



# The Beauty and Joy of Computing

## Lecture #3 Abstraction II



### What I Wish I Knew When I Started My SW Career

Among the advice given:

- Don't be afraid to learn on job
- Never ask for permission unless it would be reckless not
- Exercise
- Long hours: sometimes ok, usually harmful
- Learn as much as you can. It's hard, and it takes work





# Abstraction (revisited): Numbers

- Number bases, including binary and decimal, are used for reasoning about digital data.
- Bits represent binary data using base two digits: zero and one.
- Hexadecimal, or base-16, is often used in reasoning about data e.g., colors in images.
- Different bases help in reasoning about digital data; digital data is stored in bits.

000000100000  
000111011100  
001000000100  
011011011011  
011000000011  
001000100010  
001010001010  
000101110010  
000010000100  
000001111000



# Base 10 #s, Decimals

---

**Digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9**

**Example:**

$$3271 = 3271_{10} =$$

$$(3 \times 10^3) + (2 \times 10^2) + (7 \times 10^1) + (1 \times 10^0)$$





# Base 2 #s, Binary (to Decimal)

---

Digits: 0, 1 (binary digits → bits)

Example: "1101" in binary? ("0b1101")

$$\begin{aligned} 1101_2 &= (1 \times 2^3) + (1 \times 2^2) + (0 \times 2^1) + (1 \times 2^0) \\ &= 8 + 4 + 0 + 1 \\ &= 13 \end{aligned}$$





# Base 16 #s, Hexadecimal (to Decimal)

**Digits:** 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F  
10, 11, 12, 13, 14, 15

**Example: "A5" in Hexadecimal?**

$$0xA5 = A5_{16} = (10 \times 16^1) + (5 \times 16^0)$$

$$= 160 + 5$$

$$= 165$$





# Decimal vs Hexadecimal vs Binary

- **N bits =  $2^N$  things**

- **4 Bits**

- 1 "Nibble"
- 1 Hex Digit = 16 things

- **8 Bits**

- 1 "Byte"
- 2 Hex Digits = 256 things
- Full color is often 256 Red, 256 Blue, 256 Green (#4A00FF)

D	H	B
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111



bjc

# (Cal) Smallest to Largest?



a)  $0xC < 0b1010 < 11$

b)  $0xC < 11 < 0b1010$

c)  $11 < 0b1010 < 0xC$

d)  $0b1010 < 11 < 0xC$

e)  $0b1010 < 0xC < 11$





# Convert FROM decimal TO binary

- E.g., 13 to binary?
- Start with the columns

~~13~~  
~~5~~  
~~1~~  
 0

2 <sup>3</sup> =8	2 <sup>2</sup> =4	2 <sup>1</sup> =2	2 <sup>0</sup> =1
1	1	0	1

- Left to right, is (column)  $\leq$  number n?
  - If yes, put how many of that column fit in n, subtract col \* that many from n, keep going.
  - If not, put 0 and keep going. (and Stop at 0)







# Convert FROM decimal TO hexadecimal

- E.g., 165 to hexadecimal?
- Start with the columns

~~165~~  
~~5~~  
 0

16 <sup>3</sup> = 4096	16 <sup>2</sup> = 256	16 <sup>1</sup> = 16	16 <sup>0</sup> = 1
0	0	10 (A)	5

- Left to right, is (column)  $\leq$  number n?
  - If yes, put how many of that column fit in n, subtract col \* that many from n, keep going.
  - If not, put 0 and keep going. (and Stop at 0)





# Convert Binary $\leftrightarrow$ Hexadecimal

## ▪ Binary $\rightarrow$ Hex? Easy!

- Always left-pad with 0s to make full nibbles, then look up!
- E.g., **0b11110** to Hex?
  - **0b11110  $\rightarrow$  0b00011110**
  - Then look up: **0x1E**

## ▪ Hex $\rightarrow$ Binary? Easy!

- Just look up, drop leading 0s
  - **0x1E  $\rightarrow$  0b00011110  $\rightarrow$  0b11110**

D	H	B
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111





# (Cal) Why do we use different bases?



- a) Binary is used by computers, since transistors are bistable (at two values)
- b) Hex is used by humans for encoding binary information because it's 4 times more efficient (number of chars)
- c) Decimal because we have 10 fingers
- d) The fact that computers use binary is below our level of abstraction
- e) All of the above



# Abstraction (revisited): Digital Data

- A combination of abstractions is used to represent digital data.
- At the lowest level all digital data are represented by bits.
  - Bits can represent anything!
- Bits are grouped to represent higher-level abstractions including numbers and characters.
  - Logical values? 0 → False, 1 → True
  - Colors? 00 → Red, 01 → Green, 10 → Blue
  - Characters? 00000 → 'a', 00001 → 'b', ...
- Higher-level abstractions such as Internet protocol (IP) packets, images, and audio files are comprised of groups of bits that represent different parts of the abstractions.



# Interpretation of a Binary Sequence...

- ...depends on how it is used (e.g., as instruction, number, text, sound, or image).
- The sequence of bits that represents...
  - ...an instruction may also represent data processed by that instruction.
  - ...a character/letter may also represent a number.
  - ...a color in an image may also represent a sound in an audio file.

*(Wikipedia)*





# Detail Removal Often Comes At A Cost

- **Removing detail isn't universally a positive thing.**
  - The simplification often takes out the subtle aspects of the original
  - Cliff notes not always better than novel!



**The London Underground 1928 Map & Harry Beck 1933 map.**





# Overflow and Roundoff

## ▪ Overflow

- When the number of represented things exceeds digits allocated for it.
- E.g., Odometer rollover
  - 99999 → 00000
- E.g., Adding  $15 + 2$  using 4 bits:
  - $0b1111 + 0b10 = 0b1$

## ▪ Roundoff error

- When the true real number can't be stored exactly given the encoding due to the fixed number of bits
  - E.g.,  $\pi = 3.14$
- Sometimes this error accumulates causing problems!





# Summary: Abstractions everywhere!

- Applications and systems are designed, developed, and analyzed using levels of hardware, software, and conceptual abstractions.
  - E.g., Mobile apps and systems
  - E.g., Web services (both an application and a system)
- This course will include examples of abstractions used in modeling the world, managing complexity, and communicating with people as well as with machines.

