th_rms=0;
         chan[ch].ms_set=0;
     else chan[ch].state=acquisition;
```

}

4.4.4 Pull-in

At the point of confirmation we have confirmed to a high degree of confidence that a signal has been found. But, because the correlation peak is so wide in frequency we may be very far off in frequency. The pull-in state attempts to track the signal by using a combination of frequency and phase tracking to lock on the carrier. In addition a code tracking loop is implemented to track the signal in code.

In order to avoid transients the loops are not immediately closed. An x ms delay is built into the code loop and y ms delay is built into the carrier loop. Both loops are updated every millisecond. Since we don't want the tracking state to start in the middle of a data bit we stay in pull-in for at least the required number of ms and then is extended until the end of a data bit. For the last m ms of pull-in the average correlation value, phase error and data bit sync is checked to decide whether or not to go into the tracking state. In addition pull-in is the final step in detection. The pull-in range is approximately 2/3T or 667 Hz for a 1 ms integration interval.

4.4.4.1 Code Tracking

The code tracking loop is a classic DLL updated every millisecond.

MORE STUFF NEEDED

4.4.4.2 Carrier Tracking

The carrier tracking loop has both a phase locked loop (PLL) and a frequency locked loop (FLL). A phase locked loop tracks with less noise but is limited in the phase error it can track. The FLL works with large phase errors but it has more noise. In either case since both correlators are about ¼ of a chip from the peak they both have equally valid phase data. Because of this the correlation results from both inphase and both quadrature correlators are added. Since it is likely that the carrier frequency is far away from the receiver carrier DCO setting the loop starts out weighted toward a FLL and it's weighting is decreased as a function of time until the PLL dominates. Figure 4-11 and 4-12 show the FLL weighting and some sample data collected during a pull-in.

Figure 4-11 PLL Weighting

Figure 4-12 Carrier Phase during Pull-In

4.4.4.3 Bit synchronization

The data message is transmitted at a rate of 20 ms per bit or 50 Hz. Since the correllators dump data at 1 ms intervals each bit lasts for 20 samples. The start of a data bit can be detected by noting when the phase of the signal has changed by 180 degrees. As seen in figure 4-13 each channel in the GP 2021 has a counter that counts the number correlator dumps and runs from 0 to 19 and rolls over. The algorithm used in this routine as shown in figure 4-14 sets this counter to 0 when the carrier phase changes from +-90 degrees with a tolerance of ~10 degrees to a carrier phase of -+90 degrees also with a tolerance of ~10 degrees. As shown in the state diagram a transition to state 4 or tracking is not allowed unless the ms counter is set.

Figure 4-13 Bit Synchronization

```
void ch_pull_in(char ch)
   long ddf,ddcar,theta_e,wdot_gain;
  long q_sum, i_sum, theta, theta_dot;
   long prompt_mag, dith_mag;
   prompt_mag=rss(chan[ch].i_prompt,chan[ch].q_prompt);
   dith_mag =rss(chan[ch].i_dith,chan[ch].q_dith);
   chan[ch].sum+=prompt_mag+dith_mag;
//
// code tracking loop
   if ( prompt_mag != 0 || dith_mag != 0)
      chan[ch].dfreq=((prompt_mag - dith_mag) <<14)</pre>
                                         /(prompt_mag+dith_mag)*pull_code_k;
      ddf = (chan[ch].dfreq-chan[ch].dfreq1) *pull_code_d;
      if ( chan[ch].ch time > 2 )
                                             // don't close the code loop
                                             // for 2 ms to avoid transients
            chan[ch].code_freq = ((chan[ch].dfreq+ddf)>>14)+chan[ch].code_freq;
            ch_code(ch,chan[ch].code_freq);
   chan[ch].dfreq1=chan[ch].dfreq;
// carrier tracking loop
   g sum=chan[ch].g dith+chan[ch].g prompt;
   i_sum=chan[ch].i_dith+chan[ch].i_prompt;
   if (i_sum !=0 || q_sum !=0) theta=fix_atan2(q_sum,-i_sum);
   else theta=chan[ch].old_theta;
   theta_dot=theta-chan[ch].old_theta;
   chan[ch].ms_count++;
// check to see if we are at the edge of a data bit
   if ( sign(q_sum) ==-sign(chan[ch].old_q_sum) && (a_missed & test[ch]) == 0
```

```
&& labs(labs(theta) -25736) < 4096
         && labs(labs(chan[ch].old_theta)-25736)<4096)
{
                             // if yes set the counter to 1
    chan[ch].ms count=0;
    ch epoch load(ch,0x1);
                             // load it to ms counter on GP 2021
    chan[ch].ms set=1;
                              // set flag to say we have bit sync
chan[ch].old_theta = theta;
       (theta> 0) theta_e = theta-25736;
else if (theta<=0) theta = theta+25736;
if (chan[ch].ch_time>pull_in_time-phase_test) chan[ch].th_rms+=
                                                (theta_e*theta_e)>>14;
if (labs(theta_dot) < 32768L)
    if (q_sum != 0 || i_sum !=0)
      wdot gain=chan[ch].ch time/499;
      wdot_gain*=wdot_gain;
      wdot_gain*=wdot_gain;
       chan[ch].dcarr=pull_carr_k*(theta_dot*5/(1+wdot_gain)+theta_e);
       ddcar=(chan[ch].dcarr-chan[ch].dcarr1)*pull_carr_d;
                                          // don't close the loop for
       if ( chan[ch].ch_time > 5 )
                                          // 5 ms to avoid transients
             chan[ch].carrier_freq = ((chan[ch].dcarr+ddcar)>>14)+
                                     chan[ch].carrier_freq;
             ch_carrier(ch, chan[ch].carrier_freq);
       }
   }
chan[ch].dcarr1=chan[ch].dcarr;
chan[ch].old_q_sum=q_sum;
chan[ch].ch_time++;
chan[ch].ms_count=chan[ch].ms_count%20;
if (chan[ch].ch_time>=pull_in_time && chan[ch].ms_count==19) // done with
                                                              // pull-in
                                                        // wait until end of
{
    chan[ch].avg=chan[ch].sum/pull in time/2;
                                                       // a data bit
    chan[ch].th rms=fix sqrt(chan[ch].th rms/phase test);
    if (chan[ch].avg>14*rms/10 && chan[ch].th_rms<12000 && chan[ch].ms_set)
                                              // go to track
            chan[ch].avg=chan[ch].avg*20;
                                              // if code and carrier track
            chan[ch].state=track;
                                              // and the ms counter is set
            chan[ch].t count=0;
            chan[ch].sum=0;
            chan[ch].q_dith_20=0;
            chan[ch].q_prom_20=0;
            chan[ch].i_dith_20=0;
            chan[ch].i_prom_20=0;
            if (ch==0)
            {
                 debug_counter=0;
                 store_code=chan[ch].code_freq;
                 store carrier=chan[ch].carrier freq;
            chan[ch].dfreq=0;
    else
                                              // else go back to acquisition
```

4.4.5 Tracking State

The tracking state is very similar to pull-in state except for two areas. The carrier loop commands are computed at 1000 Hz and the code loop commands are computed at 50 Hz. Also, whenever a code loop command is computed the data bit is determined and sent to the pream routine which finds the preamble in the navigation message and synchronizes up to the TOW message and checks the subframe number.

MORE STUFF NEEDED

4.4.5.1 Code Tracking

As can be seen in figure 4-15 the tracking state code tracking loop is very similar to the pull-in state tracking loop. The addition of carrier aiding allows the bandwidth to be decreased from xx Hz in the pull-in state to xx Hz. Since the code tracking loop will lose lock when carrier lock is lost this does not appear to penalize the performance.

MORE STUFF NEEDED

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Figure 4-15 Tracking State Code Tracking Loop

Since this is the loop used when measurements are made an analysis of the noise tracking is presented.

As given in reference 1

$$\sigma_{tDLL} = \lambda_c \sqrt{\frac{2F_1 d^2 B_n}{c / n_0} \left[2(1 - d) + \frac{4F_2 d}{Tc / n_0} \right]}$$

Where:

 σ_{tDLL} = 1-sigma thermal noise code tracking jitter

F1 = DLL discriminator correlator factor (dimensionless)

= 1 for time shared tau-dithered early/late correlator

= $\frac{1}{2}$ for dedicated early and late correlators

d = correlator spacing between early, prompt, and late (chips)

Bn = code loop noise bandwidth (Hz)

c/n0 = carrier to noise power expressed as a ratio

= $10^{\text{C/No/10}}$ for C/No in dB-Hz

T = predetection integration time (sec)

F2 = DLL discriminator type factor (dimensionless)

= 1 for early/late type discriminator

= $\frac{1}{2}$ for dot product type discriminator

 λc = the code length of 293.05 m/chip for C/A-code

The GP2021 chipset along with OpenSourceGPS uses an F1 of 1/2, d=1/2, and F2=1. The other parameters are ...

Figure 4-16 shows the expected performance of OpenSourceGPS code tracking jitter vs C/No

Figure 4-16 Code Tracking jitter vs C/No

4.4.5.2 Carrier Tracking

Since this is the loop used when measurements are made an analysis of the noise tracking is presented. As given in reference xx:

$$\sigma_{tPLL} = \frac{\lambda_L}{2\pi} \sqrt{\frac{B_n}{c / n_0} \left[1 + \frac{1}{2T \, c/n_0} \right]}$$

Where:

 σ_{tPLL} = 1-sigma thermal noise code tracking jitter

Bn = carrier loop noise bandwidth (Hz)

= carrier to noise power expressed as a ratio = 10^{C/No/10} for C/No in dB-Hz c/n_0

T = predetection integration time (sec)

= the carrier frequency wave length of 0.1903 m/cycle for L1 $\lambda_{\rm L}$

Figure 4-17 shows the expected performance of OpenSourceGPS carrier tracking jitter vs C/No

MORE STUFF NEEDED

Figure 4-17 Carrier Tracking jitter vs C/No

4.4.5.3 Message Synchronization

Message synchronization starts by detecting the message preamble. To do this it uses a 62 bit split and offset fifo data structure. Figure 4-18 illustrates how this was set up. Two 32 bit registers are linked at the 30th bit of first register. This allows 2 message words to be checked for parity and have enough data to analyze the TLM and HOW words. The routine uses a set of nested comparisons to reduce the computation time. The first 8 bits of the TLM word is the preamble and the first 17 bits of the HOW word is a truncated TOW Count. Bits 20-22 of the HOW word are the subframe ID.

MORE STUFF NEEDED

Figure 4-18 Preamble Detection

In order to save time the preamble is checked in several stages.

The algorithm is a follows:

Check for preamble or inverse of preamble bits
Check parity of word 0
Check parity of word 1
Check subframe number (1-5)
Check TOW against receiver time

When all of these checks pass we know that the current data bit is bit 59 of the nav message (counting from 0).

The next thing we set is the transmission bit time into the week. Since the message time is the start of the next subframe we set the bit time to 240 bits less than the TOW.

The navigation message itself is continuously recorded into a circular register. When the subframe number is found we can determine the offset bit number in this register. This value tells the navigation message decoding routine where the message starts.

```
void pream(char ch, char bit)
  static unsigned long pream=0x22c00000L;
  unsigned long parity0, parity1;
  static unsigned long pb1=0xbb1f3480L,pb2=0x5d8f9a40L,pb3=0xaec7cd00L;
  static unsigned long pb4=0x5763e680L,pb5=0x6bb1f340L,pb6=0x8b7a89c0L;
  unsigned long TOWs, HOW, TLM, TLMs;
  int sfid_s;
  if (chan[ch].fifo1&0x2000000L)
        chan[ch].fifo0=(chan[ch].fifo0<<1)+ 1;
  }
  else
  {
        chan[ch].fifo0=chan[ch].fifo0<<1;</pre>
  chan[ch].fifo1=(chan[ch].fifo1<<1)+bit;</pre>
  if (chan[ch].fifo0&0x4000000L)
        TLM = chan[ch].fifo0^0x3fffffc0L;
  }
  else
  {
        TLM = chan[ch].fifo0;
  if (chan[ch].fifo1&0x4000000L)
        HOW = chan[ch].fifo1^0x3fffffc0L;
  }
  else
  {
        HOW = chan[ch].fifo1;
  if (((pream^TLM)&0x3fc00000L)==0)
                                      // preamble pattern found?
        parity0=(xors(TLM & pb1)<<5)+(xors(TLM & pb2)<<4)+
                     (xors(TLM \& pb3) << 3) + (xors(TLM \& pb4) << 2) +
                     (xors(TLM & pb5) << 1) + (xors(TLM & pb6));
        if (parity0 == (TLM \& 0x3f)) // is parity of TLM ok?
              parity1=(xors(HOW & pb1)<<5)+(xors(HOW & pb2)<<4)+
                                 (xors(HOW \& pb3) << 3) + (xors(HOW \& pb4) << 2) +
                                 (xors(HOW & pb5) << 1) + (xors(HOW & pb6));
              if (parity1==(HOW \& Ox3f)) // is parity of HOW ok?
```

```
{
                  sfid_s=int((HOW \& 0x700)>>8); // compute the subframe id
                                                 // number
                  TLMs=(TLM>>2) & 0x3fff;
                  if (sfid s==1)
                                      // synchronize on subframe 1 if TOW matches
                                      // clock within 300 seconds
                    TOWs = (HOW \& 0x3ffffffffL) >> 13;
                    d_tow=clock_tow-TOWs*6+5; // +5 since TOW is 6 sec ahead
                    if (labs(dtow)<300)
                        chan[ch].offset=chan[ch].t_count-59;
                        ch_epoch_load(ch,(0x1f&ch_epoch_chk(ch))|0xa00); //cwk
                        if (chan[ch].offset<0.0) chan[ch].offset+=1500;</pre>
                        chan[ch].tr_bit_time=TOWs*300-240;
                        chan[ch].TOW=TOWs*6;
                        chan[ch].tow_sync=1;
                        thetime=thetime-d tow;
                        clock_tow=TOWs*6-5;
                        chan[ch].sfid=sfid_s;
                        chan[ch].TLM=TLMs;
                  }
// allow resync on other subframes if TOW matches clock to 3 seconds
// this should improve the re-acquisition time
                  else if (sfid_s>1 && sfid_s<6)
                    TOWs = (HOW \& 0x3fffffffL) >> 13;
                    d tow=clock tow-TOWs*6+5; // +5 since TOW is 6 sec ahead
                    if (labs(d_tow)<3)
                        chan[ch].offset=chan[ch].t_count-59-(sfid_s-1)*300;
                        ch_epoch_load(ch, (0x1f&ch_epoch_chk(ch)) | 0xa00);
                        if (chan[ch].offset<0.0) chan[ch].offset+=1500;</pre>
                        chan[ch].tr_bit_time=TOWs*300-240;
                        chan[ch].tow_sync=1;
                        chan[ch].TOW=TOWs*6;
                        chan[ch].sfid=sfid s;
                        chan[ch].TLM=TLMs;
                    }
               }
             }
// a 1500 bit frame of data is ready to be read
  if ((chan[ch].t_count-chan[ch].offset)%1500==0) chan[ch].frame_ready=1;
      4.4.5.4 Ch_track listing
void ch_track(char ch)
     long ddf,ddcar,q_sum,i_sum;
     chan[ch].ms_count=(++chan[ch].ms_count)%20; // Software ms count
     chan[ch].g dith 20+=chan[ch].g dith;
                                                    // 20 ms summed q dith
```

```
// 20 ms summed i_dith
     chan[ch].i_dith_20+=chan[ch].i_dith;
                                                 // 20 ms summed i_prompt
     chan[ch].i_prom_20+=chan[ch].i_prompt;
//
// now the carrier phase locked loop
    q_sum=chan[ch].q_dith+chan[ch].q_prompt;
    i_sum=chan[ch].i_dith+chan[ch].i_prompt;
    if ( q_sum != 0 || i_sum != 0)
chan[ch].dcarr=(i_sum<<14)*trk_carr_k*sign(q_sum)/rss(q_sum,i_sum);//check
       ddcar=(chan[ch].dcarr-chan[ch].dcarr1)*trk_carr_d;
       chan[ch].carrier_freq=((chan[ch].dcarr+ddcar)>>14)+chan[ch].carrier_freq;
      ch_carrier(ch, chan[ch].carrier_freq);
    chan[ch].old_q_sum=q_sum;
    chan[ch].dcarr1=chan[ch].dcarr;
//
    if (chan[ch].ms_count==19) // process code loop and data bit
      chan[ch].tr_bit_time++;
      chan[ch].prompt_mag=rss(chan[ch].i_prom_20,chan[ch].q_prom_20);
      chan[ch].dith_mag =rss(chan[ch].i_dith_20,chan[ch].q_dith_20);
      chan[ch].sum+=chan[ch].prompt_mag+chan[ch].dith_mag;
// code tracking loop
       if ( chan[ch].prompt_mag != 0 || chan[ch].dith_mag != 0)
// with carrier aiding
           ddf=((chan[ch].prompt_mag-chan[ch].dith_mag)*2048)/
            (chan[ch].prompt_mag+chan[ch].dith_mag)*trk_code_k;
           chan[ch].dfreq+=ddf;
           chan[ch].code_freq = (chan[ch].dfreq/trk_code_d+ddf)/256+
            (carrier ref-chan[ch].carrier freq)/cc scale +code ref;
                                                                   // here
was >>12
           ch code (ch, chan[ch].code freq);
       chan[ch].dfreq1=chan[ch].dfreq;
      chan[ch].bit=bsign(chan[ch].q_prom_20+chan[ch].q_dith_20);//bsign is data
bit
      pream(ch,chan[ch].bit); // see if we can find the preamble
      chan[ch].message[chan[ch].t_count]=chan[ch].bit;
       if (ch==0 && debug_counter<4500)
           i_prompta[debug_counter]=ddf;
           q_prompta[debug_counter]=chan[ch].dfreq;
           i_dithera[debug_counter]=chan[ch].prompt_mag;
           q_dithera[debug_counter]=chan[ch].dith_mag;
           car_freq[debug_counter]=chan[ch].carrier_freq;
           chip freq[debug counter]=chan[ch].code freq;
           data bit[debug counter]=chan[ch].bit;
           debug counter++;
      chan[ch].t_count++;
```

4.4.6 Miscellaneous Functions

4.4.6.1 RSS

The RSS or Root Sum Square is used to determine the amplitude of the signal which has been separated into its inphase and quadrature components. This is needed during the pull-in state when the phase is unknown, in the tracking state it is no longer needed since the phase is driven to produce a maximum value of the inphase component while the quadrature component is used as the error signal. A number of methods have been documented. The method used in OpenSourceGPS is the xx method

```
RSS \approx \max(a,b) + \min(a,b)/2
/*****************************
FUNCTION rss(long a, long b)
RETURNS long integer
PARAMETERS
     a long integer
        b long integer
PURPOSE
     This function finds the fixed point magnitude of a 2 dimensional vector
WRITTEN BY
    Clifford Kelley
**********************************
//inline long rss(long a,long b )
long rss(long a, long b)
  long result, c, d;
  c=labs(a);
  d=labs(b);
```

```
if (c==0 && d==0) result=0;
else
{
    if (c>d) result=(d>>1)+c;
    else result=(c>>1)+d;
}
return (result);
}
```

As illustrated in Figure 4-19 this method produces a maximum error of

MORE STUFF NEEDED

Figure 4-19 RSS Algorithm Error

4.4.6.2 fix Sqrt

The Sqrt algorithm uses Newtons method for a 32 bit long integer. It iteratively solves this equation.

```
PURPOSE
     This function finds the fixed point square root of a long integer
WRITTEN BY
     Clifford Kelley
*******************************
long fix_sqrt(long x)
 long xt, scr;
 int i;
 i=0;
 xt=x;
 do
    xt=xt>>1;
    i++;
 } while (xt>0);
 i = (i >> 1) + 1;
 xt=x>>i;
 do
    scr=xt*xt;
    scr=x-scr;
    scr=scr>>1;
    scr=scr/xt;
    xt=scr+xt;
 } while (scr!=0);
 xt=xt<<7;
 return(xt);
```

4.4.6.3 fix atan2

The pull-in state uses a two dimensional arc tangent function that computes the phase of the signal by using the inphase and quadrature components. The basic function is a quadrant dependent version of this equation:

$$\theta = x - \frac{2x^3}{9}$$

While this is not a taylor power series expansion it has a smaller error than the equivalent truncated taylor power series. As illustrated in Figure 4-20 this approximation produces an error of less than x% at its worst.

MORE STUFF NEEDED

Figure 4-20 Fix Atan2 Error Function

```
/*******************************
FUNCTION fix_atan2(long y,long x)
RETURNS long integer
PARAMETERS
          x long in-phase fixed point value
          y long quadrature fixed point value
PURPOSE
     This function computes the fixed point arctangent represented by
     x and y in the parameter list
     1 \text{ radian} = 16384
     based on the power series f-f^3*2/9
WRITTEN BY
     Clifford Kelley
     Fixed for y==x added special code for x==0 suggested by Joel Barnes, UNSW
*******************************
long fix_atan2(long y,long x)
 long result,n,n3;
 if ((x==0) && (y==0))
       return(0); // invalid case
 if (x>0 \&\& x>=labs(y))
           n = (y << 14) /x;
           n3=((((n*n)>>14)*n)>>13)/9;
           result=n-n3;
  }
```

4.7 Position/Velocity/Time Computations

4.7.1 Satellite Location Algorithms

4.7.1.1 Almanac

As mentioned before the almanac is low accuracy orbit description used to calculate what satellites are expected to be visible for channel/PRN allocation.

```
/******************************
FUNCTION satpos_almanac(float time, char n)
RETURNS None.
PARAMETERS
                time
                     float time of week
               n
                     char satellite prn
PURPOSE
       THIS SUBROUTINE CALCULATES THE SATELLITE POSITION
       BASED ON ALMANAC DATA
        - RADIUS OF SATELLITE AT TIME T
    SLAT - SATELLITE LATITUDE
    SLONG- SATELLITE LONGITUDE
        - TIME FROM START OF WEEKLY EPOCH
    ETY - ORBITAL ECCENTRICITY
        - TIME OF APPLICABILITY FROM START OF WEEKLY EPOCH
    TOA
        - ORBITAL INCLINATION
    INC
    RRA - RATE OF RIGHT ASCENSION
    SQA - SQUARE ROOT OF SEMIMAJOR AXIS
    LAN - LONGITUDE OF NODE AT WEEKLY EPOCH
    AOP - ARGUMENT OF PERIGEE
        - MEAN ANOMALY AT TOA
    MA
WRITTEN BY
     Clifford Kelley
ecef satpos_almanac( float time, char n)
     double ei,ea,diff,r,ta,la,aol,xp,yp,d_toa;
     ecef result;
/*
     MA IS THE ANGLE FROM PERIGEE AT TOA
     d_toa=time-gps_alm[n].toa;
     if (d_toa>302400.0) d_toa=d_toa-604800.0;
     else if (d_toa<-302400.0)d_toa=d_toa+604800.0;
     ei=gps_alm[n].ma+d_toa*gps_alm[n].w;
     ea=ei;
     do
        diff=(ei-(ea-gps_alm[n].ety*sin(ea)))/(1.-gps_alm[n].ety*cos(ea));
```

```
ea=ea+diff;
      } while (fabs(diff) > 1.0e-6);
/*
      EA IS THE ECCENTRIC ANOMALY
      if (qps alm[n].ety != 0.0)
      ta=atan2(sqrt(1.-pow(gps_alm[n].ety,2))*sin(ea),cos(ea)-gps_alm[n].ety);
      else
      ta=ea;
      TA IS THE TRUE ANOMALY (ANGLE FROM PERIGEE)
* /
      r=pow(gps_alm[n].sqa,2)*(1.-pow(gps_alm[n].ety,2)*cos(ea));
      R IS THE RADIUS OF SATELLITE ORBIT AT TIME T
      aol=ta+gps_alm[n].aop;
     AOL IS THE ARGUMENT OF LATITUDE
            LA IS THE LONGITUDE OF THE ASCENDING NODE
      la=gps_alm[n].lan+(gps_alm[n].rra-omegae)*d_toa-gps_alm[n].toa*omegae;
      xp=r*cos(aol);
      yp=r*sin(aol);
      result.x=xp*cos(la)-yp*cos(gps_alm[n].inc)*sin(la);
      result.y=xp*sin(la)+yp*cos(gps_alm[n].inc)*cos(la);
      result.z=yp*sin(gps_alm[n].inc);
      return(result);
}
```

4.7.1.2 Ephemeris

The ephemeris routine computes the precise position of the satellite in ecef and the satellites atomic clock offset from GPS time. The methodology is similar to the almanac routine with the addition of more second order corrections.

```
/****************************
FUNCTION satpos_ephemeris(double t, char n)
RETURNS None.
PARAMETERS
               t double
                        time of week
               n char
                         satellite prn
PURPOSE
    THIS SUBROUTINE CALCULATES THE SATELLITE POSITION
    BASED ON BROADCAST EPHEMERIS DATA
        - RADIUS OF SATELLITE AT TIME T
    Crc - RADIUS COSINE CORRECTION TERM
    Crs - RADIUS SINE
                      CORRECTION TERM
    SLAT - SATELLITE LATITUDE
```

```
SLONG- SATELLITE LONGITUDE
    TOE - TIME OF EPHEMERIS FROM START OF WEEKLY EPOCH
         - ORBITAL INITIAL ECCENTRICITY
    TOA - TIME OF APPLICABILITY FROM START OF WEEKLY EPOCH
    INC - ORBITAL INCLINATION
    IDOT - RATE OF INCLINATION ANGLE
    CUC - ARGUMENT OF LATITUDE COSINE CORRECTION TERM
    CUS - ARGUMENT OF LATITUDE SINE CORRECTION TERM
    CIC - INCLINATION COSINE CORRECTION TERM
    CIS - INCLINATION SINE CORRECTION TERM
    RRA - RATE OF RIGHT ASCENSION
    SQA - SQUARE ROOT OF SEMIMAJOR AXIS
    LAN - LONGITUDE OF NODE AT WEEKLY EPOCH
    AOP - ARGUMENT OF PERIGEE
    MA
         - MEAN ANOMALY AT TOA
    DN
         - MEAN MOTION DIFFERENCE
WRITTEN BY
     Clifford Kelley
************************************
eceft satpos_ephemeris(double t,char n)
     double ei, ea, diff, ta, aol, delr, delal, delinc, r, inc;
      double la,xp,yp,bclk,tc,d_toc,d_toe;
      double xls, yls, zls, rangel, tdot, satang, xaz, yaz;
     double az:
     ecef north, east, up;
     eceft result;
//
//
     MA IS THE ANGLE FROM PERIGEE AT TOA
//
     d toc=t-qps eph[n].toc;
     if (d_toc>302400.0) d_toc=d_toc-604800.0;
     else if (d_toc<-302400.0)d_toc=d_toc+604800.0;
     bclk=qps eph[n].af0+qps eph[n].af1*d toc+qps eph[n].af2*d toc*d toc
        -gps_eph[n].tgd;
     tc=t-bclk;
      d_toe=tc-gps_eph[n].toe;
      if (d toe>302400.0) d toe=d toe-604800.0;
           else if (d_toe<-302400.0)d_toe=d_toe+604800.0;
           ei=gps_eph[n].ma+d_toe*(gps_eph[n].wm+gps_eph[n].dn);
      ea=ei;
      do
      diff=(ei-(ea-gps\_eph[n].ety*sin(ea)))/(1.0E0-gps\_eph[n].ety*cos(ea));
      ea=ea+diff;
            } while (fabs(diff) > 1.0e-12);
     bclk=bclk-4.442807633E-10*gps_eph[n].ety*gps_eph[n].sqra*sin(ea);
           result.tb=bclk;
//
//
      ea is the eccentric anomaly
//
     ta=atan2(sqrt(1.00-pow(gps\_eph[n].ety,2))*sin(ea),cos(ea)-gps\_eph[n].ety);
//
      TA IS THE TRUE ANOMALY (ANGLE FROM PERIGEE)
//
```

```
//
      aol=ta+qps_eph[n].w;
//
      AOL IS THE ARGUMENT OF LATITUDE OF THE SATELLITE
//
//
//
       calculate the second harmonic perturbations of the orbit
//
      delr = qps_eph[n].crc*cos(2.0*aol)+qps_eph[n].crs*sin(2.0*aol);
      delal =gps_eph[n].cuc*cos(2.0*aol)+gps_eph[n].cus*sin(2.0*aol);
      delinc=qps\_eph[n].cic*cos(2.0*aol)+qps\_eph[n].cis*sin(2.0*aol);
//
//
      R IS THE RADIUS OF SATELLITE ORBIT AT TIME T
//
      r=pow(gps_eph[n].sqra,2)*(1.00-gps_eph[n].ety*cos(ea))+delr;
      aol=aol+delal;
      inc=gps_eph[n].inc0+delinc+gps_eph[n].idot*d_toe;
//
//
      LA IS THE CORRECTED LONGITUDE OF THE ASCENDING NODE
//
      la=qps_eph[n].w0+(qps_eph[n].omegadot-omegae)*d_toe-
                    omegae*gps_eph[n].toe;
      xp=r*cos(aol);
      yp=r*sin(aol);
      result.x=xp*cos(la)-yp*cos(inc)*sin(la);
      result.y=xp*sin(la)+yp*cos(inc)*cos(la);
      result.z=yp*sin(inc);
      result.az=0.0;
      result.el=0.0;
      if (rec_pos_xyz.x != 0.0 || rec_pos_xyz.y != 0.0 || rec_pos_xyz.z != 0.0)
/*
      CALCULATE THE POSITION OF THE RECEIVER
* /
      north.x=-cos(rec_pos_llh.lon) *sin(rec_pos_llh.lat);
     north.y=-sin(rec_pos_llh.lon) *sin(rec_pos_llh.lat);
     north.z= cos(rec pos llh.lat);
      east.x=-sin(rec pos llh.lon);
      east.y= cos(rec pos llh.lon);
      east.z=0.0;
      up.x=cos(rec_pos_llh.lon)*cos(rec_pos_llh.lat);
      up.y=sin(rec_pos_llh.lon)*cos(rec_pos_llh.lat);
      up.z=sin(rec_pos_llh.lat);
/*
     DETERMINE IF A CLEAR LINE OF SIGHT EXISTS
      xls =result.x-rec_pos_xyz.x;
      yls =result.y-rec_pos_xyz.y;
      zls =result.z-rec_pos_xyz.z;
      range1=sqrt(xls*xls+yls*yls+zls*zls);
      tdot=(up.x*xls+up.y*yls+up.z*zls)/range1;
      if (tdot >= 1.00) satang=pi/2.0;
      else if (tdot \leq -1.00) satang=-pi/2.0;
      else satang=asin(tdot);
      xaz=east.x*xls+east.y*yls;
      yaz=north.x*xls+north.y*yls+north.z*zls;
```

```
if (xaz !=0.0 || yaz !=0.0) az=atan2(xaz,yaz);
  else az=0.0;
  result.el=satang;
  result.az=az;
}
return(result);
}
```

4.7.2 Range corrections

4.7.2.1 Troposphere

The lower part of the atmosphere (the Troposphere) has an index of refraction slightly more that 1.0 which is largely independent of the frequency. This causes the radio signal to slow down and thus makes the range measurement larger than it actually is. For the most part this effect is predictable and a number of models have been used to compensate for it.

The model used in OpenSourceGPS is:

$$Dt_{tropo} = \frac{2.47e^{-0.000133*HAE}}{\sin(el) + 0.0121}$$

This is based on Black and xx in reference xx.

The magnitude and trend of this correction is apparent in figure 4-21.

MORE STUFF NEEDED

Figure 4-21 Troposphere Correction

4.7.2.2 Ionosphere

In addition the charged particles in the upper part of the atmosphere (the Ionosphere) also slow down the signal. In this case the delay is a function of frequency and if two frequency measurements are available this delay can be measured with high precision. Since L2 is not available to this receiver we use the ionopheric correction data provided in the navigation message. This data is provided in page 51 of the almanac.

```
double tropo_iono(char ch,float az,float el,double gps_time)
  double d Trop, alt factor;
  double d Ion, psi, phi, lambdai, phim, per, x, F, amp, t;
// Try a simple troposphere model
  if (current loc.hae>200000.0) alt factor=0.0;
  else if (current_loc.hae<0.0) alt_factor=1.0;</pre>
  else alt_factor=exp(-current_loc.hae*1.33e-4);
  if (m_tropo==1) d_Trop=2.47/(sin(el)+.0121)*alt_factor/c;
  else d_Trop=0.0;
  tropo[ch]=d_Trop;
  if (d_Trop<0.0) printf("el=%lf, hae=%lf",el,current_loc.hae);</pre>
// Use an ionosphere model
  if (m_iono==1)
       psi=0.0137/(el/pi+0.11)-.022;
       phi=current_loc.lat/pi+psi*cos(az);
               (phi > 0.416) phi = 0.416;
       else if (phi <-0.416) phi=-0.416;
       lambdai=current_loc.lon/pi+psi*sin(az)/cos(phi*pi);
       t=43200.0*lambdai+qps time-int((43200.0*lambdai+qps time)/86400.)*86400.;
       if (t<0.0) t=t+86400.0;
       phim=phi+0.064*cos((lambdai-1.617)*pi);
//
//
   If available from the nav message use its Ionosphere model
       if (b0 != 0.0 && al0 != 0.0)
            per=b0+b1*phim+b2*phim*phim+b3*phim*phim*phim;
            amp=al0+al1*phim+al2*phim*phim+al3*phim*phim;
//
// else try this set of default iono model parameters
//
       else
       {
            per=b0+b1*phim+b2*phim*phim+b3*phim*phim*phim;
            amp=al0+al1*phim+al2*phim*phim+al3*phim*phim*phim;
       if (per <72000.0) per=72000.0;
       x=2.*pi*(t-50400.)/per;
       F=1.0+16.0*pow(0.53-el/pi,3);
       if (amp < 0.0) amp=0.0;
       if (fabs(x) < 1.5707) d_Ion=F*(5.0e-9+amp*(1.0-x*x/2.+x*x*x*x/24.0));
                              d_{Ion=F*5.0e-9};
       else
```

```
}
else d_Ion=0.0;
iono[ch]=d_Ion;
return(d_Trop+d_Ion);
}
```

4.7.2.3 Satellite clock

The satellite clocks are allowed to run freely with an occasional reset when the clock drifts far enough off that the navigation message cannot correct for it.

The navigation message gives the offset AF0 and linear drift AF1 of the satellite atomic clock with respect to GPS time. The navigation message includes a time acceleration term but it's purpose was to take into account the relativistic effects. Since the equation is easy to implement the receiver is expected to compute it and AF2 is set to zero.

MORE STUFF NEEDED

4.7.3 Other effects

4.7.3.1 Sagnac effect

The Sagnac effect is the consequence of computing positions in a rotating coordinate system as if they were occurring in an inertial coordinate system. In a GPS receiver this effect occurs when computing the position of the satellites and receiver in ECEF. Since the radio signal was transmitted a number of milliseconds before being received the satellite position must be rotated back to match the coordinate systems at the time when the signals are received.

MORE STUFF NEEDED

4.7.3.2 Relativistic effects

While a number of relativistic effects produce measurable errors the one explicitly taken into account of in OpenSourceGPS is the clock error produced by the gravitational potential as the satellite moves through it orbit.

4.7.4 Computing Pseudorange

When a TIC occurs the state of the PRN code registers is latched and read whenever a navigation fix is scheduled.

The transmission time from the satellite is determined by adding the number of data bits into the week to the PRN code counter and the measured phase

Before the pseudorange is used to compute position it is subjected to a number of integrity checks. Early in the development of OpenSourceGPS a number of problems were encountered where the code register data were out of bounds. This was later isolated to data bus loading problems. While these checks are still in the code the primary integrity problem is the PRN code ambiguity. This condition occurs about 1 in every 10,000 pseudorange measurements. Fortunately though it is easy to detect. As described in the GP2021 manual page xx this is due to the fact that the C/A code only has 1023 code states which is not an integer power of 2. As illustrated in figure 4-22 when the PRN code generator resets from 2045 -> 0 there is a slight delay and instead of a measurement of 2046 is read. When this occurs the measurement from the channel is ignored.

MORE STUFF NEEDED

4.7.5 Computing Delta-Pseudorange

Once the position is computed the velocity is computed using either the carrier trackin loop DCO setting (CTL) or the integrated carrier phase or ICP.

```
unsigned int
                  i, ms, chip, phase;
   int meas_bit_time_rem;
   long meas_bit_time_offset;
   ecef
         rp_ecef;
  eceft dm_gps_sat[13],dp_gps_sat[13];
  tr avg=0.0;
  n=1:
  for (ch=0;ch<=11;ch++)
      meas_bit_time_offset=0;
      ms=chan[ch].epoch & 0x1f;
      chip=chan[ch].code_phase;
      phase=chan[ch].code_dco_phase;
      bit=chan[ch].epoch>>8;
      chan[ch].int_carr_phase=chan[ch].carrier_counter+
                                       float (chan[ch].d carr phase) / 1024.;
      if (out_debug)
       {
               ch, chan[ch].prn, chan[ch].meas_bit_time, bit, ms, chip, phase, chan[ch].state,
         qps_eph[chan[ch].prn].valid,qps_eph[chan[ch].prn].health,
          chan[ch].tow_sync,chan[ch].CNo);
         if (ICP_CTL==0) fprintf(debug, "%ld\n", chan[ch].doppler);
                         fprintf(debug, "%lf\n", chan[ch].int_carr_phase);
         else
// Use only satellites being tracked with valid ephemeris data
   (valid subframe 1,2,3), good health, high enough raw snr, and
// valid phase data
      meas_bit_time_rem = chan[ch].meas_bit_time%50;
      if ( meas_bit_time_rem == bit+1 ) meas_bit_time_offset = -1;
       if ( meas bit time rem == bit-1 ) meas bit time offset = +1;
      if ( meas_bit_time_rem == 0 && bit == 49 ) meas_bit_time_offset = -1;
      if ((chan[ch].meas_bit_time+meas_bit_time_offset)%50==bit &&
          chan[ch].state==track && chan[ch].CNo>33 &&
                   gps eph[chan[ch].prn].valid==1 &&
                    gps_eph[chan[ch].prn].health==0 &&
                   chan[ch].tow_sync==1 && phase<1024 && chip<2046)
       {
         tr_time[n] = (chan[ch].meas_bit_time + meas_bit_time_offset)*.02 +
                                    ms/1000.0+chip/2.046e6+phase/2.046e6/1024.;
            tr ch[n]=ch;
            tr_avg+=tr_time[n];
            n++;
n_track=n-1;
TIC_dt=i_TIC_dt*175.0e-9; //each clock count is 175 ns
// if (ICP_CTL==1)TIC_dt=TIC_dt/float(nav_tic); //use basic TIC interval for ICP
if (out_debug) fprintf(debug,"n_track= %d\n",n_track);
for (i=1;i<=n track;i++)</pre>
      track sat[i]=satpos ephemeris(tr time[i],chan[tr ch[i]].prn);
      // process Carrier Tracking Loop or Integrated Carrier Phase
      if(ICP_CTL==0)// satellite velocity
```

```
dm_gps_sat[i]=satpos_ephemeris(tr_time[i]-
TIC_dt/2.0, chan[tr_ch[i]].prn); //for CTL
dp_gps_sat[i]=satpos_ephemeris(tr_time[i]+TIC_dt/2.0,chan[tr_ch[i]].prn);
                d sat[i].x=(dp qps sat[i].x-dm qps sat[i].x)/TIC dt-
track_sat[i].y*omegae;
                d_sat[i].y=(dp_gps_sat[i].y-
dm_gps_sat[i].y)/TIC_dt+track_sat[i].x*omegae;
                d_sat[i].z=(dp_gps_sat[i].z-dm_gps_sat[i].z)/TIC_dt;
          meas_dop[i]=(chan[tr_ch[i]].doppler-33010105L)*42.574746268e-3;
}
       else
                dm_gps_sat[i] = satpos_ephemeris(tr_time[i] -
TIC_dt/float(nav_tic),chan[tr_ch[i]].prn); //for ICP
                dp_gps_sat[i]=track_sat[i];
                d_sat[i].x=(dp_gps_sat[i].x-
dm_gps_sat[i].x)/TIC_dt*float(nav_tic)-track_sat[i].y*omegae;
                d_sat[i].y=(dp_gps_sat[i].y-
dm_gps_sat[i].y)/TIC_dt*float(nav_tic)+track_sat[i].x*omegae;
          d_sat[i].z=(dp_qps_sat[i].z-dm_qps_sat[i].z)/TIC_dt*float(nav_tic);
          meas_dop[i] = chan[tr_ch[i]].int_carr_phase/TIC_dt*float(nav_tic)-
1.405396826e6;
             t_cor[i]=track_sat[i].tb-
tropo_iono(tr_ch[i],track_sat[i].az,track_sat[i].el,tr_time[i]);
             dt[i]=m_time[1]-(tr_time[i]-t_cor[i]);
      if (n_{track}=4)
       rpvt=pos_vel_time(n_track);
       cbias=rpvt.dt;
       clock_error=rpvt.df;
       m time[1]=m time[1]-cbias;
       rp ecef.x=rpvt.x;
       rp_ecef.y=rpvt.y;
       rp_ecef.z=rpvt.z;
       rp_llh=ecef_to_llh(rp_ecef); // last section to open up
       if (rp_1lh.hae>-2000.0 && rp_1lh.hae< 18000 ) // a quick reasonableness
check
       {
   Translate velocity into North, East, Up coordinates
//
            velocity();
(sqrt (pow (receiver.vel.north, 2.0) +pow (receiver.vel.east, 2.0) +pow (receiver.vel.up
,2.0))<514.0)
                  if (fabs(clock_error) < 5.0) clock_offset = clock_error;</pre>
                  if (almanac valid==1) status=navigating;
                  if (align t==1)
                    old TIC cntr=TIC cntr;
                    delta m time= modf(m time[1],&ipart);
```

```
if (nav_up<1.0)
                          delta_m_time=modf(delta_m_time/nav_up,&ipart);
                          if (delta_m_time>0.5) m_error=(delta_m_time-
1.0) *nav up;
                         else m error=delta m time*nav up;
                    }
                    else
                    {
                         if (delta_m_time>0.5) m_error=(delta_m_time-
1.0)/nav_up;
                         else m_error=delta_m_time/nav_up;
                    TIC_cntr=(TIC_ref-m_error*TIC_ref/10)*(1.0-
clock_offset*1.0e-6);
                    program_TIC(TIC_cntr);
                  rec_pos_llh.lon=rp_llh.lon;
                  rec_pos_llh.lat=rp_llh.lat;
                  rec_pos_llh.hae=rp_llh.hae;
                  current_loc.lon=rp_llh.lon;
                  current_loc.lat=rp_llh.lat;
                  current_loc.hae=rp_llh.hae;
                  rec_pos_xyz.x=rp_ecef.x;
                  rec_pos_xyz.y=rp_ecef.y;
                  rec_pos_xyz.z=rp_ecef.z;
//
   Calculate DOPS
//
                  dops(n_track);
                                             // see if this is the problem
                  if (out_pos==1) fprintf(stream,"time = %20.101f, lat=
%lf,long= %lf,hae= %lf ",
      m_time[1],rec_pos_llh.lat*r_to_d,rec_pos_llh.lon*r_to_d,rec_pos_llh.hae);
         if (out_vel==1) fprintf(stream, "vn= %lf, ve= %lf, vu= %lf ",
         receiver.vel.north, receiver.vel.east, receiver.vel.up);
         if (out_time==1) fprintf(stream," clock= %lf ",clock_offset);
         if (out_pos || out_vel || out_time) fprintf(stream, "hdop= %f, vdop=
%f,tdop= %f\n",hdop,vdop,tdop);
//
//
      Since we have a valid position/velocity narrow the doppler search window
//
      to +-5 doppler bins
//
                  search max f=5;
                  m_{time[0]} = m_{time[1]};
       }
       else
                  m_{time[1]=m_{time[1]+TIC_dt*(1.0+clock_offset/1.e6); // less}
than 4 sats
                  rp ecef.x=0.0;
                  rp ecef.y=0.0;
                  rp ecef.z=0.0;
                  rpvt.xv=0.0;
                  rpvt.yv=0.0;
```

```
rpvt.zv=0.0;
      if (out_kalman==1) // Kalman filter output
                 fprintf(kalm,
                 "time %20.101f, rpx %15.101f, rpy %15.101f, rpz %15.101f, ",
                  m_time[1],rp_ecef.x,rp_ecef.y,rp_ecef.z);
                 fprintf(kalm, "rvx %15.10lf, rvy %15.10lf, rvz %15.10lf, Nsats
%d\n",
                   rpvt.xv,rpvt.yv,rpvt.zv,n_track);
      for (i=1;i<=n_track;i++)</pre>
                 chan[tr_ch[i]].Pr=(m_time[1]-(tr_time[i]-t_cor[i]))*c;
                 chan[tr_ch[i]].dPr=meas_dop[i]*lambda;
                 if (out_kalman==1) // Kalman filter output
                      fprintf(kalm," PRN %2d, px %20.10lf, py %20.10lf, pz
%20.10lf, ",
     chan[tr_ch[i]].prn,track_sat[i].x,track_sat[i].y,track_sat[i].z);
                      fprintf(kalm," vx %16.10lf, vy %16.10lf, vz %16.10lf,
                      d_sat[i].x,d_sat[i].y,d_sat[i].z);
                      fprintf(kalm," Pr %20.10lf, dPr %16.10lf\n",
                      chan[tr_ch[i]].Pr,chan[tr_ch[i]].dPr);
      }
}
/***********************************
FUNCTION velocity (void)
RETURNS None.
PARAMETERS None.
PURPOSE To convert velocity from ecef to local level (WGS-84) axes
WRITTEN BY
     Clifford Kellev
************************
void velocity(void)
   receiver.north.x=-cos(rec_pos_llh.lon)*sin(rec_pos_llh.lat);
   receiver.north.y=-sin(rec_pos_llh.lon)*sin(rec_pos_llh.lat);
   receiver.north.z= cos(rec_pos_llh.lat);
   receiver.east.x=-sin(rec_pos_llh.lon);
   receiver.east.y= cos(rec_pos_llh.lon);
// receiver.east.z=0.0;
   receiver.up.x=cos(rec_pos_llh.lon)*cos(rec_pos_llh.lat);
   receiver.up.y=sin(rec_pos_llh.lon)*cos(rec_pos_llh.lat);
   receiver.up.z=sin(rec pos llh.lat);
      receiver.vel.north = rpvt.xv*receiver.north.x + rpvt.yv*receiver.north.y
```

4.7.6 Computing Position

The method used in the software is LS or Least Squares method which minimizes the square of the difference from the measured range from each satellite and a position fix.

$$x = (H^T H)^{-1} H^T z$$
$$x = (H^T W^{-1} H)^{-1} H^T W^{-1} z$$

The position is solved iterativly starting with the center of the earth if no position is available or the last known solution. This can generally be accomplished in fewer than 4 iterations.

MORE STUFF NEEDED

4.7.7 Computing Velocity

Once the position is computed the velocity is computed using either the carrier trackin loop DCO setting (CTL) or the integrated carrier phase or ICP. Since the satellite-receiver geometry has been resolved the velocity can be solved directly.

```
INPUTS:
    pseudo_range[nsl] Vector of measured range from satellites to the receiver
       sat_location[nsl][3] Array of satellite locations in ECEF when the signal
                                                was sent
            number of satellites used
    nsl
OUTPUTS:
    RP[3]
            VECTOR OF RECEIVER POSITION IN ECEF (X,Y,Z)
            RECEIVER CLOCK BIAS FROM GPS TIME
    CBTAS
VARIABLES USED:
            SPEED OF LIGHT IN VACUUM IN M/S
    C
    S[6][5] MATRIX USED FOR SOLVING FOR RECEIVER POSITION CORRECTION
    B[5]
            RESULTING RECEIVER CLOCK BIAS & POSITION CORRECTIONS
            TEMPORARY RECEIVER POSITION
   X, Y, Z
    Т
            TEMPORARY RECEIVER CLOCK BIAS
    R[5]
            RANGE FROM RECEIVER TO SATELLITES
IF THE POSITION CANNOT BE DETERMINED THE RESULT OF RP
WILL BE (0,0,0) THE CENTER OF THE EARTH
WRITTEN BY
     Clifford Kelley
*******************
pvt pos vel time( int nsl)
{
  double dd[5][5],r,ms[5][13],pm[5][13],bm[13],br[5],correct_mag,x,y,z,t;
  double a1,b1,c1,d1,e1,f1,q1,h1,i1,j1,k1,l1,m1,n1,o1,p1,denom,alpha;
 int i, j, k, nits;
 pvt result;
// USE ITERATIVE APPROACH TO SOLVING FOR THE POSITION OF
// THE RECEIVER
 nits=0;
 t=0.0;
 x=rec_pos_xyz.x;
  y=rec_pos_xyz.y;
 z=rec_pos_xyz.z;
  do
    for (i=1;i<=nsl;i++)
//
     Compute range in ECI at the time of arrival at the receiver
//
           alpha=(t-dt[i])*omegae;
            r=sqrt(pow(track_sat[i].x*cos(alpha)-track_sat[i].y*sin(alpha)-x,2)+
pow(track_sat[i].y*cos(alpha)+track_sat[i].x*sin(alpha)-y,2)+
                        pow(track sat[i].z-z,2));
           bm[i]=r-(dt[i]-t)*c;
           ms[1][i] = (track sat[i].x*cos(alpha)-track sat[i].y*sin(alpha)-x)/r;
           ms[2][i]=(track_sat[i].y*cos(alpha)+track_sat[i].x*sin(alpha)-y)/r;
           ms[3][i] = (track_sat[i].z-z)/r;
```

```
ms[4][i]=1.0;
       a1=0.;b1=0.;c1=0.;d1=0.;
       e1=0.; f1=0.; g1=0.; h1=0.;
       i1=0.; i1=0.; k1=0.; l1=0.;
      m1=0.; n1=0.; o1=0.; p1=0.;
       for (k=1; k<=ns1; k++)
             a1+=ms[1][k]*ms[1][k];
             b1+=ms[1][k]*ms[2][k];
             c1+=ms[1][k]*ms[3][k];
             d1+=ms[1][k]*ms[4][k];
//
       e1+=ms[2][k]*ms[1][k];
                                for completeness, the matrix is symmetric
             f1+=ms[2][k]*ms[2][k];
             g1+=ms[2][k]*ms[3][k];
             h1+=ms[2][k]*ms[4][k];
//
       i1+=ms[3][k]*ms[1][k];
//
       j1+=ms[3][k]*ms[2][k];
             k1+=ms[3][k]*ms[3][k];
             11+=ms[3][k]*ms[4][k];
//
      m1+=ms[1][k];
//
       n1+=ms[2][k];
//
       o1+=ms[3][k];
             p1+=ms[4][k];
        o1=11; m1=d1; n1=h1; e1=b1; i1=c1; j1=q1;
/*
        SOLVE FOR THE MATRIX INVERSE
* /
            denom=(k1*p1-l1*o1)*(a1*f1-b1*e1) + (l1*n1-j1*p1)*(a1*q1-c1*e1) +
                  (j1*o1-k1*n1)*(a1*h1-d1*e1) + (l1*m1-i1*p1)*(c1*f1-b1*g1) +
                  (i1*o1-k1*m1)*(d1*f1-b1*h1) + (i1*n1-j1*m1)*(c1*h1-d1*g1);
            dd[1][1]=f1*(k1*p1-l1*o1)+g1*(l1*n1-j1*p1)+h1*(j1*o1-k1*n1);
            dd[1][2]=e1*(11*o1-k1*p1)+q1*(i1*p1-11*m1)+h1*(k1*m1-i1*o1);
            dd[1][3]=e1*(j1*p1-n1*l1)-i1*(f1*p1-n1*h1)+m1*(f1*l1-j1*h1);
            dd[1][4]=e1*(n1*k1-j1*o1)+i1*(f1*o1-n1*g1)+m1*(j1*g1-f1*k1);
//
            dd[2][1]=b1*(11*o1-k1*p1)+j1*(c1*p1-d1*o1)+n1*(d1*k1-c1*11);
            dd[2][1]=dd[1][2];
            dd[2][2]=a1*(k1*p1-l1*o1)+c1*(l1*m1-i1*p1)+d1*(i1*o1-k1*m1);
            dd[2][3]=a1*(11*n1-j1*p1)+i1*(b1*p1-n1*d1)+m1*(j1*d1-b1*11);
            dd[2][4]=a1*(j1*o1-n1*k1)-i1*(b1*o1-n1*c1)+m1*(b1*k1-c1*j1);
//
            dd[3][1]=b1*(q1*p1-h1*o1)-f1*(c1*p1-o1*d1)+n1*(c1*h1-d1*q1);
            dd[3][1]=dd[1][3];
//
            dd[3][2]=a1*(o1*h1-q1*p1)+e1*(c1*p1-o1*d1)+m1*(d1*q1-c1*h1);
            dd[3][2]=dd[2][3];
            dd[3][3]=a1*(f1*p1-h1*n1)+b1*(h1*m1-e1*p1)+d1*(e1*n1-f1*m1);
            dd[3][4]=a1*(n1*g1-f1*o1)+e1*(b1*o1-c1*n1)+m1*(c1*f1-b1*g1);
//
            dd[4][1]=b1*(h1*k1-q1*l1)+f1*(c1*l1-d1*k1)+j1*(d1*q1-c1*h1);
            dd[4][1]=dd[1][4];
//
            dd[4][2]=a1*(q1*11-h1*k1)-e1*(c1*11-d1*k1)+i1*(c1*h1-d1*q1);
            dd[4][2]=dd[2][4];
            dd[4][3]=a1*(j1*h1-f1*l1)+e1*(b1*l1-d1*j1)+i1*(d1*f1-b1*h1);
//
            dd[4][3]=dd[3][4];
            dd[4][4]=a1*(f1*k1-q1*i1)+b1*(q1*i1-e1*k1)+c1*(e1*i1-f1*i1);
            if (denom <= 0.0)
```

```
// something went wrong
              result.x=1.0;
                                   // set solution to near center of earth
              result.y=1.0;
              result.z=1.0;
              result.dt=0.0;
            else
            {
              for (i=1; i \le 4; i++)
                    for (j=1; j<=4; j++) dd[i][j]=dd[i][j]/denom;
               for (i=1;i<=nsl;i++)
                    for (j=1; j <=4; j++)
                    {
                         pm[j][i]=0.0;
                         for (k=1; k \le 4; k++) pm[j][i] += dd[j][k]*ms[k][i];
              }
             for (i=1; i <=4; i++)
                   br[i]=0.0;
                   for (j=1; j<=nsl; j++)br[i]+=bm[j]*pm[i][j];
             nits++;
             x=x+br[1];
             y=y+br[2];
             z=z+br[3];
             t=t-br[4]/c;
             correct_mag=sqrt(br[1]*br[1]+br[2]*br[2]+br[3]*br[3]);
  } while ( correct_mag > 0.01 && correct_mag < 1.e8 && nits < 10);</pre>
  result.x=x;
  result.y=y;
  result.z=z;
  result.dt=t;
//
   Now for Velocity
//
//
  for (i=1;i<=nsl;i++)
       alpha=(dt[i]-t)*omegae;
       r = sqrt(pow(track_sat[i].x*cos(alpha)-track_sat[i].y*sin(alpha)-x,2)+
                     pow(track_sat[i].y*cos(alpha)+track_sat[i].x*sin(alpha)-
y, 2) +
                     pow(track_sat[i].z-z,2));
       bm[i]=((track_sat[i].x*cos(alpha)-track_sat[i].y*sin(alpha)-
x)*d_sat[i].x+
                     (track_sat[i].y*cos(alpha)+track_sat[i].x*sin(alpha)-
y) *d_sat[i].y+
                     (track_sat[i].z-z)*d_sat[i].z)/r-meas_dop[i]*lambda;
  for (i=1; i <=4; i++)
        br[i]=0.0;
        for (j=1; j<=nsl; j++)br[i]+=bm[j]*pm[i][j];
```

```
result.xv=br[1]+y*omegae;  // get rid of earth
result.yv=br[2]-x*omegae;  // rotation rate
result.zv=br[3];
result.df=br[4]/c*1000000.0; // frequency error in parts per million (ppm)
return(result);
}
```

4.8 NMEA Serial Output

4.9 Miscellaneous Algorithms

4.9.1 ECEF and Latitude/Longitude/Height Conversions

```
/*****************************
FUNCTION ecef_to_llh(ecef pos)
RETURNS position in 11h structure
PARAMETERS
                   ecef
              pos
PURPOSE
         Convert a position in in cartesian ecef coordinates to
                Geodetic WGS 84 coordinates
Based on equations found in Hoffman-Wellinhoff
WRITTEN BY
     Clifford Kelley
llh ecef_to_llh(ecef pos)
 double p,n,thet,esq,epsq;
 11h result;
 p=sqrt (pos.x*pos.x+pos.y*pos.y);
 thet=atan(pos.z*a/(p*b));
 esq = 1.0-b*b/(a*a);
 epsq=a*a/(b*b)-1.0;
 result.lat=atan((pos.z+epsq*b*pow(sin(thet),3))/(p-esq*a*pow(cos(thet),3)));
 result.lon=atan2(pos.y,pos.x);
 n=a*a/sqrt(a*a*cos(result.lat)*cos(result.lat) +
     b*b*sin(result.lat)*sin(result.lat));
 result.hae=p/cos(result.lat)-n;
 return(result);
/******************************
FUNCTION llh_to_ecef(llh pos)
RETURNS position in ecef structure
PARAMETERS
                   llh
               pos
PURPOSE
         Convert a position in Geodetic WGS 84 coordinates to cartesian
                ecef coordinates
Based on equations found in Hoffman-Wellinhoff
WRITTEN BY
     Clifford Kelley
********************************
ecef llh_to_ecef(llh pos)
```

```
double n;
ecef result;
n=a*a/sqrt(a*a*cos(pos.lat)*cos(pos.lat)+b*b*sin(pos.lat)*sin(pos.lat));
result.x=(n+pos.hae)*cos(pos.lat)*cos(pos.lon);
result.y=(n+pos.hae)*cos(pos.lat)*sin(pos.lon);
result.z=(b*b/(a*a)*n+pos.hae)*sin(pos.lat);
return(result);
}
```

Satfind

Satfind uses the receiver position, time, and almanac to predict satellites in view, their azimuth, elevation and Doppler shift of the signal

```
/*******************************
FUNCTION satfind()
RETURNS None.
PARAMETERS None.
PURPOSE
     THIS FUNCTION DETERMINES THE SATELLITES TO SEARCH FOR
     WHEN ALMANAC DATA IS AVAILABLE
WRITTEN BY
     Clifford Kelley
*******************************
satvis satfind(char i)
     float tdot, az;
  float satang,alm_time,almanac_date;
  double range1, range2, xls, yls, zls, xaz, yaz;
  long jd_yr;
  ecef gpspos1, gpspos2, north, east, up;
  satvis result;
  int jd_m;
  struct tm *qmt;
  double time_s;
     INITIALIZE ALL THE CONSTANTS
*/
//
     gotoxy(1,24);
     printf("->satfind");
     putenv(tzstr);
     tzset();
   thetime=time(NULL);
     gmt=gmtime(&thetime);
// set up the correct time
     if (gmt->tm\_mon <= 1)
```

```
jd_yr =365.25*(gmt->tm_year-1.+1900.);
        jd_m = 30.6001*(qmt->tm_mon+14.);
     else
        jd vr=365.25*(qmt->tm year+1900.);
        jd m = 30.6001*(qmt -> tm mon + 2.);
     time s=qmt->tm min/1440.+qmt->tm sec/86400.+1720981.5+qmt->tm hour/24.
      +jd_yr+jd_m+gmt->tm mday;
     qps_week=int((time_s-2444244.5)/7.);
     almanac_date=gps_alm[i].week*7.0+2444244.5;
  if (qps_week-qps_alm[i].week>512) almanac_date+=1024*7.0;
  alm_time=(time_s-almanac_date) *86400.;
  clock_tow=(time_s-gps_week*7.-2444244.5)*86400.;
/*
      CALCULATE THE POSITION OF THE SATELLITES
  if (gps_alm[i].inc > 0.0 && i>0)
     gpspos1=satpos_almanac(alm_time,i);
      gpspos2=satpos_almanac(alm_time+1.0,i);
     CALCULATE THE POSITION OF THE RECEIVER
     rec_pos_xyz=llh_to_ecef(current_loc);
     north.x=-cos(current loc.lon)*sin(current loc.lat);
     north.y=-sin(current_loc.lon)*sin(current_loc.lat);
  north.z= cos(current_loc.lat);
  east.x=-sin(current_loc.lon);
  east.y= cos(current_loc.lon);
    east.z=0.0;
  up.x=cos(current_loc.lon)*cos(current_loc.lat);
  up.y=sin(current_loc.lon)*cos(current_loc.lat);
  up.z=sin(current_loc.lat);
     DETERMINE IF A CLEAR LINE OF SIGHT EXISTS
     xls =gpspos1.x-rec_pos_xyz.x;
     yls =qpspos1.y-rec_pos_xyz.y;
     zls =qpspos1.z-rec_pos_xyz.z;
     range1=sqrt(xls*xls+yls*yls+zls*zls);
     tdot=(up.x*xls+up.y*yls+up.z*zls)/range1;
     xls = xls/range1;
     yls =yls/range1;
     zls =zls/range1;
      range2=sqrt (pow (gpspos2.x-rec_pos_xyz.x-rpvt.xv,2)+
                              pow(gpspos2.y-rec_pos_xyz.y-rpvt.yv,2)+
                              pow(gpspos2.z-rec_pos_xyz.z-rpvt.zv,2));
      if (tdot >= 1.00) satang=pi/2.0;
      else if ( tdot \leftarrow -1.00 ) satang=-pi/2.0;
     else satang=asin(tdot);
     xaz=east.x*xls+east.y*yls;
     yaz=north.x*xls+north.y*yls+north.z*zls;
     if (xaz !=0.0 || yaz !=0.0) az=atan2(xaz,yaz);
```

```
else az=0.0;
    result.x=gpspos1.x;
    result.y=gpspos1.y;
    result.z=gpspos1.z;
    result.elevation=satang;
    result.azimuth =az;
    result.doppler = (range1-range2)*5.2514;
}
// gotoxy(1,24);
// printf("satfind->");
    return(result);
}
```

4.9.2 Dilution of Precision (DOP)

Early in the development of GPS it was clear that the two major effects on positioning error were the accuracy of measuring the range to the satellite and the geometry between the receiver and the satellitges. It was convenient to compute these two performance parameters separately. As long as the ranging error from one satellite to the next are uncorrelated and approximately the same this is a good approximation. Early receivers which had a limited number of channels used DOP as a means to decide which satellites to track.

$$\operatorname{cov}(dx) = E(dx, dx^{T})$$
$$\operatorname{cov}(dx) = (H^{T}H)^{-1}\sigma_{x}$$

Where H is the matrix of line of sight vectors from the receiver to the satellite in the locally level earth axes.

$$H = \begin{bmatrix} R1_{x} & R1_{y} & R1_{z} & 1 \\ R2_{x} & R2_{y} & R2_{z} & 1 \\ R3_{x} & R3_{y} & R3_{z} & 1 \\ \vdots & \vdots & \ddots & \vdots \\ RN_{x} & RN_{y} & RN_{z} & 1 \end{bmatrix}$$

The result is a 4x4 matrix which is divided up into sections.

```
      NDOP
      .
      .
      .

      .
      EDOP
      .
      .

      .
      .
      VDOP
      .

      .
      .
      .
      TDOP
```

EDOP = East Dilution of Precision NDOP = North Dilution of Precision VDOP = Vertical Dilution of Precision These are typically combined in a number of ways to produce

```
HDOP = \sqrt{NDOP^2 + EDOP^2} Horizontal Dilution of Precision
PDOP = \sqrt{NDOP^2 + EDOP^2 + VDOP^2} Position Dilution of Precision
GDOP = \sqrt{NDOP^2 + EDOP^2 + VDOP^2 + TDOP^2} Geometric Dilution of Precision
/**********************************
FUNCTION dops (int nsl)
RETURNS None.
PARAMETERS
                 nsl int
PURPOSE
     This routine computes the dops
INPUTS:
      sat_location[nsl][3] Array of satellite locations in ECEF when the signal
                                               was sent
            number of satellites used
    receiver position
OUTPUTS:
   hdop = horizontal dilution of precision (rss of ndop & edop)
   vdop = vertical dilution of precision
   tdop = time dilution of precision
   pdop = position dilution of precision (rss of vdop & hdop)
   gdop = geometric dilution of precision (rss of pdop & tdop)
WRITTEN BY
     Clifford Kelley
******************************
void dops( int nsl)
 double r,xls,yls,zls;
// double det;
 int i;
 Matrix H(nsl, 4), G(4, 4);
 receiver.north.x=-cos(rec_pos_llh.lon)*sin(rec_pos_llh.lat);
 receiver.north.y=-sin(rec_pos_llh.lon)*sin(rec_pos_llh.lat);
 receiver.north.z= cos(rec_pos_llh.lat);
 receiver.east.x=-sin(rec_pos_llh.lon);
 receiver.east.y= cos(rec_pos_llh.lon);
//receiver.east.z=0.0;
 receiver.up.x=cos(rec_pos_llh.lon)*cos(rec_pos_llh.lat);
 receiver.up.y=sin(rec_pos_llh.lon)*cos(rec_pos_llh.lat);
```

```
receiver.up.z=sin(rec_pos_llh.lat);
 for (i=1;i<=nsl;i++)
 {
//
     Compute line of sight vectors
//
//
      xls=track_sat[i].x-rec_pos_xyz.x;
      yls=track_sat[i].y-rec_pos_xyz.y;
      zls=track_sat[i].z-rec_pos_xyz.z;
      r=sqrt(xls*xls+yls*yls+zls*zls);
      H(i,1)=(xls*receiver.north.x+yls*receiver.north.y+zls*receiver.north.z)/r;
      H(i,2) = (xls*receiver.east.x+yls*receiver.east.y)/r;
     H(i,3)=(xls*receiver.up.x+yls*receiver.up.y+zls*receiver.up.z)/r;
      H(i, 4) = 1.0;
 }
// G=(H.transpose()*H).inverse(); //for Alberto's library
 G = (H.t()*H).i();
                                   // for Newmat library
 hdop=sqrt (G(1,1)+G(2,2));
 vdop=sqrt(G(3,3));
 tdop=sqrt(G(4,4));
 pdop=sqrt(G(1,1)+G(2,2)+G(3,3));
 gdop=sqrt(G(1,1)+G(2,2)+G(3,3)+G(4,4));
// gotoxy(1,24);
// printf("->dops");
```

4.9.3 Self Test

Before the program runs a quick self test is conducted to be confident that the digital interface from the computer to the GP2021 is working properly. The method used is to send two bit patterns to register 0xF2 (data retention register) and the data bus test register and read them back to confirm the data bus is working.

```
printf("data line error\n");
    printf("indata55x=%x , indataaax=%x\n",indata55x,indataaax);
    printf("indataaay=%x , indata55y=%x\n",indataaay,indata55y);
}
if (error==1) exit(0);
}
```

4.9.4 Navigation Message Decoding

In order to determine when a new navigation message is available every time a new frame of data is detected it is decoded. If the IODC and IODE are already available the message is discarded. If a new IODC or IODE is detected the message is decoded.

The decoding of the navigation message is directly taken from the ICD-GPS-200. Since the parity scheme used by GPS cannot do error correction or detect more than one bit in error a number of integrity checks are made to assure that the navigation message is reasonable.

MORE STUFF NEEDED

```
/************************
FUNCTION navmess()
RETURNS None.
PARAMETERS None.
PURPOSE
     This function assembles and decodes the 1500 bit nav message
     into almanac and ephemeris messages
WRITTEN BY
    Clifford Kelley
3-2-2002 Made corrections suggested by Georg Beverle GFZ
*******************************
void navmess(char prn, char ch)
 int i, j, k;
 unsigned long isgra, ie, iomega0;
 long iaf0,iomegadot;
 char itgd, iaf2;
// int icapl2;
 int iweek, iura, ihealth, iodc, iaf1;
 unsigned int itoe, itoc;
// int fif;
 int iode, icrs, idn, icuc, icus, icic, iomegad;
 int icis, icrc, idoe, idot;
 unsigned int iae, iatoa;
 static i4page, i5page;
 int i4data, i5data, isv, iaomegad;
 long iaaf0,iaaf1,iadeli,iaomega0,im0,inc0,iw;
 unsigned long iasgr;
 long iaw, iam0, scale, ia0, ia1;
```

```
char ial0, ial1, ial2, ial3, ibt0, ibt1, ibt2, ibt3;
  int itot,iWNt,idtls,iWNlsf,iDN,idtlsf;//WNa
  int sfr, word, i4p, i5p;
  double r_sqra,r_inc0,r_ety;
  float d toe;
//
//
      assemble the 1500 data bits into subframes and words
//
//
      gotoxy(1,24);
      printf("->navmess prn %d ch %d",prn,ch);
    d_toe=clock_tow-gps_eph[prn].toe;
    if (d_toe>302400.0) d_toe=d_toe-604800.0;
    else if (d_toe<-302400.0)d_toe=d_toe+604800.0;
       \dot{1}=0;
       for (sfr=1;sfr<=5;sfr++)</pre>
         for (word=1; word<=10; word++)</pre>
              scale=536870912L;
              sf[sfr][word]=0;
              for (i=0; i \le 29; i++)
                     if (chan[ch].message[(j+chan[ch].offset)%1500]==1)
                    sf[sfr][word]+=scale;
                    scale=scale>>1;
                     j++;
              }
         }
 parity_check(); // check the parity of the 1500 bit message
//
//
     EPHEMERIS DECODE subframes 1, 2, 3
//
//
   subframe 1
//
//
     check parity of first 3 subframes, since it is a circular register
     we may have over written the first few bits so allow for word 1 of
//
//
     subframe 1 to have a problem
//
  if ((p_error[1]==0 || p_error[1]==0x200) && p_error[2]==0 && p_error[3]==0)
            iodc=int(((sf[1][3] & 0x3) <<8 ) | ((sf[1][8] & 0xFF0000L) >>16));
            iode=int(sf[2][3] >> 16);
            idoe=int(sf[3][10] >> 16);
//
        fprintf(kalm, "prn=%d iodc=%d, iode=%d,idoe=%d\n",prn,iodc,iode,idoe);
        fprintf(kalm, " eph.iode=%d,
eph.iodc=%d\n",gps_eph[prn].iode,gps_eph[prn].iodc);
// if both copies of iode agree and we have a new iode or new iodc then process
the ephemeris
            if (iode==idoe && ((iode!=gps_eph[prn].iode) ||
(iodc!=gps_eph[prn].iodc)))
                  iweek = int(sf[1][3] >> 14);
//
                  icapl2=(sf[1][3] & 0x3000) >> 12;
                  iura=int((sf[1][3] & 0xF00) >> 8);
```

```
ihealth=int((sf[1][3] \& 0xFC) >> 2);
                  itgd=int(sf[1][7] & 0xFF);
                  itoc=int(sf[1][8] & 0xFFFF);
                  iaf2=int(sf[1][9] >> 16);
                  iaf1=int(sf[1][9] & 0xFFFF);
                  iaf0=sf[1][10] >> 2;
                  if (bit test 1(iaf0,22)) iaf0=iaf0 | 0xFFC00000L;
//
//
     subframe 2
                  icrs=int(sf[2][3] & 0xFFFF);
                  idn=int(sf[2][4] >> 8);
                  im0=((sf[2][4] \& 0xFF) << 24) | sf[2][5];
                  icuc=int(sf[2][6] >>8);
                  ie=((sf[2][6] \& 0xFF) << 24) | sf[2][7];
                  icus=int(sf[2][8] >> 8);
                  isqra=(((sf[2][8] & 0xFF) << 24) | sf[2][9]);
                  itoe=int(sf[2][10] >> 8);
//
                  fif=int((sf[2][10] \& 0x80) >> 7);
// subframe 3
                  icic=int(sf[3][3] >> 8);
                  icis=int(sf[3][5] >> 8);
                  inc0=((sf[3][5] \& 0xFF) << 24) | sf[3][6];
                  iomega0=((sf[3][3] \& 0xFF) << 24) | sf[3][4];
                  icrc=int(sf[3][7] >> 8);
                  iw=((sf[3][7] \& 0xFF) << 24) | sf[3][8];
                  iomegadot=sf[3][9];
                  if (bit_test_l(iomegadot,24)) iomegadot=iomegadot |
0xFF000000L;
                  idot=int((sf[3][10] \& 0xFFFC) >> 2);
                  if (bit_test_l(idot,14)) idot=idot | 0xC000;
                  r_sqra=isqra*c_2m19;
                  r inc0=inc0*c 2m31*pi;
                  r ety=ie*c 2m33;
//
           fprintf(kalm, "sqra=%lf, inc=%lf, ety=%lf\n", r sqra, r inc0, r ety);
//
// Does this ephemeris make sense?
                  if ((r_inc0<1.05 && r_inc0>0.873) && (r_sqra>5100.0 &&
r_sqra<5200.0) &&
                         (r_{ety} < .05 \&\& r_{ety} > 0.0))
                  {
                        gps_eph[prn].valid=1;
                        gps_eph[prn].iode=iode;
                        gps_eph[prn].iodc=iodc;
                        gps_eph[prn].week=iweek;
                        gps_eph[prn].ura=iura;
                        gps_eph[prn].health=ihealth;
                        gps_eph[prn].tgd=itgd*c_2m31;
                        gps eph[prn].toc=itoc*16.0;
                        gps eph[prn].af2=iaf2*c 2m55;
                        gps_eph[prn].af1=iaf1*c_2m43;
                        gps_eph[prn].af0=iaf0*c_2m31;
```

```
gps_eph[prn].crs=icrs*c_2m5;
                        gps_eph[prn].dn=idn*c_2m43*pi;
                        gps_eph[prn].ma=im0*c_2m31*pi;
                        gps_eph[prn].cuc=icuc*c_2m29;
                        gps_eph[prn].ety=r_ety;
                        gps eph[prn].cus=icus*c 2m29;
                        gps_eph[prn].sqra=r_sqra;
                        gps_eph[prn].wm=19964981.84/pow(r_sqra,3);
                        gps_eph[prn].toe=itoe*c_2p4;
                        gps_eph[prn].cic=icic*c_2m29;
                        gps_eph[prn].cis=icis*c_2m29;
                        gps_eph[prn].inc0=r_inc0;
                        gps_eph[prn].w0=iomega0*c_2m31*pi;
                        gps_eph[prn].crc=icrc*c_2m5;
                        gps_eph[prn].w=iw*c_2m31*pi;
                        gps_eph[prn].omegadot=iomegadot*c_2m43*pi;
                        gps_eph[prn].idot=idot*c_2m43*pi;
                        if (out_debug) write_Debug_ephemeris(prn);
                else if (gps_eph[prn].valid==1 && d_toe>7200.0)
gps_eph[prn].valid=0;
 }
//
//
      ALMANAC DECODE subframes 4 and 5
//
//
      SUBFRAME 4
// check parity of subframes 4 and five and don't bother if we have the almanac
 if (p_error[4]==0 && p_error[5]==0 && almanac_valid==0 && almanac_flag==0)
             almanac_flag=1;
             i4data = int(sf[4][3] >> 22);
             i4p = int((sf[4][3] \& 0x3F0000L) >> 16);
             if (i4p != i4page && i4data==1) // i4p all we need is a page to be
                                              // read from 1 satellite
             i4page=i4p;
             if (i4page > 24 && i4page < 33)
                  isv=i4page;
                  gps_alm[isv].week=gps_week%1024;
                  iae=int(sf[4][3] & 0x00FFFFL);
                  gps_alm[isv].ety=iae*c_2m21;
                  iatoa=int(sf[4][4] >> 16);
                  gps_alm[isv].toa=iatoa*c_2p12;
                  iadeli=sf[4][4] & 0x00FFFFL;
                  if (bit_test_l(iadeli,16)) iadeli=iadeli | 0xFFFF0000L;
                  gps_alm[isv].inc=(iadeli*c_2m19+0.3)*pi;
                  iomegad=int(sf[4][5] >> 8);
                  gps alm[isv].rra=iomegad*c 2m38*pi;
                  qps alm[isv].health=int(sf[4][5] & 0x0000FF);
                  iasgr=sf[4][6];
                  gps_alm[isv].sqa=iasqr*c_2m11;
```

```
if (gps_alm[isv].sqa>0.0) gps_alm[isv].w=19964981.84/
                                                          pow(qps_alm[isv].sqa,3);
                  iaomega0=sf[4][7];
                  if (bit_test_1(iaomega0,24)) iaomega0=iaomega0 | 0xFF000000L;
                  gps alm[isv].lan=iaomega0*c 2m23*pi;
                  iaw=sf[4][8];
                  if (bit test 1(iaw,24)) iaw=iaw | 0xFF000000L;
                  gps_alm[isv].aop=iaw*c_2m23*pi;
                  iam0=sf[4][9];
                  if (bit_test_1(iam0,24)) iam0=iam0 | 0xFF000000L;
                  gps_alm[isv].ma=iam0*c_2m23*pi;
                  iaaf0=(sf[4][10] >> 13) | ((sf[4][10] & 0x1C)>>2);
                  if (bit_test_l(iaaf0,11)) iaaf0=iaaf0 | 0xFFFFF800L;
                  gps_alm[isv].af0=iaaf0*c_2m20;
                  iaaf1=(sf[4][10] | 0xFFE0) >> 5;
                  if (bit_test_l(iaaf1,11)) iaaf1=iaaf1 | 0xFFFFF800L;
                  gps alm[isv].af1=iaaf1*c 2m38;
            else if ( i4page == 55 )
                  qps_alm[prn].text_message[0]=char((sf[4][3] & 0x00FF00) >> 8);
                  qps_alm[prn].text_message[1]=char( sf[4][3] & 0x0000FF);
                  for (k=1; k \le 7; k++)
                    qps_alm[prn].text_message[3*k-1] = char(sf[4][k+3] >> 16);
                    gps_alm[prn].text_message[3*k] = char((sf[4][k+3] &
0 \times 00 FF 00) >> 8);
                    gps_alm[prn].text_message[3*k+1] = char(sf[4][k+3] &
0x0000FF);
                  }
            else if ( i4page == 56 ) // Broadcast Ionosphere Model & UTC
Parameters
                  ial0=int((sf[4][3] \& 0x00FF00) >> 8);
                  al0=ial0*c 2m30;
                  ial1 = int(sf[4][3] \& 0x0000FF);
                  al1=ial1*c 2m27;
                  ial2 = int(sf[4][4] >> 16);
                  al2=ial2*c 2m24;
                  ial3=int((sf[4][4] \& 0x00FF00) >> 8);
                  al3=ial3*c_2m24;
                  ibt0 = int(sf[4][4] \& 0x0000FF);
                  b0=ibt0*2048.;
                  ibt1 = int(sf[4][5] >> 16);
                  b1=ibt1*16384.;
                  ibt2=int((sf[4][5] \& 0x00FF00) >> 8);
                  b2=ibt2*65536.;
                  ibt3 = int(sf[4][5] \& 0x00FF);
                  b3=ibt3*65536.;
                  ia1=
                        sf[4][6];
                  if (bit_test_l(ia1,24)) ia1=ia1 | 0xFF000000L;
                  a1=ia1*c 2m50;
                  ia0 = (sf[4][7] << 8) | (sf[4][8] >> 16);
                  a0=ia0*c 2m30;
                  itot= int((sf[4][8] & 0x00FF00) >> 8);
                  tot=itot*4096;
```

```
iWNt= int(sf[4][8] & 0xFF);
      WNt=iWNt;
      idtls = int(sf[4][10] >> 16);
      if (idtls >128) idtls=idtls |0xFF00;
      dtls=idtls;
      iWNlsf=int((sf[4][9] \& 0x00FF00) >> 8);
      WNlsf=iWNlsf;
      iDN
           = int(sf[4][9] & 0x0000FF);
      DN=iDN;
      idtlsf= int(sf[4][9] >> 16);
      if (idtlsf >128) idtlsf=idtlsf |0xFF00;
      dtlsf=idtlsf;
else if (i4page == 63)
      ASV[1] = int((sf[4][3] & 0x00F000) >>12);
      ASV[2] = int((sf[4][3] \& 0x000F00) >>8);
      ASV[3] = int((sf[4][3] & 0x0000F0) >>4);
      ASV[4] = int(sf[4][3] & 0x00000F);
      ASV[5] = int(sf[4][4] >> 20);
      ASV[6] = int((sf[4][4] & 0x0F0000L) >> 16);
      ASV[7] = int((sf[4][4] \& 0x00F000) >>12);
      ASV[8] = int((sf[4][4] & 0x000F00) >> 8);
      ASV[9] = int((sf[4][4] & 0x0000F0) >> 4);
      ASV[10] = int(sf[4][4] & 0x00000F);
      ASV[11] = int(sf[4][5] >> 20);
      ASV[12] = int((sf[4][5] \& 0x0F0000L) >> 16);
      ASV[13] = int((sf[4][5] & 0x00F000) >> 12);
      ASV[14] = int((sf[4][5] & 0x000F00) >> 8);
      ASV[15] = int((sf[4][5] & 0x0000F0) >> 4);
      ASV[16] = int(sf[4][5] & 0x00000F);
      ASV[17] = int(sf[4][6] >> 20);
      ASV[18] = int((sf[4][6] & 0x0F0000L) >> 16);
      ASV[19] = int((sf[4][6] \& 0x00F000) >> 12);
      ASV[20] = int((sf[4][6] \& 0x000F00) >> 8);
      ASV[21] = int((sf[4][6] \& 0x0000F0) >> 4);
      ASV[22] = int(sf[4][6] & 0x00000F);
      ASV[23] = int(sf[4][7] >> 20);
      ASV[24] = int((sf[4][7] & 0x0F0000L) >> 16);
      ASV[25] = int((sf[4][7] & 0x00F000) >> 12);
      ASV[26] = int((sf[4][7] & 0x000F00) >> 8);
      ASV[27] = int((sf[4][7] & 0x0000F0) >> 4);
      ASV[28] = int(sf[4][7] & 0x00000F);
      ASV[29] = int(sf[4][8] >> 20);
      ASV[30] = int((sf[4][8] & 0x0F0000L) >> 16);
      ASV[31] = int((sf[4][8] \& 0x00F000) >> 12);
      ASV[32] = int((sf[4][8] \& 0x000F00) >> 8);
      SVh[25] = int(sf[4][8] \& 0x00003F);
      if (SVh[25] == 0x3f) gps_alm[25].inc=0.0;
      SVh[26] = int(sf[4][9] >> 18);
      if (SVh[26] == 0x3f) qps_alm[26].inc=0.0;
      SVh[27] = int((sf[4][9] & 0x03F000L) >> 12);
      if (SVh[27] == 0x3f) qps alm[27].inc=0.0;
      SVh[28] = int((sf[4][9] & 0x000FC0) >>6);
      if (SVh[28] == 0x3f) qps alm[28].inc=0.0;
      SVh[29] = int(sf[4][9] & 0x00003F);
      if (SVh[29] == 0x3f) gps_alm[29].inc=0.0;
```

```
SVh[30] = int(sf[4][10] >> 18);
                   if ( SVh[30] == 0x3f) gps_alm[30].inc=0.0;
                   SVh[31] = int((sf[4][10] \& 0x03F000L) >> 12);
                   if (SVh[31] == 0x3f) gps_alm[31].inc=0.0;
                   SVh[32] = int((sf[4][10] \& 0x000FC0) >>6);
                   if (SVh[32] == 0x3f) qps alm[32].inc=0.0;
      }
      }
             i5data=int(sf[5][3] >> 22);
             i5p=int((sf[5][3] \& 0x3F0000L) >> 16);
            chan[ch].page5=i5p;
            if (i5page != i5p && i5data==1)
                   i5page=i5p;
                   if ( i5page == 51 )
                          iatoa=int((sf[5][3] \& 0xFF00) >>8);
//
            atoa=iatoa*4096;
                         SVh[1] = int(sf[5][4] >> 18);
                         if (SVh[1] == 0x3f) qps_alm[1].inc=0.0;
                         SVh[2]=int((sf[5][4] \& 0x03F000L)>>12);
                         if (SVh[2] == 0x3f) qps_alm[2].inc=0.0;
                         SVh[3] = int((sf[5][4] & 0x000FC0) >> 6);
                         if (SVh[3] == 0x3f) gps_alm[3].inc=0.0;
                         SVh[4] = int(sf[5][4] & 0x00003F);
                         if (SVh[4] == 0x3f) gps_alm[4].inc=0.0;
                         SVh[5] = int(sf[5][5] >> 18);
                         if (SVh[5] == 0x3f) gps_alm[5].inc=0.0;
                         SVh[6] = int((sf[5][5] & 0x03F000L) >> 12);
                         if (SVh[6] == 0x3f) qps_alm[6].inc=0.0;
                         SVh[7] = int((sf[5][5] & 0x000FC0) >> 6);
                         if (SVh[7] == 0x3f) gps_alm[7].inc=0.0;
                         SVh[8] = int(sf[5][5] & 0x00003F);
                         if( SVh[8]==0x3f) gps_alm[8].inc=0.0;
                         SVh[9] = int(sf[5][6] >> 18);
                         if(SVh[9]==0x3f) gps_alm[9].inc=0.0;
                         SVh[10] = int((sf[5][6] \& 0x03F000L) >> 12);
                         if( SVh[10] == 0x3f) gps_alm[10].inc=0.0;
                         SVh[11] = int((sf[5][6] \& 0x000FC0) >> 6);
                         if (SVh[11] == 0x3f) qps_alm[11].inc=0.0;
                         SVh[12] = int(sf[5][6] \& 0x00003F);
                         if (SVh[12] == 0x3f) qps_alm[12].inc=0.0;
                         SVh[13] = int(sf[5][7] >> 18);
                         if (SVh[13] == 0x3f) gps_alm[13].inc=0.0;
                         SVh[14] = int((sf[5][7] \& 0x03F000L) >> 12);
                         if( SVh[14] == 0x3f) gps_alm[14].inc=0.0;
                         SVh[15] = int((sf[5][7] \& 0x000FC0) >> 6);
                         if (SVh[15] == 0x3f) qps_alm[15].inc=0.0;
                         SVh[16] = int(sf[5][7] \& 0x00003F);
                         if (SVh[16] == 0x3f) gps_alm[16].inc=0.0;
                         SVh[17] = int(sf[5][8] >> 18);
                         if (SVh[17] == 0x3f) gps_alm[17].inc=0.0;
                         SVh[18]=int((sf[5][8] & 0x03F000L)>>12);
                         if (SVh[18] == 0x3f) qps alm[18].inc=0.0;
                         SVh[19] = int((sf[5][8] \& 0x000FC0) >> 6);
                         if(SVh[19]==0x3f) gps_alm[19].inc=0.0;
                         SVh[20] = int(sf[5][8] \& 0x00003F);
```

```
if( SVh[20] == 0x3f) gps_alm[20].inc=0.0;
                        SVh[21] = int(sf[5][9] >> 18);
                        if( SVh[21] == 0x3f) gps_alm[21].inc=0.0;
                        SVh[22] = int((sf[5][9] \& 0x03F000L) >> 12);
                        if( SVh[22]==0x3f) gps_alm[22].inc=0.0;
                        SVh[23] = int((sf[5][9] \& 0x000FC0) >> 6);
                        if (SVh[23] == 0x3f) qps alm[23].inc=0.0;
                        SVh[24] = int(sf[5][9] \& 0x00003F);
                        if (SVh[24] == 0x3f) gps_alm[24].inc=0.0;
            else
            isv=i5page;
            gps_alm[isv].week=gps_week%1024;
            iae=int(sf[5][3] & 0xFFFF);
            gps_alm[isv].ety=iae*c_2m21;
            iatoa=int(sf[5][4] >> 16);
            gps_alm[isv].toa=iatoa*4096.0;
            iadeli=int(sf[5][4] & 0xFFFF);
            gps_alm[isv].inc=(iadeli*c_2m19+0.3)*pi;
            iaomegad=int(sf[5][5] >> 8);
            gps_alm[isv].rra=iaomegad*c_2m38*pi;
            gps_alm[isv].health=int(sf[5][5] & 0xFF);
            iasqr=sf[5][6];
            gps_alm[isv].sqa=iasqr*c_2m11;
            if (gps_alm[isv].sqa>0.0)
gps_alm[isv].w=19964981.84/pow(gps_alm[isv].sqa,3);
            iaomega0=sf[5][7];
            if (bit_test_1(iaomega0,24)) iaomega0=iaomega0 | 0xFF0000000L;
            gps_alm[isv].lan=iaomega0*c_2m23*pi;
            iaw=sf[5][8];
            if (bit_test_l(iaw,24)) iaw=iaw | 0xFF000000L;
            gps_alm[isv].aop=iaw*c_2m23*pi;
            iam0=sf[5][9];
            if (bit_test_1(iam0,24)) iam0=iam0 | 0xFF000000L;
            gps_alm[isv].ma=iam0*c_2m23*pi;
            iaaf0=int((sf[5][10] >> 13) | ((sf[5][10] & 0x1C)>>2));
            if (bit test l(iaaf0,11)) iaaf0=iaaf0 | 0xF800;
            gps_alm[isv].af0=iaaf0*c_2m20;
            iaaf1=int((sf[5][10] \& 0xFFE0) >> 5);
            if (bit test l(iaaf1,11)) iaaf1=iaaf1 | 0xF800;
            gps_alm[isv].af1=iaaf1*c_2m38;
}
Parity Checking
/******************************
FUNCTION parity_check(void)
RETURNS None.
PARAMETERS None.
```

```
PURPOSE checks the parity of the 5 subframes of the nav message
WRITTEN BY
     Clifford Kelley
*******************************
void parity_check(void)
 long pb1=0x3b1f3480L,pb2=0x1d8f9a40L,pb3=0x2ec7cd00L;
 long pb4=0x1763e680L,pb5=0x2bb1f340L,pb6=0x0b7a89c0L;
 int parity, m_parity;
 char d29=0,d30=0,sfm,word,b_1,b_2,b_3,b_4,b_5,b_6;
 int err_bit;
 for (sfm=1;sfm<=5;sfm++)</pre>
       p_error[sfm]=0;
       for (word=1; word<=10; word++)</pre>
            m_parity=int(sf[sfm][word] &0x3f);
      b_1=exor(d29,sf[sfm][word] & pb1) << 5;</pre>
      b_2=exor(d30,sf[sfm][word] & pb2) << 4;</pre>
      b_3=exor(d29,sf[sfm][word] & pb3) << 3;
      b_4=exor(d30,sf[sfm][word] & pb4) << 2;
      b_5=exor(0,sf[sfm][word] & pb5) << 1;
      b_6=exor(d29^d30,sf[sfm][word] & pb6);
      parity=b_1+b_2+b_3+b_4+b_5+b_6;
      err bit=0;
      if (parity != m_parity)
                 err_bit=1;
      p_error[sfm] = (p_error[sfm] << 1) + err_bit;</pre>
      if (d30==1) sf[sfm][word]=0x03fffffc0L & ~sf[sfm][word];
      sf[sfm][word]=sf[sfm][word]>>6;
      d29 = (m_parity \& 0x2) >>1;
      d30=m parity & 0x1;
  }
}
/******************************
FUNCTION exor(char bit, long parity)
RETURNS None.
PARAMETERS
                bit
                        char
                parity long
PURPOSE
                count the number of bits set in the parameter parity and
                do an exclusive or with the parameter bit
WRITTEN BY
     Clifford Kelley
***********************************
```

```
int exor(char bit, long parity)
{
   char i;
   int result;
   result=0;
   for (i=7;i<=30;i++)
   {
      if (bit_test_l(parity,i)) result++;
   }
   result=result%2;
   result=(bit ^ result) & 0x1;
   return(result);
}</pre>
```

4.9.5 Interrupt Install/Remove

Since the need to talk to the GP2021 to obtain correlation data is only a function of time and not the result of any particular event the timing function for generating this interrupt was set up to use the IBM PCs own real time clock which uses interrupt IRQ0. Since the clock is only updated every second this function is taken over by OpenSourceGPS. The interrupt install function removes the link from IRQ0 from the real time clock and re-directs it to OSGPS. The interrupt remove function reverses this process and restores the real time clock.

```
/*****************************
FUNCTION Interrupt_Install()
RETURNS None.
PARAMETERS None.
PURPOSE
     This function replaces the current IRQO Interrupt service routine with
     our own custom function. The old vector is stored in a global variable
     and will be reinstalled at the end of program execution. IRQO is
     enabled by altering the interrupt mask stored by the 8259 interrupt
     handler.
********************************
#ifdef BCPP
void Interrupt_Install()
               int_mask,i_high,i_low;
 unsigned char
 i_high=interr_int>>8;
 i_low=interr_int&0xff;
 Old_Interrupt = getvect(8 + IRQLEVEL);
 disable();
 setvect(8 + IRQLEVEL, GPS Interrupt);
 int_mask = int_mask & ~(1 << IRQLEVEL);</pre>
 outportb(0x21,int_mask); // send new mask to 8259
 enable();
// modify the timer to divide by interr_int
 outportb (0x43, 0x34);
 outportb (0x40, i low);
 outportb(0x40,i_high);
 outportb(0x20,0x20); // Clear PIC
```

```
#endif
#ifdef VCPP // MS
void Interrupt_Install()
     unsigned char
                    int_mask, i_high, i_low;
     i_high = interr_int >> 8;
     i_low = interr_int & 0xff;
     Old_Interrupt = _dos_getvect( 8 + IRQLEVEL);
     _disable();
     _dos_setvect( 8 + IRQLEVEL, GPS_Interrupt);
     int_mask = int_mask & ~(1 << IRQLEVEL);</pre>
     _outp( 0x21, int_mask );
     _enable();
     // Modify the timer to divide by interr_int
     \_outp(0x43,0x34);
     _outp( 0x40,i_low );
     _outp( 0x40, i_high );
     _outp(0x20,0x20); // Clear the PIC
}
#endif
/******************************
FUNCTION Interrupt_Remove()
RETURNS None.
PARAMETERS None.
PURPOSE
     This function removes the custom interrupt vector from the vector
     table and restores the previous vector.
*******************************
#ifdef BCPP
void Interrupt_Remove()
 unsigned char int_mask;
 outportb(0x20,0x20); // clear interrupt and allow next one int_mask = inportb(0x21); // get hardware interrupt mask
 int mask = int mask | (1 << IRQLEVEL);</pre>
 disable();
//outportb(0x21,int_mask); // send new mask to 8259
 setvect(8 + IRQLEVEL,Old_Interrupt);
```

```
// allow hardware interrupts
  enable();
                                  // clear interrupt and allow next one
  outportb (0x20, 0x20);
                                  // reset clock
  outportb (0x43, 0x34);
  outportb(0x40,0xff);
  outportb (0x40, 0xff);
#endif
#ifdef VCPP
void Interrupt_Remove()
      unsigned char int_mask;
      _outp( 0x20, 0x20);
      // PGB outportb(0x20,0x20); // clear interrupt and allow next one
      int_mask = inp(0x21);
      // PGB int_mask = inportb(0x21);  // get hardware interrupt mask
      int_mask = int_mask | (1 << IRQLEVEL);</pre>
      _disable();
      //outportb(0x21,int_mask); // send new mask to 8259
      _dos_setvect(8 + IRQLEVEL,Old_Interrupt);
                                       // allow hardware interrupts
      enable();
                                // allow hardware interrupts
// clear interrupt and allow next one
      \_outp(0x20,0x20);
                                  // reset clock
      \_outp(0x43,0x34);
      _outp(0x40,0xff);
      _{\text{outp}}(0x40,0xff);
}
#endif
```

4.9.6 GP2021 Register Commands

In some cases when speed is required the GP2021 must be accessed directly using the to_gps and from_gps functions. These are the basic building blocks for all of the functions that follow.

```
//inline void to_gps(int add,int data)
void to_gps(int add,int data)
{
  outpw(0x304,add);
  outpw(0x308,data);
}

//inline int from_gps(int add)
int from_gps(int add)
{
  outpw(0x304,add);
  return(inpw(0x308));
}

inline int accum_status(void)
{
  return(from_gps(0x82));
}

void all_accum_reset(void)
```

```
{
}
void data_tst(int data)
  to_gps(0xf2,data);
unsigned int ch_epoch(char ch)
 return(from_gps((ch<<3)+4));
unsigned int ch_epoch_chk(char ch)
 return(from_gps((ch<<3)+7));
long ch_carrier_cycle(char ch)
  long result;
 result=from_gps((ch<<3)+6);
 result=result << 16;
 result=result+from_gps((ch<<3)+2);
  return(result);
}
int ch_code_DCO_phase(char ch)
 return(from_gps((ch<<3)+5));
void ch_code_incr_hi(char ch,int data)
 to_gps((ch<<3)+0x5,data);
void ch_code_incr_lo(char ch,int data)
  to_gps((ch<<3)+0x6, data);
int ch_code_phase(char ch)
return(from_gps((ch<<3)+0x1));
int ch_carrier_DCO_phase(char ch)
  return(from_gps((ch<<3)+0x3));
void carr_incr_hi(char ch,int data)
 to_gps((ch<<3)+0x3,data);
```

```
void carr_incr_lo(char ch,int data)
 to_gps((ch<<3)+0x4,data);
void ch_cntl(char ch,int data)
// printf("ch=%d port=%x\n",ch,port(ch<<3));</pre>
 to_gps(ch<<3,data);
void all_cntl(int data)
 to_gps(0x70,data);
void multi_cntl(int data)
 to_gps(0x60,data);
}
int ch_i_track(char ch)
 return(from_gps((ch<<2)+0x84));
int ch_q_track(char ch)
 return(from_gps((ch<<2)+0x85));
int ch_i_prompt(char ch)
  return(from_gps((ch<<2)+0x86));
int ch_q_prompt(char ch)
 return(from_gps((ch<<2)+0x87));
void ch_accum_reset(char ch)
 to_gps((ch<<2)+0x85,0);
void ch_code_slew(char ch,int data)
 to_gps((ch<<2)+0x84,data);
void all code slew(int data)
 to_gps(0x70,data);
```

```
void data_retent_w(int data)
 to_gps(0xe4,data);
int data_retent_r(void)
  return(from_gps(0xe4));
void data_bus_test_w(int data)
  to_gps(0xf2,data);
int data_bus_test_r(void)
  return(from_gps(0xf2));
inline int meas_status(void)
  return(from_gps(0x81));
}
void program_TIC(long data)
 unsigned int high, low;
 high=int(data>>16);
 low =int(data & 0xffff);
 to_gps(0x6d,high);
 to_gps(0x6f,low);
}
void reset cntl(int data)
 to_gps(0x7f,data);
void ch_carrier(char ch,long freq)
 int freq_hi, freq_lo;
 unsigned int add;
 freq_hi=int(freq>>16);
 freq_lo=int(freq&0xffff);
  add = (ch << 3) + 3;
  outpw(0x304, add);
  outpw(0x308,freq_hi);
  add++;
  outpw(0x304, add);
  outpw(0x308,freq_lo);
}
void ch_code(char ch,long freq)
```

```
int freq_hi,freq_lo;
  unsigned int add;
  freq_hi=int(freq>>16);
  freq_lo=int(freq&0xffff);
  add=(ch << 3) + 5;
  outpw (0x304, add);
  outpw(0x308,freq_hi);
  add++;
  outpw(0x304,add);
  outpw(0x308,freq_lo);
void ch_epoch_load(char ch,unsigned int data)
  to_gps((ch<<3)+7,data);
void ch_on(char ch)
 ch_status=ch_status | bit_pat[ch];
 reset_cntl(ch_status);
void ch_off(char ch)
 ch_status=ch_status & !bit_pat[ch];
  reset_cntl(ch_status);
}
void system_setup(int data)
 to_gps(0x7e,data);
void test_control(int data)
 to_gps(0x7c,data);
void status_latch(void)
  to_gps(0x80,0);
void io_config(int data)
  to_gps(0xf0,data);
```