

The Beauty and Joy of Computing

Lecture #19 **Limits of Computing**

Algorithms Determine "Character"

A new startup called "Upstart" is making a name by trying to use algorithms to determine "character" traits about who is mostly likely to pay a loan back. They try to give loans to people who are less likely to qualify using metrics like college graduation or SAT scores.



http://mobile.nytimes.com/bloqs/bits/2015/07/26/usinq-algorithms-to-determine-character/

Admin Notes

- Schedule (see website)
- Next Week Lots of guests!
- HKN Surveys
 - Please come, bonus points!



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Introduction to Complexity **Theory**



- CS research areas:
 - Artificial Intelligence
 - Biosystems & Computational Biology
 - Database Management Systems
 - Graphics
 - Human-Computer Interaction
 - Networking
 - Programming Systems
 - Scientific Computing
 - Security
 - Systems

 - Complexity theory



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Let's revisit algorithm complexity

- Problems that...
 - are tractable with efficient solutions in reasonable time
 - are intractable
 - are solvable approximately, not optimally
 - have no known efficient solution
 - are not solvable



Tractable with efficient sols in reas time

 Recall our algorith n complexity lecture we've got several common orders of growth

- Constant
- Logarithmic
- Linear Quadratic
- Cubic Exponential

- Order of growth is polynomial in the size of the problem
- Searching for an item in a collection
 - Sorting a collection
- Finding if two numbers in a collection are
- These problems are called being "in P" (for polynomial)



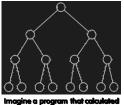






en.wikipedia.org/wiki/Intractability_(complexity) #Intractability Intractable problems

- Problems that can be solved, but not solved fast enough
- This includes exponential problems
 - E.g., f(n) = 2ⁿ
 - as in the image to the right
- This also includes polytime algorithm with a huge exponent
 - E.g, $f(n) = n^{10}$
- Only solve for small n



Imagine a program that calculated something important at each of the bottom circles. This tree has height n but there are 2° bottom circles!

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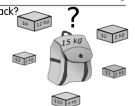


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(Cal) Peer Instruction

What's the most you can put in your knapsack?

- a) \$10
- b) \$15
- c) \$33
- d) \$36
- e) \$40



Knapsack Problem

You have a backpack with a weight limit (here **15kg**), which boxes (with weights and values) should be taken to maximize value?

(any # of each box is available)

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Heuristics, NP, NP-Hard, NP-Complete

solvable approximately, not optimally in reas time

- A problem might have an optimal solution that cannot be solved in reasonable time
 - E.g., optimization problems such as "find the best/smallest"
- BUT if you don't need to know the perfect solution, there might exist "approximation" algorithms which could give pretty good answers in reasonable time
- Heuristic: a technique that may allow us to find an approximate solution (e.g., valuable stuff first!)
- Some problems cannot be solved using any algorithm. (e.g., finding a robot path to a blocked-off area)



Knapsack Problem
You have a backpack with a weight
limit (here 15kg), which boxes (with
reights and values) should be taken to
maximize value?

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en.wikipedia.org/wiki/P \$3D NP problem

Have no known efficient solution

- Solving one of them would solve an entire class of them!
 - We can transform one to another, i.e., reduce
 - A problem P is "hard" for a class C if every element of C can be "reduced" to P
- If you're "in NP" and "NP-hard", then you're "NP-complete"
- -2 -3 15

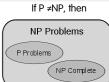
Subset Surn Problem

Are there a handful of these numbers
(at least 1) that add together to get 0?

- If you guess an answer, can I <u>verify it</u> in polynomial time?
 - Called being "in NP
 - Non-deterministic (the "guess" part)
 Polynomial



- This is THE major unsolved problem in Computer Science!
 - One of 7 "millennium prizes" w/a \$1M reward
- All it would take is solving ONE problem in the NP-complete set in polynomial time!!
 - Huge ramifications for cryptography, others

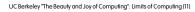


- Other NP-Complete
 - Traveling salesman who needs most efficient route to visit all cities and return home



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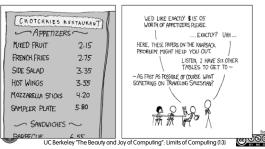




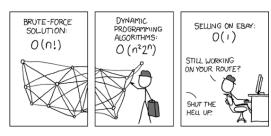


XKCD #287, NP-Complete

MY HOBBY: EMBEDDING NP-COMPLETE PROBLEMS IN RESTAURANT ORDERS



XKCD #399, Travelling Salesman





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Decidability

Problems NOT solvable

- Decision problems answer YES or NO for an infinite # of inputs
- E.g., is N prime?
- E.g., is sentence S grammatically correct?
- An algorithm is a solution if it correctly answers YES/NO in a finite amount of time
- A problem is decidable if it has a solution



www.cql.uwaterloo.ca/-csk/halt/

Alan Turina "Are all problems decidable?"
(people used to believe this was true) Turing proved it wasn't for CS!

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Proof by Contradiction

- Infinitely Many Primes?
- Assume the contrary, then prove that it's impossible
 - Only a finite set of primes, $numbered\ p_1,\,p_2,\,...,\,p_n$
 - Consider $q=(p_1 \bullet p_2 \bullet \dots \bullet p_n)+1$
 - $\circ\quad \mbox{Dividing q by }p_{i}\mbox{ has remainder 1}$
 - q either prime or composite · If prime, q is not in the set
 - If composite, since no p_i divides q,
 - there must be another p that does that is not in the set.
 - So there's infinitely many primes



Given a program and some input, will that program eventually stop? (or will it loop)

Assume we could write it, then let's prove a contradiction

 ${\mathscr F}$ Turing's proof : The Halting Problem

- 1. write Stops on Self?
- 2. Write Weird
- 3. Call Weird on itself







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Example 2 Conclusion

- Complexity theory important part of CS
- If given a hard problem, rather than try to solve it yourself, see if others have tried similar problems
- If you don't need an exact solution, many approximation algorithms help



into popular culture, here show the Simpsons 3D episode!

Some not solvable!

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