

## Algebra\_Assignment 02

**Q5:**

Use the elementary operations, find the row- echelon matrix

$$\text{a/ } A = \begin{pmatrix} 1 & 2 \\ -1 & 1 \\ 2 & 3 \end{pmatrix}; \quad \text{b/ } B = \begin{pmatrix} 1 & 2 & 1 \\ -1 & 1 & 3 \\ 2 & 7 & 6 \end{pmatrix} \quad \text{c/ } C = \begin{pmatrix} 3 & -5 & 4 \\ 2 & -1 & 3 \\ 1 & 2 & 5 \end{pmatrix}$$

$$\text{d/ } D = \begin{pmatrix} 1 & 2 & -1 & 0 \\ -1 & 2 & 4 & 2 \\ 3 & 6 & -3 & 0 \end{pmatrix} \quad \text{e/ } E = \begin{pmatrix} 1 & 1 & -1 & 0 \\ 3 & 4 & 2 & 1 \\ -2 & 0 & -1 & -3 \end{pmatrix}$$

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**Q6:**

Use the elementary operations, find the row- echelon matrix

$$a/ A = \begin{pmatrix} 6 & 0 & 4 \\ 2 & 6 & 8 \\ -3 & 4 & 1 \end{pmatrix}$$

$$b/ B = \begin{pmatrix} 1 & 1 & 2 & 3 \\ 2 & 5 & 7 & 2 \\ 1 & 8 & 3 & 1 \end{pmatrix}$$

$$c/ C = \begin{pmatrix} 1 & 1 & 1 & 3 \\ 2 & 5 & 7 & 2 \\ 1 & 2 & 3 & 1 \end{pmatrix}$$

$$d/ D = \begin{pmatrix} 1 & 1 & 1 & 3 \\ 2 & 5 & 7 & 0 \\ 1 & 2 & 3 & 1 \end{pmatrix}$$

$$e/ E = \begin{pmatrix} -2 & 1 & 3 & 4 \\ 1 & -3 & 2 & -3 \\ -1 & -2 & 5 & 1 \end{pmatrix}$$

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**Q7:**

Given  $A^{-1} = \begin{pmatrix} 1 & -1 & 3 \\ 2 & 0 & 5 \\ -1 & 1 & 0 \end{pmatrix}$ . Find a matrix  $X$  such that

$$\text{a/ } AX = \begin{pmatrix} 1 \\ -1 \\ 3 \end{pmatrix} \quad \text{b/ } AX = \begin{pmatrix} 1 & -1 & 2 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \end{pmatrix} \quad \text{c/ } XA = \begin{pmatrix} 1 & 2 & -1 \\ 3 & 1 & 1 \end{pmatrix}$$

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**Q8:**

Find  $A$  when

$$a/ (3A)^{-1} = \begin{pmatrix} 1 & 2 \\ 0 & -2 \end{pmatrix} \quad b/ (I + 2A)^{-1} = \begin{pmatrix} 2 & 1 \\ 3 & 2 \end{pmatrix}$$

$$c/ (A^{-1} - 2I)^T = -2 \begin{pmatrix} 1 & 4 \\ 3 & 1 \end{pmatrix}$$

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**Q9:**

Solve for X

$$a/ \begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix} X = \begin{pmatrix} 1 & -1 \\ 3 & 3 \end{pmatrix}$$

$$b/ ABXC = B^T$$

$$c/ AX^TC = B$$

(where  $A, B$  and  $C$  are  $n \times n$  invertible matrices)

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### Q10:

Find  $A^{-1}$  if

a/  $A^2 - 6A + 5I = 0$

b/  $A^2 + 3A - I = 0$

c/  $A^4 = I$