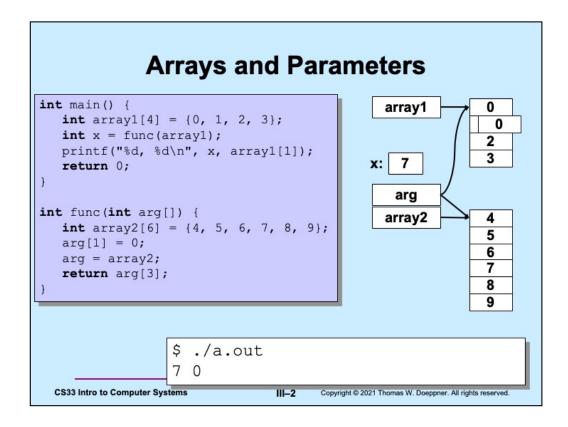


Some of the slides in this lecture are either from or adapted from slides provided by the authors of the textbook "Computer Systems: A Programmer's Perspective," 2<sup>nd</sup> Edition and are provided from the website of Carnegie-Mellon University, course 15-213, taught by Randy Bryant and David O'Hallaron in Fall 2010. These slides are indicated "Supplied by CMU" in the notes section of the slides.



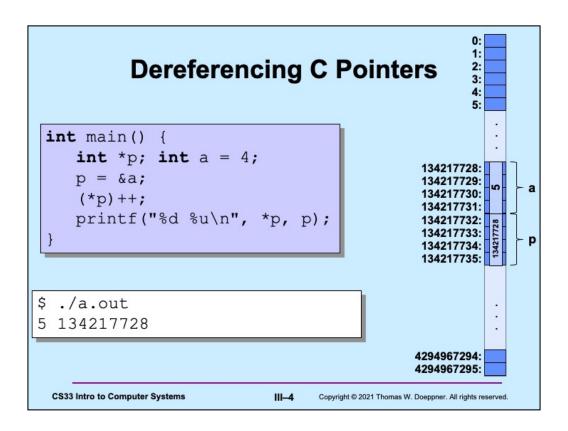
In this example, we've declared **array1** and **array2** in **main** and **func**. Both declarations allocate storage for arrays of **int**s. Both **array1** and **array2** refer (by pointing to the first elements) to the storage allocated for the arrays. These are literal (constant) values – they can't be changed.

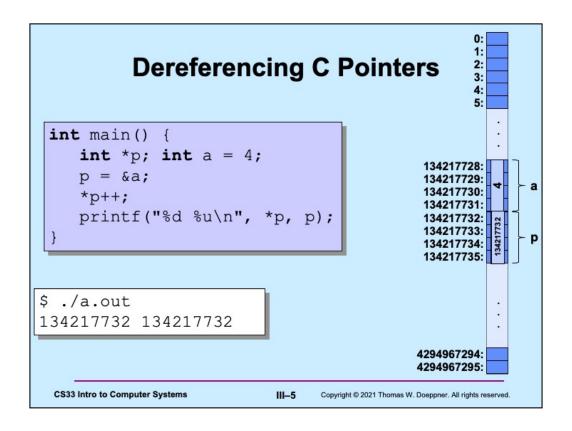
In the definition of **func**, **arg** is a parameter that acts as a variable that's initialized with whatever is passed to **func**. In the slide, **func** is called with **array1** as the argument. Thus, **arg** is initialized with **array1**, which means it's initialized with a pointer to the first element of the array referred to by **array1**. But this initial value of **arg** is not permanent -- we're free to change it, as we do when we assign **array2** to **arg**.

### **Arrays and Parameters**

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Operator precedence is hard to remember! ("++" takes precedence over "\*".)

# Dereferencing C Pointers int main() { int \*p; int a = 4; p = &a; ++\*p; printf("%d %u\n", \*p, p); } \$ ./a.out 5 134217728 Copyright © 2021 Thomas W. Doeppner. All rights reserved.

Here it's clear that the \* operator is applied before the ++ operator.

## Quiz 1

```
int func(int arg[]) {
    arg++;
    return arg[0];
}
int main() {
    int A[3]={10, 11, 12};
    printf("%d\n",
        func(A));
}
```

### What's printed?

- a) 10
- b) 11
- c) 12
- d) indeterminate

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# 

Note that '\0' is represented as a byte containing all zeroes.

A single character (such as '\0') is enclosed in single quotes and, of course, is just that character. A string of characters (such as "hello") ends with a null character and is enclosed with with double quotes).

# Strings int main() { printf("%s","Hello"); return 0; } \$ ./a.out Hello\$ CS33 Intro to Computer Systems III-9 Copyright © 2021 Thomas W. Doeppner. All rights reserved.

We use the %s format code to print a string.

Since we didn't explicitly output a newline character, the prompt for the next command goes on the same line as the string that was printed.

```
Strings

int main() {
   printf("%s\n","Hello");
   return 0;
}

$ ./a.out
Hello
$

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```

We've added the newline character to the format specifier of printf – the prompt now appears on the next line.

# void printString(char s[]) { int i; for(i=0; s[i]!='\0'; i++) printf("%c", s[i]); } int main() { printString("Hello"); printf("\n"); return 0; } Tells C that this function does not return a value CS33 Intro to Computer Systems III-11 Copyright © 2021 Thomas W. Doeppner. All rights reserved.

We can also print a single character at a time. Note the test for the null character to determine whether we've reached the end of the string.

### 1-D Arrays

· If T is a datatype (such as int), then

T n[6]

declares n to be an array of six T's

- the type of each element goes before the identifier
- the number of elements goes after the identifier
- · What is n's type?

T[6]

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Note that to declare something, say n, to be of type "T[6]", we must put the identifier between the element type and the size: T[6].

### 2-D Arrays

- Suppose T is a datatype (such as int)
- T n[6]
  - declares n to be an array of (six) T
  - the type of n is T[6]
- Thus T[6] is effectively a datatype
- Thus we can have an array of T[6]
- T m[7][6]
  - m is an array of (seven) T[6]
  - m[i] is of type T[6]
  - m[i][j] is of type T

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Note that even though we might think of "int [6]" as being a datatype, to declare "n" to be of that type, we must write "int n[6]" — the size of the array goes just after the identifier, the type of each array element goes just before the identifier.

	Example
T k:	
T m[6]:	
T n[7][6]:	
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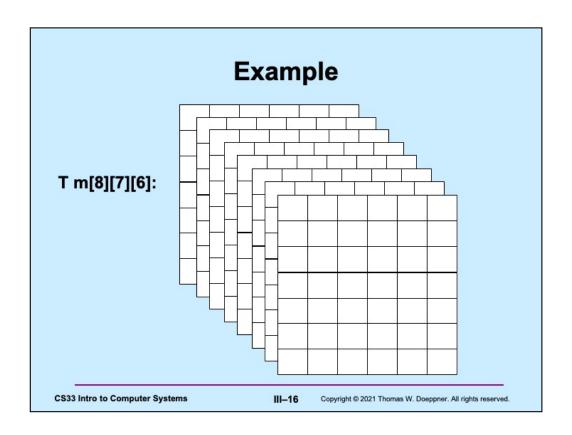
At the top we have k, which is of type T. Next, we have m, which is effectively of type T[6], but is an array of 6 T. Finally, we have n, which we may consider to be an array of seven T[6], or a 2-D array (7x6] of T. Each row of n is a 1-D array.

# 3-D Arrays

- How do we declare an array of eight T[7][6]?
  - T p[8][7][6]
  - p is an array of (eight) T[7][6]
  - p[i] is of type T[7][6]
  - p[i][j] is of type T[6]
  - p[i][j][k] is of type T

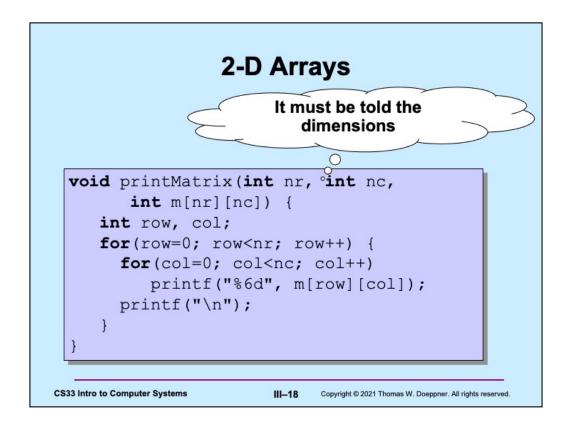
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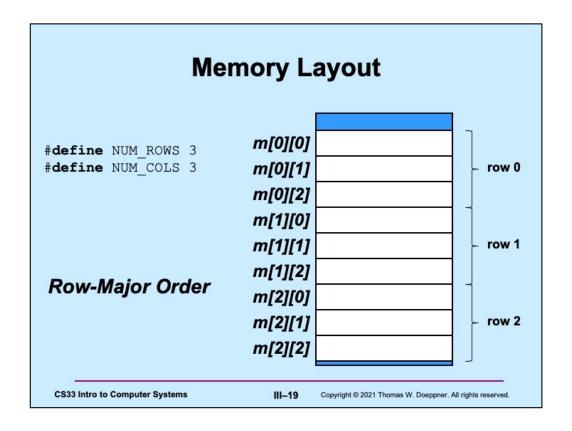
```
2-D Arrays
                            $ ./a.out
                                          1
                                  0
                                                 2
                                                         3
 #define NUM ROWS 3
                                                         7
                                  4
                                          5
                                                 6
 #define NUM COLS 4
                                                10
                                                        11
 int main() {
     int row, col;
     int m[NUM ROWS][NUM COLS];
     for(row=0; row<NUM ROWS; row++)</pre>
        for(col=0; col<NUM COLS; col++)</pre>
           m[row][col] = row*NUM COLS+col;
     printMatrix(NUM ROWS, NUM COLS, m);
     return 0;
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                           III-17
                                 Copyright © 2021 Thomas W. Doeppner. All rights reserved.
```

Here we initialize a 2D array, then call a function (described in the next slide) to print it.



We print the array by rows.

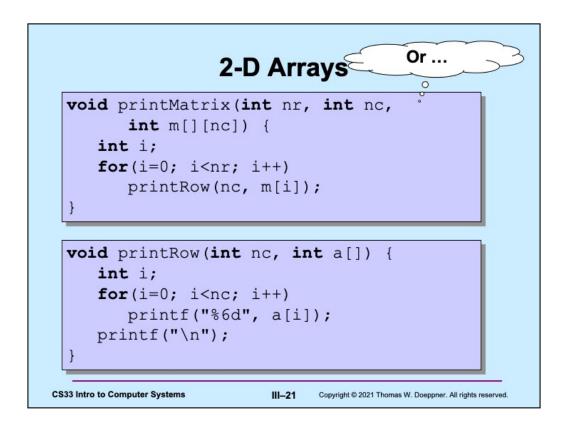
Note that the parameter  $\mathbf{m}$  is dimensioned by the previous parameters  $\mathbf{nr}$  and  $\mathbf{nc}$ . It's important that  $\mathbf{nr}$  and  $\mathbf{nc}$  appear in the parameter list before  $\mathbf{m}$ .



C arrays are stored in **row-major order**, as shown in the slide. The idea is that the left index references the row, the right index references the column. Thus, C arrays are stored row-by-row. Thus, to index into a 2D array, we need to know how large each row is (i.e., how many columns there are). But it's not necessary, for indexing purposes, to know how many rows there are.

# void printMatrix(int nr, int nc, int m[][nc]) { int row, col; for(row=0; row<nr; row++) { for(col=0; col<nc; col++) printf("%6d", m[row][col]); printf("\n"); }</pre> CS3 Intro to Computer Systems ### Copyright © 2021 Thomas W. Doeppner. All rights reserved.

As we mentioned for 1-D arrays, when an array is passed to a function, what is passed is a pointer to its first element. For a 1-D array, say an array of ints, that first element is an int. For a 2-D array, the first element is a 1-D array, since a 2-D array is an array of 1-D arrays. Thus, what's passed to printMatrix in the slide is a pointer to the first row of the matrix, which is a 1-D array of ints.



Note that m is an array of arrays (in particular, an array of 1-D arrays).

```
2D as 1D
       1
           2
                                             3
                                                     5
                                                              7
                                         2
               7
       5
           6
 int A2D[2][4];
                                int A1D[8];
int AccessAs1D(int A[], int Row, int Col, int RowSize) {
    return A[Row*RowSize + Col];
int main(void) {
    int A2D[2][4] = \{\{0, 1, 2, 3\}, \{4, 5, 6, 7\}\};
    int *A1D = &A2D[0][0];
    int x = AccessAs1D(A1D, 1, 2, 4);
                                               $ ./a.out
    printf("%d\n", x);
                                               6
                                               $
    return 0;
                               III-22
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                                     Copyright © 2021 Thomas W. Doeppner. All rights reserved.
```

While it's convenient to think of something as being a 2D array, its elements are stored linearly in memory. Thus, as shown in the slide where we are calling **AccessAs1D** to get the value of A2D[1][2], given a pointer to a 2D array, we can access its elements as if it were a 1D array.

### Quiz 2

### Consider the array

int A[3][3];

- which element is adjacent to A[2][2] in memory?
  - a) A[1][2]
  - b) A[2][1]
  - c) none of the above

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### Quiz 3

### Consider the array

```
int A[4][4];
int *B = &A[0][0];
B[8] = 8;
```

- which element of A was modified?
  - a) A[3][2]
  - b) A[2][4]
  - c) A[2][0]
  - d) none of the above

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## **Number Representation**

- · Hindu-Arabic numerals
  - developed by Hindus starting in 5th century
    - » positional notation
    - » symbol for 0
  - adopted and modified somewhat later by Arabs
    - » known by them as "Rakam Al-Hind" (Hindu numeral system)
  - 1999 rather than MCMXCIX
    - » (try doing long division with Roman numerals!)

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### Which Base?

```
1999
      - base 10
          » 9·100+9·101+9·102+1·103
      - base 2
          » 11111001111
               • 1·20+1·21+1·22+1·23+0·24+0·25+1·26+1·27+1·28+1·29+1·210
      - base 8
          » 3717
               · 7-80+1-81+7-82+3-83
          » why are we interested?

    base 16

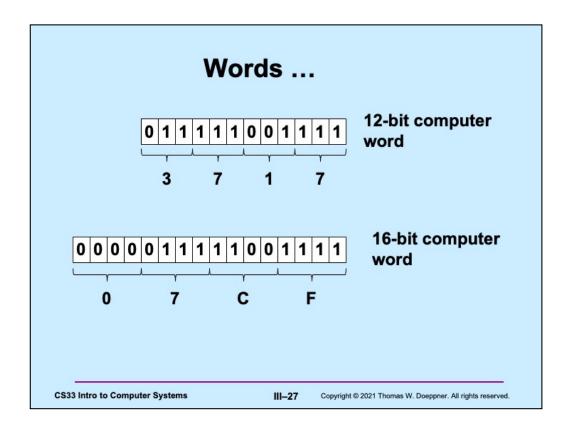
          » 7CF
               · 15-160+12-161+7-162
          » why are we interested?
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                                       III-26
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```

Base 2 is known as "binary" notation.

Base 8 is known as "octal" notation.

Base 10 is known as "decimal" notation.

Base 16 is known as "hexadecimal" notation. Note that "hexa" is derived from the Greek language and "decimal" is derived from the Latin language. Many people feel you shouldn't mix languages when you invent words, but IBM, who coined the term "hexadecimal" in the 1960s, didn't think their corporate image could withstand "sexadecimal".



Note that a byte consists of two hexadecimal digits, which are sometimes known as "nibbles". A 32-bit computer word would then have eight nibbles; a 64-bit computer word would have sixteen nibbles.

Note that for the moment we consider only unsigned integers: i.e., integers whose values are nonnegative.

### Algorithm ... void baseX(unsigned int num, unsigned int base) { char digits[] = {'0', '1', '2', '3', '4', '5', '6', ... }; char buf[8\*sizeof(unsigned int)+1]; int i; for (i = sizeof(buf) - 2; i >= 0; i--) { buf[i] = digits[num%base]; num /= base; **if** (num == 0) break; } buf[sizeof(buf) - 1] = $'\0';$ printf("%s\n", &buf[i]); **CS33 Intro to Computer Systems** III-28 Copyright @ 2021 Thomas W. Doeppner. All rights reserved.

This function prints the base **base** representation of **num**. The "%" operator yields the remainder. E.g., "10%3" evaluates to 1: the remainder after dividing 10 by 3. (Note that the "…" is not heretofore unexplained C syntax, but is shorthand for "fill this in to the extent needed.")

```
Or ...

$ bc
obase=16
1999
7CF
$
```

"bc" (it stands for basic calculator, or perhaps better calculator) is a standard Unix command that handles arbitrary-precision arithmetic. Among its features is the ability to specify which base to use for input and output of numbers. The default base for both input and output is ten. Setting *obase* to 16 sets the base for output to 16. Similarly, one can change the base for input numbers by setting *ibase*. Note that names of digits beyond 9 are upper-case letters (to avoid syntax issues when using variables, which are constrained to using lower-case letters).

## Quiz 4

- What's the decimal (base 10) equivalent of 25<sub>16</sub>?
  - a) 19
  - b) 33
  - c) 35
  - d) 37

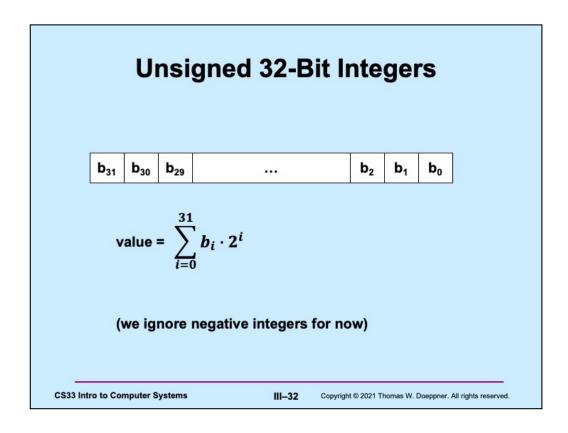
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	mal w
Byte = 8 bits	Hex Decimal
– binary 000000002 to 111111112	0 0 0000
- decimal: 010 to 25510	1 1 0001 2 2 0010
	3 3 0011
<ul> <li>hexadecimal 00<sub>16</sub> to FF<sub>16</sub></li> </ul>	4 4 0100
» base 16 number representation	5 5 0101
» use characters '0' to '9' and 'A' to 'F'	6 6 0110 7 7 0111
» write FA1D37B <sub>16</sub> in C as	8 8 1000
• 0xFA1D37B	9 9 1001
• 0xfa1d37b	A 10 1010 B 11 1011
· VAIATUS/D	B 11 1011 C 12 1100
	D 13 1101
	E 14 1110
	F 15 1111

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Note that C also supports numbers written in octal (base-8) notation. They are written with a leading 0. Thus 016 is the same as 14, which is the same as 0xe.

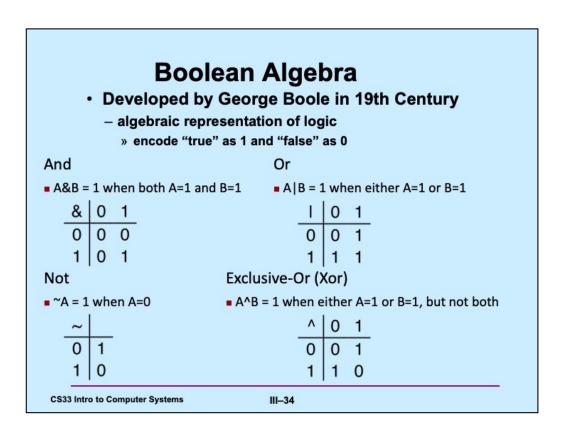


If a computer word is to be interpreted as an unsigned integer, we can do so as shown in the slide for 32-bit integers. Thus integers are represented in binary (base-2) notation in the computer. We'll discuss representing negative integers in an upcoming lecture.

### **Storing and Viewing Ints**

Here n is an *unsigned int* whose value is 57 (expressed in base 10). As we've seen, it's represented in the computer in binary. When we print its value using printf, we choose to view it in the base specified by the format code. %b means binary, %u means decimal (assuming an unsigned int), and %x means hexadecimal.

Note, in the arguments for *printf*, that the format string is in two parts. C allows you to do this: "string 1" "string 2" is treated the same as "string1 string2".



## **General Boolean Algebras**

- · Operate on bit vectors
  - operations applied bitwise

· All of the properties of boolean algebra apply

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# Example: Representing & Manipulating Sets

```
    Representation
```

```
- width-w bit vector represents subsets of \{0, ..., w-1\}
- a_j = 1 iff j ∈ A
01101001 \{0, 3, 5, 6\}
```

```
76543210
01010101 { 0, 2, 4, 6 }
76543210
```

### Operations

```
      & intersection
      01000001
      { 0, 6 }

      | union
      01111101
      { 0, 2, 3, 4, 5, 6 }

      ^ symmetric difference
      00111100
      { 2, 3, 4, 5 }

      ~ complement
      10101010
      { 1, 3, 5, 7 }
```

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### **Bit-Level Operations in C**

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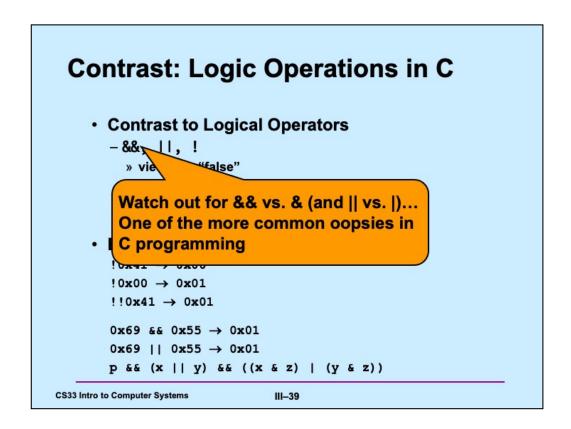
```
Contrast: Logic Operations in C
     · Contrast to Logical Operators
        -8.4, ||, !
          » view 0 as "false"
          » anything nonzero as "true"
          » always return 0 or 1
          » early termination/short-circuited execution

    Examples (char datatype)

        !0x41 \rightarrow 0x00
        !0x00 \rightarrow 0x01
        !!0x41 \rightarrow 0x01
        0x69 && 0x55 → 0x01
        0x69 | | 0x55 \rightarrow 0x01
        p && (x || y) && ((x & z) | (y & z))
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                                 III-38
```

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In the last example, there's no need to evaluate the complicated expression following p if p is false, since we know the final result will be false.



### Quiz 5

- Which of the following would determine whether the next-to-the-rightmost bit of Y (declared as a char) is 1? (l.e., the expression evaluates to true if and only if that bit of Y is 1.)
  - a) Y & 0x02
  - b) !((~Y) & 0x02)
  - c) none of the above
  - d) both a and b

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Recall that a char is an 8-bit integer.

	Argument x	01100010
<ul> <li>Left Shift: x &lt;&lt; y</li> <li>shift bit-vector x left y positions</li> </ul>	<< 3	00010 <i>000</i>
<ul> <li>throw away extra bits on left</li> </ul>	Log. >> 2	00011000
<ul><li>» fill with 0's on right</li><li>• Right Shift: X &gt;&gt; y</li></ul>	Arith. >> 2	00011000
- shift bit-vector x right y positions		
<ul><li>» throw away extra bits on right</li><li>– logical shift</li></ul>	Argument x	10100010
» fill with 0's on left	<< 3	00010 <i>000</i>
<ul> <li>arithmetic shift</li> <li>replicate most significant bit on left</li> </ul>	Log. >> 2	<i>00</i> 101000
Undefined Behavior	Arith. >> 2	<i>11</i> 101000
<ul><li>shift amount &lt; 0 or ≥ word size</li></ul>		

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Why we need both logical and arithmetic shifts should be clear by the end of an upcoming lecture. If one is applying a right shift to an **int**, it is an arithmetic right shift. Why this is so will be explained in the upcoming lecture (it has to do with the representation of negative numbers). Though we haven't yet explained the datatype "unsigned int" (which we will soon), when a right shift is applied to an **unsigned int**, it is a logical shift.