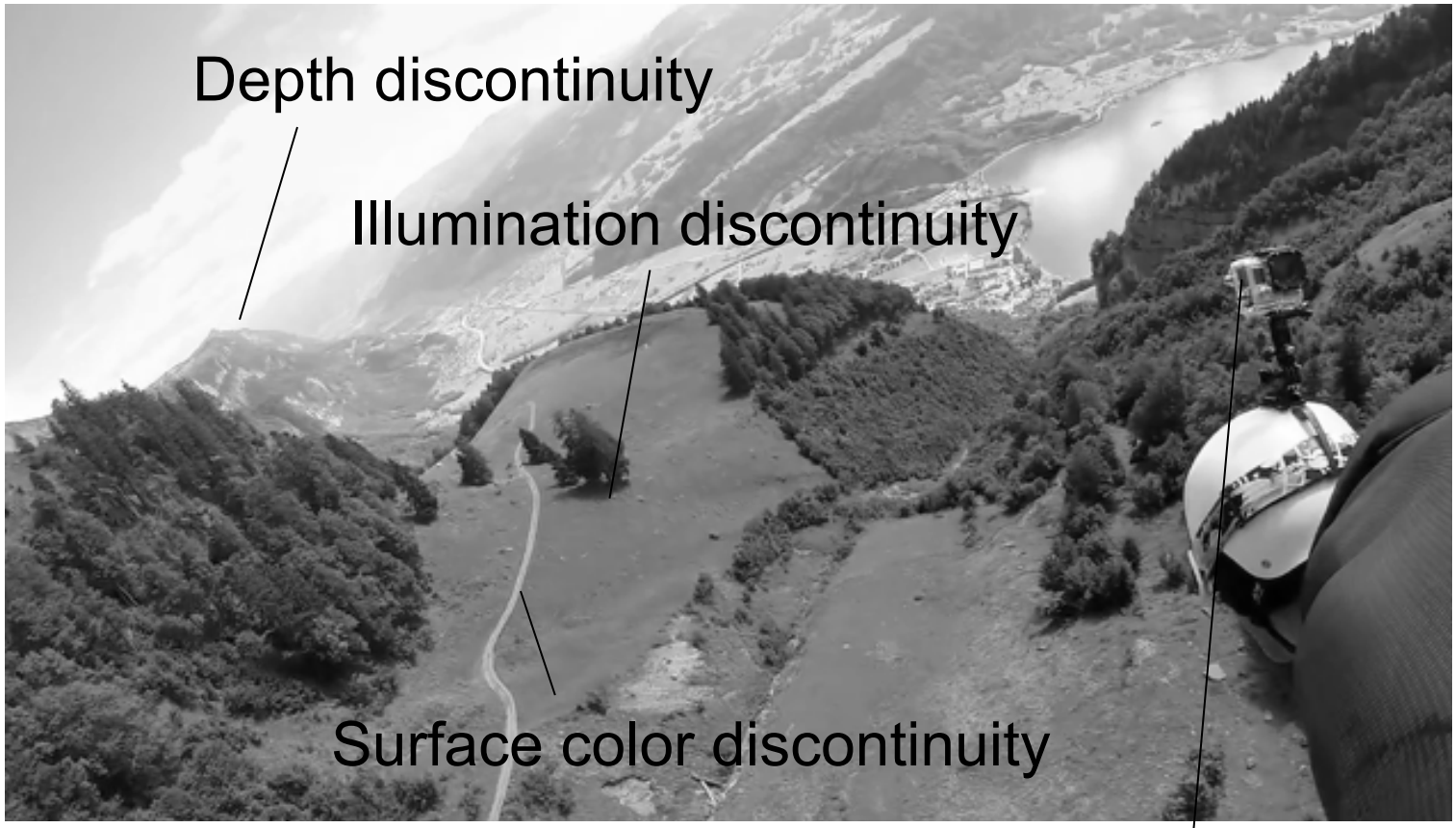
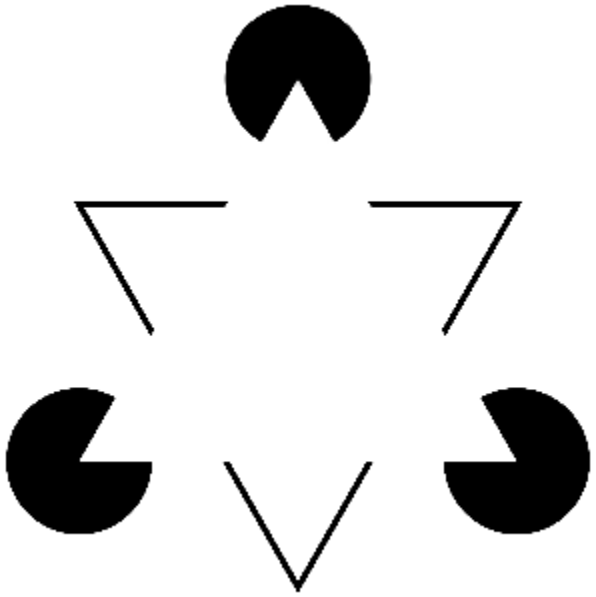
Edge Formation Factors



Kanizsa Triangle



Canny Edge Detection

$$B(i,j) = \begin{cases} 1 & \text{if } I(i,j) \text{ is edge} \\ 0 & \text{if } I(i,j) \text{ is not edge} \end{cases}$$

Objective: to localize edges given an image.

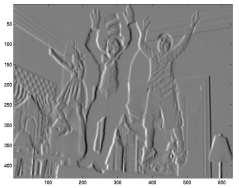
Original image, I

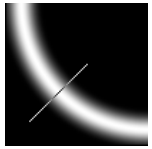
Binary image indicating edge pixels

Edge map image, B

Canny Edge Detection

1. Filter image by derivatives of Gaussian
2. Compute magnitude of gradient
3. Compute edge orientation
4. Detect local maximum
5. Edge linking





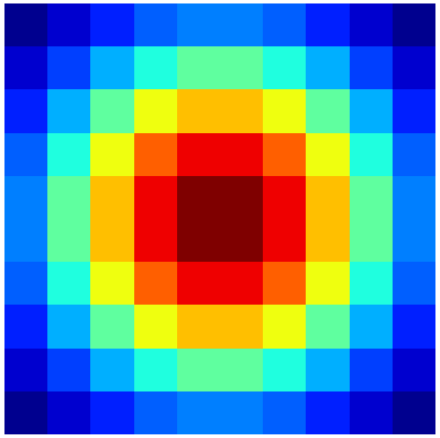
1) Compute Image Gradient

the first order derivative of Image I in x, and in y direction

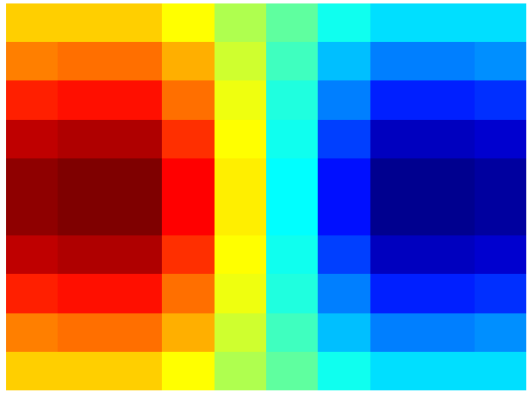
Edge Detection, Step 1, Filter out noise and compute derivative:

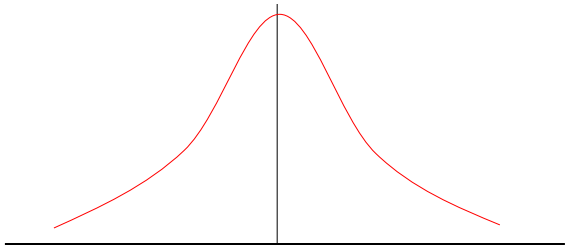
$$(\frac{\delta}{\delta x} \otimes G)$$

Gradient of Gaussian

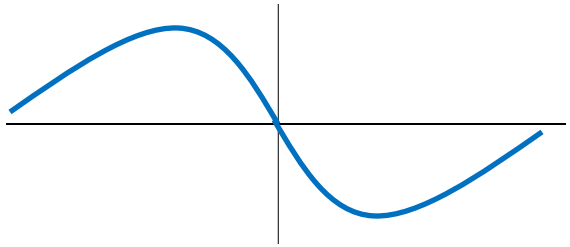


$$\frac{\delta}{\delta x}$$





$$\frac{\delta}{\delta x}$$

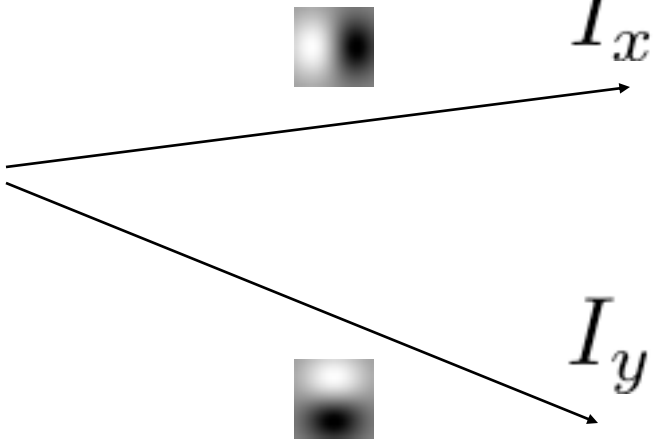


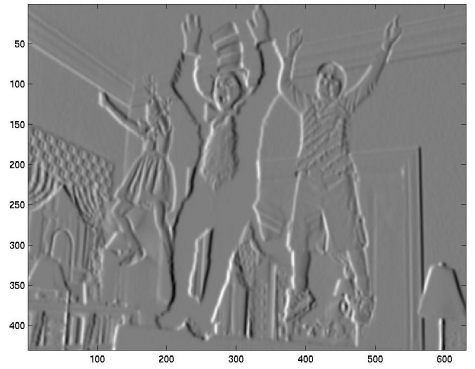
Edge Detection, Step 1, Filter out noise and compute derivative:

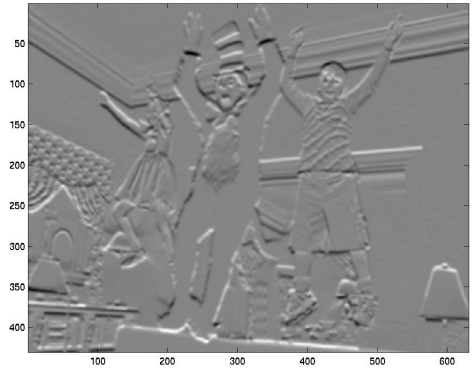
Image

$$\otimes\left(\frac{\delta}{\delta x} \otimes G\right)$$

Smoothed Derivative



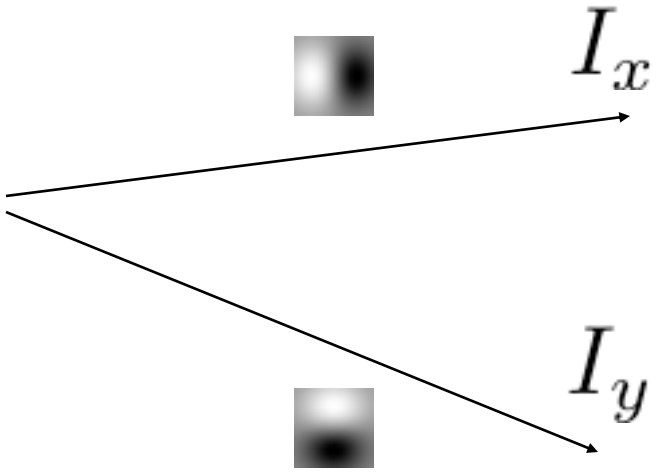


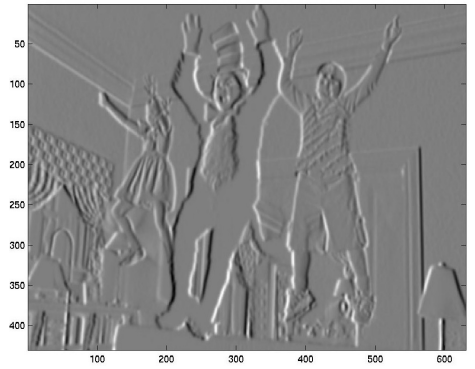


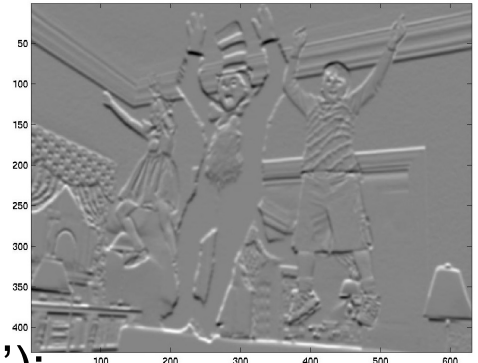
Edge Detection, Step 1, Filter out noise and compute derivative:

Python:

```
dx, dy = np.gradient(G, axis = (1,0))
Ix = signal.convolve2d(I,dx,'same')
Iy = signal.convolve2d(I,dy,'same')
```







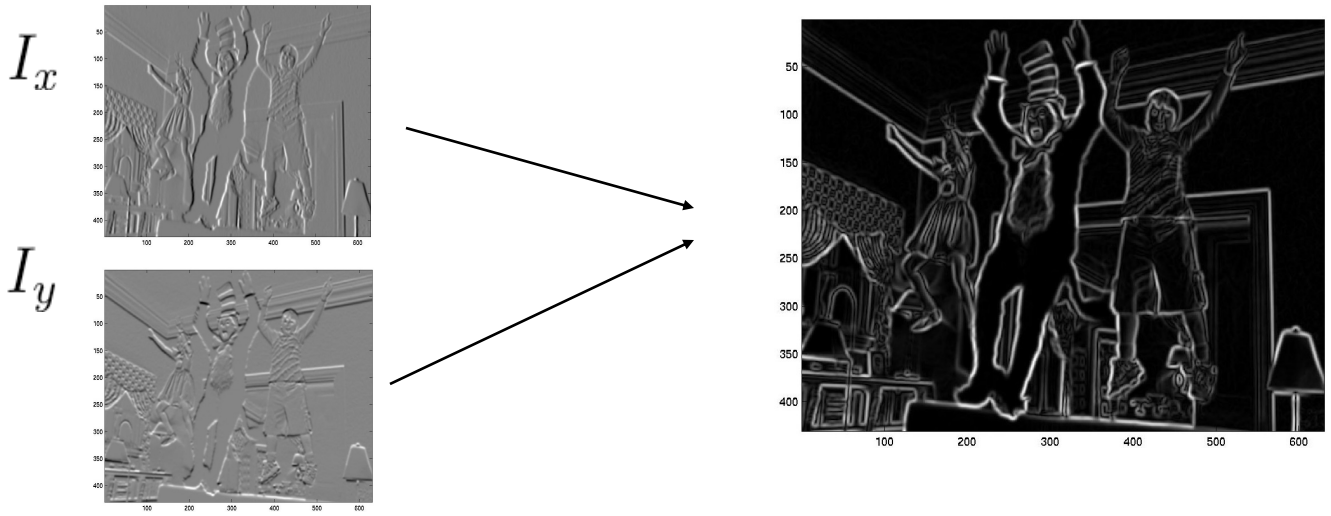
MATLAB:

```
>> [dx,dy] = gradient(G); % G is a 2D gaussain
>> Ix = conv2(I,dx,'same'); Iy = conv2(I,dy,'same');
```

Edge Detection: Step 2
Compute the magnitude of the gradient

Python:
Im = math.sqrt(Ix*Ix + Iy*Iy);

Matlab:
>> Im = sqrt(Ix.*Ix + Iy.*Iy);



We know roughly where are the edges, but we need their precise location.