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Models for hierarchical inheritance structures in object-oriented programming languages

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Abstract

Object-oriented programming languages allows to write programs in which *objects* have different kinds of relations and interactions: a complex system!

The object paradigm states a list of rules that facilitate the code reuse. Probably the most important mechanism that leads to a minimal effort is the inheritance relation.

Inheritance allows the construction of multilevel hierarchies, which can be modeled by directed acyclic graphs.

How do programmers use inheritance? Which kind of graphs arise from hierarchical relations? What quantity governs the optimization?

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Chapter 1

Object-oriented paradigm

Object-oriented programming is the most used programming paradigm in today software design. It allows an intelligent code reuse through inheritance and polymorphism, and it is probably the only one programming paradigm that allows to design huge projects with a cooperative effort.

Programs and libraries written in an object-oriented language are composed through the concept of *objects*, which can be seen as modular code, composed by data and methods. Objects can interact with each other and there may be different kinds of relations among them.

Through the concept of objects, the whole set of programs can be seen as a huge complex system, with many small elements which interact and cooperate to achieve the same goal, that is the purpose for which each program has been made.

One of the most important relation that can binds objects is the inheritance: a rule introduced in object-oriented programming languages in order to facilitate and make automatic the reuse of code.

The relation of inheritance arranges objects in hierarchies: when an object inherits from one another, we can imagine a small graph with two nodes connected by a directed link, for example from the original object to the one that has inherited the code. Then we can add lots of other objects to this graph, and make it enormous and complex, due to the possibility to inherit code from different objects and due to the fact that there is no limit in the number of objects that can inherits code from the same object.

Such hierarchies are the starting point of this work.

1.1 A little terminology

Class and objects

Object is the word used to refer to an instance of a *class*: there may be lots of objects of the same type in a program built through the code implemented in a class. In this thesis there is no necessity to distinguish this two concepts and words will be used without distinctions.

Abstract classes

An abstract class is a class that can not be instantiated and so that can never becomes an object. Such class contains methods that has no implementation, but only a declaration.

Superclasses and subclasses

When a class inherits from another class, the first is called the *superclass* of the second, while the second is a *subclass* of the first.

The subclass inherits from the superclass its *public code*.

Multiple Inheritance

Multiple inheritance occurs when a subclass has more than one superclass. Many programming languages allows this possibility, as C++ and Python, while in others it is limited (as in Java) or even not allowed.

Multilevel Inheritance

Multilevel inheritance occurs when a subclass has inherited from one (or more) superclass that is itself the subclass of another one class.

In all programming languages studied in this thesis, multilevel inheritance is allowed, but there exist a way to prevent the inheritance from a class in Java and C++, through a specific keyword inserted in the class that is considered *final* for the hierarchy.

1.2 Object-oriented programming languages

There are many object-oriented programming languages, with lots of differences among them but united by the object paradigm. To give a complete overview of inheritance hierarchies, three different programming languages have been chosen to data analysis: C++ [Bja], Java [Sun] and Python [Gui].

This thesis can not contains a whole course for three programming languages, but it is however useful to highlight some important differences, in order to give the tools to judge the data analysis.

C++ language

Among the three languages, C++ is the oldest and the one that has spread the object-oriented paradigm.

It has been designed to improve *C language*, adding features as virtual functions, operator overloading, references, keywords to control the store-free of memory, and, obviously, the object-oriented paradigm.

It is a typed language and supports multiple inheritance.

Java language

Java has been designed to be a secure and portable programming language.

Its syntax is identical to the one of C++, but its inheritance rules has some peculiarity. Multiple inheritance is not available in the common sense: a class can inherits code only from one superclass, but it can also inherits declarations of functions and variables from any number of a special kind of classes, called *interfaces*.

In general, rules have been created in order to reduce complexity in programs and to keep the code as simple as possible without limiting its capabilities. Some examples are the prohibition to overload operators, the deletion of the instruction go to and of the multiple inheritance.

Python language

Python has been designed with the goals of be useful in any purpose and to allow a really fast programming.

The syntax is quite different respect to the other two languages, since its design philosophy is to allow to express concepts in the minimum possible lines of code and since it is strongly dynamically typed.

It allows multiple inheritance as well as C++, without any limitation.

1.3 Complex noisy data

A complex system analysis always begins from a set of chaotic, complex and noisy data.

Internet is the open-source code home and allows to obtain a huge amount of libraries and programs in any programming languages. The noisy data subject of the following analysis has been downloaded from GitHub [PJ], the largest code hoster in the world [GVSZ14].

Hierarchical inheritance structures can be easily modeled as directed acyclic graphs, and then the dataset is a huge ensemble of different kinds of graphs.

In graphs terminology, the oudegree of a node is the quantity which describes the number of nodes pointed by a link from such node. Since it describes how many classes inherit from such class, such relation means speciation.

The indegree instead represents the multiple inheritance, and so it describes the number of classes from which the selected class has inherited code.

Another important point is that each program is made to perform a task, and then each hierarchy is done to solve a problem or a subtask of the whole program.

In principle all classes in a hierarchy can be directly used in programs, excluding abstract classes, but only some of these classes becomes real objects, while the other nodes have structural purposes only.

Chapter 2

Minimal Effort model

The dataset is large and noisy. A model is needful to guide the data analysis and to give an interpretation to all results.

The guiding idea of the Minimal Effort model is that inheritance is designed to better promote code reuse and, in this sense, to minimize the effort of writing programs.

The model is a mean field approximation for graphs and allows to obtain some interesting features, useful in all next chapters.

2.1 Reuse and Effort

Programs are created to perform tasks and solve problems and, in objectoriented programming, each task is performed with modular code, the objects, often organized in hierarchies.

In a first approach, let's suppose that only terminal nodes of inheritance graphs are effective solution of the problem, while all nodes at higher levels are made for code reuse purposes only.

Terminal nodes are the leaves of the tree which represents the hierarchy. Leaves are given by the problem, but rules are needed in order to build the whole tree from its leaves. How can we group leaves in different levels? Which principle may guide us?

2.1.1 Why use inheritance?

Assuming that inheritance most reliable effect in graph structure is code reuse, we can start from the $\mathfrak n$ classes which represent the solution of the problem.

Suppose that the implementations of two of this classes are very similar. Then you can move common code lines in a third node, in the upper level of this tree.

In this way, one can avoid of writing twice the common lines, creating a node that share its lines with two leaves. In this sense, we are guided by a minimum effort principle. Obviously one can group more than two nodes and try to absorb in higher level all common lines of leaves code.

The function effort ${\tt E}$ of a tree is defined simple as

$$E = \sum_{\sigma}^{n} cost(\sigma)$$

a sum over all nodes, were each node cost is normalized as

$$cost(\sigma) = 1 - \varepsilon$$

were ε represent the fraction of code that inheritance permits to save.

2.1.2 Competition

The trivial minimum is reached when all leaves can share all its code in one upper node, and so when all leaves are identical. To avoid triviality we need a contrasting mechanism: competition arise from the fact that leaves are different in its implementation and more are the classes that one is trying to group together and less is the number of code lines that can be shared, and so $\varepsilon = \varepsilon(\mathfrak{m})$.

To find an explicit form for $\varepsilon(\mathfrak{m})$, consider each class as made of an unordered sequence of k symbols. The number of available symbols is \mathcal{S} and symbols are equally likely. Symbols that compose classes represent functions, or private variables, or something that can considered as a unity for the code at this abstracted level.

How much code can be shared by \mathfrak{m} nodes? The probability to draw a selected symbol in a sequence of trials with replacement is given by the Binomial distribution of parameters $p=\frac{1}{S}$ and k as the number of trials. We can calculate the probability to find the selected symbol once or more as 1 less the probability to not find the selected symbol, and so

$$p = 1 - \left(1 - \frac{1}{\mathcal{S}}\right)^{\mathsf{k}}$$

Now suppose $S \to \infty$ and $k \to \infty$ and define β as

$$\beta = \frac{\mathsf{k}}{\mathcal{S}}$$

In this limit, we can expand

$$e^{-\beta} = \lim_{S \to +\infty} \left(1 - \frac{1}{S}\right)^{\beta S}$$

and then we can rewrite the probability to find a selected symbol in a sequence of extractions as

$$p = 1 - e^{-\beta}$$

Consider \mathfrak{m} indipendent sets of k extractions. The probability to find the selected symbol in all \mathfrak{m} sets is simply

$$\rho = \left(1 - e^{-\beta}\right)^{\mathfrak{m}}$$

We are interesting in the fraction of code $\varepsilon(\mathfrak{m})$ that \mathfrak{m} nodes can share. Since all symbols are equal for our groupment, we can multiply the last result by \mathcal{S} , and divided it by the length of the sequence k to normalize the result.

$$\varepsilon(\mathfrak{m}) = \frac{\mathcal{S}}{\mathsf{k}} \left(1 - e^{-\beta} \right)^{\mathfrak{m}} = \frac{1}{\beta} \left(1 - e^{-\beta} \right)^{\mathfrak{m}} \equiv e^{-\alpha \mathfrak{m}}$$

It is now possible to evaluate the cost of each single node and then of each graph.

$$cost(\sigma) = 1 - e^{-\alpha \mathfrak{m}}$$

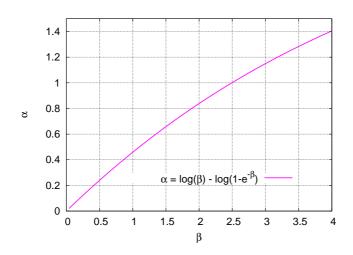


Figure 2.1: α and β - α is small for small β , and viceversa.

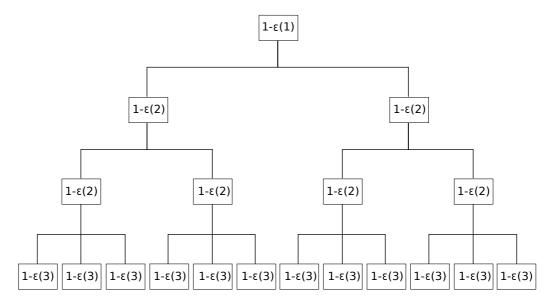


Figure 2.2: **Mean field tree** - The Minimal Effort model estimates the effort necessary to build a graph as the sum of the cost of each node.

2.2 Numerical solutions 9

2.1.3 Minimizing the effort

Despite the simplicity of the functional E, it's not easy to make calculation keeping the whole complex structure of all possible trees. We need to simplify the topology.

Levels are labeled l, where the level l = 0 correspond to the set of leaves and the level l = L is the set containing only the root. At each level l, the tree is essentially a set of nodes $\mathfrak{n}(l)$.

We can estimate the mean number of brothers that each node may have. It is given by the number of nodes at a level $\mathfrak{n}(l)$ divided by number of available parents, and so the number of nodes at successive level $\mathfrak{n}(l+1)$

$$\mathfrak{m}(l) = \frac{\mathfrak{n}(l)}{\mathfrak{n}(l+1)}$$

Forgetting all details, let's consider a tree configuration all expressed by the number of nodes at each level, ignoring which nodes are linked together and which are not.

$$\{\mathfrak{n}(l)\}_{l=0}^{\mathtt{L}} = \{\mathfrak{n}(0), \mathfrak{n}(1), \dots, \mathfrak{n}(\mathtt{L}) \equiv 1\}$$

With this simplification we can rewrite the effort as a sum over levels, and then

$$\mathrm{E}[\mathrm{L}, \{\mathfrak{n}(l)\}] = \sum_{l=0}^{\mathrm{L}-1} \left[1 - \varepsilon \left(\frac{\mathfrak{n}(l)}{\mathfrak{n}(l+1)}\right)\right] \mathfrak{n}(l)$$

And expliciting the function ε we obtain

$$E[L, {n(l)}] = \sum_{l=0}^{L-1} \left(1 - e^{-\alpha \frac{n(l)}{n(l+1)}}\right) n(l)$$
 (2.1)

It is now possible to obtain the minimum of the Effort E respect to the total number of levels L and the number of nodes at each level $\mathfrak{n}(l)$.

$$\mathtt{E}^* = \min_{\mathtt{L}\,\{\mathfrak{n}(l)\}}\mathtt{E}[\mathtt{L},\{\mathfrak{n}(l)\}]$$

2.2 Numerical solutions

Despite the lack of details of tree shape, the model allows the study of some important quantities, like nodes mean degree or population at each level. In this section are shown results of numerical simulations about this quantities with different parameters.

The minimization of Effort functional (2.1) has been made with the interior point method implemented in the program Wolfram Mathematica [Wol]. The numbers of nodes, which is a discrete quantities by definition, are allowed to be real numbers in minimization process.

2.2.1 Finding optimal depth

The Effort E is minimized respect to the number of nodes at each level $\{n(l)\}$ and the depth L, which is the maximum level accessible by the tree, that is populated by only one node, the root.

Free parameters of the model are $\mathfrak{n}(0)$, which is defined by the number of leaves, or the number of nodes necessary to solve the problem for which the tree has been created, and α which represents the abstractability.

Fixing reasonably values for these parameters, as $\mathfrak{n}(0) = 1000$ and $\alpha = 0.1$, we can look for the optimal depth L* which minimize E.

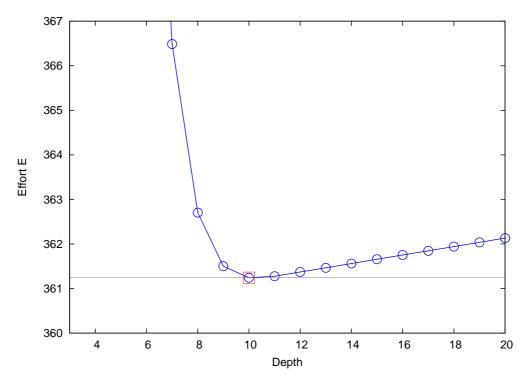


Figure 2.3: The Effort as a function of depth - When $\alpha = 0.1$ and $\mathfrak{n}(0) = 1000$, simulations show that the Effort is minimal for L = 10.

The numerical solution leads to $L^* = 10$, as showed in figure 2.3.

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Population at each level

When the depth is optimal, the number of nodes is exponential in its dependence from the level, as shown in figure 2.4.

Starting from a depth value lower respect to the optimal one and increasing it, the function representing the population at each level increases, approaching gradually the exponential function.

When optimal tree is reached, a further depth increase is ineffective to modify significantly the Effort value. The tree structure changes with the depth increase, but only near the optimal depth. When this point is passed of two units, tree structure remains substantially unchanged and the only one effect of depth increase is the addition of a node at the top of the graph, and so the addition of a new root linked with the old one only.

Outdegree mean

Simulations of function $\mathfrak{m}(l)$ reveal the change in behavior of population distribution respect to fixed depth.

The ratio between the number of nodes of two consecutive levels is ever increasing with levels until the optimal depth is reached. Then this quantity tends to be decreasing with levels, as shown in figure 2.4.

This behavior is telling us that the effort is minimized when the outdegree mean is substantially constant with levels.

While number of nodes are allowed to be real number, levels are discrete quantities. We can then suppose that the minimum of functional E is somewhere between L=10 and L=11.

2.2.2 Varying number of leaves

In order to complete this analysis, we have to study how results change varying the fixed initial parameters. In this section, the abstractability is fixed $\alpha = 0.1$.

The parameter $\mathfrak{n}(0)$ is the one which governs the total number of nodes of the tree. The dependence between nodes and leaves is linear, while the number of nodes is an exponential function of nodes for optimal trees, as showed in 2.5. There is a small deviation caused by the discrete nature of levels, that is visible when the level approach the root.

The optimal depth, the one which minimizes the Effort, moves with the number of leaves. The minimum grows while the number of leaves $\mathfrak{n}(0)$ grows too. The dependence is almost linear, discretized by levels, as showed in 2.6 at the left hand side.

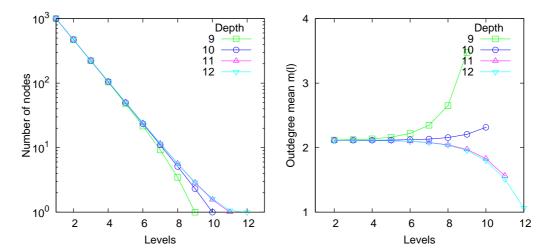


Figure 2.4: Distribution of nodes and outdegree mean for different values of depth - When the depth is optimal, L = 10, nodes distribution is exponential, as showed in the left hand side figure. The right hand side shows that the optimal depth is the one for which outdegree vary as less as possible with levels. The costant function is often non accessible due to the fact that levels are discretized.

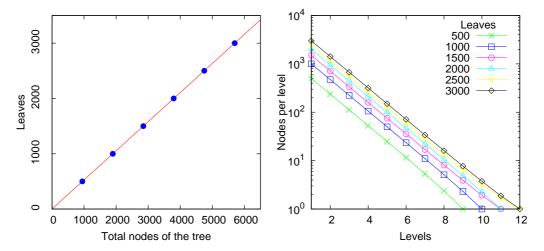


Figure 2.5: Leaves and nodes of optimal trees - The figure on the left hand side shows that the dependence between total nodes and fixed initial leaves is linear. The linear fit leads to $y(x) \sim x/2 + 2$. At the right hand side, populations of nodes at each level of optimal depth for different values of leaves.

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Keeping $\alpha=0.1$ fixed, and moving the number of leaves, we can observe the particular behavior of the outdegree mean as a function of levels showed at the right hand side of figure 2.6. The optimal tree is the one whose outdegree mean is constant respect to levels. When the constant function is not accessible, the nearest function is chosen as optimal. This is the reason for which the derivative of outdegree respect to levels is oscillatory as a function of number of leaves.

2.2.3 Varying abstractability α

The parameter α quantifies the portion of code that can be abstracted in higher levels, and so it represents the number of lines that nodes have in common. In this section, the number of leaves is fixed $\mathfrak{n}(0) = 1000$.

Numerical simulations show that if α is high, the optimal depth is low and vice versa. The position of minimum Effort respect to depth moves linearly with α , as showed in the left hand side of figure 2.7.

The outdegree mean increses with α , while its derivative remains oscillatory due to discrete levels. See figure 2.7.

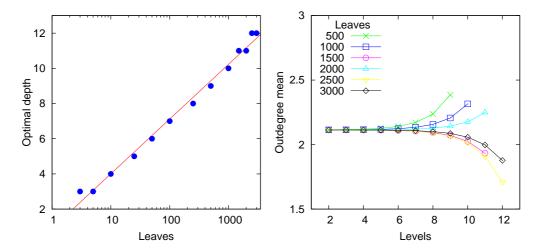


Figure 2.6: Optimal depth and outdegree mean for different values of leaves - The optimal depth increases with the number of leaves as $y(x) \sim x/1000 + 9$. At the right hand side, the outdegree mean as a function of levels for optimal depth.

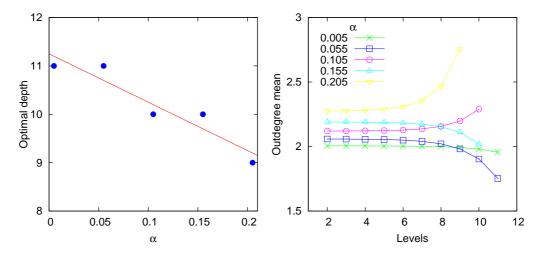


Figure 2.7: Optimal depth and outdegree mean for different values of α - The optimal depth decreases with the number of leaves as $y(x) \sim 11-10x$. At the right hand side, the outdegree mean as a function of levels for optimal depth.

Chapter 3

Sharing Tree model

The Minimal Effort model is a *mean field model*, needful to capture interesting behaviors in object-oriented programming, but it is useful also to introduce a *microscopic model*, the Sharing tree model, which gives a method to create inheritance structures and so that allows the construction of Monte Carlo trees for comparisons.

3.1 Random objects

Our starting point is a set of \mathcal{N} classes which represents the computer science solution of a given problem.

Consider each class composed by a set of different symbols randomly extracted from an alphabet. While the alphabet represents the whole writable code, each symbol represents a unity of code, as in the mean field model.

Each class is composed by a set of k symbols, and there are \mathcal{S} symbols equally likely in the alphabet. This is a first approximation that allows to find analytic results, but in principle not all unity of code are equally important and used and not all classes have the same size.

The measure of the size of a code is an open question. The most popular method is *counting source line of code*, divided in physical lines (the whole code) and logical lines (the number of statements), but it is not necessarily an honest method. The same task can be performed by two different programs of different sizes and with different statements and you can not know in advance whether the best program is the largest or the smallest.

It is a reasonable starting point to consider classes of the same size, represented by k, and a simplified alphabet where the $\mathcal S$ symbols are equally likely.

Sharing Tree model

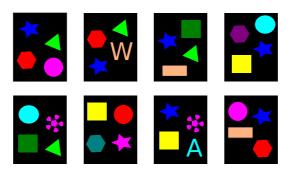


Figure 3.1: Example of initial sets - In this $\mathcal{N}=8$ classes, only $\mathfrak{n}=6$ contain the most common symbol, the blue star.

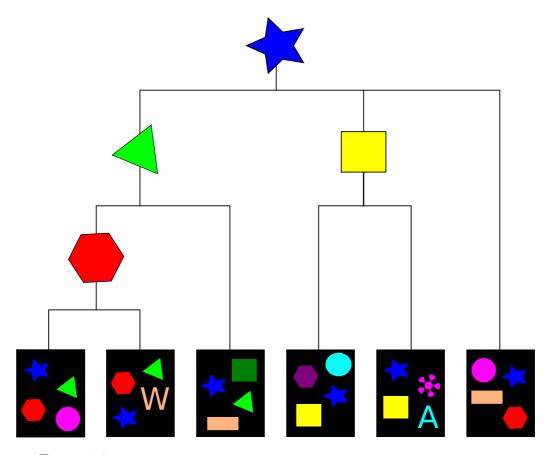


Figure 3.2: Sharing Tree - The most common symbol rule allows the creation of a tree. The $\mathfrak n$ classes represent the leaves, while each symbol chosen as the most common represents an internal node.

3.2 Building the structure

Once selected the \mathcal{N} classes, rules are necessary to decide the structure of the tree. And so, how can we group classes in order to build a tree structure?

As a first step, select the symbol that appears more often in the \mathcal{N} classes. Keep classes with this symbol and delete the others. This symbol will be our root, and so the part of the code that all nodes of our tree have in common. With the excluded classes one can in principle constructs other trees, but for now let just delete them.

Next step is to select the symbol that appear more often in the remaining $\mathfrak n$ classes. This symbol represents the second node of the tree, connected only to the root for now.

If j classes contain this second symbol, we need to find a most common symbol for the $\mathfrak{n}-j$ remaining classes. The symbol is the third node, connected to the root. This process is iterated for all remaining classes until clustering is finished. The most common symbol groups all the classes in sets composed by different elements and with different number of element in each group. Also sets of one class are allowed: they are reminders of groupment, appearing once or even more times if the reminder is composed of more classes that have nothing in common and for which the most common symbol rule does not work.

Each symbol used to group classes represents a node connected to the root, but represents also a set of classes that have been groupped with such symbol.

When a group contain a single class, it means that its process is finished, but for each group with two or more classes the process can be iterated. The number of iterations necessary to finally arrive to all sets of one class only is L, and it is exactly the depth of the tree. In fact, each step increases tree depth by one while it decreases the available symbols and the elements of each class by one (for this reason, k can not be too small!).

Therefore, the process is finished when no group contains more than one class or when classes have no more symbols to share.

3.3 Most common symbol

The key concept underlying the mechanism that grows trees from classes is the *most common symbol rule*. Selecting the symbol that appears more often, we are applying an optimization principle: we are not interested in a random groupment, but in the best groupment in a certain defined sense.

It is not trivial to describe how the most common symbol is distributed,

Sharing Tree model

but with some calculations we can obtain lots of interesting results that substantially solve the model.

Then, to be quantitatively and to find analytical solutions we must find the answer to a probabilistic question: what is the occurrence of the most common symbol in $\mathcal N$ sets of k draws from an alphabet of $\mathcal S$ symbols without replacement?

The answer to this question is central for the model. Each groupment done to build the tree follow the same most common symbol rule. The analytic solution that we are looking for can be applied iteratively with opportune parameters in order to describe the distribution of the number of classes in each set and at each step. In a certain number of steps, sets become singletons and the process is over.

3.3.1 Find a symbol in a sequence

Unlike from the choice made in the Minimal Effort model, in Sharing Tree model symbols in a sequence can not be repeated. Such refinement simplifies following calculation but also approaches the model to real classes in which code repetition does not have a well defined sense.

Thus, the probability to find a selected symbol in one sequence is given by the hypergeometric distribution

$$p = \frac{\binom{\mathcal{S}-1}{\mathsf{k}-1}}{\binom{\mathcal{S}}{\mathsf{k}}} = \frac{\mathsf{k}!(\mathcal{S}-1)!}{\mathcal{S}!(\mathsf{k}-1)!}$$

3.3.2 How many classes for each symbol?

In how many classes such symbol appears? The answer is given by the Binomial distribution of \mathcal{N} trials in which the symbol can appears or not with probability p.

The Binomial distribution then describes the occurrence w of each symbol in the $\mathcal N$ sequences. We can compute the probability that w classes contain a selected symbol with

$$Pr(w) = \binom{\mathcal{N}}{w} p^w (1-p)^{\mathcal{N}-w}$$

3.3.3 What about the most common symbol?

In the Sharing tree model, optimization is carried by the choice of the most common symbol, and not any of them.

Let's say that each symbol $s \in \mathcal{S}$ appears in w_s classes. The set $\{w_s\}_{s=1}^{\mathcal{S}}$ contains \mathcal{S} random variables independent and identically distributed, and the most common symbol is the one that appears ω times

$$\omega = \max \{w_1, \dots, w_{\mathcal{S}}\}\$$

In order to find the distribution of the occurrence of the most common symbol, it is necessary to do some calculations. Therefore, consider the cumulative distribution function of ω

$$F_{\omega}(y) = Pr(\omega \leq y)$$

Since ω is the maximal occurrence and w_s are independent, it holds that

$$Pr(\omega \le y) = Pr(w_1 \le y, w_2 \le y, \dots, w_{\mathcal{S}} \le y)$$
$$= Pr(w_1 \le y)Pr(w_2 \le y) \dots Pr(w_{\mathcal{S}} \le y)$$

and since all w_s have the same cumulative mass function, we can write

$$F_{\omega}(y) = F_{w}^{\mathcal{S}}(y)$$

The probability distribution of ω can now be obtained as the probability that $\omega \leq y$ minus the probability that $\omega \leq y - 1$, and so

$$Pr(y = \omega) = Pr(\omega \le y) - Pr(\omega \le y - 1)$$
$$= F_w^{\mathcal{S}}(y) - F_w^{\mathcal{S}}(y - 1)$$

3.3.4 Probability distribution of most common symbol

The occurrence of the most common symbol is now straightforward. Remembering that w_s are binomial random variables, the occurrence ω of the most common symbol is therefore distributed as

$$\Psi(\omega) = \left(\sum_{i=0}^{\omega} \operatorname{Bin}(\mathcal{N}, i)\right)^{\mathcal{S}} - \left(\sum_{i=0}^{\omega-1} \operatorname{Bin}(\mathcal{N}, i)\right)^{\mathcal{S}}$$

Making explicit the formula of the Binomial distribution, we have finally obtained the distribution of the occurrence of the most common symbol

$$\Psi(\omega) = \left(\sum_{i=0}^{\omega} {N \choose i} p^i (1-p)^{N-i}\right)^{\mathcal{S}} - \left(\sum_{i=0}^{\omega-1} {N \choose i} p^i (1-p)^{N-i}\right)^{\mathcal{S}}$$

Examples of this distribution for different parameters are shown in figures 3.3 and 3.4.

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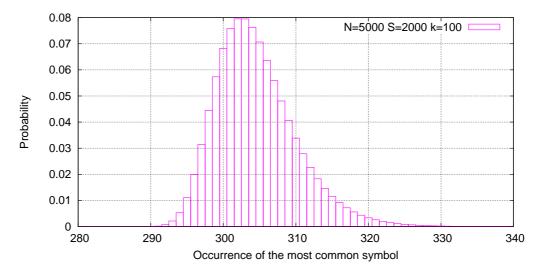


Figure 3.3: The function $\Psi(\omega)$ - This figure represent the probability distribution of the occurrence of the most common symbol in 5000 sequences of 100 extracted symbols (without repetitions) from an alphabet of 2000 symbols.

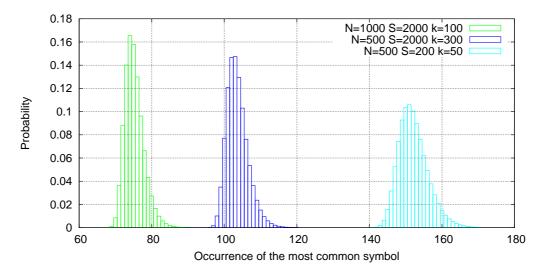


Figure 3.4: $\Psi(\omega)$ for different parameters - Some examples of the probability distribution of the occurrence of the most common symbol for different parameters.

3.3.5 Mean occurrence of the most common symbol

To make the calculations less demanding, it is often useful to deal with the mean instead of the whole distribution. We can obtain $\langle \omega \rangle$ expanding

$$\langle \omega \rangle = \sum_{\omega=1}^{\mathcal{N}} \omega \Psi(\omega)$$

To obtain the final simplified formula, some calculations are needed and in order to ease the notation, we can define a_{ω} as

$$a_{\omega} = \left(\sum_{i=0}^{\omega} {N \choose i} p^{i} (1-p)^{N-i}\right)^{S}$$

and then rewrite $\Psi(\omega)$ as

$$\Psi(\omega) = a_{\omega} - a_{\omega - 1}$$

Inserting the formula in the mean occurrence of the most common symbol, we have

$$\langle \omega \rangle = \sum_{\omega=1}^{\mathcal{N}} \omega \left(a_{\omega} - a_{\omega-1} \right)$$

which is a telescopic series, that allows an important simplification

$$\langle \omega \rangle = 1 (a_1 - a_0) + 2 (a_2 - a_1) + \dots + \mathcal{N} (a_{\mathcal{N}} - a_{\mathcal{N}-1})$$

= $\mathcal{N} a_{\mathcal{N}} - a_0 - a_1 - \dots - a_{\mathcal{N}-1}$

Furthermore, considering that $a_{\mathcal{N}}$ is the sum over all possible cases of a probability, it is equal to 1. Then we finally obtain

$$\langle \omega \rangle = \mathcal{N} - \sum_{j=0}^{\mathcal{N}-1} a_j$$

Thus, the mean of the distribution of the occurrence of the most common symbol is explicitly

$$\langle \omega \rangle = \mathcal{N} - \sum_{j=0}^{N-1} \left(\sum_{k=0}^{j} {N \choose k} p^k (1-p)^{N-k} \right)^{\mathcal{S}}$$

With this formula, we can study directly how parameters change the mean of the number of leaves (but not of total nodes) of simulated trees, as shown in figure 3.5. Considering that, at each step, the groupment of classes in the process is done with the same rule, the formula for $\langle \omega \rangle$ can be applied iteratively to find the mean of the number of classes in each set and for each step of the recursive groupment.

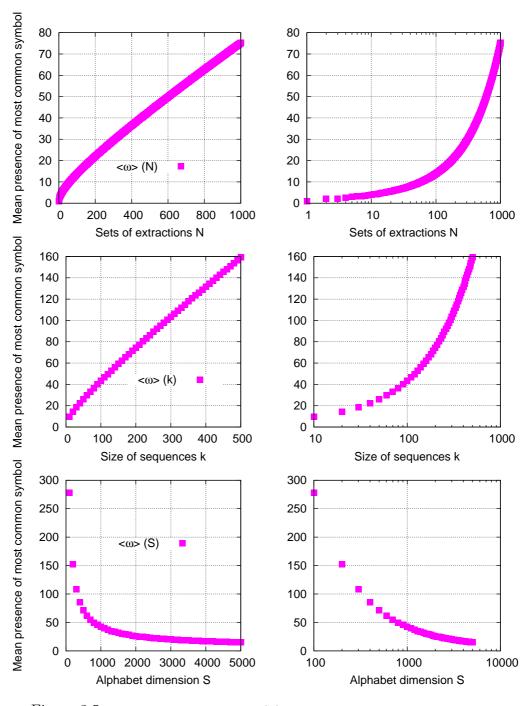


Figure 3.5: The mean occurrence $\langle \omega \rangle$ - In the first figure, $\mathcal S$ and k are fixed at $\mathcal S=2000$ and k = 100 while and $\langle \omega \rangle$ is plotted as a function of $\mathcal N$. In the second figure $\mathcal N=500$ and $\mathcal S=2000$. In the third one, $\mathcal N=500$ and k = 50.

3.4 Sharing process 23

3.4 Sharing process

The recipe to build the tree can be seen also as the set of rules defining a process.

At each step, the recipe suggest to look for the symbol that appear more often and to group classes inspired by most common symbol rule.

Following the iteration, the number of nodes are $x_0 = \mathcal{N}, x_1, \dots, x_L = 1$. Each time we divide classes in *with* or *without* the most common symbol, the process generate η subprocesses, with η the minimum number of subgroups necessary to cover all available classes.

Consider only the main process, that starts from \mathcal{N} classes and that divides them into 2 subgroups, iteratively until the x_{L} is reached. All other subprocesses behave in the same manner with the opportune initial condition.

The mean number of elements of a group at each step t is given by

$$f(x_t, t) = x_t - \sum_{i=0}^{x_t - 1} \left(\sum_{i=0}^{j} {x_t \choose i} \Pi_t^i (1 - \Pi_t)^{x_t - i} \right)^{S - t}$$

where Π_t is obtained with the hypergeometric distribution and considering that if a symbol has been used as the most common then it cannot be reused, and so at each step $S \to S - 1$ and $k \to k - 1$.

$$\Pi_t = \frac{\binom{\mathcal{S}-1-t}{\mathsf{k}-1-t}}{\binom{\mathcal{S}-t}{\mathsf{k}-t}} = \frac{\Gamma(\mathcal{S}-t)\Gamma(\mathsf{k}-t+1)}{\Gamma(\mathsf{k}-t)\Gamma(\mathcal{S}-t+1)}$$

The process for the mean number of elements can so be defined as

$$x_{t+1} = f(x_t, t)$$

where $x_0 = x(0)$ and is equal to \mathcal{N} for the main process.

3.5 Monte Carlo simulations

What kind of trees arise from Sharing Tree Monte Carlo simulations? To give an answer to this question, I have written a C++ code integrated with the library for data analysis. The program is well optimized and fast and each tree is obtained few seconds or less for all parameters that have been chosen.

In this section are presented simulations and the study of the behavior of trees while varying parameters.

24 Sharing Tree model

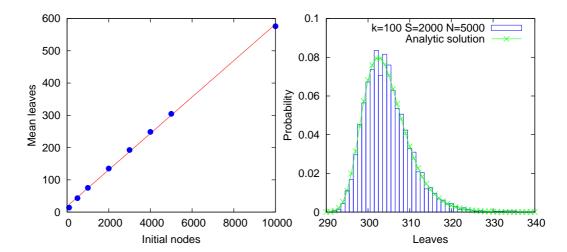


Figure 3.6: Initial nodes and number of leaves - Mean number of leaves is a linear function of the initial number of nodes. The fit leads to y = 0.06x + 18 when k = 100 and S = 2000. The function $\Psi(\omega)$ explains perfectly the leaves distribution.

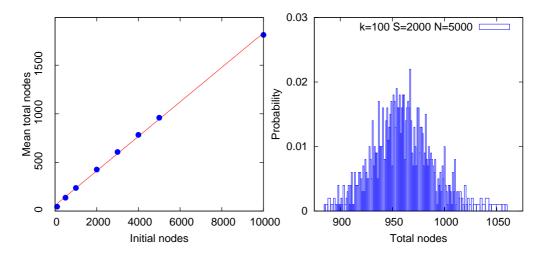


Figure 3.7: Total nodes for different initial nodes - While the distribution of total nodes is broad, its mean is linear in the number of initial nodes, with y = 0.2x + 58.7 when k = 100 and S = 2000.

3.5.1 Initial nodes and leaves

This model doesn't allow to fix the number of leaves of a tree, but only the number of initial nodes between which leaves will be selected. Once fixed the \mathcal{N} initial nodes, the tree will be built with a number of leaves which dependence from this parameter has been obtained in the previous section and showed in figure 3.5.

In the range in which simulations has been done, the mean number of leaves \mathfrak{n} is substantially linear respect to the number of initial nodes \mathcal{N} , as shown on the left hand side of figure 3.6. This means that we can easily decide the mean number of leaves of simulated trees multiplying the number of initial nodes by the factor obtained from the linear fit.

The simulated distribution perfectly matches the analytic solution for the distribution of the most common symbol, as shown on the right hand side of figure 3.6, where the function $\Psi(\omega)$ exactly overlap the distribution of the number of leaves once fixed \mathcal{N} , \mathcal{S} and k.

3.5.2 Total number of nodes

The number of nodes in a tree consists in the number of leaves increased by the number of symbols used by the process. Due to the random nature of the number of leaves, the total number of nodes in a tree is usually a broad distribution.

Anyway, the mean is a linear function of the initial nodes and this allows to easily control the mean number of nodes of trees.

3.5.3 Trees depth

The depth L represents the number of steps in which all sets of classes, or sequences, have become singletons. In simulations, it has a sharp distribution, as showed on the right hand side of figure 3.8.

It is not surprising, since the number of classes in sets is strongly suppressed by each step of the process, with a small variance that decreases as a function of the number of classes, as deducible from figures 3.5 and 3.4.

The mean depth is a logarithmic function of initial nodes, as shown on the left hand side of figure 3.8. Since initial nodes are a linear function of total nodes, the logarithmic behavior of the depth is exactly the same result obtained from the Minimal Effort model. This is an optimal behavior for comparisons with data. 26 Sharing Tree model

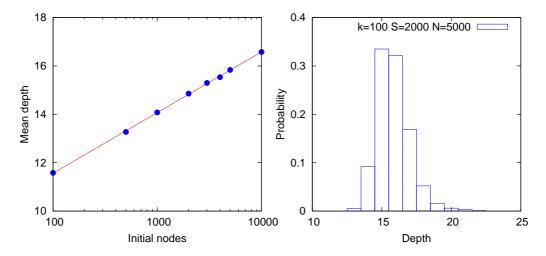


Figure 3.8: **Depth for different initial nodes** - Depth of trees has a sharp distribution, and the mean is a logarithmic function of the initial nodes, as $y = 1.1 \log(x) + 6.6$.

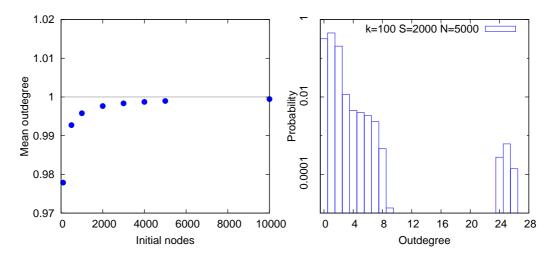


Figure 3.9: Outdegrees for different initial nodes - The mean of outdegrees approaches 1 for increasing number of initial nodes, while outdegrees distribution show a bizarre sharp peak for high outdegree.

3.5.4 Outdegrees

The outdegrees distribution shows an interesting behavior. While its mean approaches the value of 1 for increasing number of initial nodes, as shown on the left hand side of figure 3.9, the distribution of outdegrees is concentrated in low outdegree, but with a sharp peak of occurrence for high outdegree, as shown on the right hand side of 3.9.

This means that some nodes share their code with lots of nodes, or in model terminology, that few symbols are used to group lots of nodes that have little more in common.

The gap in the distribution of outdegrees between the *normal nodes* and *special nodes* gradually becomes more and more pronounced while the number of initial node becomes higher, as detailed shown in figure 3.10.

This behavior can be investigated more closely studying the outdegree as a function of some variable, and this will be done in next section.

3.5.5 Outdegree mean per level

A useful description of trees topology is the outdegree mean as a function of levels. In the Minimal Effort model we have seen how this function is coupled with the depth and that it shows a growth close to the root, strong or weak depending on the depth of the tree.

The microscopic rules of the Sharing Tree model lead to a very similar behavior. As shown on the top of figure 3.11, simulations build trees with an outdegree mean that grows with levels and that has a strong growth near the root.

Parameters govern the position and the height of peaks. In the bottom of figure 3.11, k and \mathcal{S} are fixed, while \mathcal{N} varies. The increase of the number of initial nodes moves the peak, and the depth, to higher levels and to higher outdegrees mean. More nodes need to been grouped, but they does not have many symbols in common.

On the top of figure 3.12, the varying parameter is k. When k is small, the depth is small since few symbols are available for groupment. When k grows, they height of the peaks does not change since it is coupled only with the number of leaves, and so with the number of initial nodes.

On the bottom of figure 3.12, \mathcal{S} is varying. The depth change with \mathcal{S} and peaks move slowly while the number of possible symbols in \mathcal{S} increases.

The behavior of outdegree mean as a function of level can be changed through the probability of each symbol in the alphabet. In all this chapter, all symbols in alphabet are equally likely, but if some symbols would have more probability to be chosen in the extractions respect the others, we may

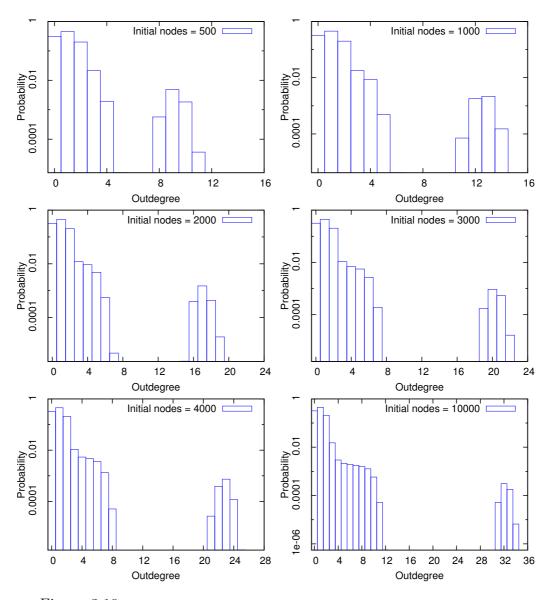


Figure 3.10: Outdegrees distribution for different initial nodes - The gap in the distribution of outdegrees becomes more and more pronounced while the number of initial node becomes higher.

expect a decline of peaks for higher depths. If there are few symbols with which we can initially group classes, then the outdegree mean of high levels will be lower, at least for one level. This argument will be useful in data analysis.

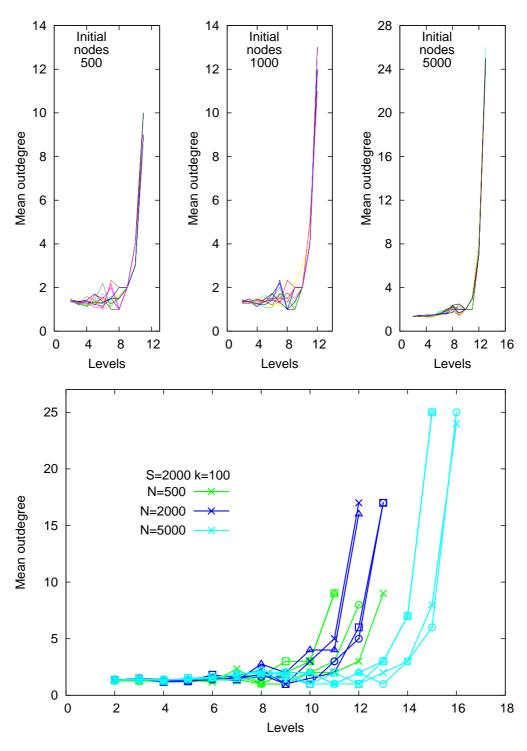


Figure 3.11: Outdegree mean per level - On the top, the figure shows some examples of outdegree mean as a function of levels for different initial nodes and with fixed depth. The figure on the bottom shows how the parameter $\mathcal N$ can change the simulated trees.

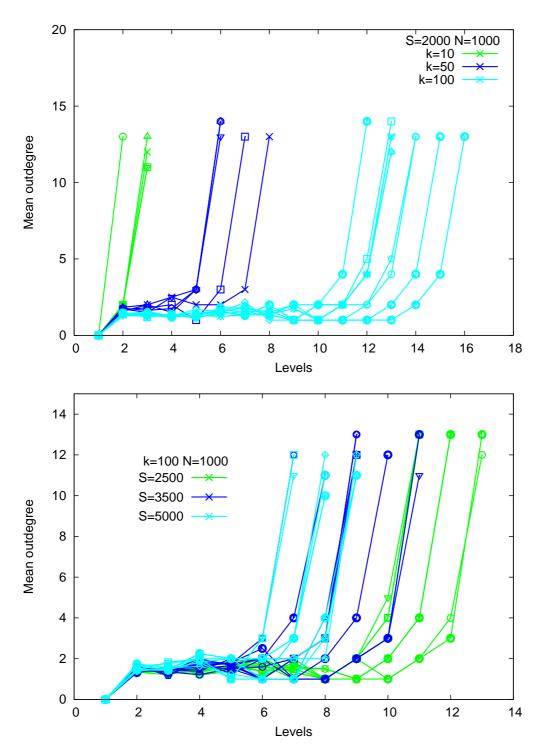


Figure 3.12: Outdegree mean per level - Figures shows how parameters move the main quantities in simulated trees, as the depth and outdegrees distribution.

Chapter 4

Data analysis

How do programmer use inheritance? What kinds of graphs appear from hierarchical relations? In this chapter we analyze real hierarchical structures made by Internet programmers community, among which appear users as Google, Facebook, Twitter and Microsoft [MWe].

4.1 Dataset

The dataset is composed by a huge amount of projects downloaded from GitHub, the actual largest code host on the web [GVSZ14]. GitHub offers to its over 9.1 millions users [Git], source code management (directly from the program Git [Lin]) that allows a cooperative programming among all users.

Inheritance hierarchies have been obtained directly from packages through different steps and with a particular attention to possible data bias and programs bugs.

4.1.1 10 millions of hierarchies

Packages have been downloaded in November 2014, and they have been chosen with a research by name (the whole alphabet) and by programming language (C++, Java, Python).

In detail, the dataset studied in this thesis contains:

- 17333 C++ projects (3233447 hierarchies)
- 25318 Java projects (3504681 hierarchies)
- 20010 Python projects (2491603 hierarchies)

Almost 10 millions of inheritance hierarchies!

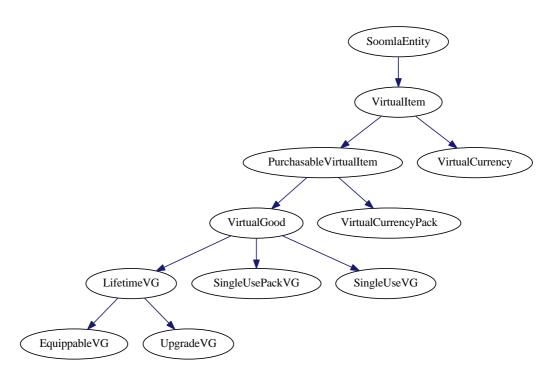


Figure 4.1: **Example of hierarchical inheritance structure** - This is one of the graphs contained in the project Soomla Cocos2dx.

4.2 Graphs sizes 35

4.1.2 Data conversion

Hierarchies reconstruction have been done by a series of scripts (see A.3 for examples) and with the aid of Doxygen [vH], a program for code documentation.

Doxygen is not built to reconstruct inheritance hierarchies, but among its tools there is the possibility of obtaining a graph for each class that reconstructs its hierarchy *upward* (eventually sister-classes are not included in graph). Cutting and pasting all the pieces of graphs, one can rebuild the whole hierarchy. This step has been done with the aim of gvpr, an *awk* [Bri] inspired programming language useful for graphs manipulation.

Once obtained the hierarchies in the standard graphs format (.dot), data have been finally converted in adjacency list.

To analyze adjacency list I have written a C++ library (see A.1) that allows the characterization of graphs (to calculate depth, to find roots and leaves, to assign levels to each node, to find eventually nodes not connected, ...) and allows to obtain all principal statistical quantities, distributions and scatterplots.

To complete the analysis, I have written some C and bash scripts and lots of Gnuplot scripts to graphical representation of results.

4.1.3 Templates and bias

Analyzing converted data I came across some problems about their structure and composition.

For example, Doxygen consider as inheritance even the relation among a template class and all instances of its template variable. Since I don't consider such relation as inheritance, I wrote a script to exclude fake links among classes.

The second important problem was about data redundancy. Due to the sharing nature of open source code, it often happens that some big libraries are contained in slightly different versions in many packages. I can't exclude all redundancy from data, but I made some general controls to exclude packages that caused the most obvious bias. I considered instead as good packages those whose libraries are not comparable to the naked eye, since they contain information useful for my analysis.

4.2 Graphs sizes

The first important approach to noisy data is the sizes distribution. Graphs sizes and complexity is in some way coupled with the complexity

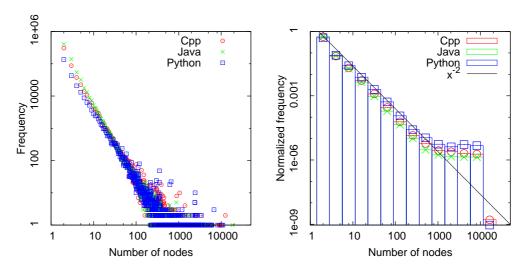


Figure 4.2: Distribution of the number of nodes in hierarchies - The number of nodes composing the graphs has a power law distribution. The exponent $\sim x^{-2}$ is universal despite differences between the three languages.

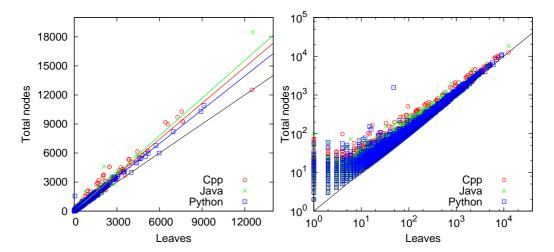


Figure 4.3: Leaves and total nodes - If a point representing a graph is near the black line, it means that almost all nodes of the graph are leaves, and so that only few nodes contain the shared code, while lots of classes inherit it.

4.2 Graphs sizes 37

of problems for which the whole set of programs is made for. In this thesis, I am not investigating the *problems space*, that is true head of such distribution, but the whole following analysis will feel the consequences of sizes distribution.

The size of a directed acyclic graph can be defined in different ways. For our purposes, it is important to consider two main quantities: the number of nodes (and so of classes) which is the effective representation of hierarchy purpose, and the depth of graphs, which is the amount representing the hierarchies optimization.

4.2.1 Solutions sizes

Consider each hierarchy as the solution for a computer science problem, or task. How many classes are necessary to solve problems?

First of all, we analyze the total number of nodes of a graph (i.e. the number of classes of each hierarchy), the most important quantity to define the size of structures.

Plotting this quantity for each graph for each package, as showed in figure 4.2, we find a power law distribution with a small exponent ($\sim x^{-2}$).

Despite the differences among C++, Java and Python, this behavior is universal: hierarchies sizes are distributed in the same way, regardless the language in which they are built. This is the first interesting result that arise from the analysis: in principle, programming languages can be used to perform different tasks and they are designed in different ways and for different purposes. This seems not to influence the structure of inheritance hierarchies, at least in sizes distribution.

4.2.2 Sharing classes

Not all classes of a hierarchy are directly used in programs: for example abstract classes cannot be instantiated, and in general some classes can be built for sharing code purposes, abstracting concepts in *super classes*.

While, in first approximation, we cannot know if an internal node is used or not, we can be sure that the leaves of each hierarchy are instantiable and that such classes are made to solve the task.

How many are the leaves compared to the total number of classes? How many classes share their code?

The answer is shown in figure 4.3: the vast majority of classes in each hierarchy are leaves, i.e. classes that can be used in programs.

This result give us an important clue to argue that inheritance graphs take place only for high abstractability. If almost all nodes are leaves, as

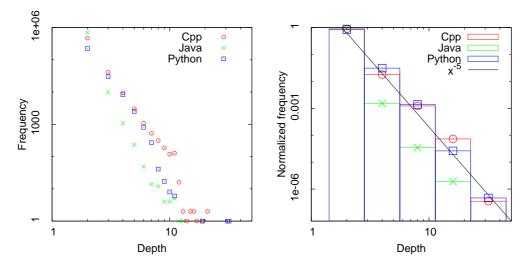


Figure 4.4: **Distribution of depth of each hierarchy** - While C++ and Python have the same power law distribution ($\sim x^{-5}$), Java structures are systematically less deeper than other languages.

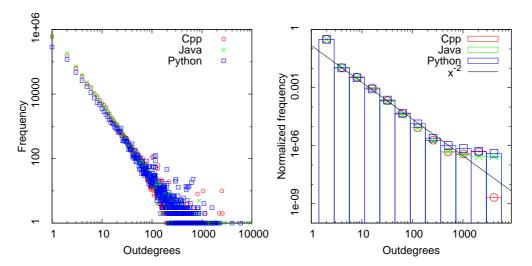


Figure 4.5: **Distribution of outdegrees of all nodes of all graphs** - The outdegree quantifies the number of classes that inherit code from the same class. Its power law behavior can be caused by the power law distribution of the number of nodes of each graph, showed in figure 4.2.

4.3 Code shareability 39

happens in data, only few nodes are responsible to keep all code that can be shared, while many nodes inherit it. The shared code must be useful for lots of classes, and lots of classes must have something in common.

This behavior make us also to think about a general small depth of graphs, and in next section we will check it.

4.2.3 Depth of hierarchies

Hierarchies depth is a surprisingly small quantity: also the largest structures have at most eleven or twelve levels, while the vast majority of graphs have a depth equal to two or three. This result is the second clue that supports the idea for which abstractability is high in all real hierarchies.

Another important result given by figure 4.4 is that Java language does not behave as C++ and Python: depths distribution of Java hierarchies is consistently below the other two distributions. The reasons of this discrepancy can be found directly in Java inheritance implementation rules. In Java, multiple inheritance is allowed only by a special kind of relation given by the keywords *interface* and *implements*. *Interface* is the kind of class that can be inherited without limitations about the multiple inheritance, but *implements* is the keyword that the class which inherits the interface must have: an interface cannot contains *implementation*, but only declarations of methods and functions. The reasons for which a class inherits from interfaces is code reuse as well, but not in the sense expressed by models in sections 2 and 3.

This and other features has been inserted in Java language in order to obtain a simpler and more secure programming. We can expect other differences in data between Java and the other two languages. We can say that Java inheritance rules give rise to less deeper hierarchies respect to other languages (especially C++ from which Java is developed), and in this sense they have a simplified effect as hoped by Java designers.

4.3 Code shareability

The outdegree quantifies the number of classes that inherit code from the same class. The power law distribution of graphs sizes affects outdegrees distribution (over all nodes of all graphs), which appears as a power law with the same exponent ($\sim x^{-2}$). This is not a surprising result, since regardless the outdegrees distribution of each graph, its sum over all graphs (which sizes are power law distributed) will have a power law shape as well. See figure 4.5.

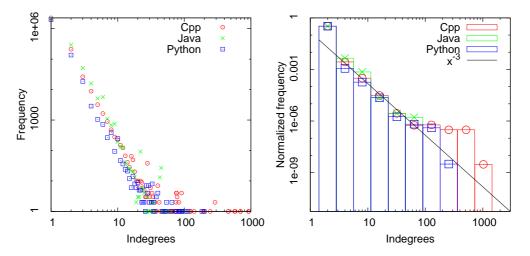


Figure 4.6: Distribution of indegrees of all nodes of all graphs - Indegrees are systematically less than outdegrees and distributions have a strong cutoff, especially for Java hierarchies.

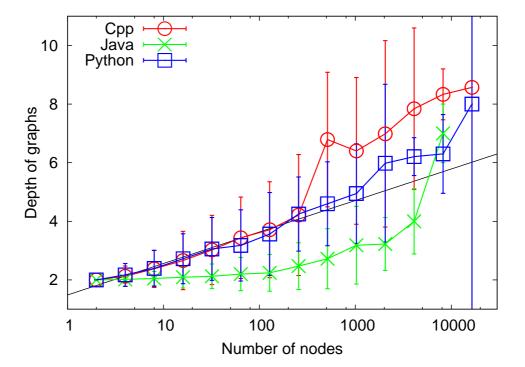


Figure 4.7: **Depth VS Nnodes** - Depth of graphs seems a logarithmic function of the number of object for C++ and Python, while the depth is almost constant in Java hierarchies. The fit for C++ and Python give $y \sim 0.5 \log(x) + 1.5$

For this reason, it's important to look at outdegrees distribution of each graph. Is the outdegrees distribution a real power law or it is an effect caused by the sizes?

As showed in figure 4.8, the power law appears as distribution of outdegrees also in single graphs, at least for biggest hierarchies. Outdegrees distribution is therefore the results of the sum of many power laws.

4.4 Tree approximation

Models presented in sections 3 and 2 schematize hierarchies through trees, while inheritance structures can be in principle directed acyclic graphs. The main difference between this two kind of graphs is in the number of indegrees of each node: if a graph is a tree, all nodes can have at most one indegree, while indegrees have no restrictions for a directed acyclic graph.

In programming languages, multiple inheritance is often not recommended, except in cases where actually required. In data we can observe multiple inheritance, but it is systematically less than single inheritance, as expected. When indegrees distribution is compared to outdegrees distribution in a hierarchy, as in figure 4.8, one can observe how outdegree is the first main quantity to keep into account in an object-oriented hierarchy model.

The outdegrees distribution shows power law behavior with a small exponent ($\sim x^{-2}$ or even less), while indegrees distribution shows a power law behavior with a large exponent ($\sim x^{-3}$ and often more), large enough to allow a first approach considering the indegree constant and equal to its mean, that is about 1. In this sense, tree approximation is an excellent first approach to this system.

Distribution of indegrees of all nodes of all graphs shows a power law behavior, with exponent $\sim x^{-3}$ (see figure 4.6). The three programming languages have quite different behaviors. In Python only the 0.1% of nodes has outdegree greater than one and no one class has more than 300 indegrees. In Java, indegrees are often more respect to other languages, as expected from an *interfaces programming*, but all class has less than 100 indegrees. In C++ indegrees can reach 1000 classes.

4.5 Lateral growth

Graphs are complex structures and their topology has lots of features. A way to give a summary look into its shape is asking in which way the depth is coupled to the number of objects in hierarchies, in order to have an idea

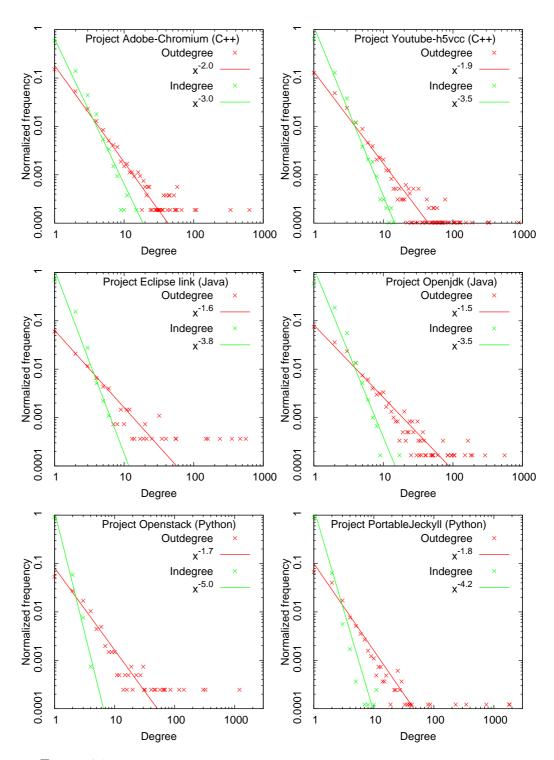


Figure 4.8: Comparison between indegrees and outdegrees - The different exponent for indegree and outdegree in each graph shows how tree approximation is an excellent first approach to this system.

4.5 Lateral growth 43

about the ratio of the *vertical* dimension (i.e. the depth) and the *horizontal* dimension (i.e. the number of objects in levels).

4.5.1 Horizontal and vertical dimensions

Plotting the depth versus the number of objects for each graph allow to reconstruct a distribution of occurrence for each programming language, which means and standard deviations are showed in figure 4.7.

Python and C++ behave in the same way: the depth is in good approximation a logarithmic function of the number of objects (at least for most of sizes). For Java hierarchies, instead, the depth is almost a constant function of the number of classes that grows only for big graphs sizes. Both results are descriptive of a *later growth* of graphs instead of a vertical one.

Consider two hierarchies with a very different number of objects. Despite the gap between the two effective sizes of the structures, we may expect two graphs with similar depths, at most one increased or decreased by one respect the other, especially for Java structures.

The logarithmic behavior of the depth as a function of the number of objects is well captured by the Sharing Tree model and the Effort model. Both mean field hierarchies and simulated trees well describe this feature.

4.5.2 Shallow is better

A really interesting result is the change in behavior of the depth as a function of the number of objects, as highlight in figure 4.9 through a heat map for each programming language.

In object-oriented programming languages there are general advices that suggest to keep hierarchies as shallow as possible, in order to avoid the antipattern known as *Yo-yo problem* [TGP89]. If inheritance graph is too much long and complicated, then a programmer that has to read and understand the hierarchy, has to keep flipping between different parts of the code.

For these reasons, the huge amount of shallow hierarchies was foreseeable. But what happens when hierarchy size get over 1000 classes?

The artificial attempt to keep hierarchies as shallow as possible seems to fail, and all hierarchies show a depth greater than that expected.

Can the guess for which *shallow is better* be wrong? If shallow hierarchies are produced by a false assumption, can the optimization be achieved through deep hierarchies?

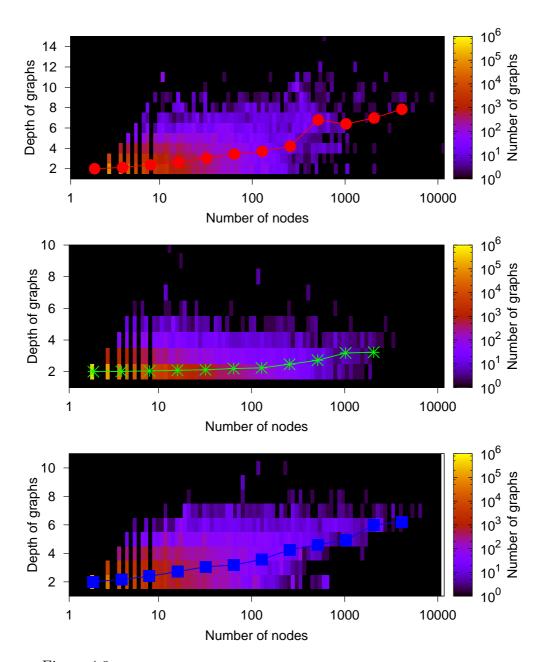


Figure 4.9: **Depth VS nodes in C++, Java and Python hierarchy** - Colors (used in log scale) are representative of how many graphs have the x number of nodes and depth equal to y. Colors represent the whole distribution, while lines trace the mean. Comparison of this three trends is given in figure 4.7.

4.6 Vertical balancing 45

4.6 Vertical balancing

Inspired by models, we can investigate more accurately the topology of hierarchies studying the behavior of the outdegree mean of nodes as a function of the levels. Is it constant across graphs? If not, where are situated objects with the most shared code?

4.6.1 Code shareability per level

Once established that graphs are wider than high, we can probe the *vertical balancing*. An interesting quantity that we can study as a function of a vertical variable (i.e. of levels) is the outdegree mean of nodes.

When the outdegree is high, the code contained in classes is shared with lots of other classes: high outdegree means high shareability.

Some examples of this function are given in figures 4.10 and 4.11. We can observe that the outdegree mean is a quantity that tends to grow with levels, with pronounced peaks close to the root.

Why this behavior? Why the outdegree mean grows with level?

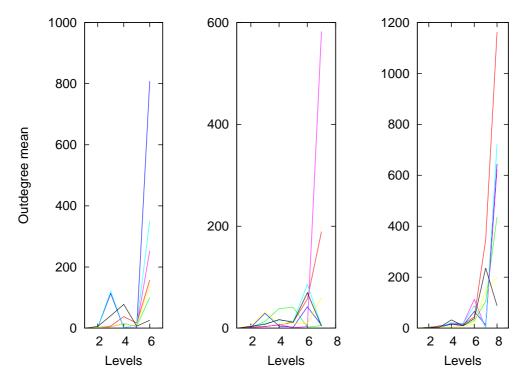


Figure 4.10: Outdegree mean for Cpp hierarchies - Examples of structure with more than 1000 nodes and depth equal to 6, 7 and 8 (in order).

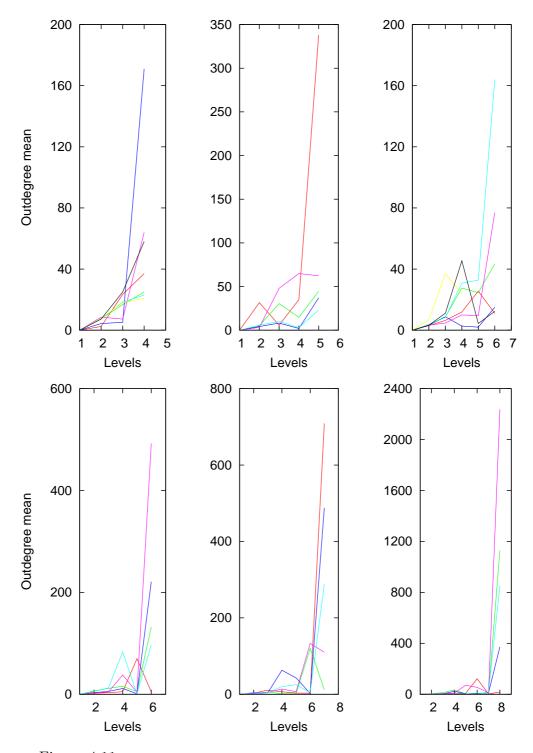


Figure 4.11: Outdegree mean for Java and Python hierarchies - In the upper side figures, examples of Java structure with more than 500 nodes and depth equal to 4, 5 and 6 (in order). The other figures represent examples of python structure with more than 500 nodes and depth equal to 6, 7 and 8 (in order).

4.6.2 Shallow regime

Thanks to the mean field model (Effort model), we can give an interpretation to the growth of outdegree with levels.

We have showed in chapter 2 how the outdegree mean behavior, as function of levels, is very sensible to *depth constrain* and that it can have a strong growth close to the root in the case of insufficient depth. This is exactly the situation in which we find inheritance hierarchies in data.

This is yet another clue that leads us to argue that *shallow hierarchies* are not the best solution. Code reuse appears not optimized by a decrease of the depth in Effort model, and data appears as trapped in an artificial *shallow regime*.

A most efficient documentation system could avoid the *yo-yo problem* as well as decreasing the depth of hierarchies, without sacrificing the optimal depth.

4.7 Optimal or random?

The models proposed in this thesis are based on the assumption that inheritance graphs are made with optimizing spirit. This is a perfectly reasonable assumption since there are no reasons to hypothesize that inheritance arise from chaos.

Anyway, it is interesting to compare Sharing Tree graphs with graphs obtained through models completely random and made without optimization mechanisms.

4.7.1 Random Branching Tree model

A Random Branching Tree can be built starting from an initial node, the root, and choosing a distribution with a well-defined mean.

As a first step, we extract a random variable from the distribution: the extraction represents the root outdegree and so the number of nodes that are connected to the root. Once added new nodes, the process is iterated for each new node until a certain condition is reached.

The outdegree mean in function of levels is obviously a constant value, equal to the mean of the chosen distribution for the outdegree. Simulations are shown in figure 4.12.

Which random mechanism can be introduced to obtain a non constant function?

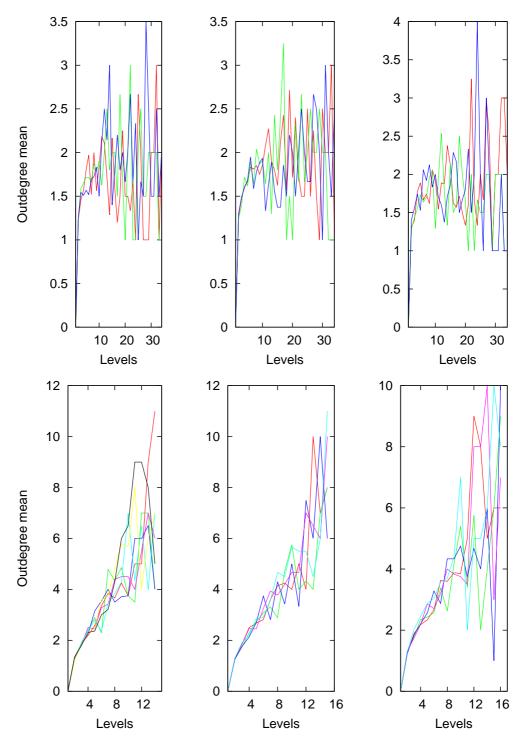


Figure 4.12: Random branching tree and Pang-Maslov models simulation - The outdegree mean in function of levels does not reproduce the behavior observed in data.

4.7.2 Pang-Maslov model

The Pang-Maslov model [PM13] can be used to construct a tree. Consider an initial node an a process for which, at each step, a new node arrives and sticks to one of the existing nodes. The process can be iterated until a certain condition is reached.

This model prevents the constancy of outdegree mean, since the older nodes have had more chance of being chosen by another node, and so they must have an outdegree greater than young nodes. Growth, however, is constant and it does not represent well the behavior of outdegree mean in data.

4.7.3 Sharing Tree comparison

Through the Sharing Tree model, we can can produce Monte Carlo trees to explicitly compare optimization ideas with data. Some examples are given in figure 4.13.

The outdegree mean has not a trivial behavior due to its strong growth close to the root, that is also the main feature observable in data.

Therefore, there is a very good agreement between data and optimization models.

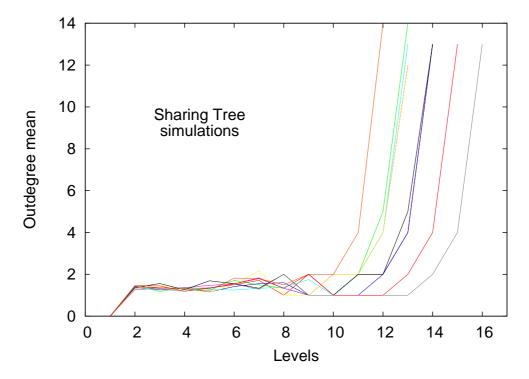


Figure 4.13: Sharing Tree Monte Carlo simulations - The Sharing Tree model well capture the behave of the outdegree mean as function of levels. In simulations, parameters are $\mathcal{N}=1000$, k=100 and $\mathcal{S}=2000$.

Chapter 5

Conclusions

The noisy data have proved to be full of interesting informations: they have showed universal behaviors among object-oriented programming languages but they also highlight structural differences in inheritance management.

Hierarchical sizes distribution is universal

Hierarchies sizes distribution is power law distributed and there are no differences among the three programming languages.

The speciation of classes has an universal behavior

Despite the differences among C++, Java and Python, the speciation is used in the same manner, and so the distribution of the number of classes that inherits code from a selected class is the same.

Multiple inheritance is ever less used than speciation

The multiple inheritance is used with differences between the three languages. It is always used less than speciation, even in Java, where it has a different and more useful meaning.

Hierarchies are shallow

The vast majority of graphs have a depth equal to two or three while the deeper hierarchies have at most a depth of about eleven, or twelve.

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Java hierarchies are shallower

Java hierarchies show a depth sistematically lower than the Python and C++, while graph sizes behave in the same way.

The depth is a logarithmic function of the hierarchy size

In C++ and Python, the mean of depths of hierarchies as a function of the number of classes has a logarithmic behavior.

Huge hierarchies behave differently

The depth of huge hierarchies doesn't fit the logarithmic behavior of small and medium hierarchies. It is systematically over such function.

Speciation is a function of levels

Classes that does lots of speciation are always at the higher levels.

The Minimal Effort model gives a link between the hierarchical structures and the effort done to build them. It allows to give an interpretation to data, and it is a guide to key quantities.

The Sharing Tree model extends the mean field model and allows Monte Carlo simulations. The mechanism implemented is close to the natural approach of programmers in objects organization and Sharing Monte Carlo trees well reproduce the data hierarchies.

The depth is the central quantity for optimization mechanism, since it governs the hierarchical structures for fixed size and the proportion between the vertical and the horizontal dimension. Programmers seems to follow the advise to keep the depth as shallow as possibile to avoid the yo-yo problem instead of looking for the optimal structure for code reuse.

The optimization resulting from the competition between the reuse and the abstractability of the code seems to play an important role in the construction of hierarchical inheritance structures in object-oriented programming languages.

Appendix A

Source code

A.1 Library for data analysis

In this section, some of the classes implemented in the library are listed. Classes omitted are Scatterplot, Lineplot and Distribuzioni that allow a suitable print of data obtainable by the following classes.

A.1.1 class Node

A class that realize the concept of node.

node.hpp

```
1 ||#ifndef _NODE_HPP_
   #define _NODE_HPP_
3
   #include <string>
4
   #include <vector>
   #include <iostream>
    using namespace std;
9
10
    class Node {
11
12
      public:
13
        //Costruttore/Distruttore
        Node();
14
15
        ~Node();
16
        //Assegnamento
17
18
        Node & operator = (Node & obj);
19
        //Funzioni
20
21
        void Add_edge_in(size_t number);
        void Add_edge_out(size_t number);
22
23
24
        //Set
```

```
25
        void Set_level(size_t level);
26
        void Set_Rlevel(size_t Rlevel);
27
28
        //Get
29
        size_t Get_Npar() const;
30
        size_t Get_Nsons() const;
        size_t Get_level() const;
31
32
        size_t Get_Rlevel() const;
33
34
        size_t Get_son(size_t i) const;
35
        size_t Get_par(size_t i) const;
36
37
38
     private:
39
        vector < size_t > _edgein;
40
        vector < size_t > _edgeout;
41
       size_t _level;
42
        size_t _Rlevel;
43
44
   };
45
46 #endif
```

node.cpp

```
#include "node.hpp"
2
3
4
   Costruttore
5
6
  Node::Node(): _level(0), _Rlevel(0) {};
7
8
  Assegnamento
  -----*/
g
10
  Node &Node::operator=(Node &obj){
11
   _edgein=obj._edgein;
12
   _edgeout=obj._edgeout;
   _level=obj._level;
13
14
    _Rlevel=obj._Rlevel;
15
    return *this;
16
  /*-----
17
18
             -----*/
19
  Node::~Node(){
20
21
   _edgein.clear();
22
    _edgeout.clear();
23
  };
  /*-----
24
25
   Functions
26
  -----*/
27
  void Node::Add_edge_in(size_t number){
   bool found = false;
28
29
    for(size_t i=0; i<_edgein.size(); i++) {</pre>
30
     if(number == _edgein[i]) found = true;
31
32
    if(!found) {
33
     _edgein.push_back(number);
34
35 || };
```

```
-----*/
36 ||
  void Node::Add_edge_out(size_t number){
37
38
    bool found = false;
39
    for(size_t i=0; i<_edgeout.size(); i++) {</pre>
40
      if(number == _edgeout[i]) found = true;
41
    if(!found) {
42
43
      _edgeout.push_back(number);
44
  ||};
45
          ______
46
47
   Set
48
49
  void Node::Set_level(size_t level){
50
    if(_level<level) _level=level;</pre>
51
  };
52
53
  void Node::Set_Rlevel(size_t Rlevel){
    if(_Rlevel < Rlevel) _Rlevel = Rlevel;</pre>
54
  };
55
56
57
   Get
        -----*/
58
59
  size_t Node::Get_Npar() const {
60
   return _edgein.size();
61
                            -----*/
63
  size_t Node::Get_Nsons() const {
64
    return _edgeout.size();
  };
65
  /*----*/
66
67
  \verb|size_t Node|:: Get_level()| const \{ \\
68
   return _level;
  };
69
70
71
  size_t Node::Get_Rlevel() const {
72
   return _Rlevel;
73
     -----*/
74
75
  \verb|size_t Node|:: Get_son(size_t i) const \{ |
76
   return _edgeout[i];
  };
77
79
  size_t Node::Get_par(size_t i) const {
80
    return _edgein[i];
81
      -----*/
```

A.1.2 class Graph

The class Graph is central for the library. It allows to obtain all main quantities about a graph, or a tree.

graph.hpp

```
1 | #ifndef _GRAPH_HPP_
2 | #define _GRAPH_HPP_
```

```
3 |
   #include <string>
4
   #include <vector>
   #include <fstream>
   #include <cmath>
   #include <map>
8
   #include <set>
g
   #include "node.hpp"
10
11
   #include "funzioni.hpp"
12
13
   using namespace std;
14
15
   class Graph {
16
      public:
17
18
        //Costruttori/Distruttore
19
        Graph();
20
        Graph(const char *edgefile);
21
        ~Graph();
22
23
        //Assegnamento
24
        Graph & operator = (const Graph & obj);
25
26
27
        void HTD(double **scores, string **namescores, size_t nrows);
28
29
30
        void set(vector<size_t> from, vector<size_t> to, bool connection = 0)
31
        void clear();
32
33
        //Get
34
        size_t depth();
35
        size_t Nnodes();
36
        size_t Nnodes(size_t level);
37
        size_t RNnodes(size_t level);
38
        size_t diamonds();
39
40
        size_t Nleaves();
41
42
        size_t outdeg(size_t nodo);
        size_t indeg(size_t nodo);
43
44
45
        size_t brothers(size_t level);
46
        size_t Rbrothers(size_t level);
47
48
        vector < size_t > leaves_depth();
49
        vector < size_t > nodes_depth();
50
51
        vector < size_t > indegrees();
52
        vector < size_t > outdegrees();
        vector < size_t > leaves_indegrees();
53
54
        vector < size_t > roots_outdegrees();
55
        vector < double > mean_Routdegrees();
56
57
        vector < double > mean_outdegrees();
58
59
        vector < size_t > Kin();
60
        vector < size_t > Kout();
61
        //Statistics
62
        double mean_depth();
```

```
64
         double mean_leaves_depth();
65
         double mean_Rdepth();
66
         double mean_outdeg();
         double mean_Routdeg(size_t level);
67
68
         double mean_outdeg(size_t level);
69
70
         double cost(double lambda);
71
         double cost(size_t nodo, double lambda);
72
         double recursive_cost(double lambda);
73
         double recursive_cost(size_t nodo, double lambda);
74
75
           OVERLOADING DEL <<
 76
         friend ostream &operator<<(ostream &os, Graph &g);</pre>
77
 78
       private:
79
         Node *_nodes;
         size_t _Nnodes;
80
81
         size_t *_ordernodes;
 82
         size_t *_Rordernodes;
83
         vector < size_t > _leaves;
         vector < size_t > _roots;
84
85
         size_t _diamonds;
86
         bool \ \_{\tt diamonds\_check};
87
88
         vector < size_t > _Kin;
89
         vector < size_t > _Kout;
90
91
         void find_levels();
92
         void find_reversed_levels();
93
         void find_leaves();
94
         void find_roots();
95
         void visita(size_t node, std::set<size_t> &visitati);
96
         void find_connection();
97
         void find_Kin();
98
         void visita_down(size_t node, std::set<size_t> &visitati);
         void find_Kout();
99
100
         void visita_up(size_t node, std::set<size_t> &visitati);
101
         void find_diamonds();
         void visita_diamond(size_t analyzed, size_t node, std::set<size_t> &
102
             visitati, std::set<size_t> &diamanti);
103 | };
104 | #endif
```

graph.cpp

```
1 | #include "graph.hpp"
2
  /*-----
3 |
4
  Costruttori
  -----*/
5
  Graph::Graph(): _nodes(NULL), _ordernodes(NULL), _Rordernodes(NULL),
6
    _diamonds(0), _diamonds_check(0) {};
7
               -----*/
  Graph::Graph(const char *edgefile): _ordernodes(NULL), _Rordernodes(NULL)
     , \_diamonds(0), \_diamonds\_check(0) {
9
   fstream f;
10
   string help;
   vector < string > from, to;
11
12
   f.open(edgefile,ios::in);
```

```
14
     f>>help;
15
      \mathbf{while}(!f.eof()){
16
        from.push_back(help);
       f>>help;
17
18
        to.push_back(help);
19
        f>>help;
20
21
            f.close();
22
23
      if (from.size()!=to.size())  {
24
       cerr<<"Graph:: costruttore - controlla il file di input!"<<endl;</pre>
25
26
      if (from.size() == 0 || to.size() == 0) {
27
        cerr << "Graph:: costruttore - creazione di grafo mononodo!" << endl;</pre>
28
        _Nnodes=1;
29
        _nodes = new Node;
        _roots.push_back(0);
30
31
        _leaves.push_back(0);
32
        _nodes[0].Set_level(1);
33
        _nodes[0].Set_Rlevel(1);
34
        _ordernodes=new size_t;
35
        _ordernodes[0]=0;
36
        _Rordernodes=new size_t;
37
        _Rordernodes[0]=0;
38
     }
39
      else {
40
        map < string , size_t > conversione;
41
        size_t cont=0;
42
        for(size_t i=0; i<from.size(); i++) {</pre>
          if(conversione.find(from[i]) == conversione.end()) {
43
44
            conversione[from[i]]=cont;
45
            cont++;
46
          if(conversione.find(to[i]) == conversione.end()) {
47
48
            conversione[to[i]]=cont;
49
            cont++:
50
          }
51
52
        _Nnodes = conversione.size();
53
        _nodes = new Node[_Nnodes];
        -
//Costruzione del grafo
54
55
        for(size_t i=0;i<from.size();i++){</pre>
56
          if(from[i] == to[i]) {
57
            cerr << "Graph:: set - Loop, padre di se stesso!" << endl;</pre>
58
            continue; // loooooop :(
59
60
          _nodes[conversione[from[i]]].Add_edge_out(conversione[to[i]]);
61
          _nodes[conversione[to[i]]].Add_edge_in(conversione[from[i]]);
62
63
        find_roots();
64
        find_connection();
65
        find_levels();
66
        find_leaves();
67
        find_reversed_levels();
68
69
   };
70
71
    Assegnamento
72
                    -----*/
73
   Graph &Graph::operator=(const Graph &obj){
74
      (*this).clear();
     _Nnodes=obj._Nnodes;
```

```
76
      _leaves=obj._leaves;
 77
      _roots=obj._roots;
 78
      _diamonds=obj._diamonds;
79
      _diamonds_check=obj._diamonds_check;
 80
      _Kin=obj._Kin;
      _Kout=obj._Kout;
81
      _ordernodes = new size_t[_Nnodes];
82
 83
      _Rordernodes = new size_t[_Nnodes];
      _nodes = new Node[_Nnodes];
84
85
      for(size_t i=0; i<_Nnodes; i++) {</pre>
       _ordernodes[i]=obj._ordernodes[i];
86
87
        _Rordernodes[i]=obj._Rordernodes[i];
88
        _nodes[i]=obj._nodes[i];
89
90
      return *this;
91
    };
92
93
94
95
    Graph::~Graph(){
96
      if(_nodes!=NULL) {
        if(_Nnodes==1) delete _nodes;
else delete[] _nodes;
97
98
99
100
      if(_ordernodes!=NULL) {
101
        if(_Nnodes==1) delete _ordernodes;
        else delete[] _ordernodes;
102
103
104
      if(_Rordernodes!=NULL) {
        if(_Nnodes == 1) delete _Rordernodes;
105
106
        else delete[] _Rordernodes;
107
      _nodes = NULL;
108
109
      _ordernodes = NULL;
110
      _Rordernodes = NULL;
      _leaves.clear();
111
112
      _roots.clear();
113
      _Nnodes = 0;
   ||};
114
    /*-----
115
116
      Settings
    -----*/
117
    void Graph::set(vector<size_t> from, vector<size_t> to, bool connection )
       {
119
      clear();
      if (from.size()!=to.size()) {
120
121
       cerr<<"Graph:: set - controlla i vettori in input!"<<endl;</pre>
122
123
      if (from.size()==0 || to.size()==0) {
124
        cerr << "Graph:: set - creazione di grafo mononodo!" << endl;</pre>
125
        _Nnodes=1;
        _nodes = new Node;
126
127
        _roots.push_back(0);
128
        _leaves.push_back(0);
129
        _nodes[0].Set_level(1);
130
        _nodes[0].Set_Rlevel(1);
        _ordernodes=new size_t;
131
132
        _ordernodes[0]=0;
133
        _Rordernodes=new size_t;
134
        _Rordernodes[0]=0;
135
136
      else {
```

```
137
        map < size_t , size_t > conversione;
138
        size_t cont=0;
139
        for(size_t i=0; i<from.size(); i++) {</pre>
          if(conversione.find(from[i]) == conversione.end()) {
140
141
           conversione[from[i]]=cont;
142
           cont++;
143
144
          if(conversione.find(to[i]) == conversione.end()) {
145
           conversione[to[i]]=cont;
146
            cont++;
147
         }
148
        }
149
        _Nnodes = conversione.size();
        _nodes = new Node[_Nnodes];
150
151
        //Costruzione del grafo
152
        for(size_t i=0;i<from.size();i++){</pre>
153
         if(from[i] == to[i]) {
154
           cerr << "Graph:: set - Loop, padre di se stesso!" << endl;
155
           continue; // loooooop :(
156
157
          _nodes[conversione[from[i]]].Add_edge_out(conversione[to[i]]);
158
          _nodes[conversione[to[i]]].Add_edge_in(conversione[from[i]]);
159
160
        find_roots();
161
        if(connection == 0) find_connection();
162
        find_levels();
163
        find_leaves();
164
        find_reversed_levels();
165
      }
166
    };
167
    /*----*/
168
    void Graph::clear(){
169
      if(_nodes!=NULL) {
170
        if(_Nnodes==1) delete _nodes;
171
        else delete[] _nodes;
172
173
      if(_ordernodes!=NULL) {
174
        if(_Nnodes==1) delete _ordernodes;
        else delete[] _ordernodes;
175
176
177
      if(_Rordernodes!=NULL) {
        if(_Nnodes == 1) delete _Rordernodes;
178
179
        else delete[] _Rordernodes;
180
      _nodes = NULL;
181
      _ordernodes = NULL;
182
      _Rordernodes = NULL;
183
184
      _leaves.clear();
185
      _roots.clear();
186
      _Kin.clear();
187
      _Kout.clear();
188
      _Nnodes = 0;
189
      _diamonds_check = 0;
190
      _diamonds = 0;
    ን:
191
    /*----
192
193
     Finding \dots
    -----*/
194
195
    void Graph::find_levels(){
196
      size_t iter_level=1, help;
      vector<size_t> support1, support2;
197
     //selezionare le root del grafo
```

```
199
       for(size_t i=0;i<_roots.size();i++){</pre>
200
         support1.push_back(_roots[i]);
201
       //percorrere il grafo top-down per definire i livelli
202
203
       while(support1.size()!=0){
204
         iter_level++;
205
         for(size_t i=0;i<support1.size();i++){</pre>
206
           for(size_t j=0;j<_nodes[support1[i]].Get_Nsons();j++){</pre>
207
             help=_nodes[support1[i]].Get_son(j);
208
              _nodes[help].Set_level(iter_level);
209
             support2.push_back(help);
210
           }
211
         support1.clear();
212
213
         iter_level++;
214
         for(size_t i=0;i<support2.size();i++){</pre>
215
           for(size_t j=0;j<_nodes[support2[i]].Get_Nsons();j++){</pre>
216
             help=_nodes[support2[i]].Get_son(j);
217
              _nodes[help].Set_level(iter_level);
218
             support1.push_back(help);
219
           }
220
221
         support2.clear();
222
223
       //salvo l'indice delle posizioni dei nodi ordinati secondo il loro
           livello
224
       _ordernodes=new size_t[_Nnodes];
225
       for (size\_t i=0; i < \_Nnodes; i++) \_ordernodes[i]=i;
226
       size_t vettore[_Nnodes];
227
       for(size_t i=0;i<_Nnodes;i++) vettore[i]=_nodes[i].Get_level();</pre>
228
       quicksort(_Nnodes, vettore, _ordernodes);
229
     };
230
231
     void Graph::find_reversed_levels(){
      size_t iter_level=1, help;
232
233
       vector < size_t > support1, support2;
       //selezionare le leaves del grafo
234
235
       for(size_t i=0;i<_leaves.size();i++){</pre>
236
         support1.push_back(_leaves[i]);
237
238
       //percorrere il grafo down-top per definire i livelli
239
       while(support1.size()!=0){
240
         iter_level++;
241
         for(size_t i=0;i<support1.size();i++){</pre>
           for(size_t j=0;j<_nodes[support1[i]].Get_Npar();j++){</pre>
242
243
             help=_nodes[support1[i]].Get_par(j);
244
             _nodes[help].Set_Rlevel(iter_level);
245
             support2.push_back(help);
246
           }
247
248
         support1.clear();
249
         iter_level++;
250
         for(size_t i=0;i<support2.size();i++){</pre>
251
           for(size_t j=0;j<_nodes[support2[i]].Get_Npar();j++){</pre>
252
             help=_nodes[support2[i]].Get_par(j);
253
              _nodes[help].Set_Rlevel(iter_level);
254
             support1.push_back(help);
255
           }
256
257
         support2.clear();
```

```
259
      //salvo l'indice delle posizioni dei nodi ordinati secondo il loro
          livello
260
       _Rordernodes=new size_t[_Nnodes];
      for(size_t i=0;i<_Nnodes;i++) _Rordernodes[i]=i;</pre>
261
262
      size_t vettore[_Nnodes];
263
      for(size_t i=0;i<_Nnodes;i++) vettore[i]=_nodes[i].Get_Rlevel();</pre>
264
      quicksort(_Nnodes, vettore, _Rordernodes);
265
    };
266
    /*-
        */
267
    void Graph::find_leaves(){
268
      for(size_t i=0;i<_Nnodes;i++) {</pre>
269
        if(\_nodes[i].Get\_Nsons()==0) {
          _leaves.push_back(i);
270
271
          _nodes[i].Set_Rlevel(1);
272
273
      }
274
    };
275
276
    void Graph::find_roots(){
277
      for(size_t i=0;i<_Nnodes;i++) {</pre>
278
        if(_nodes[i].Get_Npar()==0) {
279
          _roots.push_back(i);
          _nodes[i].Set_level(1);
280
281
        }
282
      }
283
    };
284
          -----*/
285
    void Graph::find_connection() {
286
      std::set<size_t> supporto, tosave;
287
      //cerco componente piu' grande
      for (size_t i=0; i<_roots.size(); i++) {</pre>
288
289
        if(supporto.find(_roots[i]) == supporto.end()) {
290
          visita(_roots[i], supporto);
          if(supporto.size() > tosave.size()) tosave = supporto;
291
292
          supporto.clear();
293
294
295
      if(tosave.size() != _Nnodes) {
296
        cerr < "Graph:: Errore! Il grafo non e' connesso (o non ci sono radici
           )!"<<endl;
297
        vector < size_t > new_from , new_to;
298
        for (std::set<size_t>::iterator i = tosave.begin(); i != tosave.end()
            ; i++) {
299
          for(size_t j=0; j<_nodes[*i].Get_Nsons(); j++){</pre>
300
            new_from.push_back(*i);
301
            new_to.push_back(_nodes[*i].Get_son(j));
302
303
304
         (*this).clear();
305
        this->set(new_from,new_to, 1);
306
      }
307
    }
    /*-----/
308
309
    void Graph::find_Kin() {
310
      std::set<size_t> linkati_up;
      for(size_t i=0; i<_Nnodes; i++) {</pre>
311
312
        visita_up(i,linkati_up);
313
        _Kin.push_back(linkati_up.size()-1);
314
        linkati_up.clear();
315
```

```
316
   || }
317
318
                     -----*/
    void Graph::find_Kout() {
319
320
      std::set<size_t> linkati_down;
321
      for(size_t i=0; i<_Nnodes; i++) {</pre>
322
        visita_down(i,linkati_down);
323
        _Kout.push_back(linkati_down.size()-1);
324
        linkati_down.clear();
325
      }
   || }
326
327
328
    void Graph::find_diamonds() {
329
     std::set<size_t> linkati;
330
      std::set<size_t> diamanti;
331
      for(size_t i=0; i<_Nnodes; i++) {</pre>
        visita_diamond(i,i,linkati, diamanti);
332
333
        linkati.clear();
334
335
      _diamonds = diamanti.size();
336
      _diamonds_check = 1;
337
    }
338
        ______
339
     {\it Visiting} ...
340
341
    //per vedere se il grafo e' connesso
    void Graph::visita(size_t node, std::set<size_t> &visitati) {
      std::set<size_t> linkati;
343
344
      visitati.insert(node);
345
      for (size_t j=0; j<_nodes[node].Get_Nsons(); j++) {</pre>
346
       linkati.insert(_nodes[node].Get_son(j));
347
348
      for (size_t j=0; j<_nodes[node].Get_Npar(); j++) {</pre>
349
        linkati.insert(_nodes[node].Get_par(j));
350
       for \ (std::set < size\_t > :: iterator \ j = linkati.begin(); \ j != linkati.end() 
351
          ; j++) {
352
         if(visitati.find(*j) == visitati.end()) {
353
          visita(*j, visitati);
354
355
      }
   };
356
357
358
    void Graph::visita_up(size_t node, std::set<size_t> &visitati) {
359
      std::set<size_t> linkati;
360
      visitati.insert(node);
361
      for (size_t j=0; j<_nodes[node].Get_Npar(); j++) {</pre>
362
        linkati.insert(_nodes[node].Get_par(j));
363
364
      for (std::set<size_t>::iterator j = linkati.begin(); j != linkati.end()
          ; j++) {
         if(visitati.find(*j) == visitati.end()) {
365
366
          visita_up(*j, visitati);
367
368
      }
369
   || };
370
371
    void Graph::visita_down(size_t node, std::set<size_t> &visitati) {
372
      std::set<size_t> linkati;
373
      visitati.insert(node);
      for (size_t j=0; j<_nodes[node].Get_Nsons(); j++) {</pre>
374
       linkati.insert(_nodes[node].Get_son(j));
```

```
376
377
      for (std::set<size_t>::iterator j = linkati.begin(); j != linkati.end()
          ; j++) {
378
        if(visitati.find(*j) == visitati.end()) {
379
         visita_down(*j, visitati);
380
381
      }
382
    };
383
384
    void Graph::visita_diamond(size_t analyzed, size_t node, std::set<size_t>
        &visitati, std::set<size_t> &diamanti) {
385
      std::set<size_t> linkati;
386
      visitati.insert(node);
387
      for (size_t j=0; j<_nodes[node].Get_Npar(); j++) {</pre>
388
        linkati.insert(_nodes[node].Get_par(j));
389
390
      if (_diamonds_check == 0 ) {
391
        for (std::set<size_t>::iterator j = linkati.begin(); j != linkati.end
            (); j++) {
392
          if(visitati.find(*j) == visitati.end()) {
393
            visita_diamond(analyzed, *j, visitati, diamanti);
394
395
          else {
396
            diamanti.insert(analyzed);
397
           break:
398
         }
399
        }
400
      }
401
402
403
404
405
406
    size_t Graph::brothers(size_t level) {
407
      size_t cont=0;
408
      for(size_t i=0;i<_Nnodes;i++){</pre>
409
        if(_nodes[_ordernodes[i]].Get_level() == level) cont++;;
410
        if(_nodes[_ordernodes[i]].Get_level()>level) break;
411
412
      return cont;
413
    }
    /*-----/
414
415
    size_t Graph::Rbrothers(size_t level) {
416
      size_t cont=0;
417
      for(size_t i=0;i<_Nnodes;i++){</pre>
       if(_nodes[_Rordernodes[i]].Get_Rlevel() == level) cont++;;
418
419
        if (\_nodes [\_Rordernodes [i]]. \\ Get \_Rlevel () > level) \ break;
420
      }
421
      return cont;
422
    }
423
                            424
    size_t Graph::depth() {
425
      return _nodes[_ordernodes[_Nnodes-1]].Get_level();
426
    }
427
428
    size_t Graph::Nnodes() {
     return _Nnodes;
429
    7
430
    /*-----/
431
432
    size_t Graph::outdeg(size_t nodo) {
433
     return _nodes[_ordernodes[nodo]].Get_Nsons();
434 | }
```

```
435 || /*-----*/
436
   size_t Graph::indeg(size_t nodo) {
437
    return _nodes[_ordernodes[nodo]].Get_Npar();
   || }
438
439
   /*----*/
440
   size_t Graph::Nnodes(size_t level) {
441
     size_t control=0, sum=0;
442
     for(size_t i=0;i<_Nnodes;i++){</pre>
443
      control=_nodes[_ordernodes[i]].Get_level();
444
       if(control==level) sum++;
       if(control>level) break;
445
446
     }
447
     return sum;
  || }
448
   /*-----*/
449
450
   size_t Graph::RNnodes(size_t level) {
451
    size_t control=0, sum=0;
452
     for(size_t i=0;i<_Nnodes;i++){</pre>
       control=_nodes[_Rordernodes[i]].Get_Rlevel();
453
       if(control == level) sum ++;
454
455
       if(control>level) break;
456
457
     return sum;
458
   }
459
   /*----*/
460
   size_t Graph::diamonds() {
    if (_diamonds_check == 0) {
462
      find_diamonds();
463
    return _diamonds;
464
465
   };
   /*-----/
466
467
   size_t Graph::Nleaves() {
468
    return _leaves.size();
469
   }
470
471
   vector < size_t > Graph::leaves_depth() {
472
     vector < size_t > depths;
     for(size_t i=0;i<_leaves.size();i++)</pre>
473
474
       depths.push_back(_nodes[_leaves[i]].Get_level());
475
    return depths;
  ||};
476
477
        -----*/
   vector < size_t > Graph::nodes_depth() {
478
479
    vector < size_t > depths;
480
    for(size_t i=0;i<_Nnodes;i++)</pre>
481
       depths.push_back(_nodes[i].Get_level());
482
    return depths;
  };
483
484
   /*----*/
   vector < size_t > Graph::leaves_indegrees(){
485
    vector < size_t > indegrees;
486
487
    for(size_t i=0;i<_leaves.size();i++)</pre>
488
       indegrees.push_back(_nodes[_leaves[i]].Get_Npar());
489
    return indegrees;
  ||};
490
491
   vector < size_t > Graph::roots_outdegrees(){
492
     vector < size_t > outdegrees;
493
494
     for(size_t i=0;i<_roots.size();i++)</pre>
       outdegrees.push_back(_nodes[_roots[i]].Get_Nsons());
495
    return outdegrees;
```

```
497 || };
      -----*/
498
499
   vector < size_t > Graph::indegrees(){
500
     vector<size_t> indegrees;
501
     for(size_t i=0;i<_Nnodes;i++)</pre>
502
       indegrees.push_back(_nodes[i].Get_Npar());
503
     return indegrees;
504
   };
505
   vector<size_t> Graph::outdegrees(){
506
     vector < size_t > outdegrees;
507
508
     for(size_t i=0;i<_Nnodes;i++)</pre>
509
       outdegrees.push_back(_nodes[i].Get_Nsons());
510
     return outdegrees:
511
   }:
       -----*/
512
   vector < double > Graph::mean_Routdegrees(){
513
514
     vector < double > outdegrees;
515
     for(size_t i=0;i<depth();i++)</pre>
516
      outdegrees.push_back(mean_Routdeg(i+1));
     return outdegrees;
517
518
   };
       519
520
   vector < double > Graph::mean_outdegrees(){
521
     vector < double > outdegrees;
522
     for(size_t i=0;i<depth();i++)</pre>
523
      outdegrees.push_back(mean_outdeg(i+1));
524
     return outdegrees;
   };
525
        -----*/
526
527
   vector<size_t> Graph::Kin(){
528
     find_Kin();
529
     return _Kin;
   }
530
531
   vector<size_t> Graph::Kout(){
532
533
     find_Kout();
534
     return _Kout;
535
   }
   /*-----
536
537
    Statistics
538
539
   double Graph::mean_depth(){
540
    size_t sum=0;
541
     for(size_t i=0;i<_Nnodes;i++)</pre>
542
     sum+=_nodes[i].Get_level();
543
     return double(sum)/_Nnodes;
544
   };
        -----*/
545
546
   double Graph::mean_leaves_depth(){
547
     size_t sum=0;
     for(size_t i=0;i<_leaves.size();i++)</pre>
548
549
      sum+=_nodes[_leaves[i]].Get_level();
550
     return double(sum)/_leaves.size();
   };
551
   /*-----/
552
553
   double Graph::mean_Rdepth(){
554
     size_t sum=0;
555
     for(size_t i=0;i<_Nnodes;i++)</pre>
556
      sum += _nodes[i].Get_Rlevel();
     return double(sum)/_Nnodes;
557
```

```
559 || /*-----*/
560 double Graph::mean_outdeg(){
561
     size_t sum=0,cont=0;
     for(size_t i=0;i<_Nnodes;i++){</pre>
562
563
      sum+=_nodes[i].Get_Nsons();
564
       cont++;
565
566
     return double(sum)/cont;
   ||};
567
   /*-----/
568
569
   double Graph::mean_outdeg(size_t level){
570
     size_t sum=0,cont=0;
571
     for(size_t i=0;i<_Nnodes;i++){</pre>
572
       if(_nodes[i].Get_level() == level){
573
        sum+=_nodes[i].Get_Nsons();
574
         cont++;
575
576
     }
577
     return double(sum)/cont;
578
  };
    /*-----*/
579
580
   double Graph::mean_Routdeg(size_t level){
581
     size_t sum=0,cont=0;
582
     for(size_t i=0;i<_Nnodes;i++){</pre>
583
       if(_nodes[i].Get_Rlevel() == level){
584
        sum+=_nodes[i].Get_Nsons();
585
        cont++;
586
587
     }
588
     return double(sum)/cont;
589
   };
    /*-----/
590
591
   double Graph::cost(double lambda) {
592
     double sum = 0.;
593
     for(size_t i=0;i<_Nnodes;i++)</pre>
594
      sum += cost(i, lambda);
595
     return sum/_Nnodes;
   };
596
   /*-----*/
597
598
  double Graph::cost(size_t nodo, double lambda) {
599
     size_t Npar = _nodes[nodo].Get_Npar();
     size_t kout = 0;
600
601
     for(size_t i=0;i<Npar;i++){</pre>
602
       size_t par = _nodes[nodo].Get_par(i);
603
       kout += _nodes[par].Get_Nsons();
604
     if(Npar == 0) return 1.0;
605
606
     else return 1.0 - exp(-lambda*kout);
607
  | };
   /*-----/
608
609
   double Graph::recursive_cost(double lambda) {
610
     double sum = 0.:
611
     for(size_t i=0;i<_Nnodes;i++)</pre>
612
      sum += recursive_cost(i, lambda);
613
     return sum/_Nnodes;
614 || };
615
   double Graph::recursive_cost(size_t nodo, double lambda) {
616
617
     size_t Npar = _nodes[nodo].Get_Npar();
618
     size_t kout = 0;
     double prev = 0.0;
619
     for (size_t i=0; i < Npar; i++) {</pre>
```

```
size_t par = _nodes[nodo].Get_par(i);
621
622
        kout += _nodes[par].Get_Nsons();
623
        prev += recursive_cost(par, lambda);
624
625
      prev /= Npar;
626
      if(Npar == 0) return 1.0;
627
      else return prev - exp(-lambda*kout);
628
629
630
      Miscellaneous
                     -----*/
631
632
    void Graph::HTD(double **scores, string **namescores, size_t nrows){
633
      size_t position, Npar, dad;
      //applico l'algoritmo top-down al grafo
634
635
      for(size_t i=0;i<_Nnodes;i++){</pre>
636
        position=_ordernodes[i];
637
        Npar=_nodes[position].Get_Npar();
638
        for(size_t k=0;k\leq nrows;k++){
639
          for(size_t j=0;j<Npar;j++){
640
            dad=_nodes[position].Get_par(j);
641
            if(scores[k][position] > scores[k][dad]){
642
              scores[k][position]=scores[k][dad];
643
              namescores[k][position]=namescores[k][dad];
644
645
          }
646
        }
647
      }
648
    };
649
    std::ostream &operator << ( std::ostream &os, Graph &g) {
650
651
      os<<0<<endl;
652
      for(size_t i=0; i<g._Nnodes; i++){</pre>
        for(size_t j=0; j<g._nodes[i].Get_Nsons(); j++){
  os<< i+1 << "\t" << g._nodes[i].Get_son(j)+1<< "\n";</pre>
653
654
655
      }
656
657
      return os;
    };
658
             -----*/
659
```

A.1.3 class Packagegraph

This class is a tool that allows to analyze automatically more graphs at the same time.

packagegraph.hpp

```
#ifndef _PACKAGEGRAPH_HPP_

#define _PACKAGEGRAPH_HPP_

#include <string>
#include <vector>
#include <fstream>
#include "node.hpp"
#include "graph.hpp"
#include "funzioni.hpp"
```

```
11 || using namespace std;
12
13
    class Packagegraph {
14
15
        //Costruttori/Distruttore
16
17
        Packagegraph();
18
        Packagegraph(const char *edgefile);
19
        ~Packagegraph();
20
21
        //Assegnamento
        Packagegraph &operator=(Packagegraph &obj);
22
23
24
        //Setting
        void add(Graph *g);
25
26
        void clear();
27
28
        //Get
29
        string name();
30
        size_t N();
31
        size_t depth(size_t i);
32
        size_t Nnodes(size_t i);
33
        size_t outdeg(size_t grafo,size_t nodo);
34
        size_t indeg(size_t grafo,size_t nodo);
35
        size_t Nleaves(size_t grafo);
36
37
38
        void set_name(string name);
39
40
        //Quantities
41
        size_t max_depth();
        size_t Nnodes(size_t i, size_t level);
42
43
        size_t RNnodes(size_t i, size_t level);
44
45
        //Order Parameters
        size_t diamanti();
46
47
        size_t diamanti(size_t i);
48
        double cost(size_t grafo, double lambda);
49
        double recursive_cost(size_t grafo, double lambda);
50
51
        //Means
        double mean_Nnodes();
52
53
        double mean_depth();
54
        double mean_Rdepth();
55
        double mean_leaves_depth();
        double mean_leaves_depth(size_t i);
56
57
        {\bf double\ mean\_outdeg(size\_t\ grafo);}
58
59
        double mean_meandepth();
        double mean_depth(size_t i);
60
61
        double mean_meanRdepth();
62
        vector < size_t > brothers(size_t graph);
63
64
        vector < size_t > Rbrothers(size_t graph);
65
66
67
        //Distributions
68
        vector < size_t > indegrees();
69
        vector < size_t > outdegrees();
70
        vector < size_t > nodes_depth();
71
        vector<size_t> indegrees(size_t i);
```

```
73 |
        vector < size_t > outdegrees(size_t i);
74
        vector < size_t > nodes_depth(size_t i);
75
76
        vector < double > mean_Routdegrees(size_t grafo);
77
        vector <double> mean_outdegrees(size_t grafo);
78
79
        vector < size_t > roots_outdegrees();
80
        vector < size_t > roots_outdegrees(size_t i);
81
        vector < size_t > leaves_indegrees();
82
83
        vector < size_t > leaves_depth();
84
85
        vector < size_t > leaves_indegrees(size_t i);
        vector < size_t > leaves_depth(size_t i);
86
87
88
      private:
        vector < Graph *> _grafi;
89
90
        size_t _Ngrafi;
91
        string _nome;
92
   };
93
94 #endif
```

packagegraph.cpp

```
1 | #include "packagegraph.hpp"
2
       -----
3
4
   Costruttori
   -----*/
6
   Packagegraph::Packagegraph(): _Ngrafi(0){};
7
8
   Packagegraph::Packagegraph(const char *edgefile) {
g
    fstream f;
10
    size_t help;
11
    vector < size_t > edges1, edges2;
12
    Graph *graphelp;
    _nome=edgefile; _nome.pop_back(); _nome.pop_back(); _nome.pop_back();
        _nome.pop_back();
14
    f.open(edgefile,ios::in);
15
    f>>help;
    f>>help;
16
17
     while(!f.eof()){
18
      if (help!=0) {
19
        edges1.push_back(help);
20
        f>>help;
21
        edges2.push_back(help);
22
        f>>help;
23
24
       else {
25
        graphelp = new Graph();
26
        if(edges1.size()==0 || edges2.size()==0) {
27
          f>>help;
28
          continue;
29
30
        graphelp->set(edges1,edges2);
31
        _grafi.push_back(graphelp);
32
        edges1.clear();
33
        edges2.clear();
34
        f>>help;
```

```
35
      }
    }
36
37
         f.close();
38
    if(\texttt{edges1.size()!=0} \ \&\& \ \texttt{edges2.size()!=0}) \ \{
39
      graphelp = new Graph();
40
      graphelp->set(edges1,edges2);
      _grafi.push_back(graphelp);
41
42
43
    edges1.clear();
44
    edges2.clear();
    _Ngrafi=_grafi.size();
45
46
   }:
47
48
   Asseanamento
49
50
   Packagegraph &Packagegraph::operator=(Packagegraph &obj){
51
    _Ngrafi=obj._Ngrafi;
52
    Graph* help;
53
    for(size_t i=0; i<_Ngrafi; i++) {</pre>
     help=new Graph();
54
55
      *help=*(obj._grafi[i]);
56
      _grafi.push_back(help);
57
58
    return *this;
59
   }:
60
61
62
   Packagegraph::~Packagegraph(){
63
    for(size_t i=0;i<_Ngrafi; i++){</pre>
64
65
      delete _grafi[i];
66
    _grafi.clear();
67
  };
68
69
70
   Settings
71
   -----*/
   /*-----*/
72
73
   void Packagegraph::add(Graph *g) {
74
    _grafi.push_back(g);
75
    _Ngrafi=_grafi.size();
  };
76
   /*----*/
77
78
   void Packagegraph::clear() {
79
    for(size_t i=0;i<_Ngrafi; i++){</pre>
80
     delete _grafi[i];
81
82
    _grafi.clear();
    _Ngrafi=0;
83
    _nome="";
84
85
  };
  /*--
86
87
            -----*/
88
89
   string Packagegraph::name() {
90
   return _nome;
91
   /*-----*/
92
93
   size_t Packagegraph::N() {
94
   return _Ngrafi;
  ||};
95
```

```
size_t Packagegraph::Nnodes(size_t i) {
98
    return _grafi[i]->Nnodes();
99
      100
101
   size_t Packagegraph::depth(size_t i) {
   return _grafi[i]->depth();
102
   };
103
   /*----*/
104
105
   size_t Packagegraph::outdeg(size_t grafo,size_t nodo){
106
    return _grafi[grafo]->outdeg(nodo);
107
108
109
   size_t Packagegraph::indeg(size_t grafo,size_t nodo){
   return _grafi[grafo]->indeg(nodo);
110
   }:
111
   /*-----
112
113
   Set
114
   -----*/
115
   void Packagegraph::set_name(string name) {
   _nome=name;
116
117
   ጉ:
118
119
   Quantities
120
   -----*/
121
   size_t Packagegraph::max_depth() {
122
    size_t max = depth(0);
123
    for(size_t i=0; i<_Ngrafi; i++)</pre>
124
     max = _max(depth(i),max);
125
    return max;
   };
126
   /*----*/
127
128
   size_t Packagegraph::Nnodes(size_t i, size_t level) {
   return _grafi[i]->Nnodes(level);
129
130
   };
131
   size_t Packagegraph::RNnodes(size_t i, size_t level) {
132
133
   return _grafi[i]->RNnodes(level);
134
   135
136
   size_t Packagegraph::Nleaves(size_t grafo) {
137
    return _grafi[grafo]->Nleaves();
138
   };
   /*-----
139
140
   Order parameters
141
142
   double Packagegraph::cost(size_t grafo, double lambda) {
143
    return _grafi[grafo]->cost(lambda);
144
   };
   /*----*/
145
146
   double Packagegraph::recursive_cost(size_t grafo, double lambda) {
147
    return _grafi[grafo]->recursive_cost(lambda);
148
   /*----*/
149
   size_t Packagegraph::diamanti() {
150
    size_t help=0;
151
152
    for(size_t i=0;i<_Ngrafi; i++){</pre>
     help+=_grafi[i]->diamonds();
153
154
155
    return help;
156
   };
   /*-----*/
157
158 | size_t Packagegraph::diamanti(size_t i) {
```

```
159
    return _grafi[i]->diamonds();
160 | };
161
   /*-
162
    Means
163
    -----*/
164
   double Packagegraph::mean_Nnodes(){
165
     double sum = 0;
166
    for(size_t i=0; i<_Ngrafi; i++)</pre>
167
     sum+=_grafi[i]->Nnodes();
168
    return sum/_Ngrafi;
169
  };
170
   /*-----*/
171
   double Packagegraph::mean_depth(){
172
     double sum=0;
173
     for(size_t i=0; i<_Ngrafi; i++)</pre>
174
      sum+=_grafi[i]->depth();
175
    return sum/_Ngrafi;
176
   };
177
    /*-
178
   double Packagegraph::mean_outdeg(size_t grafo){
179
     return _grafi[grafo] -> mean_outdeg();
180
   };
       -----*/
181
   /*-
182 double Packagegraph::mean_meandepth(){
183
    double sum=0;
184
     for(size_t i=0; i<_Ngrafi; i++)</pre>
     sum+=_grafi[i]->mean_depth();
185
186
     return sum/_Ngrafi;
  || <sub>};</sub>
187
   /*----*/
188
189
   double Packagegraph::mean_depth(size_t i){
190
    return _grafi[i]->mean_depth();
191
   };
   /*----*/
192
193
   double Packagegraph::mean_leaves_depth(){
    double sum=0;
194
195
     for(size_t i=0; i<_Ngrafi; i++)</pre>
      sum+=_grafi[i]->mean_leaves_depth();
196
197
     return sum/_Ngrafi;
  };
198
199
200
   double Packagegraph::mean_leaves_depth(size_t i){
201
    return _grafi[i]->mean_leaves_depth();
202
203
   /*----
204
205
206
   vector<size_t> Packagegraph::leaves_depth(size_t i){
    return _grafi[i]->leaves_depth();
207
208
   }:
209
   /*----
210
   vector<size_t> Packagegraph::brothers(size_t graph){
211
     vector < size_t > out;
212
     for(size_t i=0;i<_grafi[graph]->depth();i++) {
213
      out.push_back(_grafi[graph]->brothers(i+1));
214
215
    return out;
  ∥};
216
   /*-----/
217
   vector<size_t> Packagegraph::Rbrothers(size_t graph){
218
219
     vector < size_t > out;
     for(size_t i=0;i<_grafi[graph]->depth();i++) {
```

```
221
       out.push_back(_grafi[graph]->Rbrothers(i+1));
222
223
      return out;
   };
224
225
    /*----*/
    vector < size_t > Packagegraph::leaves_depth(){
226
227
      vector < size_t > out;
228
      for(size_t i=0;i<_Ngrafi;i++) {</pre>
229
       vector < size_t > temp = leaves_depth(i);
230
        for(size_t j=0; j<temp.size(); j++)</pre>
         out.push_back(temp[j]);
231
232
      }
233
      return out;
234 | };
235
236
    vector<size_t> Packagegraph::nodes_depth(size_t i){
237
     return _grafi[i]->nodes_depth();
238
    };
239
    vector<size_t> Packagegraph::nodes_depth(){
240
      vector < size_t > out;
241
242
      for(size_t i=0;i<_Ngrafi;i++) {</pre>
243
       vector < size_t > temp = nodes_depth(i);
244
        for(size_t j=0; j<temp.size(); j++)</pre>
245
         out.push_back(temp[j]);
246
      }
247
      return out;
248
    };
249
250
    vector<size_t> Packagegraph::leaves_indegrees(size_t i){
251
     return _grafi[i]->leaves_indegrees();
252
        253
254
    vector < size_t > Packagegraph::leaves_indegrees(){
255
      vector<size_t> out;
256
      for(size_t i=0;i<_Ngrafi;i++) {</pre>
257
        vector < size_t > temp = leaves_indegrees(i);
258
        for(size_t j=0; j<temp.size(); j++)</pre>
259
         out.push_back(temp[j]);
260
      }
261
      return out:
   };
262
263
264
    vector<size_t> Packagegraph::roots_outdegrees(size_t i){
265
     return _grafi[i]->roots_outdegrees();
266
267
    /*----*/
268
    vector<size_t> Packagegraph::roots_outdegrees(){
269
     vector < size_t > out;
270
      for(size_t i=0;i<_Ngrafi;i++) {</pre>
271
        vector < size_t > temp = roots_outdegrees(i);
272
       for(size_t j=0; j<temp.size(); j++)</pre>
273
         out.push_back(temp[j]);
274
275
      return out;
276
    };
277
278
    vector < size_t > Packagegraph::indegrees(size_t i){
279
     return _grafi[i]->indegrees();
280
    };
    /*-----*/
281
282 | vector < size_t > Packagegraph::indegrees(){
```

```
283
      vector < size_t > out;
284
      for(size_t i=0;i<_Ngrafi;i++) {</pre>
285
        vector < size_t > temp = indegrees(i);
286
        for(size_t j=0; j<temp.size(); j++)
287
         out.push_back(temp[j]);
288
289
      return out;
290
    };
291
    vector<size_t> Packagegraph::outdegrees(size_t i){
292
     return _grafi[i]->outdegrees();
294
295
    vector <double > Packagegraph::mean_Routdegrees(size_t grafo){
296
297
     return _grafi[grafo]->mean_Routdegrees();
298
299
300
    vector < double > Packagegraph::mean_outdegrees(size_t grafo){
301
     return _grafi[grafo]->mean_outdegrees();
   };
302
303
       -----*/
304
    vector<size_t> Packagegraph::outdegrees(){
305
      vector < size_t > out;
306
      for(size_t i=0;i<_Ngrafi;i++) {</pre>
       vector < size_t > temp = outdegrees(i);
307
308
        for(size_t j=0; j<temp.size(); j++)</pre>
         out.push_back(temp[j]);
309
310
311
312 | };
         -----*/
```

A.1.4 class Treemaker

This class builds trees and graphs through Sharing Tree model, Pang-Maslov model and Branching Tree model.

treemaker.hpp

```
#ifndef _TREEMAKER_HPP_
   #define _TREEMAKER_HPP_
3
  #include <string>
   #include <vector>
5
   \|#include <cmath>
   #include <map>
   #include <unordered_set>
   #include "graph.hpp"
  #include <gsl/gsl_randist.h>
#include <sys/time.h>
10
11
13
   using namespace std;
14
    class TreeMaker {
15
16
17
      public:
       //Costruttore/Distruttore
```

```
19
        TreeMaker():
20
        ~TreeMaker();
21
22
        //Funzioni a Steps
23
        Graph *YuleTree_Time(size_t Nsteps, double outdeg_mean);
24
        Graph *RussianTree_Time(size_t NrootsInit, size_t Nsteps, double
            indeg_mean);
25
        Graph *ReversedRussianTree_Time(size_t NleavesInit, size_t Nsteps,
            double outdeg_mean);
26
        void YuleTree_Time(size_t Nsteps, double outdeg_mean, vector<size_t>
27
            &from, vector<size_t> &to);
28
        void RussianTree_Time(size_t NrootsInit, size_t Nsteps, double
            indeg_mean, vector<size_t> &from, vector<size_t> &to);
29
        void ReversedRussianTree_Time(size_t NleavesInit, size_t Nsteps,
            double outdeg_mean, vector<size_t> &from, vector<size_t> &to);
30
31
        //Funzioni a Nnodes
32
        Graph *YuleTree_Nodes(size_t Nnodes, double outdeg_mean);
33
        Graph *RussianTree_Nodes(size_t NrootsInit, size_t Nnodes, double
            indeg_mean);
34
        Graph *ReversedRussianTree_Nodes(size_t NleavesInit, size_t Nnodes,
            double outdeg_mean);
35
        void YuleTree_Nodes(size_t Nodes, double outdeg_mean, vector<size_t>
36
            &from, vector<size_t> &to);
        void RussianTree_Nodes(size_t NrootsInit, size_t Nnodes, double
37
            indeg_mean, vector<size_t> &from, vector<size_t> &to);
38
        void ReversedRussianTree_Nodes(size_t NleavesInit, size_t Nnodes,
            double outdeg_mean, vector<size_t> &from, vector<size_t> &to);
39
40
        //MC
41
        Graph *MCTree(size_t NleavesInit, size_t Nsequence, size_t Nsymbols);
42
        void MCTree(size_t NleavesInit, size_t Nsequence, size_t Nsymbols,
            vector<size_t> &from, vector<size_t> &to);
43
44
45
      private:
46
        gsl_rng *r;
47
        vector < size_t > _from , _to;
48
       bool **_presenza;
49
       size_t _NleavesInit;
50
        size_t _Nnodes;
       size_t _Nsequence;
size_t _Nsymbols;
51
52
53
54
       void Simboloricorrente(vector<size_t> &supporto, vector<vector<size_t</pre>
            >> &splittati);
55
        void Ricorrente(vector<vector<size_t>> split1, size_t &esclude,
            size_t &esclude2, size_t nextnode, size_t &newnode, size_t &
            foglie);
        size_t RandomSymbol();
56
57
58
59
60
   };
61
62 | #endif
```

treemaker.cpp

```
1 | #include "treemaker.hpp"
2
3
4
            -----*/
5
6
   TreeMaker::TreeMaker() {
7
    r = gsl_rng_alloc(gsl_rng_default);
   struct timeval deltatime;
g
   gettimeofday(&deltatime, NULL);
10
    gsl_rng_set(r,deltatime.tv_usec);
11 | };
12 || /*-----
13
   Distruttore
   -----*/
14
15
   TreeMaker::~TreeMaker(){
16
   gsl_rng_free(r);
  \|_{};
17
  || /*-----
18
19
   Functions for Time
   -----*/
20
   void TreeMaker::RussianTree_Time(size_t NrootsInit, size_t Nsteps, double
21
      indeg_mean, vector<size_t> &from, vector<size_t> &to){
22
    from.clear();
23
    to.clear();
24
    size_t newnode=NrootsInit+1, rho, dad;
25
    for(size_t i=0; i<Nsteps;i++){</pre>
26
27
      rho = gsl_ran_poisson (r, indeg_mean);
28
      for(size_t j=0; j<rho; j++) {</pre>
29
       dad = floor(gsl_ran_flat (r, 1.0, newnode));
30
        from.push_back(dad);
31
        to.push_back(newnode);
32
33
      newnode++;
34
    }
  ||};
35
   /*----*/
36
   \mathbf{void} \  \, \mathsf{TreeMaker} :: \mathtt{ReversedRussianTree\_Time} \\ (\mathtt{size\_t} \  \, \mathsf{NleavesInit} \, , \, \, \mathtt{size\_t} \\
37
      Nsteps, double outdeg_mean, vector<size_t> &from, vector<size_t> &to)
      {
38
    from.clear();
39
    to.clear();
    size_t newnode=NleavesInit+1, rho, son;
40
41
42
    for(size_t i=0; i<Nsteps;i++){</pre>
43
      rho = gsl_ran_poisson (r, outdeg_mean);
44
      for(size_t j=0; j<rho; j++) {</pre>
45
        son = floor(gsl_ran_flat (r, 1.0, newnode));
46
        from.push_back(newnode);
47
        to.push_back(son);
48
49
      newnode++;
50
   };
51
       -----*/
52
   void TreeMaker::YuleTree_Time(size_t Nsteps, double outdeg_mean, vector
     size_t> &from, vector<size_t> &to){
54
    from.clear();
55
    to.clear();
```

```
56
               size_t selected = 1, generati = 1, rho=0, exrho=0;
  57
  58
               while(rho==0) rho = gsl_ran_poisson (r, outdeg_mean);
 59
  60
               for(size_t j=0; j<Nsteps;j++){</pre>
  61
                   if (rho!=0) exrho=rho;
  62
                    for(size_t i=0; i<rho; i++) {</pre>
  63
                        generati++;
  64
                        from.push_back(selected);
  65
                        to.push_back(generati);
  66
  67
                   rho = gsl_ran_poisson (r, outdeg_mean);
  68
                    if(selected == generati) {
                       selected -= exrho;
  69
  70
  71
  72
                   selected++;
  73
               }
  74
          };
  75
  76
          Graph *TreeMaker::YuleTree_Time(size_t Nsteps, double outdeg_mean) {
  77
               vector<size_t> from, to;
  78
               YuleTree_Time(Nsteps, outdeg_mean, from, to);
  79
               Graph *g=new Graph;
  80
               g->set(from, to);
  81
               from.clear();
  82
               to.clear();
  83
               return g;
          }
  84
          /*-----/
  85
 86
          Graph *TreeMaker::RussianTree_Time(size_t NrootsInit, size_t Nsteps,
                   double indeg_mean) {
  87
               vector<size_t> from, to;
  88
               RussianTree_Time(NrootsInit, Nsteps, indeg_mean, from, to);
  89
               Graph *g=new Graph;
 90
               g->set(from, to);
  91
               from.clear();
  92
               to.clear();
 93
               return g;
  94
         }
  95
 96
          \label{lem:graph} {\tt TreeMaker::ReversedRussianTree\_Time(size\_t\ NleavesInit,\ size\_t\ NleavesInit,\ size\_t\
                  Nsteps, double outdeg_mean) {
               vector < size_t > from, to;
 97
 98
               ReversedRussianTree_Time(NleavesInit, Nsteps, outdeg_mean, from, to);
 99
               Graph *g=new Graph;
100
               g->set(from, to);
101
               from.clear();
102
               to.clear();
103
               return g;
104
105
106
           Functions
107
          void TreeMaker::RussianTree_Nodes(size_t NrootsInit, size_t Nnodes,
108
                   double indeg_mean, vector<size_t> &from, vector<size_t> &to){
109
               from.clear();
110
               to.clear();
111
               std::set<size_t> linkati;
112
               size_t newnode=NrootsInit+1, rho, dad;
113
               while(linkati.size() <= Nnodes) {</pre>
```

```
115
        rho = gsl_ran_poisson (r, indeg_mean);
116
        for(size_t j=0; j<rho; j++) {</pre>
117
          dad = floor(gsl_ran_flat (r, 1.0, newnode));
118
          from.push_back(dad);
119
          linkati.insert(dad);
120
          to.push_back(newnode);
121
          linkati.insert(newnode);
122
          if (linkati.size() >= Nnodes) return;
123
124
        newnode++;
125
126
    };
127
128
    void TreeMaker::ReversedRussianTree_Nodes(size_t NleavesInit, size_t
        Nnodes, double outdeg_mean, vector<size_t> &from, vector<size_t> &to)
129
      from.clear():
130
      to.clear();
131
      std::set<size_t> linkati;
132
      size_t newnode=NleavesInit+1, rho, son;
133
134
      while(linkati.size() <= Nnodes) {</pre>
135
        rho = gsl_ran_poisson (r, outdeg_mean);
136
        for(size_t j=0; j<rho; j++) {</pre>
137
          son = floor(gsl_ran_flat (r, 1.0, newnode));
138
          from.push_back(newnode);
139
          linkati.insert(newnode);
140
          to.push_back(son);
141
          linkati.insert(son);
          if (linkati.size() >= Nnodes) return;
142
143
        }
144
        newnode++;
145
      }
146
   };
147
    void TreeMaker::YuleTree_Nodes(size_t Nnodes, double outdeg_mean, vector<</pre>
148
        size_t> &from, vector<size_t> &to){
149
      from.clear();
150
      to.clear();
151
      size_t selected = 1, generati = 1, rho=0, exrho=0;
152
153
      while(rho==0) rho = gsl_ran_poisson (r, outdeg_mean);
154
      while(generati != Nnodes) {
155
156
        if (rho!=0) exrho=rho;
157
        for(size_t i=0; i<rho; i++) {</pre>
158
          generati++;
159
          from.push_back(selected);
160
          to.push_back(generati);
161
          if (generati == Nnodes) break;
162
163
        rho = gsl_ran_poisson (r, outdeg_mean);
         if(selected == generati) {
164
165
          selected -= exrho;
166
167
        selected++;
168
   ||};
169
        -----*/
170
171
    Graph *TreeMaker::YuleTree_Nodes(size_t Nnodes, double outdeg_mean) {
172
      vector < size_t > from, to;
      YuleTree_Nodes(Nnodes, outdeg_mean, from, to);
```

```
174
      Graph *g=new Graph;
175
      g->set(from, to);
176
       from.clear();
177
      to.clear():
178
      return g;
179
    }
    /*-----/
180
181
    Graph *TreeMaker::RussianTree_Nodes(size_t NrootsInit, size_t Nnodes,
        double indeg_mean) {
182
       vector < size_t > from , to;
      RussianTree_Nodes(NrootsInit, Nnodes, indeg_mean, from, to);
183
184
      Graph *g=new Graph;
185
      g->set(from, to);
186
      from.clear();
187
      to.clear();
188
      return g;
189
    }
190
    /*----*/
191
    Graph *TreeMaker::ReversedRussianTree_Nodes(size_t NleavesInit, size_t
        Nnodes, double outdeg_mean) {
192
       vector < size_t > from , to;
193
      ReversedRussianTree_Nodes(NleavesInit, Nnodes, outdeg_mean, from, to);
194
      Graph *g=new Graph;
195
      g->set(from, to);
196
      from.clear();
197
       to.clear();
198
      return g;
199
    }
200
    void TreeMaker::MCTree(size_t NleavesInit, size_t Nsequence, size_t
201
        \label{lem:nsymbols} \verb|Nsymbols|, vector < size_t > &from , vector < size_t > &to) | \{ |
202
      from.clear();
203
      to.clear():
204
      _from.clear();
205
      _to.clear();
206
207
      _NleavesInit=NleavesInit;
208
       _Nsequence=Nsequence;
209
       _Nsymbols=Nsymbols;
210
211
      unordered_set < size_t > nodi[_NleavesInit];
212
      vector < size_t > supporto;
213
      vector < vector < size_t >> split1;
214
215
       for(size_t i=0;i<_NleavesInit;i++) supporto.push_back(i);</pre>
216
217
      for(size_t i=0; i<_NleavesInit; i++){</pre>
218
          for(size\_t j=0; j<(gsl\_ran\_flat(r, 1.0, Nsequence+1)); j++){}
219
         for(size_t j=0; j<_Nsequence; j++){</pre>
220
    riprovaci:
221
          nodi[i].insert(RandomSymbol());
222
           if(nodi[i].size()!=j+1) goto riprovaci;
        }
223
224
225
      // matrice dei simboli //
226
       _presenza=new bool*[_NleavesInit];
227
       for(size_t i=0; i<_NleavesInit; i++) _presenza[i]=new bool[_Nsymbols];</pre>
228
229
       for(size_t i=0; i<_NleavesInit; i++){</pre>
230
         for(size_t j=0; j<Nsymbols; j++){</pre>
          if(nodi[i].find(j+1)!=nodi[i].end()){
231
            _presenza[i][j]=1;
```

```
233
234
          else _presenza[i][j]=0;
235
236
      }
237
238
      size_t mas=0;
239
      size_t cont=0;
240
      size_t sim=0;
241
      for(size_t j=0; j<_Nsymbols; j++){</pre>
        for(size_t i=0; i<supporto.size(); i++){</pre>
242
         if(_presenza[supporto[i]][j]) cont++;
243
244
245
        if(mas < cont) {
246
          mas=cont;
247
          sim=j;
248
        }
249
        cont=0;
250
      }
251
252
      vector < size_t > add;
253
      split1.push_back(add);
254
      for(size_t k=0; k<supporto.size(); k++){</pre>
255
        if(\_presenza[supporto[k]][sim])\{\\
256
          split1[0].push_back(supporto[k]);
257
258
      }
259
      _Nnodes=split1[0].size();
260
261
      size_t esclude=0, esclude2=0, nextnode=1, newnode=1;
      size_t foglie=0;
262
263
264
      Ricorrente(split1, esclude, esclude2, nextnode, newnode, foglie);
265
266
      from=_from;
267
      to=_to;
      _from.clear();
268
269
      _to.clear();
270
271
      for(size_t j=0; j<_NleavesInit; j++) delete _presenza[j];</pre>
272
      delete[] _presenza;
   };
273
274
    /*-
275
    Graph *TreeMaker::MCTree(size_t NleavesInit, size_t Nsequence, size_t
        Nsymbols){
276
      vector < size_t > from, to;
      MCTree(NleavesInit, Nsequence, Nsymbols, from, to);
277
278
      Graph *g=new Graph;
279
      g->set(from, to);
280
      from.clear();
281
      to.clear();
282
      return g;
283
284
    /*----*/
285
    size_t TreeMaker::RandomSymbol(){
     return floor(gsl_ran_flat (r, 1.0, _Nsymbols+1));
286
287
    // return floor(gsl_ran_gaussian (r, 100))+(_Nsymbols/2.);
288
    };
       -----*/
289
290
    void TreeMaker::Simboloricorrente(vector<size_t> &supporto, vector<vector</pre>
       <size_t>> &splittati){
291
      vector<size_t> ecco, esclusi;
      bool chk;
```

```
293
       size_t ciclo=0, max_sum, massimo, contatore;
294
       do {
295
         massimo=0;
296
         contatore=0:
297
         for(size_t j=0; j<_Nsymbols; j++){</pre>
298
           chk=0;
299
           for(size_t h=0; h<ecco.size(); h++){</pre>
300
              if(j==ecco[h]) {
301
                chk=1;
302
                break;
303
             }
304
           }
305
           if (chk) continue;
           for(size_t i=0; i<supporto.size(); i++){</pre>
306
307
             if(_presenza[supporto[i]][j]) contatore++;
308
309
           if(massimo<contatore) {</pre>
310
             massimo=contatore;
311
             max_sum=j;
312
313
           contatore=0;
314
315
         if(massimo==0) {
316
           vector < size_t > add;
317
           if(ciclo>0){
318
              splittati.push_back(add);
319
              for(size_t k=0; k<supporto.size(); k++){</pre>
320
                splittati[ciclo].push_back(supporto[k]);
321
             }
322
323
           if(ciclo==0){
324
              for(size_t k=0; k<supporto.size(); k++){</pre>
325
                splittati.push_back(add);
326
                splittati[ciclo].push_back(supporto[k]);
327
328
329
           7
330
           break;
331
332
         vector < size_t > add;
333
         splittati.push_back(add);
334
         for(size_t k=0; k<supporto.size(); k++){</pre>
335
           if(_presenza[supporto[k]][max_sum]){
336
              splittati[ciclo].push_back(supporto[k]);
337
              _presenza[supporto[k]][max_sum]=0;
338
339
           else{
340
              esclusi.push_back(supporto[k]);
341
342
         }
343
         supporto=esclusi;
344
         esclusi.clear();
345
         ciclo++;
346
         if(supporto.size() == 0) break;
347
       } while(1);
348
     };
349
     void TreeMaker::Ricorrente(vector<vector<size_t>> split1, size_t &esclude
350
         , size_t &esclude2, size_t nextnode, size_t &newnode, size_t &foglie)
351
       vector < vector < size_t >> split2;
      vector<vector<size_t>> split3;
```

```
353
       for(size_t i=0;i<split1.size();i++){</pre>
354
          if(split1[i].size()==1) {
355
            nextnode++;
356
            foglie++;
357
            if(foglie==_Nnodes) return;
358
          if(\texttt{split1[i].size()>1})\{\\
359
360
            split2.clear();
361
            Simboloricorrente(split1[i], split2);
362
            \quad \textbf{for} (\texttt{size\_t r=0}; \texttt{r<split2.size()}; \texttt{r++}) \{
363
              newnode++;
364
               _from.push_back(nextnode);
              _to.push_back(newnode);
365
366
367
            nextnode++;
368
369
          for(size_t j=0;j<split2.size();j++) {</pre>
370
            if(split2[j].size()>1) \quad split3.push\_back(split2[j]);\\
371
372
              esclude2++:
373
              foglie++;
374
              if(foglie==_Nnodes) return;
375
376
          }
377
       }
378
       nextnode+=esclude;
379
       esclude=esclude2;
380
       esclude2=0:
       if(split2.size()!=0) Ricorrente(split3, esclude, esclude2, nextnode,
381
           newnode, foglie);
382
       else return;
    };
383
384
```

A.2 Programs for simulations and analysis

A.2.1 mrmodel.cpp

This program use the library to simulate and analyze Sharing Trees.

```
MRmodel nome nnodi kappa esse
3
  #include <iostream>
5
6
  #include <fstream>
   #include <cstdlib>
8
9
   #include "libreria.hpp"
10
   using namespace std;
11
   int main(int argc, char **argv) {
13
14
     size_t N_STEPS = 1;
     size_t NALBERI = 10;
15
16
17
     string language=argv[1];
     size_t nnodi=atoi(argv[2]);
```

```
19
      size_t kappa=atoi(argv[3]);
20
      size_t esse=atoi(argv[4]);
21
22
23
      TreeMaker alberelli;
24
      Packagegraph *scatola;
25
      scatola=new Packagegraph;
26
27
      string path="../STmodel/";
28
29
      Distribuzioni distr(path,language);
30
      Scatterplot scat(path,language);
31
32
      cerr << "ST simulation..." << endl;</pre>
33
      for(size_t n=1; n<=N_STEPS; n++) {</pre>
34
        cerr << n << " \ t ";
35
        for(size_t i=0; i<NALBERI; i++) {</pre>
36
          scatola->add(alberelli.MCTree(nnodi, kappa, esse));
37
38
        distr.outdegrees(scatola);
39
        distr.Nnodes(scatola);
40
        distr.depth(scatola);
41
        distr.leaves(scatola);
42
        distr.leaves_position(scatola);
43
44
        scat.levels_outdegrees(scatola);
45
        scat.depth_Nnodes(scatola);
46
        scat.levels_outdegmean(scatola,4);
47
        scat.Rlevels_outdegmean(scatola,1,1);
        scat.levels_Nnodes(scatola,2);
48
49
50
        scatola->clear();
51
52
      cerr << end1;
53
      distr.clear();
54
      scat.clear();
55
56
      delete scatola;
57
58
      return 0;
59 | }
```

A.2.2 tarantola.cpp

A program to obtain the whole data analysis through the library.

```
13
    int main(int argc, char **argv) {
14
15
      string path="../outputC/";
16
17
      string language=argv[1];
18
19
      Packagegraph *pac;
20
      Distribuzioni distr(path, language);
21
      Scatterplot scat(path,language);
22
      Lineplot line(path, language);
23
24
      for(int i=2; i<argc; i++) {</pre>
25
        cout << argv[i] << "\n";
        pac = new Packagegraph(argv[i]);
26
27
28
        distr.indegrees(pac);
        distr.roots_outdeg(pac);
29
30
        distr.leaves_indeg(pac);
31
        distr. Nnodes (pac);
32
        distr.depth(pac);
33
        distr.leaves_position(pac);
34
        distr.outdegrees(pac, 5, 1000);
35
36
        scat.levels_indegrees(pac);
37
        scat.levels_outdegrees(pac);
38
        scat.levels_Nnodes(pac,3);
39
        scat.levels_outdegmean(pac,4);
40
        scat.Rlevels_Nnodes(pac,3);
41
        scat.Rlevels_outdegmean(pac,3, 500);
42
        scat.LeavesIndegrees_LeavesLevels(pac);
43
        scat.depth_Nnodes(pac);
44
        scat.Vnodes_Nnodes(pac);
45
        scat.leaves_Nnodes(pac,1);
46
        scat.depth_Nnodes(pac);
47
        scat.depth_Nnodes_outdeg(pac, 5, 2);
48
        scat.meanoutdeg_Nnodes_depth(pac);
49
50
        line.outdegree(pac,5,1000);
51
        delete pac;
52
53
54
      return 0;
```

A.3 Programs for data conversion

Programs in this section are written in gvpr [GN00].

A.3.1 Papera.gv

A program to paste together the subgraphs produced by doxygen.

```
1 | #!/bin/bash
2 | BEGIN {
3 | graph_t out = graph("", "D");
```

```
4 || }
5
   N {
6
      edge_t e = fstin($);
      node(out, $.label);
7
8
      while(e) {
9
        node_t h = e.head;
10
        node_t t = e.tail;
11
12
        node_t oh = node(out, h.label);
13
        node_t ot = node(out, t.label);
14
15
        if (isEdge\_sg(out,ot,oh,0) != NULL) \ \{\\
16
          edge_t found = isEdge_sg(out,ot,oh,0);
          if(found.style != e.style)
17
18
            printf("ERRORE:: due stili diversi per lo stesso edge!\n");
19
20
21
        edge_t oe = edge_sg(out,ot,oh,0);
22
        oe.style = e.style;
        oe.color = e.color;
23
24
        e = nxtin(e);
25
26
     }
27
   }
28
   END {
29
            write(out);
30 || }
```

A.3.2 Bilimetta.gv

A program to erase templates from graphs.

```
1 |
   BEG_G {
2
      $tvtype = TV_en;
3
      graph_t out = clone(NULL, $G);
4
5
   E {
      if(\$.color=="orange") {
6
7
        edge_t linkOUT = fstout($.head);
8
        while(linkOUT) {
9
           if(isNode(out, linkOUT.tail.name) != NULL) {
             if(isNode(out, linkOUT.head.name) != NULL) {
10
               if (is Edge\_sg(out,\ is Node(out,\ link OUT.tail.name),\ is Node(out,
11
                   linkOUT.head.name), 0) != NULL) {
                 delete(out,isEdge_sg(out, isNode(out, linkOUT.tail.name),
12
                 isNode(out, linkOUT.head.name), 0));
if(isNode(out, linkOUT.head.name) != NULL) {
13
                    if(isNode(out, \$.tail.name) != NULL) {
14
15
                      edge_sg(out, isNode(out, $.tail.name), isNode(out,
                          linkOUT.head.name), 0);
16
17
18
               }
            }
19
20
21
          linkOUT = nxtout(linkOUT);
22
23
        edge_t linkIN = fstin($.head);
```

```
24
                                  while(linkIN) {
                                           if (\verb|isNode| (\verb|out,linkIN.tail.name)| != \verb|NULL && isNode| (\verb|out,linkIN.head|.
25
                                                           name) != NULL) {
 26
                                                    if (is \texttt{Edge\_sg} (\texttt{out, isNode} (\texttt{out, linkIN.tail.name}), \ is \texttt{Node} (\texttt{out, linkIN})
                                                                     .head.name), 0) != NULL){
                                                            {\tt delete(out,isEdge\_sg(out,isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,linkIN.tail.name),isNode(out,link
 27
                                                                             out,linkIN.head.name), 0));
 28
                                                            if($.tail!=linkIN.tail) {
 29
                                                                     if(isNode(out, linkIN.tail.name) != NULL) {
                                                                             if (\verb|isNode| (out, \$.tail.name) != \verb|NULL|) \{
30
31
                                                                                      edge_sg(out,isNode(out, linkIN.tail.name),isNode(out, $.
                                                                                                       tail.name),0);
 32
33
                                                           }
34
35
                                                  }
36
                                         }
37
                                           linkIN = nxtin(linkIN);
 38
                                  if (isNode(out, \$.head.name) != NULL) \{\\
39
 40
                                           delete(out, isNode(out, $.head.name));
41
42
                         }
43
                }
44
             END {
45
                         write(out);
46 | }
```

A.3.3 Numerello.gv

A program to convert .dot files in adjacency lists.

```
BEG_G {
      printf("0\n");
2
3
      $tvtype = TV_ne;
4
      int i = 1;
    }
5
6
7
    N {
8
      node_t n = $;
9
      n.mionome = i;
10
      i++:
    }
11
12
    E {
13
14
      edge_t e = $;
      node_t h = e.head;
15
16
      node_t t = e.tail;
17
      printf("%s %s\n", t.mionome, h.mionome);
18 || }
```

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