

Algebra_Assignment 02

Q5:

Use the elementary operations, find the row- echelon matrix

$$\text{a/ } A = \begin{pmatrix} 1 & 2 \\ -1 & 1 \\ 2 & 3 \end{pmatrix} ; \quad \text{b/ } B = \begin{pmatrix} 1 & 2 & 1 \\ -1 & 1 & 3 \\ 2 & 7 & 6 \end{pmatrix} \quad \text{c/ } C = \begin{pmatrix} 3 & -5 & 4 \\ 2 & -1 & 3 \\ 1 & 2 & 5 \end{pmatrix}$$

$$\text{d/ } D = \begin{pmatrix} 1 & 2 & -1 & 0 \\ -1 & 2 & 4 & 2 \\ 3 & 6 & -3 & 0 \end{pmatrix} \quad \text{e/ } E = \begin{pmatrix} 1 & 1 & -1 & 0 \\ 3 & 4 & 2 & 1 \\ -2 & 0 & -1 & -3 \end{pmatrix}$$

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Q6:

Use the elementary operations, find the row- echelon matrix

$$\text{a/ } A = \begin{pmatrix} 6 & 0 & 4 \\ 2 & 6 & 8 \\ -3 & 4 & 1 \end{pmatrix}$$

$$\text{b/ } B = \begin{pmatrix} 1 & 1 & 2 & 3 \\ 2 & 5 & 7 & 2 \\ 1 & 8 & 3 & 1 \end{pmatrix}$$

$$\text{c/ } C = \begin{pmatrix} 1 & 1 & 1 & 3 \\ 2 & 5 & 7 & 2 \\ 1 & 2 & 3 & 1 \end{pmatrix}$$

$$\text{d/ } D = \begin{pmatrix} 1 & 1 & 1 & 3 \\ 2 & 5 & 7 & 0 \\ 1 & 2 & 3 & 1 \end{pmatrix}$$

$$\text{e/ } E = \begin{pmatrix} -2 & 1 & 3 & 4 \\ 1 & -3 & 2 & -3 \\ -1 & -2 & 5 & 1 \end{pmatrix}$$

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Q7:

Given $A^{-1} = \begin{pmatrix} 1 & -1 & 3 \\ 2 & 0 & 5 \\ -1 & 1 & 0 \end{pmatrix}$. Find a matrix X such that

$$\text{a/ } AX = \begin{pmatrix} 1 \\ -1 \\ 3 \end{pmatrix} \quad \text{b/ } AX = \begin{pmatrix} 1 & -1 & 2 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \end{pmatrix} \quad \text{c/ } XA = \begin{pmatrix} 1 & 2 & -1 \\ 3 & 1 & 1 \end{pmatrix}$$

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Q8:

Find A when

$$\text{a/ } (3A)^{-1} = \begin{pmatrix} 1 & 2 \\ 0 & -2 \end{pmatrix} \quad \text{b/ } (I + 2A)^{-1} = \begin{pmatrix} 2 & 1 \\ 3 & 2 \end{pmatrix}$$

$$\text{c/ } (A^{-1} - 2I)^T = -2 \begin{pmatrix} 1 & 4 \\ 3 & 1 \end{pmatrix}$$

Q9:

Solve for X

$$a/ \begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix} X = \begin{pmatrix} 1 & -1 \\ 3 & 3 \end{pmatrix}$$

$$b/ ABXC = B^T$$

$$c/ AX^T C = B$$

(where A, B and C are $n \times n$ invertible matrices)

Q10:

Find A^{-1} if

a/ $A^2 - 6A + 5I = 0$

b/ $A^2 + 3A - I = 0$

c/ $A^4 = I$