CS 33

Introduction to C
Part 4

Number Representation

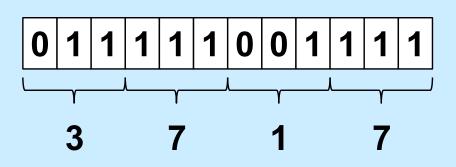
- Hindu-Arabic numerals
 - developed by Hindus starting in 5th century
 - » positional notation
 - » symbol for 0
 - adopted and modified somewhat later by Arabs
 - » known by them as "Rakam Al-Hind" (Hindu numeral system)
 - 1999 rather than MCMXCIX
 - » (try doing long division with Roman numerals!)

Which Base?

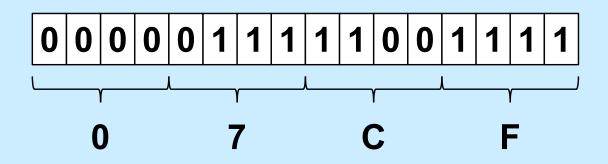
1999

- base 10
 - $9.10^{0}+9.10^{1}+9.10^{2}+1.10^{3}$
- base 2
 - » 11111001111
 - $1 \cdot 2^{0} + 1 \cdot 2^{1} + 1 \cdot 2^{2} + 1 \cdot 2^{3} + 0 \cdot 2^{4} + 0 \cdot 2^{5} + 1 \cdot 2^{6} + 1 \cdot 2^{7} + 1 \cdot 2^{8} + 1 \cdot 2^{9} + 1 \cdot 2^{10}$
- base 8
 - » 3717
 - $7.8^{0}+1.8^{1}+7.8^{2}+3.8^{3}$
 - » why are we interested?
- base 16
 - **» 7CF**
 - 15·16⁰+12·16¹+7·16²
 - » why are we interested?

Words ...



12-bit computer word



16-bit computer word

Base Conversion Algorithm

```
void baseX(unsigned int num, unsigned int base) {
   char digits[] = {'0', '1', '2', '3', '4', '5', '6', ... };
   char buf[8*sizeof(unsigned int)+1];
   int i;
   for (i = sizeof(buf) - 2; i >= 0; i--) {
      buf[i] = digits[num%base];
      num /= base:
      if (num == 0)
         break;
   buf[sizeof(buf) - 1] = ' \setminus 0';
   printf("%s\n", &buf[i]);
```

Or ...

```
$ bc
obase=16
1999
7CF
$
```

Quiz 1

- What's the decimal (base 10) equivalent of 25₁₆?
 - a) 19
 - b) 35
 - c) 37
 - d) 38

Encoding Byte Values

- Byte = 8 bits
 - binary 00000002 to 111111112
 - octal 0₈ to 377₈
 - » write 377₈ in C as
 - 0377
 - decimal: 0₁₀ to 255₁₀
 - hexadecimal 00₁₆ to FF₁₆
 - » base 16 number representation
 - » use characters '0' to '9' and 'A' to 'F'
 - » write FA1D37B₁₆ in C as
 - 0xFA1D37B
 - 0xfa1d37b

Hex Decimal Binary

•	•		•
0	0	0	0000
1	1	1	0001
2	2	2	0010
	3	3	0011
4	4	4	0100
5	5	5	0101
6	6	6	0110
7	7	7	0111
8	8	10	1000
9	9	11	1001
A	10	12	1010
В	11	13	1011
С	12	14	1100
D	13	15	1101
E	14	16	1110
F	15	17	1111

Unsigned 32-Bit Integers

$$\begin{vmatrix} \mathbf{b}_{31} & \mathbf{b}_{30} & \mathbf{b}_{29} \end{vmatrix}$$
 ... $\begin{vmatrix} \mathbf{b}_2 & \mathbf{b}_1 & \mathbf{b}_0 \end{vmatrix}$

value =
$$\sum_{i=0}^{31} b_i \cdot 2^i$$

(we ignore negative integers for now)

Storing and Viewing Ints

```
int main() {
   unsigned int n = 57;
   printf("binary: %b, decimal: %u, "
          "hex: %x\n", n, n, n);
   return 0;
   $ ./a.out
   binary: 111001, decimal: 57, hex: 39
```

Boolean Algebra

- Developed by George Boole in 19th Century
 - algebraic representation of logic
 - » encode "true" as 1 and "false" as 0

And

Or

4&B	=	Τ	wner	both	A=T	and	R=1	L
_	- 1	_						

&	0	1
0	0	0
1	0	1

Not

Exclusive-Or (Xor)

 \blacksquare A | B = 1 when either A=1 or B=1

٨	0	1
0	0	1
1	1	0

General Boolean Algebras

- Operate on bit vectors
 - operations applied bitwise

```
01101001 01101001 01101001

& 01010101 | 01010101 ^ 01010101 ~ 01010101

01000001 01111101 00111100 1010101
```

All of the properties of boolean algebra apply

Example: Representing & Manipulating Sets

Representation

```
width-w bit vector represents subsets of {0, ..., w-1}
```

$$-a_i = 1 \text{ iff } j \in A$$

01101001 { 0, 3, 5, 6 }
76543210

01010101 { 0, 2, 4, 6 }
76543210

Operations

&	intersection	01000001	{ 0, 6 }
l	union	01111101	{ 0, 2, 3, 4, 5, 6 }
٨	symmetric difference	00111100	{ 2, 3, 4, 5 }
~	complement	10101010	{ 1, 3, 5, 7 }

Bit-Level Operations in C

- Operations &, ∣, ~, ^ available in C
 - apply to any "integral" data type» long, int, short, char
 - view arguments as bit vectors
 - arguments applied bit-wise
- Examples (char datatype)

```
\sim 0x41 \rightarrow 0xBE
\sim 01000001_2 \rightarrow 10111110_2
\sim 0x00 \rightarrow 0xFF
\sim 00000000_2 \rightarrow 11111111_2
0x69 & 0x55 \rightarrow 0x41
01101001_2 & 01010101_2 \rightarrow 01000001_2
0x69 \mid 0x55 \rightarrow 0x7D
01101001_2 \mid 01010101_2 \rightarrow 01111101_2
```

Contrast: Logic Operations in C

Contrast to Logical Operators

```
- &&, ||, !
» view 0 as "false"
» anything nonzero as "true"
» always return 0 or 1
» early termination/short-circuited execution
```

Examples (char datatype)

```
!0x41 \rightarrow 0x00

!0x00 \rightarrow 0x01

!!0x41 \rightarrow 0x01

0x69 && 0x55 \rightarrow 0x01

0x69 || 0x55 \rightarrow 0x01

p && complicated_function(x)
```

Contrast: Logic Operations in C

Contrast to Logical Operators

```
- && ||, !

» vie "false"
```

Watch out for && vs. & (and || vs. |)...
One of the more common oopsies in C programming

```
!0x41 → 0x00

!0x00 → 0x01

!!0x41 → 0x01

0x69 && 0x55 → 0x01

0x69 || 0x55 → 0x01

p && complicated function(x)
```

Quiz 2

- Which of the following would determine whether the next-to-the-rightmost bit of Y (declared as a char) is 1? (I.e., the expression evaluates to true if and only if that bit of Y is 1.)
 - a) Y & 0x02
 - b) !((~Y) & 0x02)
 - c) none of the above
 - d) both a and b

Shift Operations

- Left Shift: x << y
 - shift bit-vector x left y positions
 - throw away extra bits on left
 - » fill with 0's on right
- Right Shift: x >> y
 - shift bit-vector x right y positions
 - » throw away extra bits on right
 - logical shift
 - » fill with 0's on left
 - arithmetic shift
 - » replicate most significant bit on left
- Undefined Behavior
 - shift amount < 0 or ≥ word size</p>

Argument x	01100010
<< 3	00010 <i>000</i>
Log. >> 2	00011000
Arith. >> 2	00011000

Argument x	10100010
<< 3	00010 <i>000</i>
Log. >> 2	<i>00</i> 101000
Arith. >> 2	<i>11</i> 101000

Digression

- Pre-increment
 - ++b means add one to b; the result of the expression is this new value of b
- Post-increment
 - b++ means the value of the expression is the current value of b, then add one to b
- Example

```
int b=1;
printf("%d\n", (++b)*b);
```

```
int b=1;
printf("%d\n", (b++)*b);
```

output:

4

output:

2

Global Variables

```
m can be used
#define NUM ROWS 3
                                by all functions
#define NUM COLS 4
int m[NUM ROWS][NUM COLS];
int main() {
   int row, col;
   for (row=0; row<NUM ROWS; row++)</pre>
     for (col=0; col<NUM COLS; col++)</pre>
         m[row][col] = row*NUM COLS+col;
   return 0;
```

The scope is global;

Global Variables

```
#define NUM ROWS 3
#define NUM COLS 4
int m[NUM ROWS][NUM COLS];
int main() {
   int row, col;
   printf("%u\n", m);
   printf("%u\n", &row);
   return 0;
      $ ./a.out
      8384
      3221224352
```

Global Variables are Initialized!

```
#define NUM_ROWS 3
#define NUM_COLS 4
int m[NUM_ROWS][NUM_COLS];

int main() {
   printf("%d\n", m[0][0]);
   return 0;
}
```

```
$ ./a.out
0
```

Scope

```
int a; // global variable
int main() {
   int a; // local variable
  a = 0;
  proc();
  printf("a = %d\n", a); // what's printed?
  return 0;
                     $ ./a.out
int proc() {
  a = 1;
  return a;
```

Scope (continued)

```
int a; // global variable
int main() {
  a = 2;
                        $ ./a.out
  proc(1);
   return 0;
int proc(int a) {
   printf("a = %d\n", a); // what's printed?
   return a;
```

Scope (still continued)

```
int a; // global variable
int main() {
  a = 2;
  proc(1);
  return 0; $ gcc prog.c
             prog.c:12:8: error: redefinition of 'a'
                int a;
int proc(int a) {
   int a;
   printf("a = %d\n", a); // what's printed?
   return a;
```

Scope (more ...)

```
int a; // global variable
int proc() {
      // the brackets define a new scope
      int a;
      a = 6;
   printf("a = %d\n", a); // what's printed?
   return 0;
                         $ ./a.out
```

Quiz 3

```
int a;
int proc(int b) {
   {int b=6;}
   a = b;
   return a+2;
int main() {
   {int a = proc(4);}
   printf("a = %d\n", a);
   return 0;
```

- What's printed?
 - a) 0
 - b) 4
 - c) 6
 - d) 8
 - e) nothing; there's a syntax error

Scope and For Loops (1)

```
int A[100];
for (int i=0; i<100; i++) {
    // i is defined in this scope
    A[i] = i;
}</pre>
```

Scope and For Loops (2)

```
int A[100];
initializeA(A);
for (int i=0; i<100; i++) {</pre>
  // i is defined in this scope
  if (A[i] < 0)
    break;
if (i != 100)
  printf("A[%d] is negative\n", i); reference to i is
```

syntax error: out of scope.

Lifetime

```
int count;
int main() {
   func();
   func(); // what's printed by func?
   return 0;
                        % ./a.out
int func() {
                        -38762173
   int a;
   if (count == 0) a = 1;
   count = count + 1;
  printf("%d\n", a);
   return 0;
```

Lifetime (continued)

```
int main() {
   func(1); // what's printed by func?
   return 0;
int a;
int func(int x) {
                      % ./a.out
   if (x == 1) {
     a = 1;
      func(2);
     printf("%d\n", a);
   } else
     a = 2;
   return 0;
```

Lifetime (still continued)

```
int main() {
   func(1); // what's printed by func?
   return 0;
int func(int x) {
                      % ./a.out
   int a;
   if (x == 1) {
      a = 1;
      func(2);
      printf("a = %d\n", a);
   } else
     a = 2;
   return 0;
```

Lifetime (more ...)

```
int main() {
   int *a;
   a = func();
   printf("%d\n", *a); // what's printed?
   return 0;
                       % ./a.out
23095689
int *func() {
   int x;
   x = 1;
   return &x;
```

Lifetime (and still more ...)

```
int main() {
   int *a;
   a = func(1);
   printf("%d\n", *a); // what's printed?
   return 0;
}

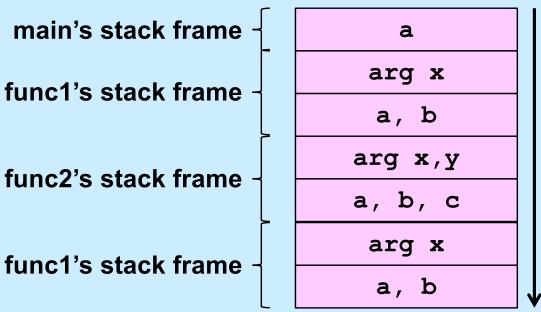
int *func(int x) {
   return &x;
}
% ./a.out
98378932
return &x;
```

Rules

- Global variables exist for the duration of program's lifetime
- Local variables and arguments exist for the duration of the execution of the function
 - from call to return
 - each execution of a function results in a new instance of its arguments and local variables

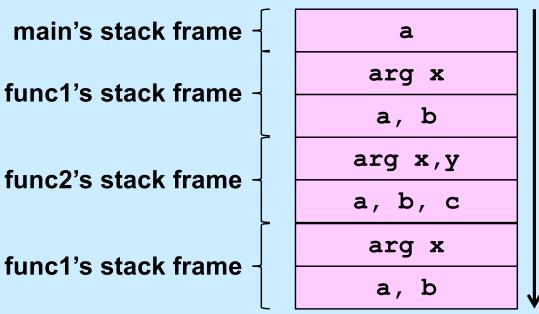
Implementation: Stacks

```
int main() {
   int a;
   func1(0);
int func1(int x) {
   int a,b;
   if (x==0) func2(a,2);
int func2(int x, int y) {
   int a,b,c;
   func1(1);
```



Implementation: Stacks

```
int main() {
   int a;
   func1(0);
int func1(int x) {
   int a,b;
   if (x==0) func2(a,2);
int func2(int x, int y) {
   int a,b,c;
   func1(1);
```



Quiz 4

```
void func(int a) {
   int b=2;
   if (a == 1) {
      func(2);
      printf("%d\n", b);
   } else {
     b = a*(b++)*b;
int main() {
   func(1);
   return 0;
```

- What's printed?
 - a) 0
 - b) 1
 - c) 2
 - d) 4

Static Local Variables

- Scope
 - like local variables
- Lifetime
 - like global variables
- Initialized just once
 - when program begins
 - implicit initialization to 0

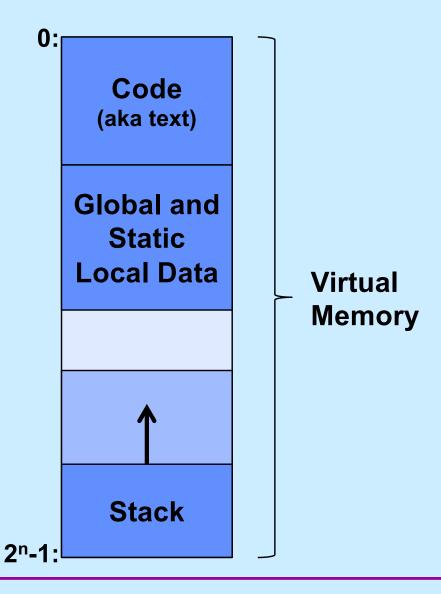
Quiz 5

```
int sub() {
  static int svar = 2;
  int lvar = 1;
  svar += lvar;
  lvar++;
  return svar;
int main() {
  sub();
 printf("%d\n", sub());
  return 0;
```

What is printed?

- a) 2
- b) 3
- c) 4
- d) 5

Digression: Where Stuff Is (Roughly)



scanf: Reading Data

```
int main() {
   int i, j;
   scanf("%d %d", &i, &j);
   printf("%d, %d", i, j);
}
```

```
$ ./a.out
3 12
3, 12
```

Two parts

- formatting instructions
 - whitespace in format string matches any amount of white space in input
 - » whitespace is space, tab, newline ('\n')
- arguments: must be addresses
 - why?

#define (again)

```
#define CtoF(cel) (9.0*cel)/5.0 + 32.0
```

Simple textual substitution:

```
float tempc = 20.0;
float tempf = CtoF(tempc);
// same as tempf = (9.0*tempc)/5.0 + 32.0;
```

Careful ...

```
#define CtoF(cel) (9.0*cel)/5.0 + 32.0
float tempc = 20.0;
float tempf = CtoF(tempc+10);
// same as tempf = (9.0*tempc+10)/5.0 + 32.0;
#define CtoF(cel) (9.0*(cel))/5.0 + 32.0
float tempc = 20.0;
float tempf = CtoF(tempc+10);
// same as tempf = (9.0*(tempc+10))/5.0 + 32.0;
```

Conditional Compilation

```
#ifdef DEBUG
  #define DEBUG_PRINT(a1, a2) printf(a1,a2)
#else
  #define DEBUG_PRINT(a1, a2)
#endif
int buggy func(int x) {
```

```
int buggy_func(int x) {
    DEBUG_PRINT("x = %d\n", x);
    // printed only if DEBUG is defined
    ...
}
```