

STAT 231

October 7, 2016

# Road map

- 5 min recap of model selection
  - PPDAC approach to STAT PROBLEMS (Ch 3).
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$\{y_1, \dots, y_n\} \rightarrow \text{SAMPLE}$



Model.

$$Y_i \sim f(y_i; \theta)$$



Test the model (Does the data agree?)

Yes

↓  
ESTIMATION

No: LOOK FOR ANOTHER MODEL

Graphical  $\rightarrow$  pdf (theoretical  
and empirical)

cdf ( " )

Q-Q plot.

Numerical: Compare observed  
frequencies to expected frequencies

## SUGGESTED MODEL

$$Y_L \sim \text{Poi}(\mu)$$

Data is arranged

# of hits, <sup>Obs</sup> Freq. ( $f_i$ ).

0	2
1	6
2	22
3	40
4	20
5	10
$\geq 6$	0

Total # of hits

$$\sum j f_j = 300 \text{ hits}$$

Av. # of ~~accidents~~

$$\hat{\mu} = 300/100 = 3$$

$Y_i$  = # of hits on a website  
in a 15 min interval.

For  $n$  days  $n = 100$ , we collect  
a sample

$\{y_1, \dots, y_{100}\}$

$y_i$  = # of <sup>hits</sup> ~~accidents~~ in day  $i$

Objective: To estimate the average  
number of hits

What is the MLE for  $\mu$ ?

(a) 20

(b) 3  $\longrightarrow$  2%

(c) 16.67

(d) 2.5

(e) ~~Cannot be determined.~~  
none of the above.

Expected frequency  
of  $r$  hits =  $\frac{e^{-\hat{\mu}} \hat{\mu}^r}{r!} \times n$

# PPDAC

Step by step algorithm to approach  
a statistical problem:

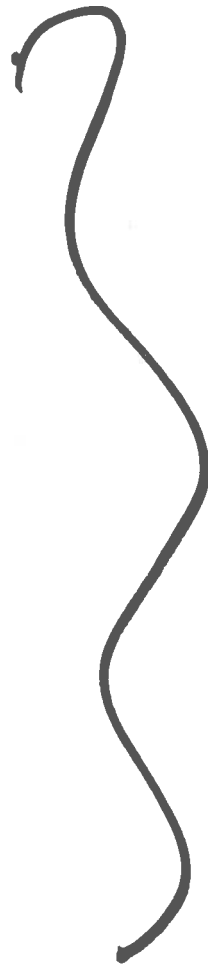
P  $\rightarrow$  Problem

P  $\rightarrow$  Plan

D  $\rightarrow$  Data

A:  $\rightarrow$  Analysis

C  $\rightarrow$  Conclusion





## Examples

- To figure out what Canadians think of cops (approval rating).
- A random sample from the phone book of K-W. and conduct interviews.

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Example 2: ~~A Flu~~ To figure out whether a new flu shot that came out is effecting in reducing Flu symptoms amongst Canadians.

## PROBLEM

- What is your target population?
- units → a member of the Target population
- variates
- attributes → characteristics of the unit

1<sup>st</sup> problem → Variate : Whether or not they approve of cops

Attribute → function of the variate

Randomly select people from the  
UW.

Control group  $\rightarrow$  placebo

Test "  $\rightarrow$  actual flu shot.

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Example 3: Suppose we want  
to find the relationship between  
Canadian  
~ parents smoking and smoking  
among children.

So A random sample is chosen from  
K-W and the test conducted.

## PLAN :

### Question:

- (a) What is the study population?
- (b) How is the data collected?

(SAMPLING PROTOCOL)

- (c) What are the possible studies?

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A study population is the population from which your sample is drawn.

In Example 1

Target pop  $\rightarrow$  set of all Canadian

Study pop  $\rightarrow$  people in K-W  
with a phone line

Study populations need not  
be a subset of the target population  
but in most cases they are.

Observational  
Cops, Smoking

Experimental  
Flu.

Estimation

Hypothesis Testing

Prediction :

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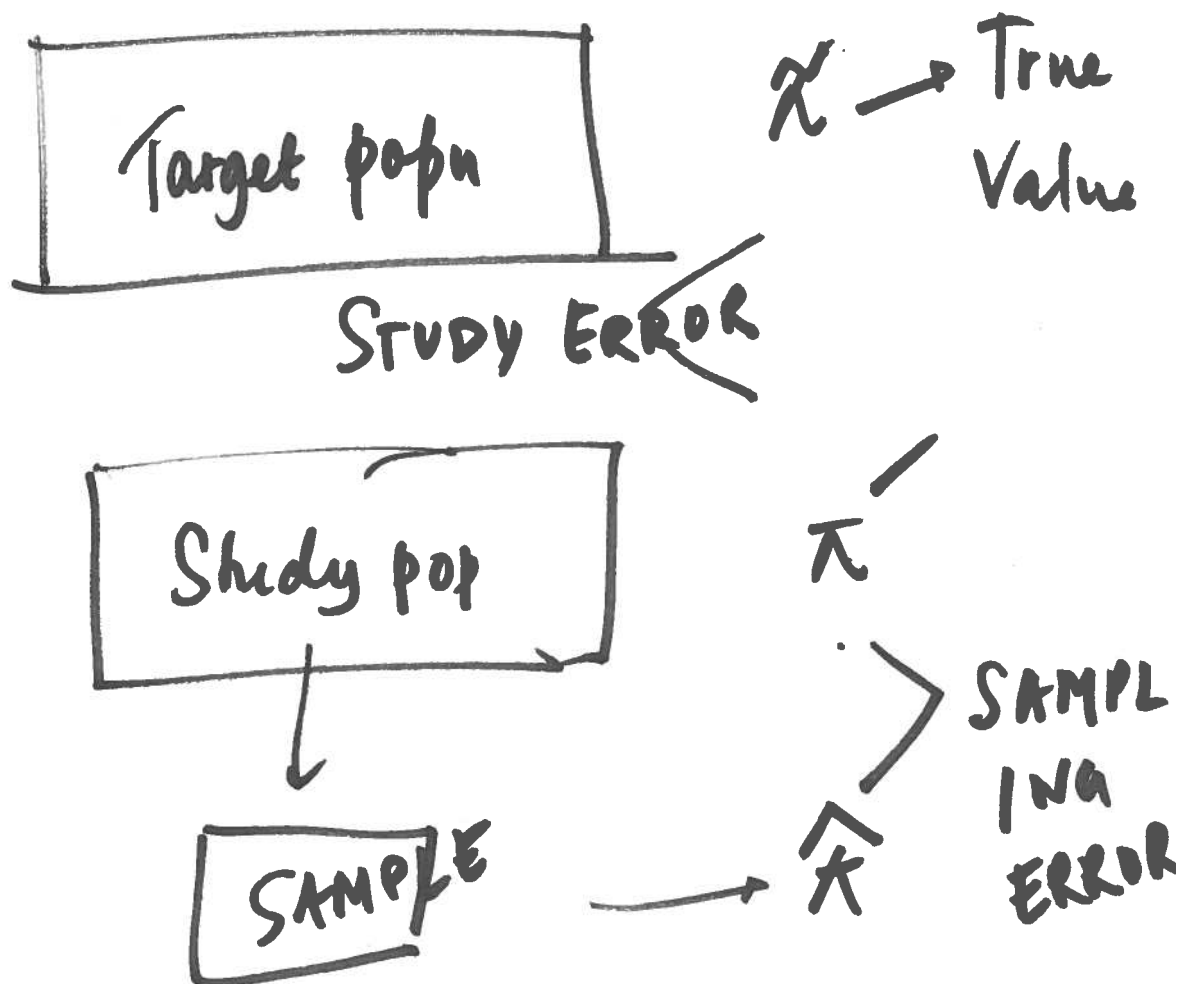
## Types of Errors

(i) STUDY ERROR

(ii) SAMPLING ERROR

(iii) MEASUREMENT ERROR.

We have to know what these errors mean, and what could be the source of it?



The difference in the value of the attribute between

Target and Study = STUDY ERROR

Study and Sample = SAMPLING  
ERROR

Measurement Errors are made when we tabulate data.