UC Berkeley EECS Sr Lecturer SOE Dan Garcia



The Beauty and Joy of Computing

Lecture #10

Recursion II



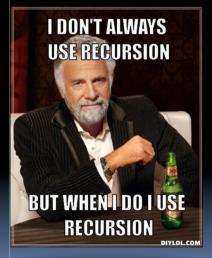
Toby Shachman created this amazing spatial programming language called "Recursive Drawing" that allows you to create drawings (even recursive ones) without typing a line of code. It's a great example of a next-generation interface...





Recursion

- Factorial Demo
- Fibonacci Demo
- Count Change







Recursion: Factorial

TRACE

6 returning

8 returning 2

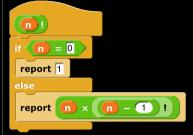
10 returning 24

bjc I

Recursion: Demonstrating n!

- Factorial(n) = n! Inductive definition:
 - n! = 1 , n = 0
 - n! = n * (n-1)!, n > 0
- Let's act 4! out...
 - "contractor" model









(Cal) Order of growth of # of calls of n!

- a) Constant
- b) Logarithmic
- c) Linear
- d) Quadratic
- e) Exponential





Recursion: Fibonacci



Recursion: Demonstrating fib(n)

Inductive definition:

$$fib(n) = fib(n-1)+fib(n-2)$$
, $n \ge 2$

$$F(n) := \begin{cases} 0 & \text{if } n = 0; \\ 1 & \text{if } n = 1; \\ F(n-1) + F(n-2) & \text{if } n > 1. \end{cases}$$

Let's act it out...

- "contractor" model
- fib(5)

n fib(n)

0	0
1	1
2	1
3	2
4	3
5	5









 \square

n < 2



(Cal) Order of growth of # of calls of fib(n)

- a) Constant
- b) Logarithmic
- c) Linear
- d) Quadratic
- e) Exponential

Chimney of Turku Energia, Turku, Finland featuring Fibonacci sequence in 2m high neon lights. By Italian artist Mario Merz for an environmental art project. (Wikipedia)







Recursion: Count Change



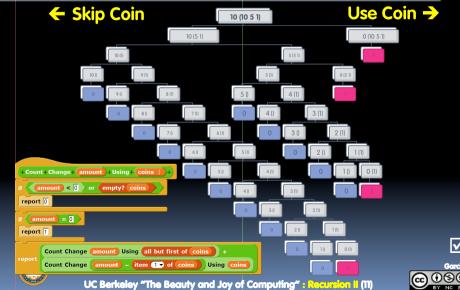
Counting Change (thanks to BH)

Given coins {50, 25, 10, 5, 1} **5** how many ways are there 2 (N, 5P) of making change? 10 • 4 (D. 2N. N5P. 10P) +Count+Change+ amount +Using+ coins : + 6 (DN, D5P, 3N, 2N5P. 1N10P, 15P) amount < 0 or empty? coins **- 100?** report 0 amount = 0 report 1 Count Change amount Using all but first of coins report Count Change amount - item 1 v of coins Using coins





Call Tree for "Count Change 10 (10 5 1)"





(Cal) "I understood Count Change"

- a) Strongly agree
- b) Agree
- c) Neutral
- d) Disagree
- e) Strongly disagree

www.nilkanth.com/my-uploads/200508/dactylfractal107.jpg









- It's important to understand the machine model
- It's often the simplest way to solve many problems
 - Esp if recursive in nature!
- Remember, trust it!
- Recursion is a very powerful idea, often separates good from great (you're great!)

Menger Cube by Dan Garcia

